

Track fitting performance in SpdRoot

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VI SPD Collaboration Meeting

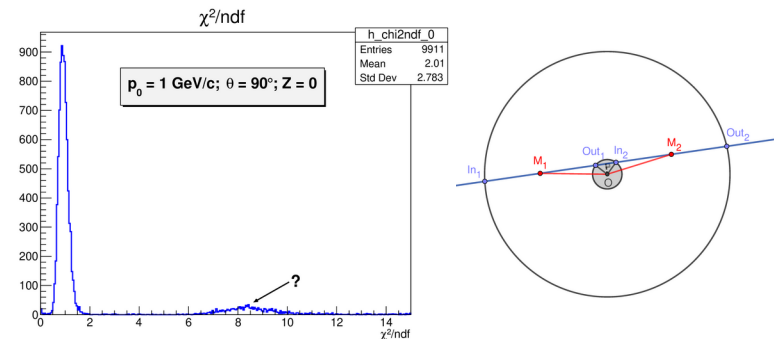
Samara, 23-27 October 2023

Introduction

- In this study I explore how well track fitting in SpdRoot works in a wide range of momenta and angles of tracks.
- The purpose of the study is to identify existing problems in the software, and try to fix them, or at least to find an explanation for the observed "anomalies".
- After that, a set of recommendations on which track quality cuts to use in physical analysis could be developed.

Introduction

- The first steps of the work in this direction were presented at the previous SPD Collaboration Meeting in April 2023.
- After that, a problem with additional hit in χ^2/ndf distribution due to incorrect drift radius calculation for hits when track crosses the wire was solved (see, e.g. SPD Physics Weekly meeting in September 19, 2023).
- Results, presented in this talk, have been already *partially* reported at the SPD Physics Weekly meetings in October 2023.

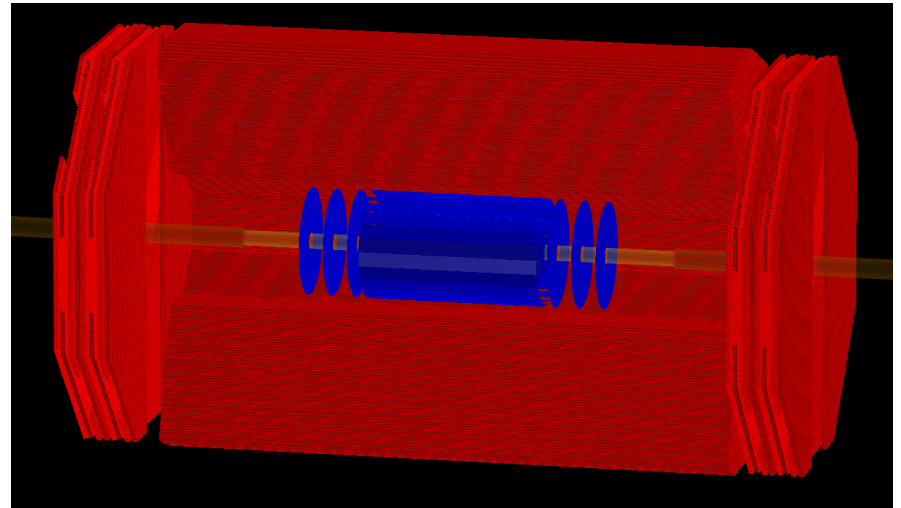


Simulation

- SpdRoot: branch **geometry-update-spring-2023**
(was merged with the master branch just a few days ago)

- Trackers:

- Inner tracker:
DSSD (3 layers, with endcaps)
- Straw tracker:
 - ♦ Barrel: 31 double layers
 - ♦ Endcaps: 8 double layers



- Artificial sample:
 π^+ , isotropical, $p_0 = 0 \dots 5 \text{ GeV}/c$ (with step $0.05 \text{ GeV}/c$), $Z_{\text{primary vertex}} = 0$,
400k events (1 particle/event).

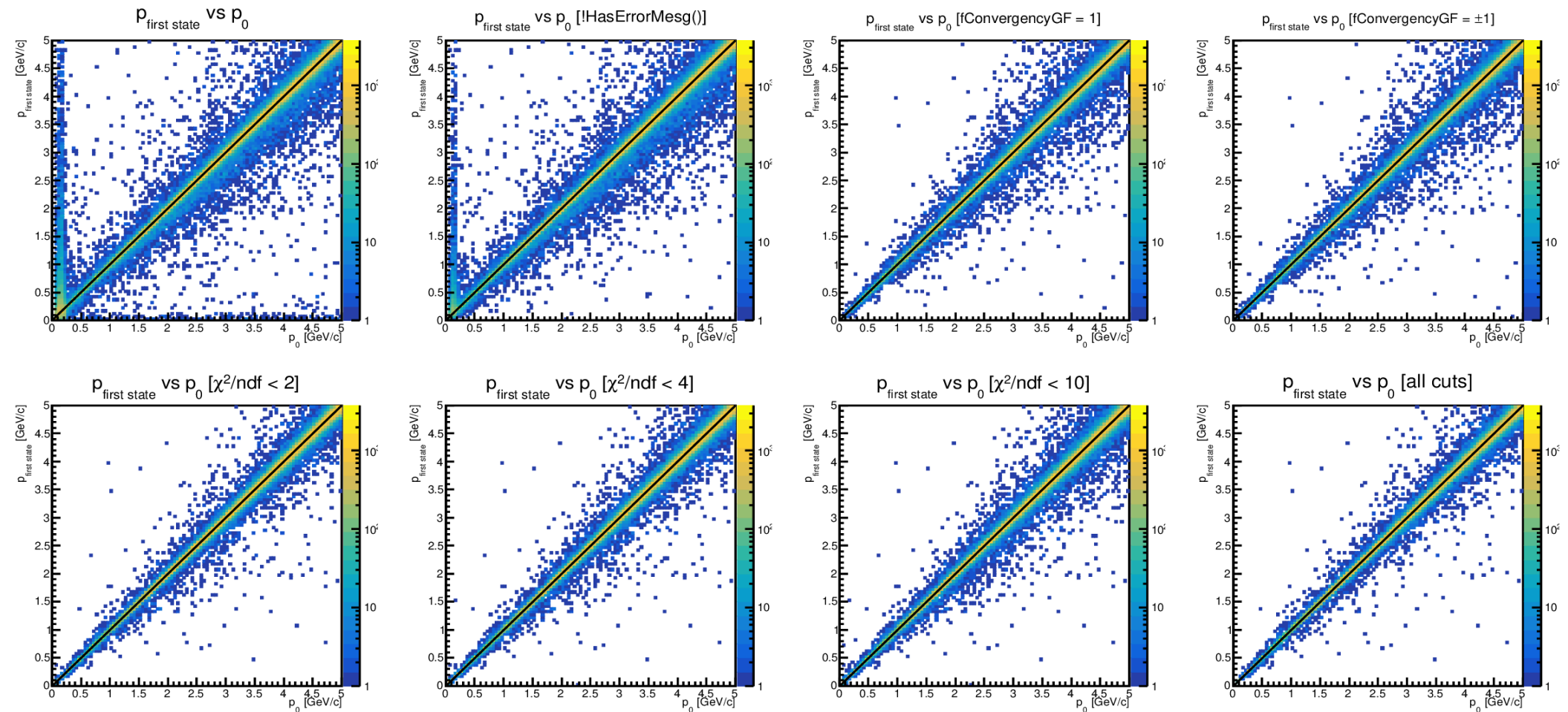
Reconstruction

- The corrected function for the drift radius calculation is used (see [my talk at SPD Physics Weekly Meeting, Sep 19, 2023](#)).
- **Ideal track finding.**
- The only requirement for a particle to be accepted as a track (in SpdMCTracksFinder) is total **N hits ≥ 3** .
- For track fitting package **GenFit2** is used inside SpdRoot.

Track fit parameters

- Track fit quality characteristics are saved in SpdTrackFitPar:
 - Error message(s)
("RKTrackRep::RKutta", "RKTrackRep::Extrap", "MaterialEffects::getMomGammaBeta",
"MaterialEffects::dEdxBetheBloch", ...)
 - **Convergency flag:**
 - 0 — not converged
 - 1 — fully converged
 - -1 — partially converged
 - NFailedHits
 - χ^2 → **χ^2 / NDF**
 - NDF
 - Forward / backward χ^2 deviation

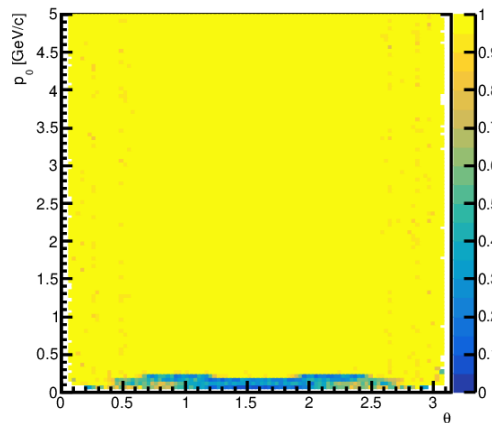
Reconstructed momentum vs true momentum



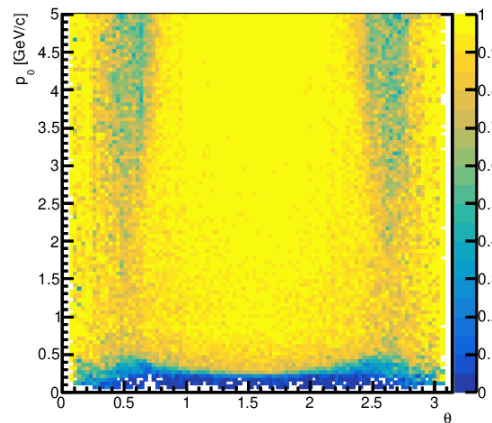
Efficiency of track quality cuts

$$\text{efficiency} = \frac{N \text{ of tracks after cut}}{N \text{ of tracks}}$$

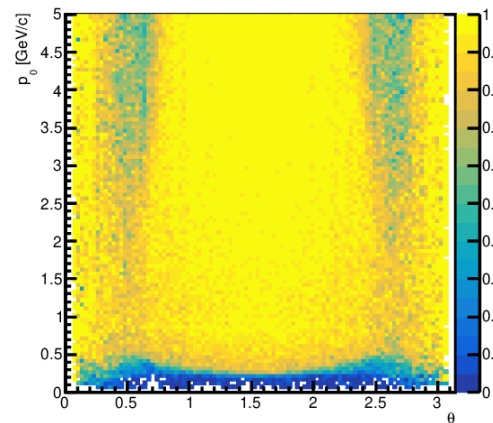
efficiency [!HasErrorMesg()]



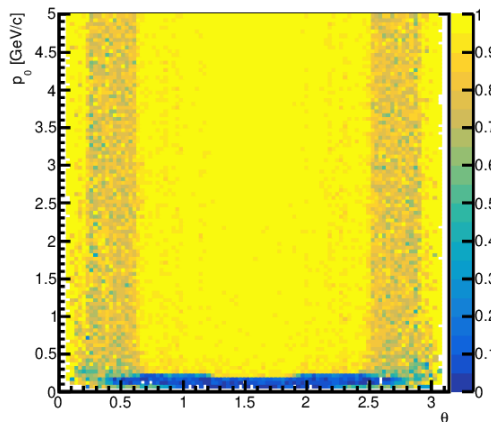
efficiency [fConvergencyGF = 1]



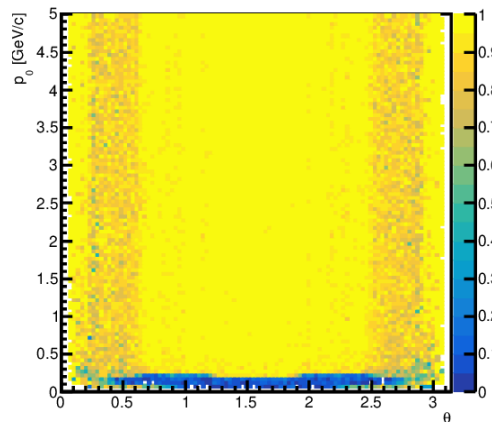
efficiency [fConvergencyGF = ±1]



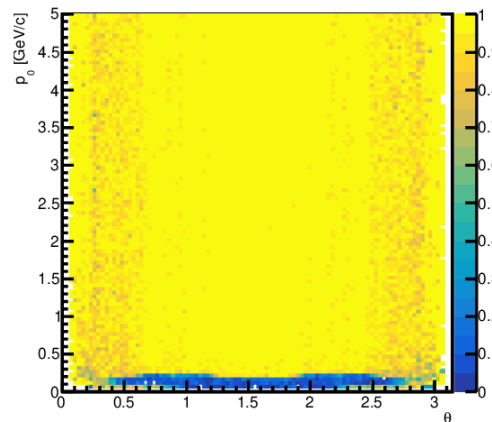
efficiency [$\chi^2/\text{ndf} < 2$]



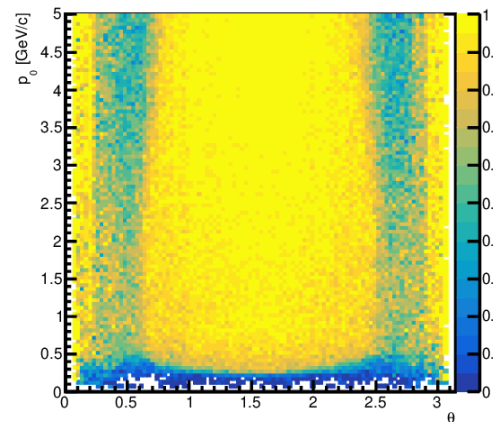
efficiency [$\chi^2/\text{ndf} < 4$]



efficiency [$\chi^2/\text{ndf} < 10$]

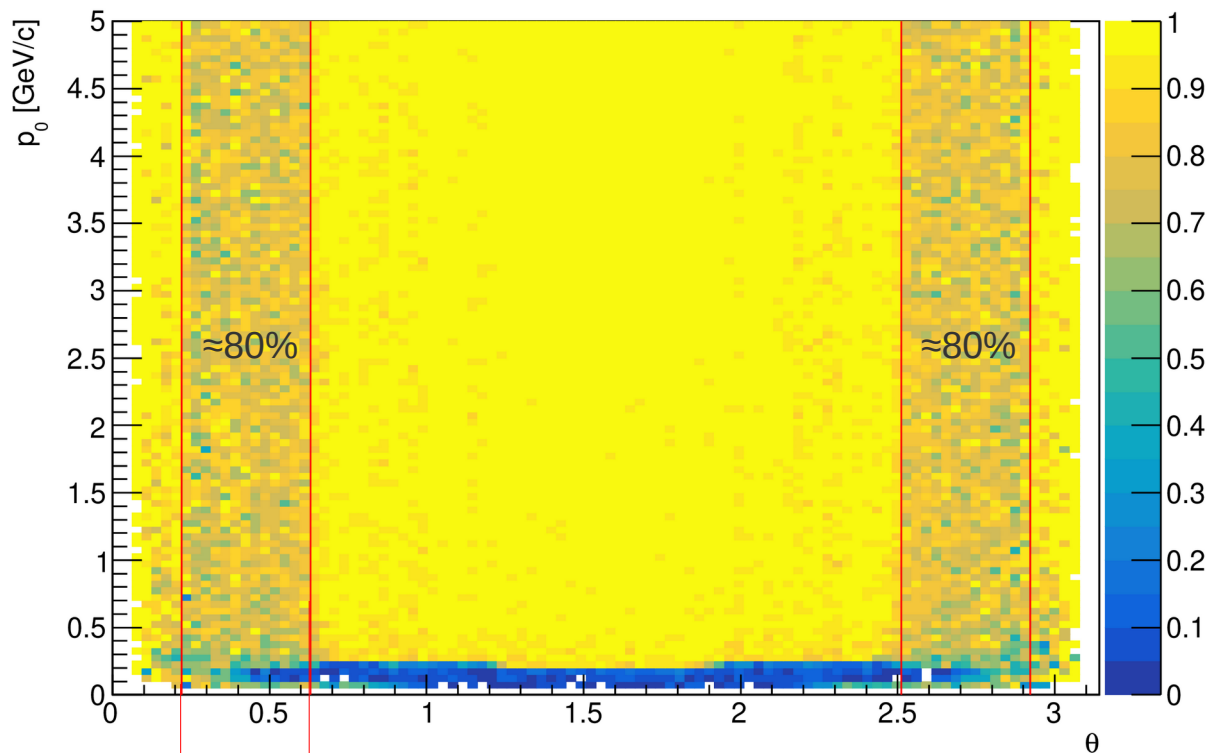


efficiency [all cuts]



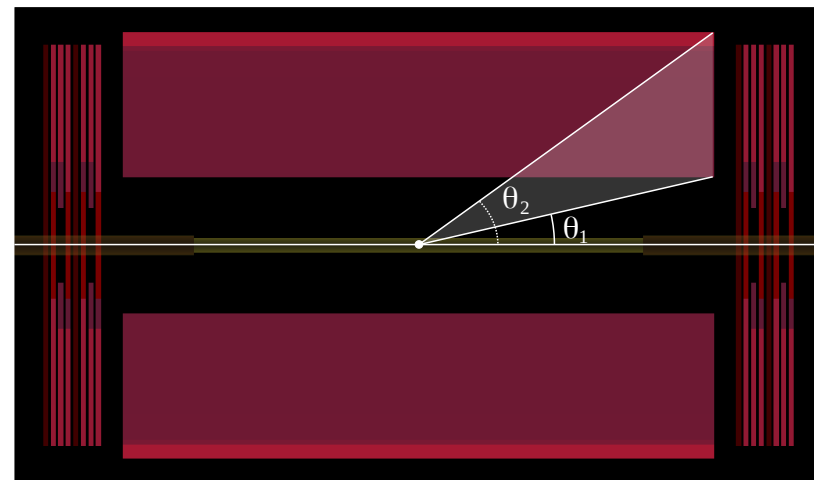
Efficiency of track quality cuts: χ^2/ndf

efficiency [$\chi^2/\text{ndf} < 2$]

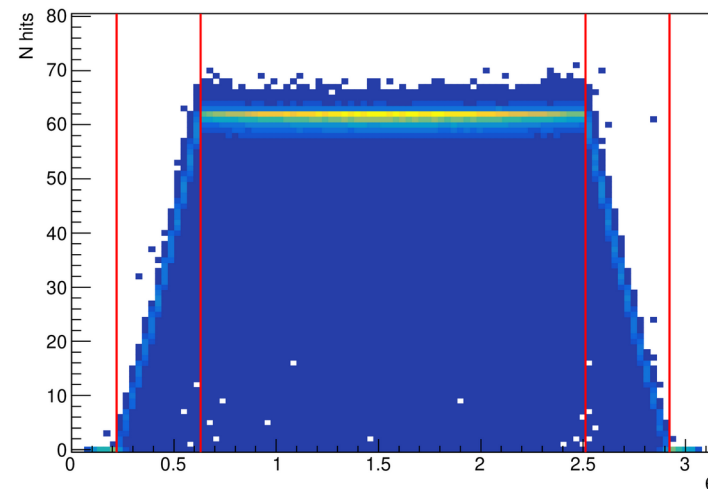


$$\theta_2 \approx 0.63 \text{ rad} \approx 36^\circ$$

$$\theta_1 \approx 0.22 \text{ rad} \approx 13^\circ$$

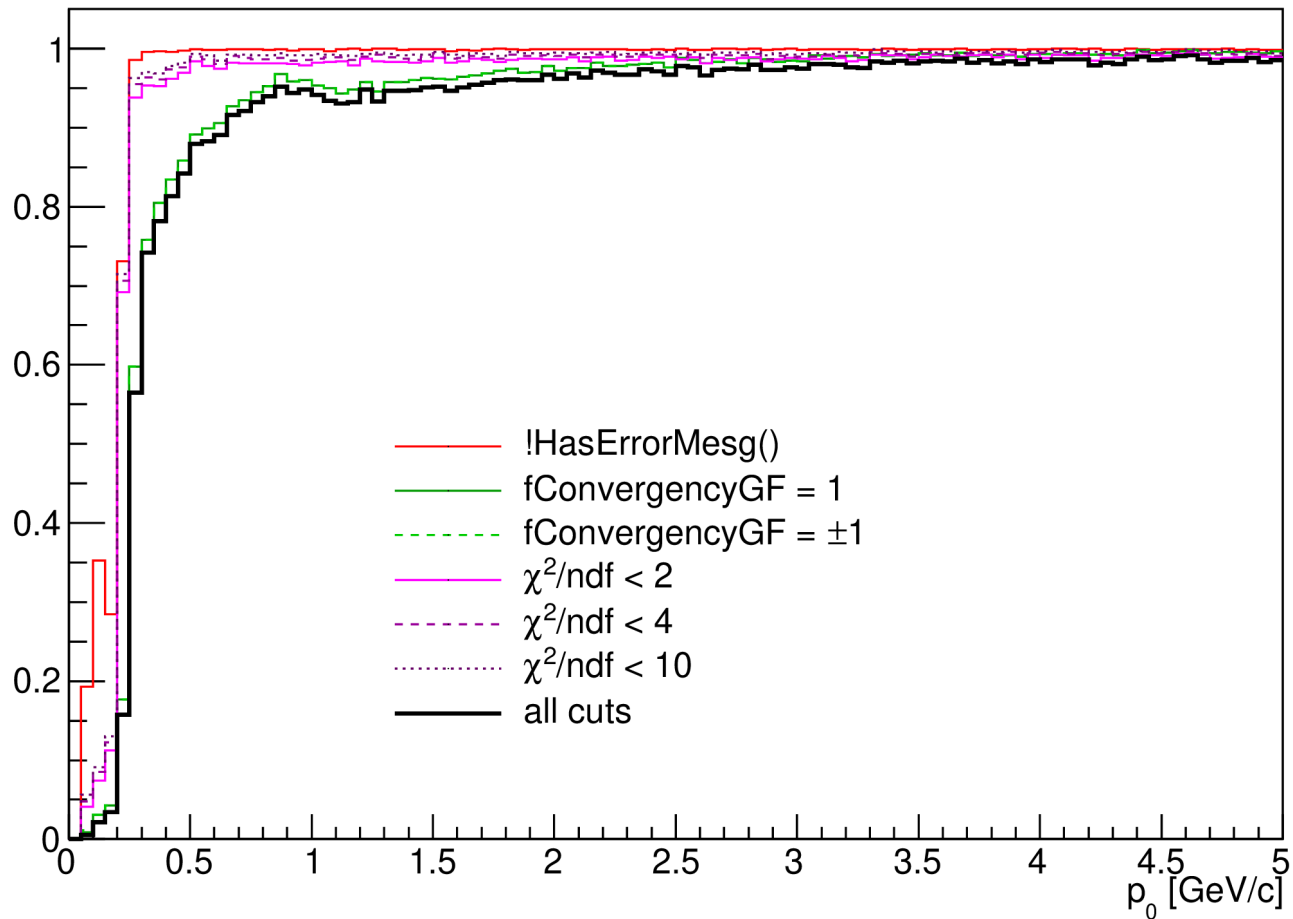


N hits TsB ($p_0 > 1 \text{ GeV}/c$)



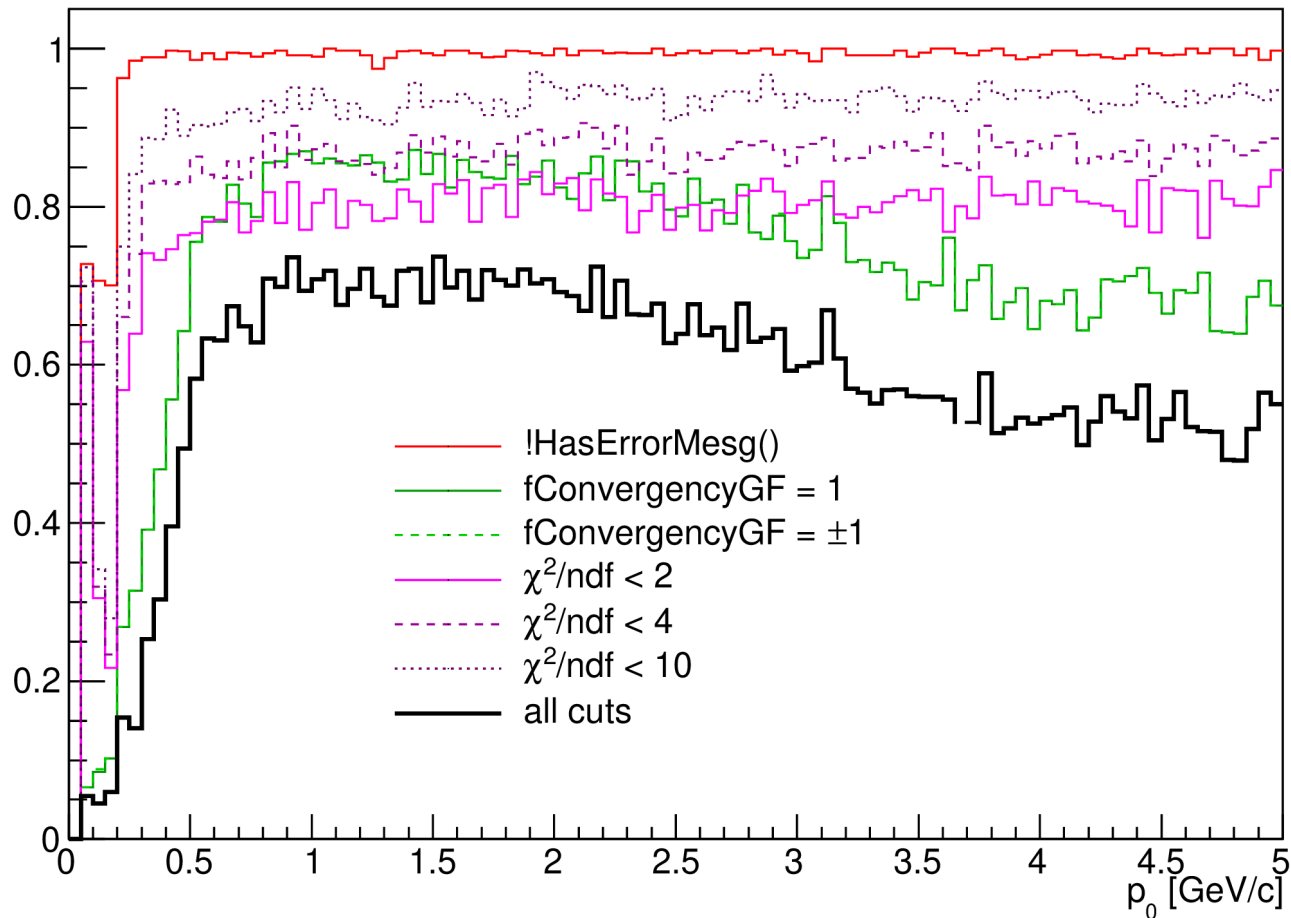
Efficiency of track quality cuts: $60^\circ < \theta < 120^\circ$

$60^\circ < \theta < 120^\circ$

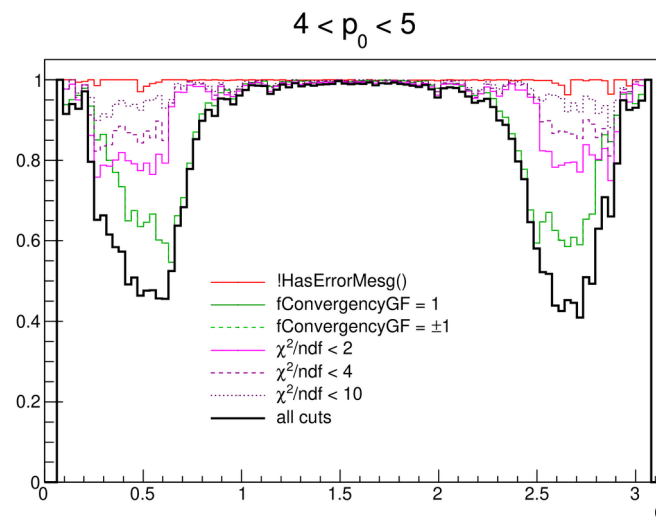
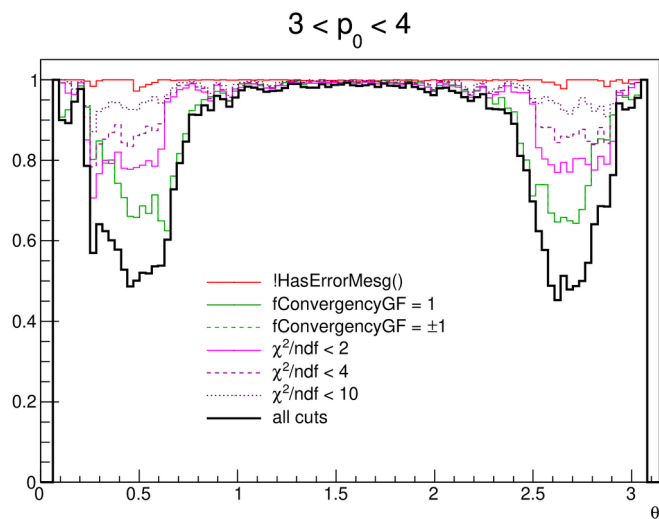
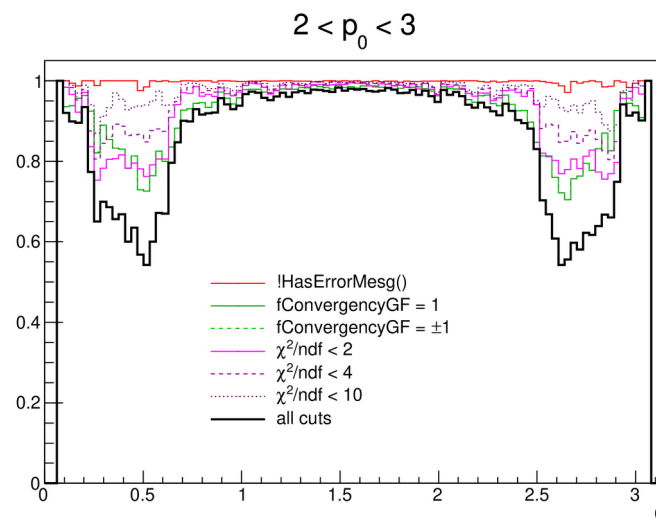
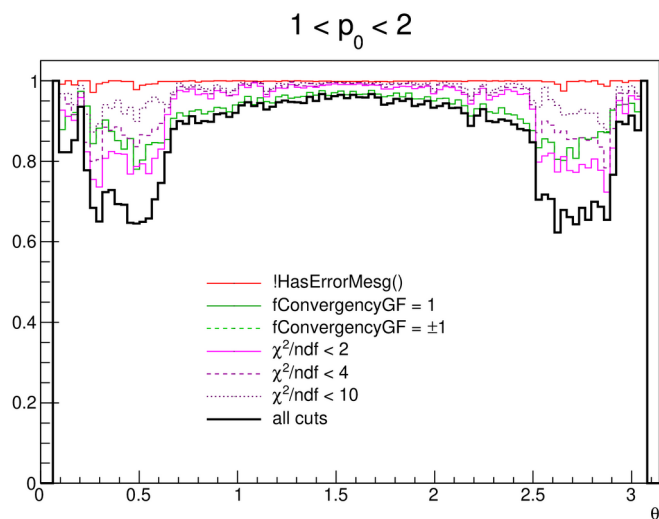


Efficiency of track quality cuts: $13^\circ < \theta < 36^\circ$

$13^\circ < \theta < 36^\circ$



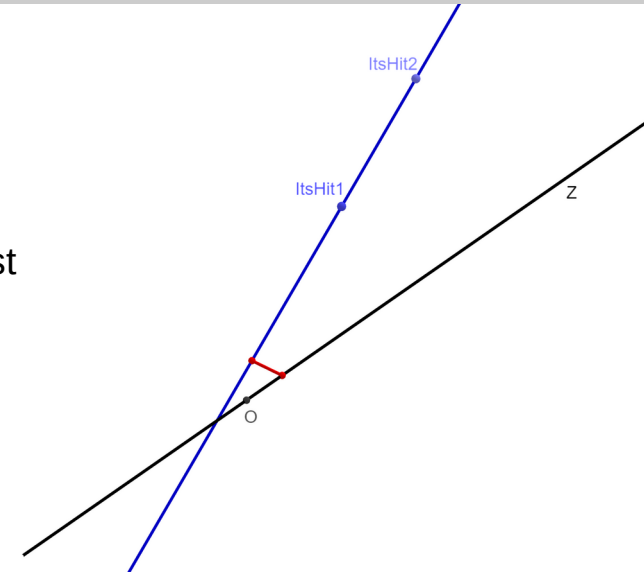
Efficiency of track quality cuts. Pions, $1 < p_0 < 5 \text{ GeV}/c$, $Z_{\text{prim.vtx.}} = 0$.



Initialisation procedure of the fit

Current initialisation procedure

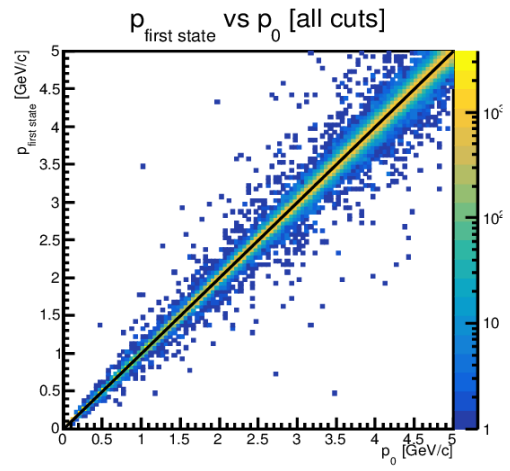
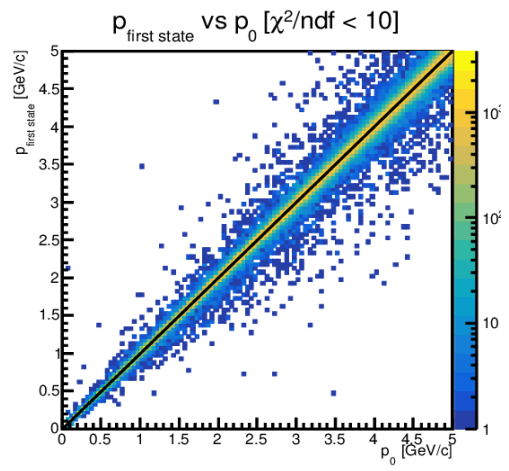
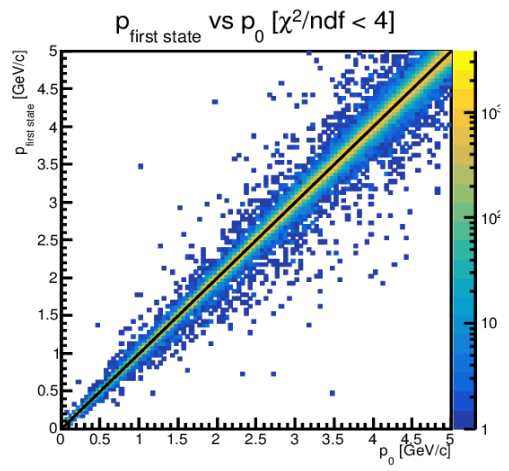
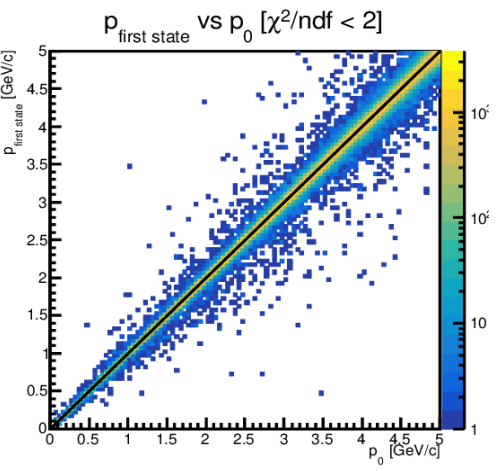
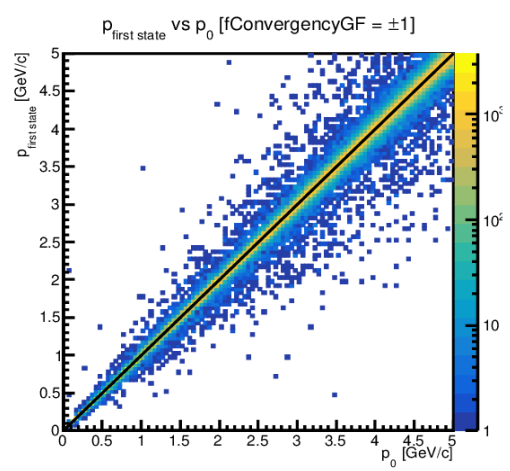
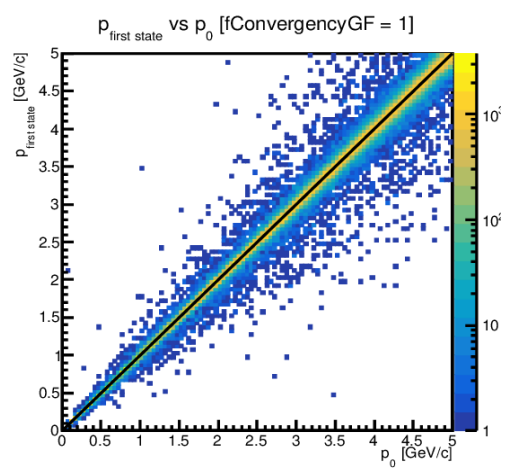
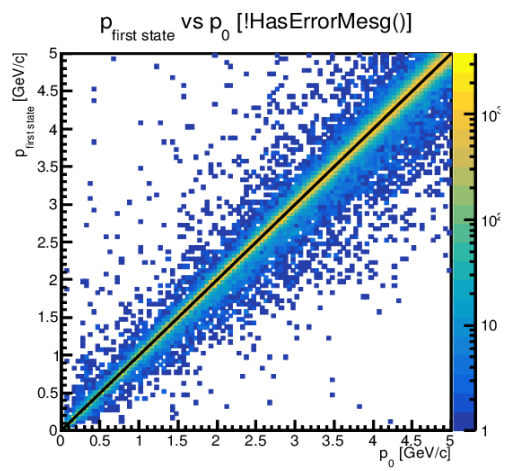
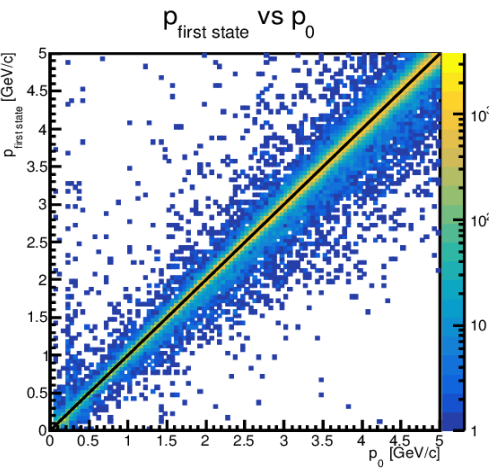
- $|p| \in [0.95; 1.05] \text{ GeV}/c$
- Momentum direction is defined from the first 2 hits in the inner tracker.
- As the vertex is taken some point on the segment connecting points of closest approach of Z axis and the line passing through the first 2 hits in the inner tracker.
- If this procedure fails (for example, if there are no hits in ITS), then program fallbacks to the second, simpler, method: $\vec{p} = (0, 0, 1) \text{ GeV}/c$, vertex = (0,0,0) with some smearing applied.



Initialisation from MC values

- It has been suggested, that the problem with convergency is caused by the bad initialisation procedure.
- To check this, we apply initialisation procedure, where initial values of momentum and position for the track fit are set **equal to the MC** values of initial momentum and production vertex of the particle.

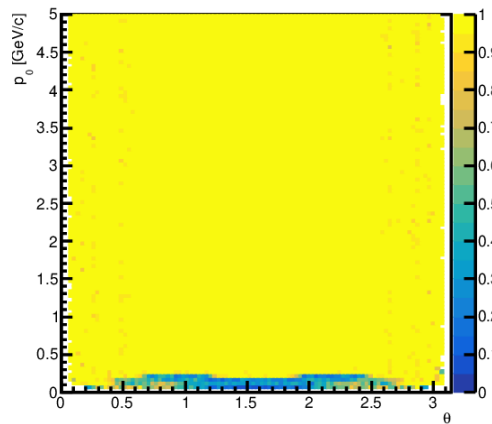
Reco momentum vs true momentum. Init. values = MC



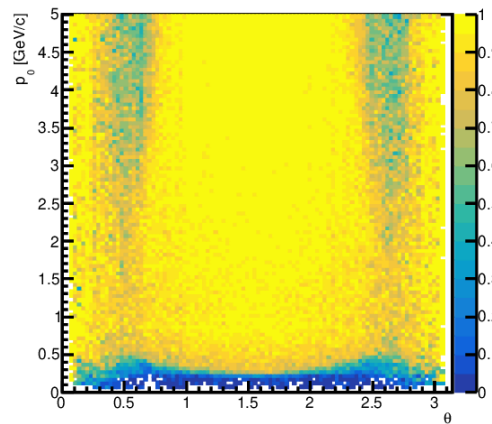
Efficiency of track quality cuts

current
initialisation
procedure

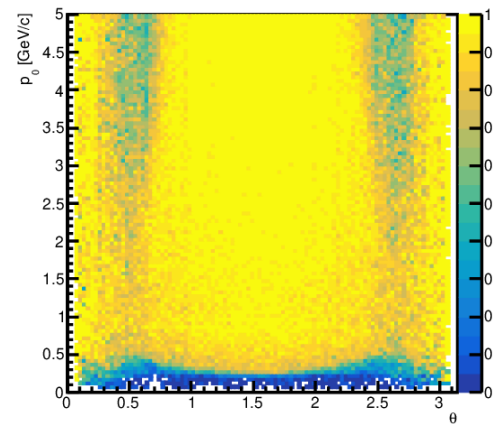
efficiency [`!HasErrorMesg()`]



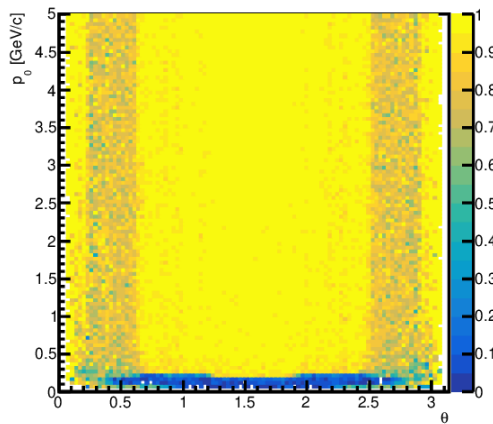
efficiency [`fConvergencyGF = 1`]



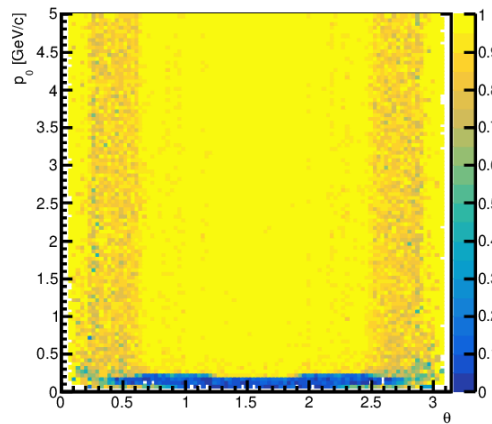
efficiency [`fConvergencyGF = ±1`]



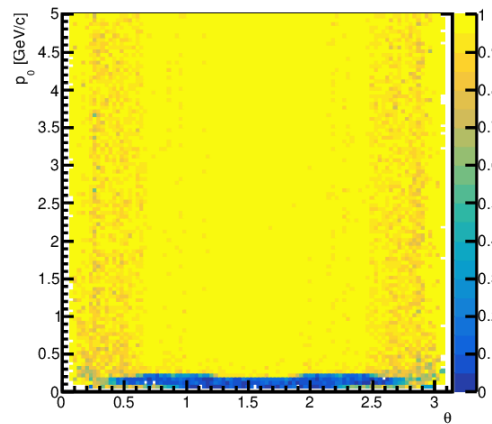
efficiency [$\chi^2/\text{ndf} < 2$]



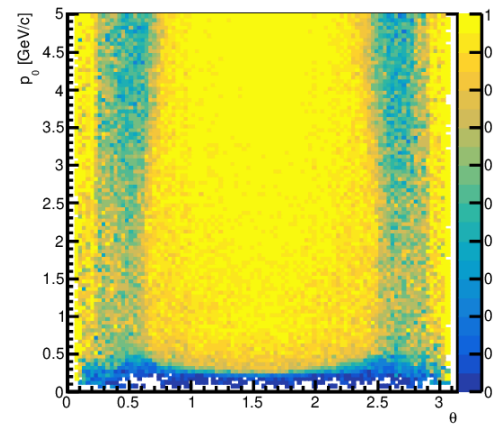
efficiency [$\chi^2/\text{ndf} < 4$]



efficiency [$\chi^2/\text{ndf} < 10$]



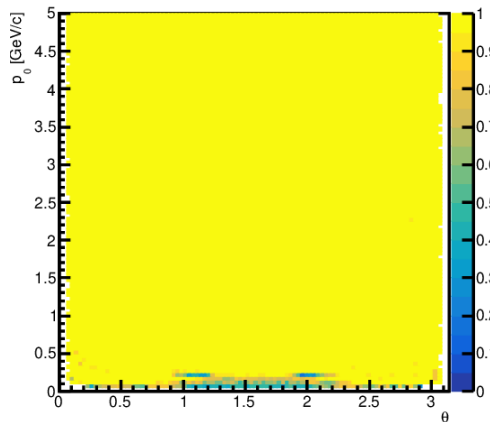
efficiency [all cuts]



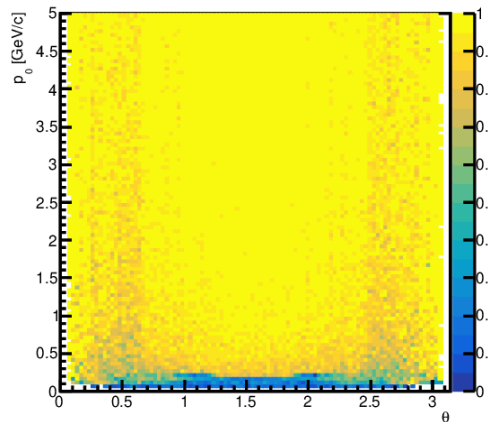
Efficiency of track quality cuts. Init. values = MC

initial values
from MC

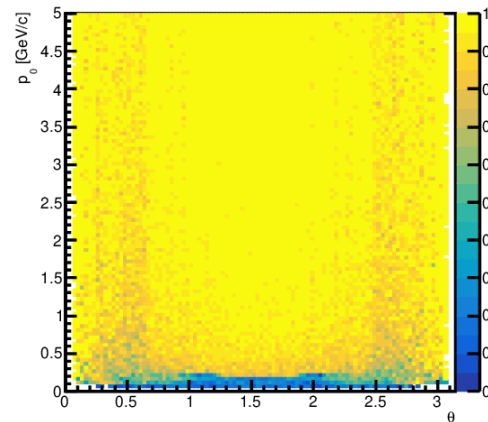
efficiency [!HasErrorMesg()]



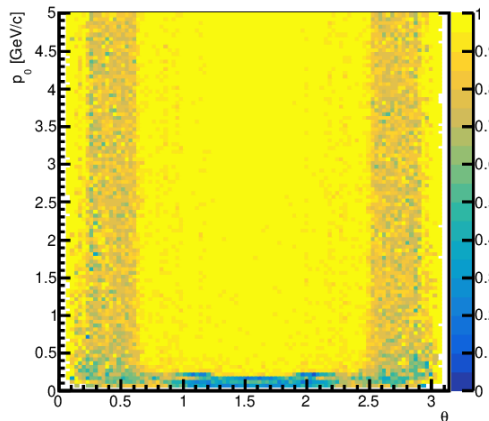
efficiency [fConvergencyGF = 1]



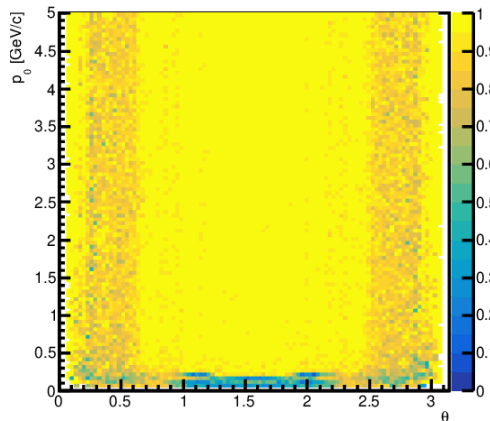
efficiency [fConvergencyGF = ±1]



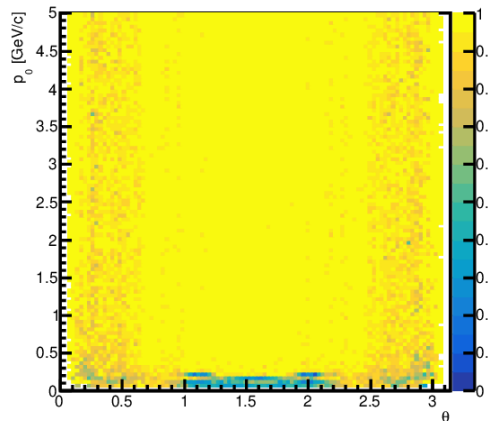
efficiency [$\chi^2/\text{ndf} < 2$]



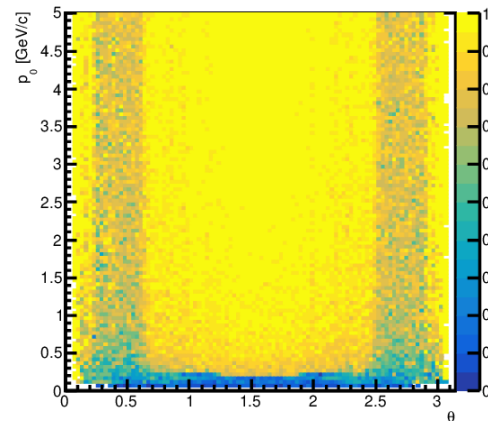
efficiency [$\chi^2/\text{ndf} < 4$]



efficiency [$\chi^2/\text{ndf} < 10$]

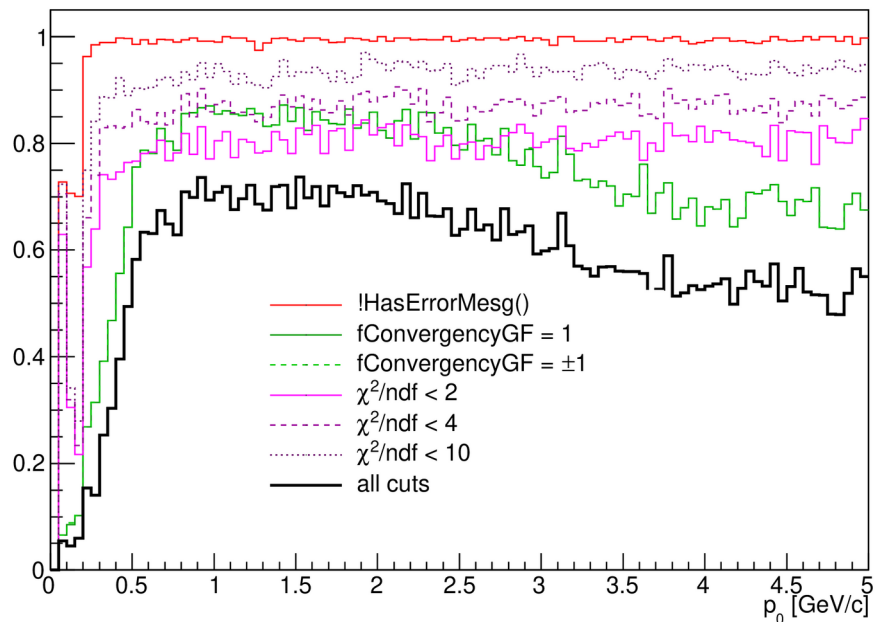


efficiency [all cuts]



Efficiency of track quality cuts: $13^\circ < \theta < 36^\circ$

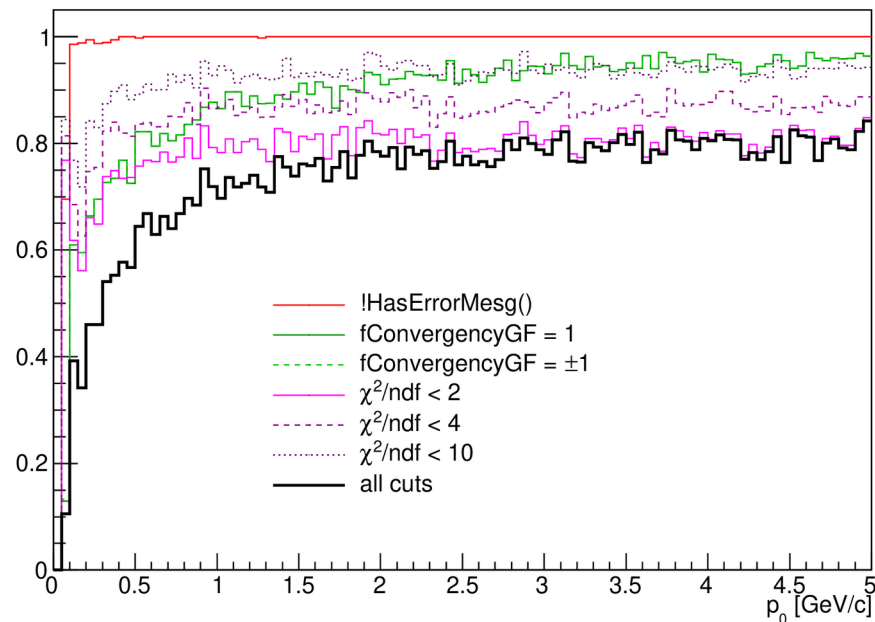
$13^\circ < \theta < 36^\circ$



current initialisation procedure



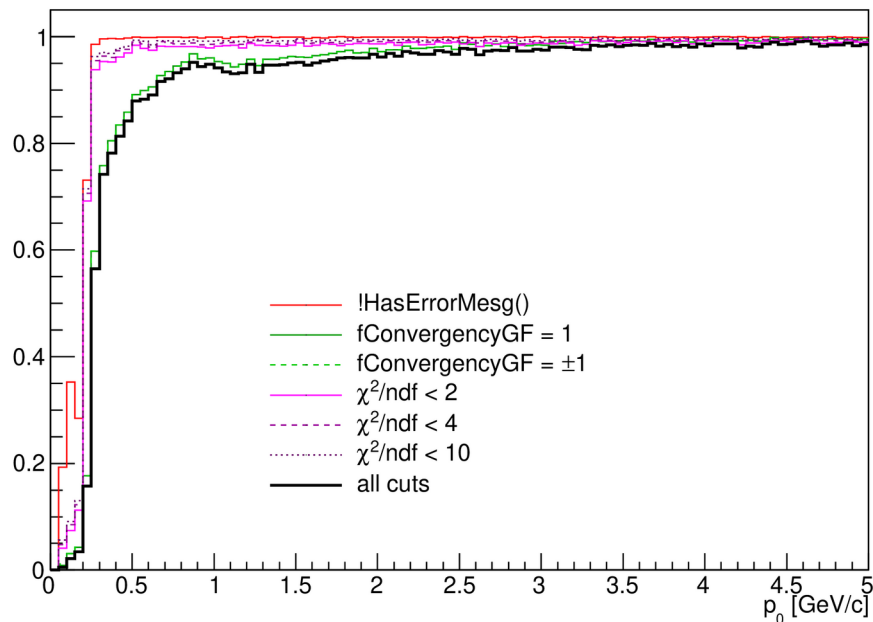
$13^\circ < \theta < 36^\circ$



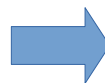
initial values from MC

Efficiency of track quality cuts: $60^\circ < \theta < 120^\circ$

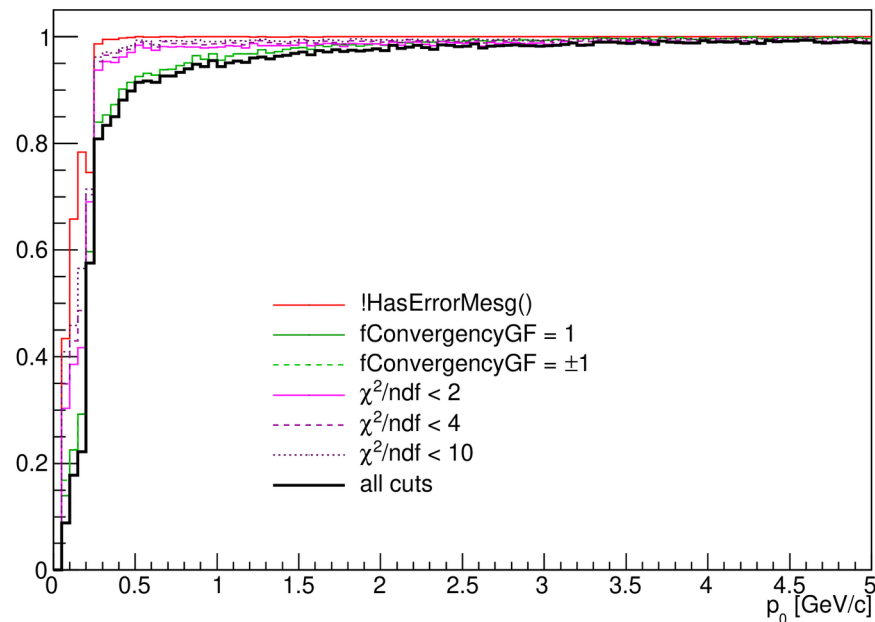
$60^\circ < \theta < 120^\circ$



current initialisation procedure

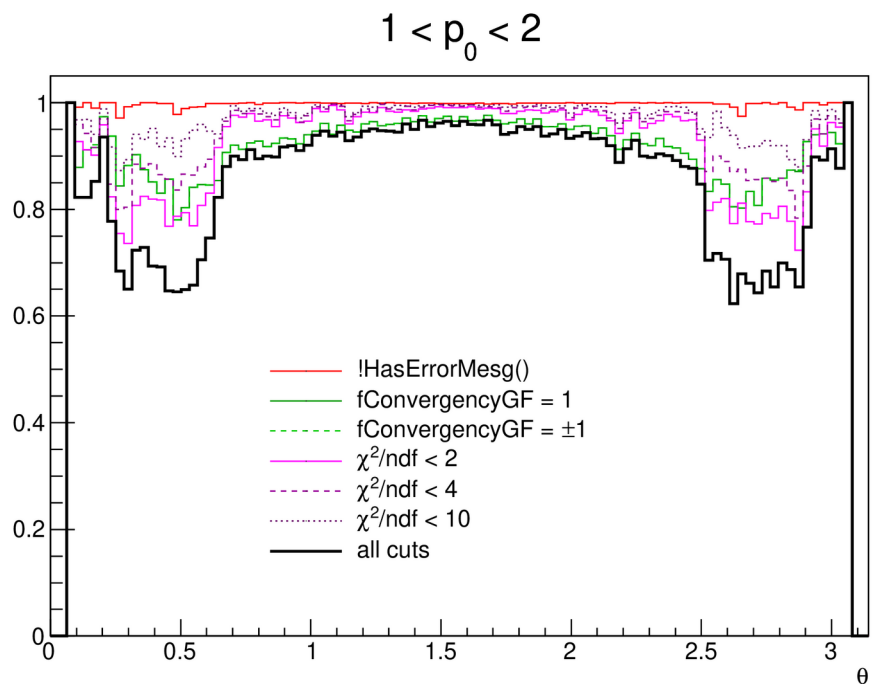


$60^\circ < \theta < 120^\circ$

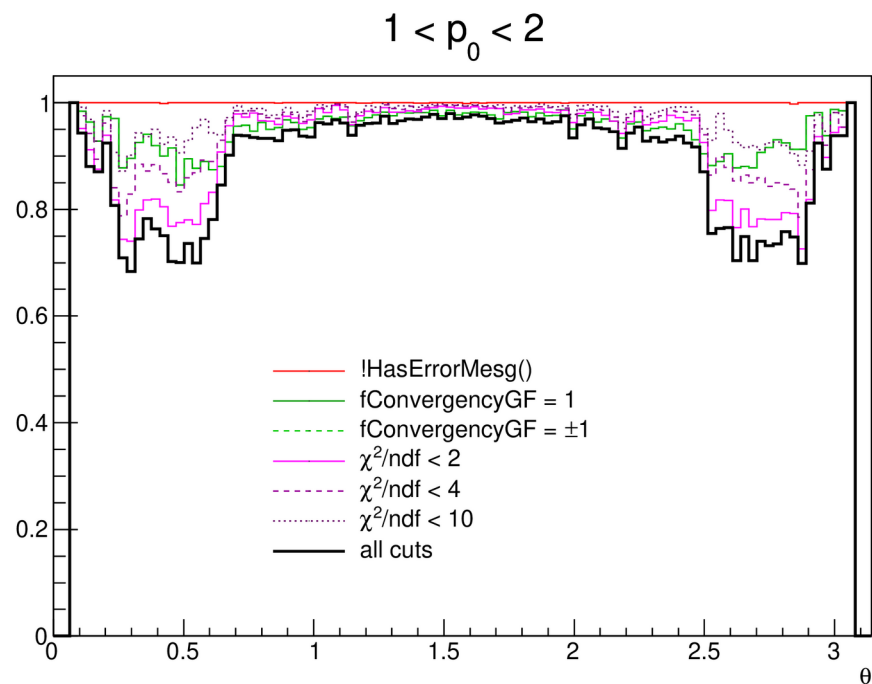


initial values from MC

Efficiency of track quality cuts. Pions, $1 < p_0 < 2 \text{ GeV}/c$, $Z_{\text{prim.vtx.}} = 0$.

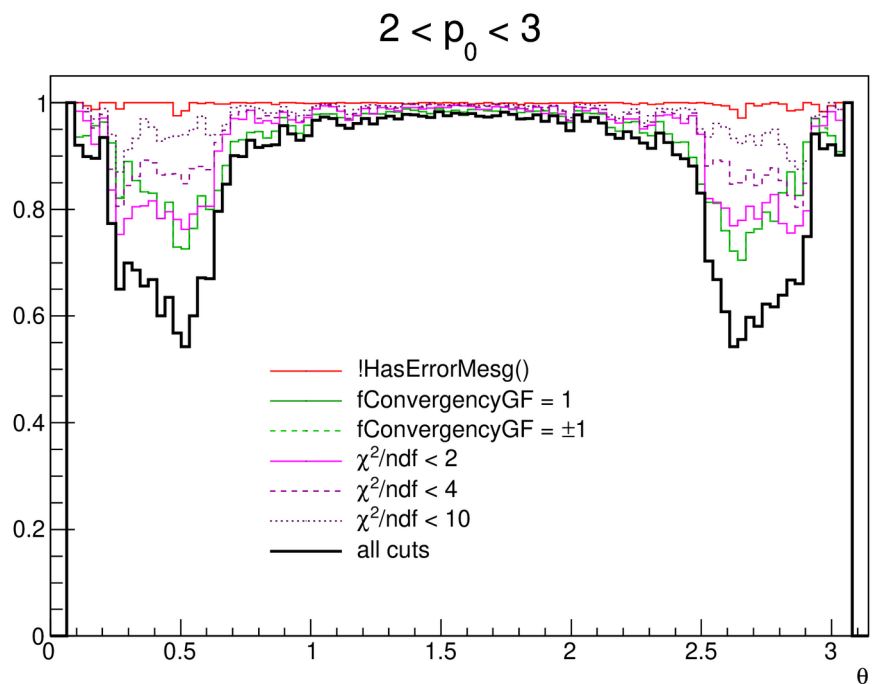


current initialisation procedure

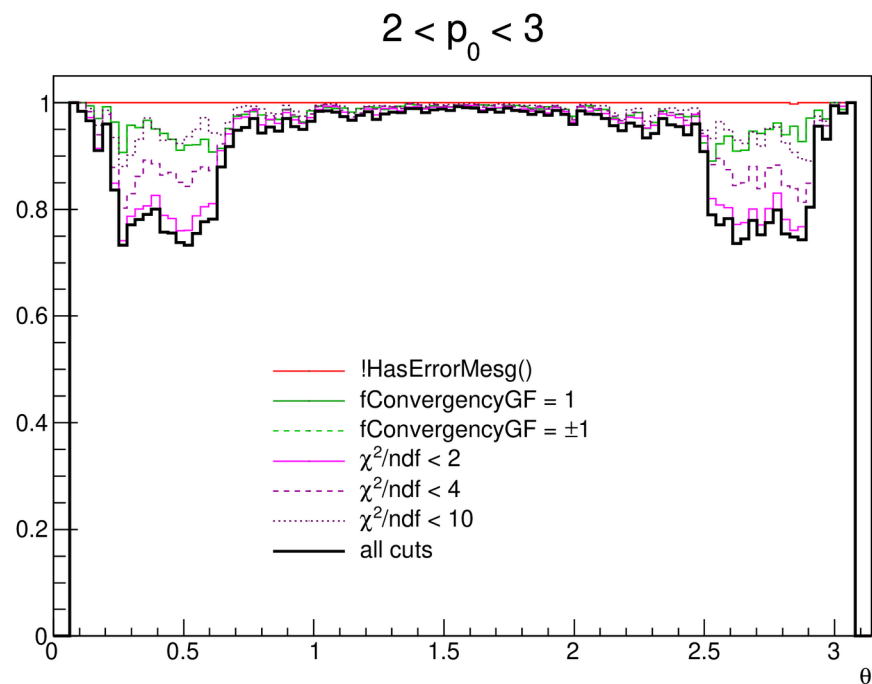


initial values from MC

Efficiency of track quality cuts. Pions, $2 < p_0 < 3 \text{ GeV}/c$, $Z_{\text{prim.vtx.}} = 0$.

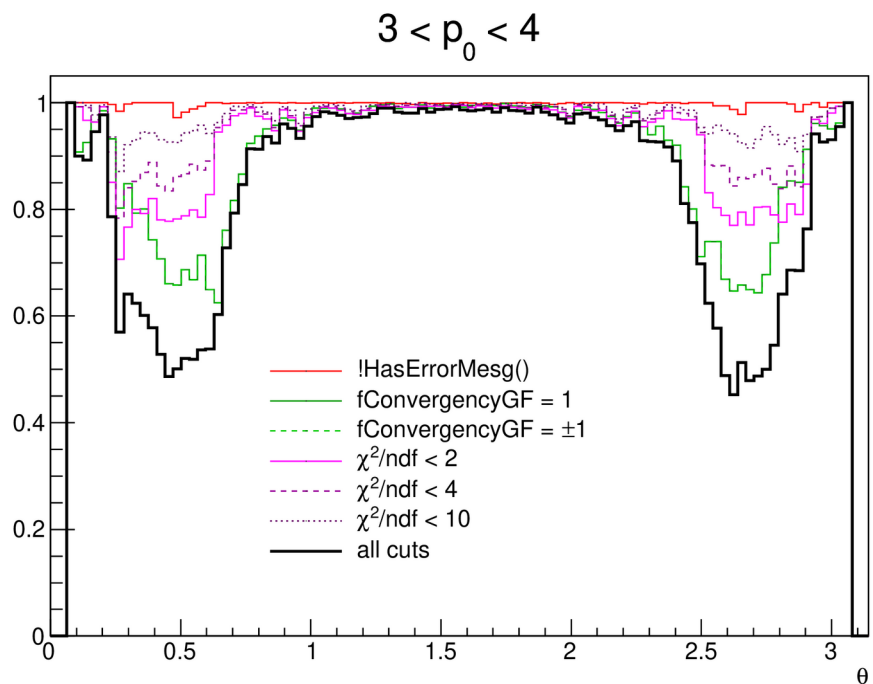


current initialisation procedure

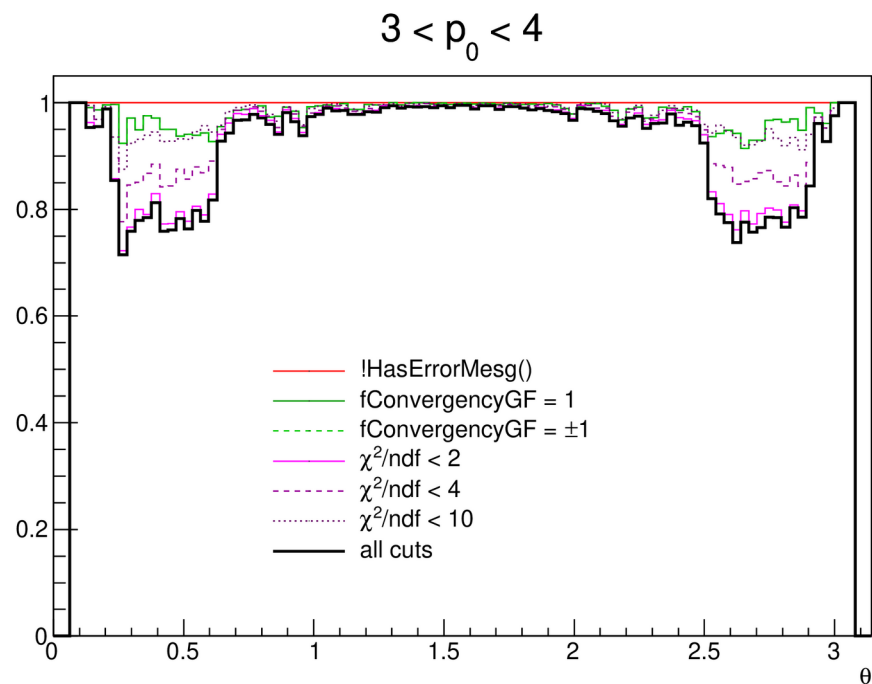


initial values from MC

Efficiency of track quality cuts. Pions, $3 < p_0 < 4 \text{ GeV}/c$, $Z_{\text{prim.vtx.}} = 0$.

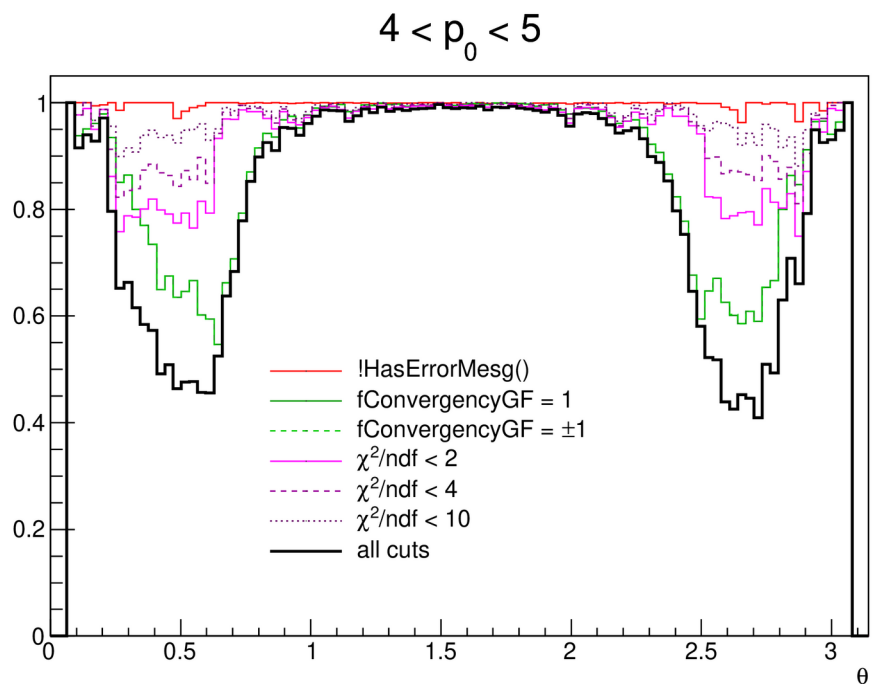


current initialisation procedure

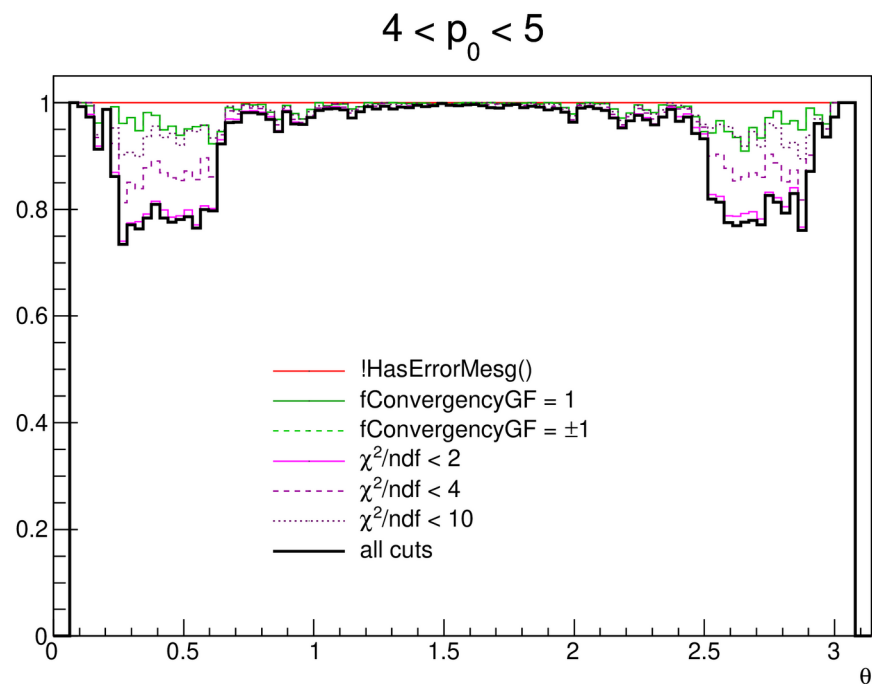


initial values from MC

Efficiency of track quality cuts. Pions, $4 < p_0 < 5 \text{ GeV}/c$, $Z_{\text{prim.vtx.}} = 0$.



current initialisation procedure



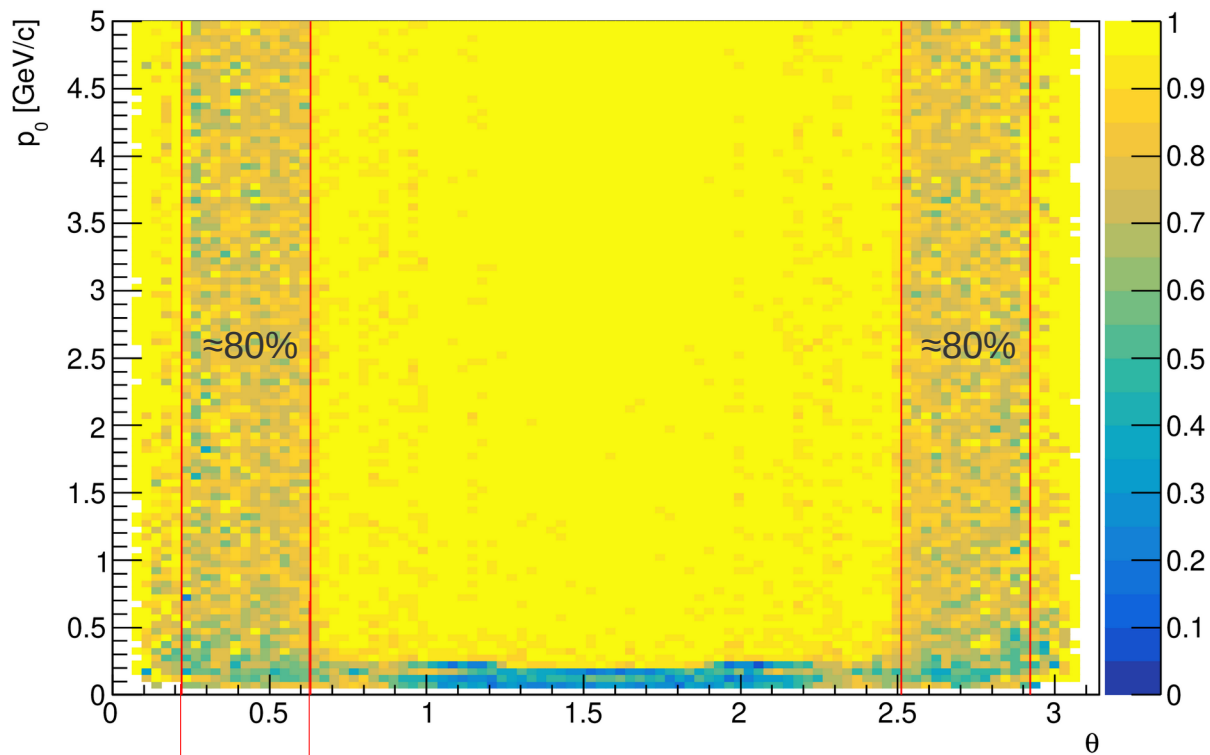
initial values from MC

Conclusions on the initialisation procedure

- Problem with convergency at high momenta was caused by a bad choice of initial track parameters.
- **We need a better initialisation procedure!**
- During the discussions at the weekly meetings, it was proposed to use as the initial values MC values with some smearing applied.
- χ^2/ndf distribution (at high momenta) is little affected by changing the initialisation procedure.

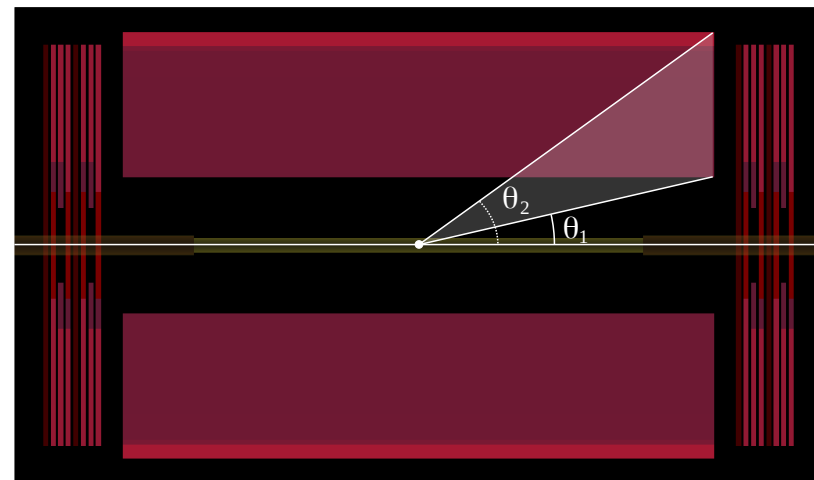
Efficiency of track quality cuts: χ^2/ndf

efficiency [$\chi^2/\text{ndf} < 2$]

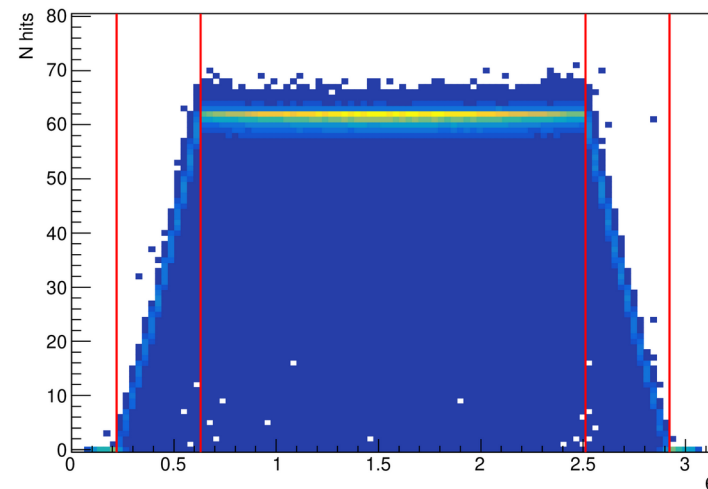


$$\theta_2 \approx 0.63 \text{ rad} \approx 36^\circ$$

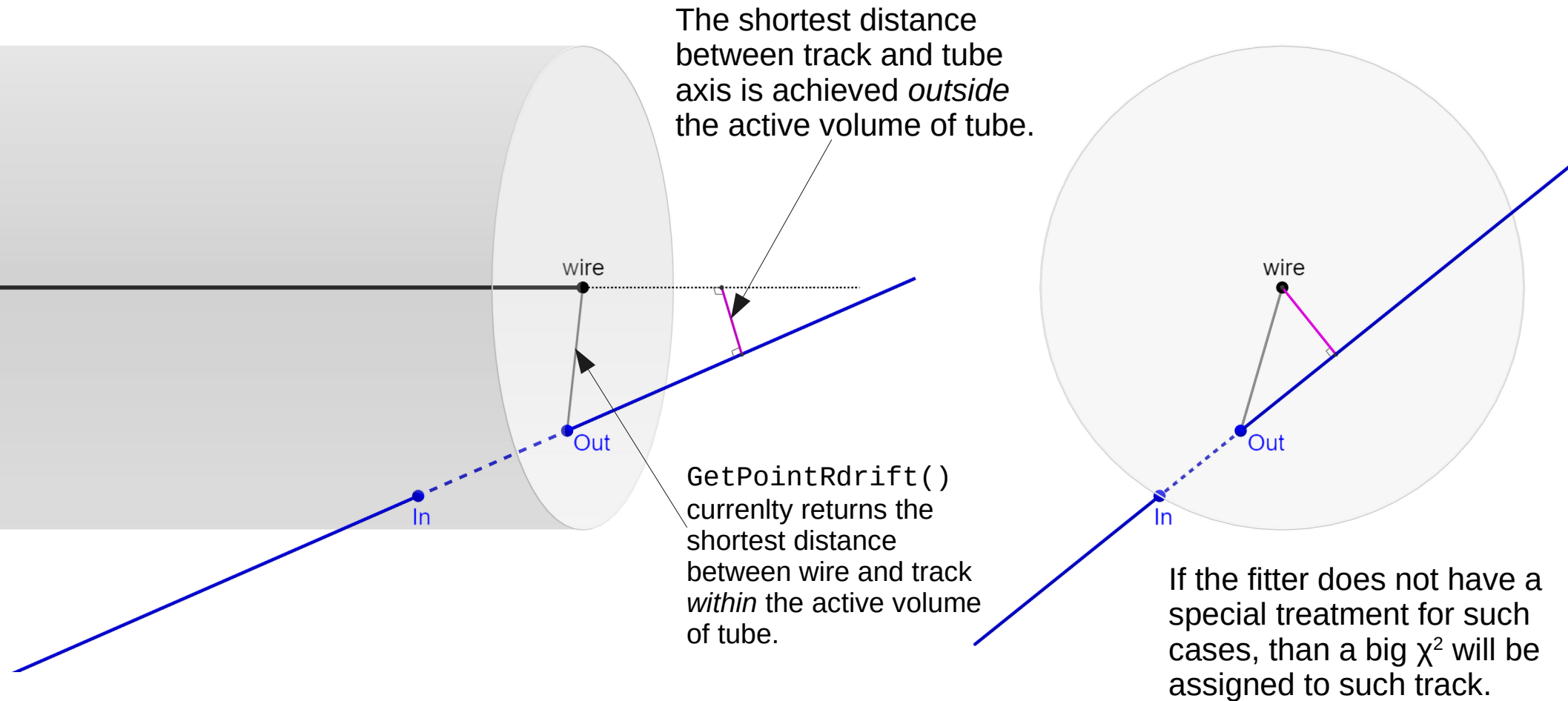
$$\theta_1 \approx 0.22 \text{ rad} \approx 13^\circ$$



N hits TsB ($p_0 > 1$ GeV/c)



Tracks passing through the end of the tube

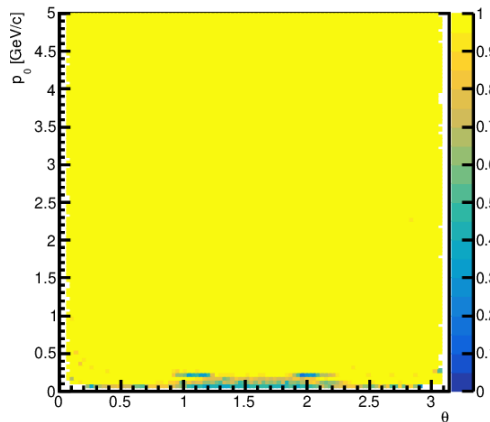


Efficiency of track quality cuts. "Ideal" Rdrift

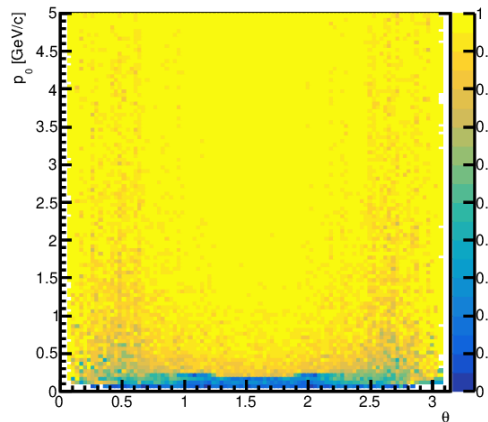
initial values
from MC

"ideal" Rdrift
(ignoring active volume
bounds)

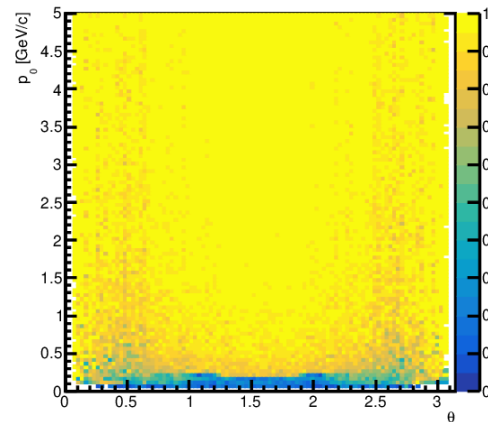
efficiency [`!HasErrorMesg()`]



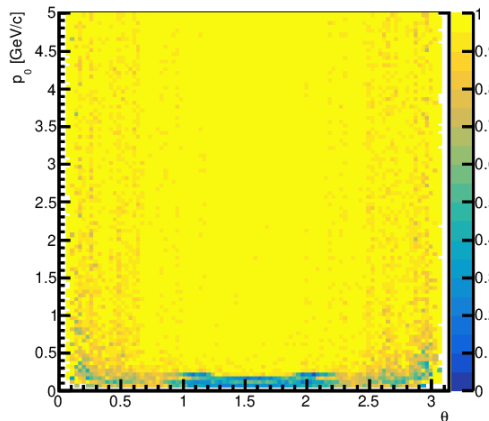
efficiency [`fConvergencyGF = 1`]



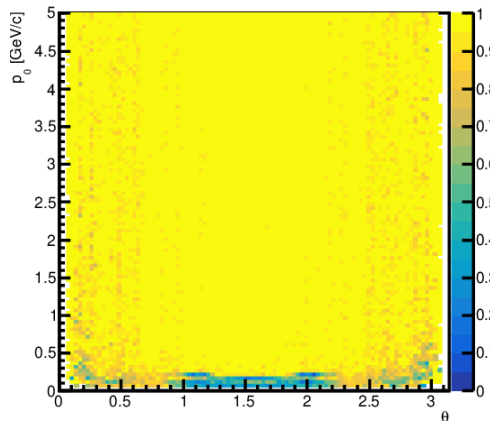
efficiency [`fConvergencyGF = ±1`]



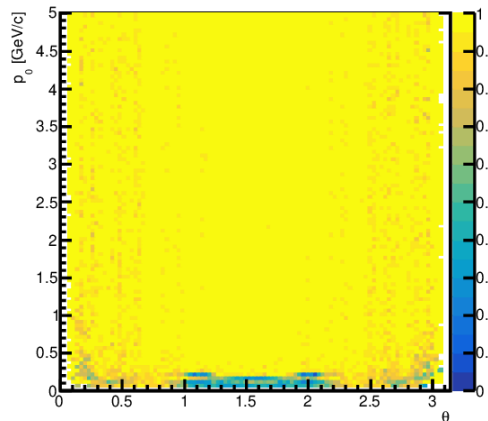
efficiency [`χ²/ndf < 2`]



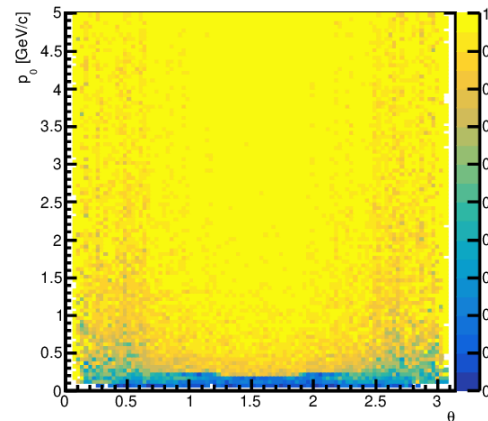
efficiency [`χ²/ndf < 4`]



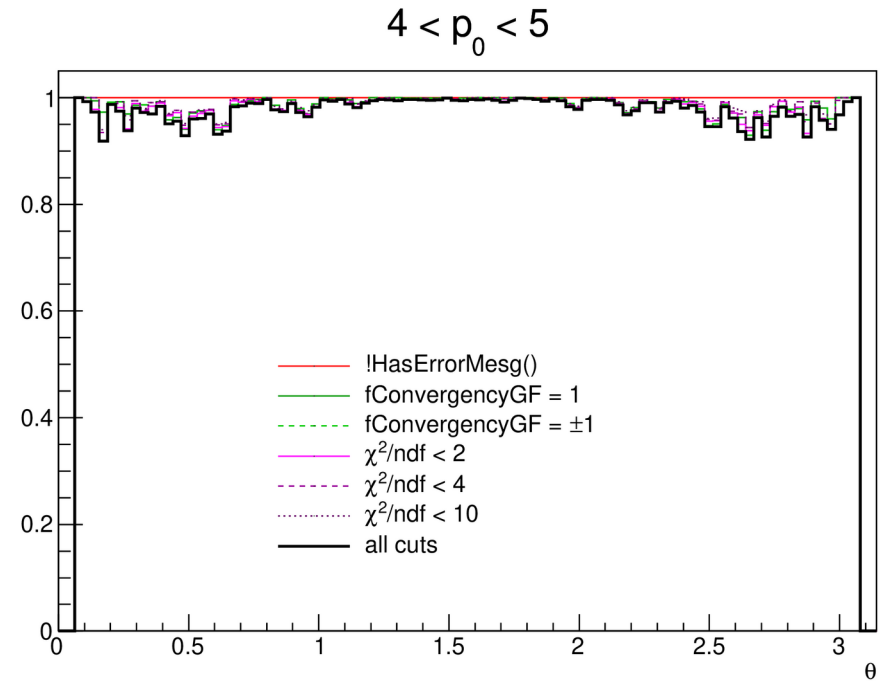
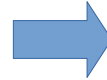
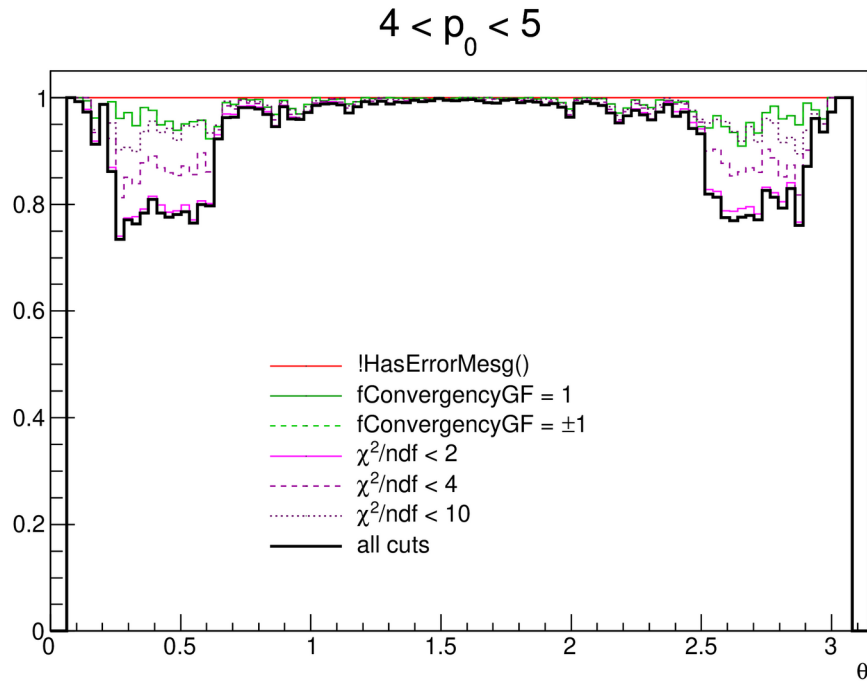
efficiency [`χ²/ndf < 10`]



efficiency [all cuts]



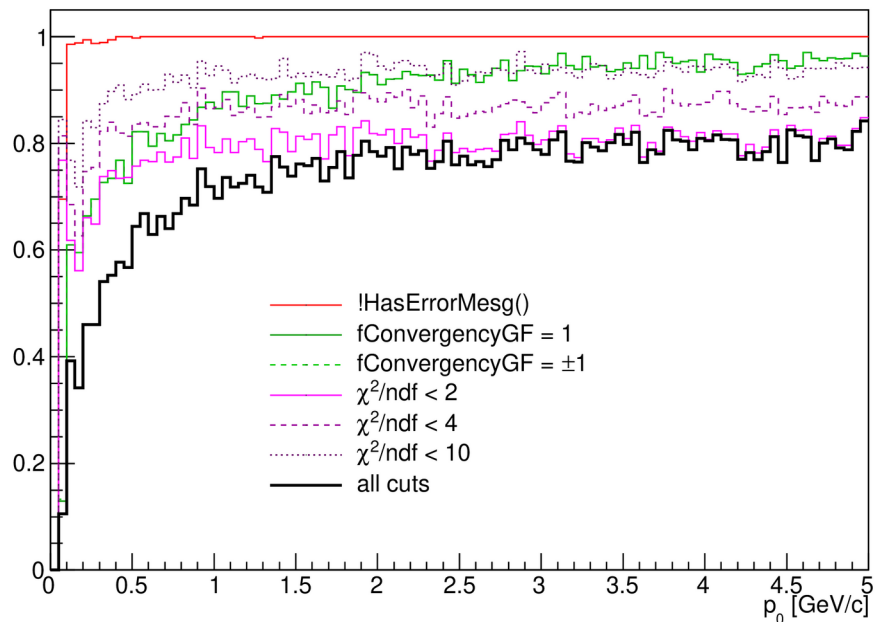
Efficiency of track quality cuts: $4 < p_0 < 5 \text{ GeV}/c$



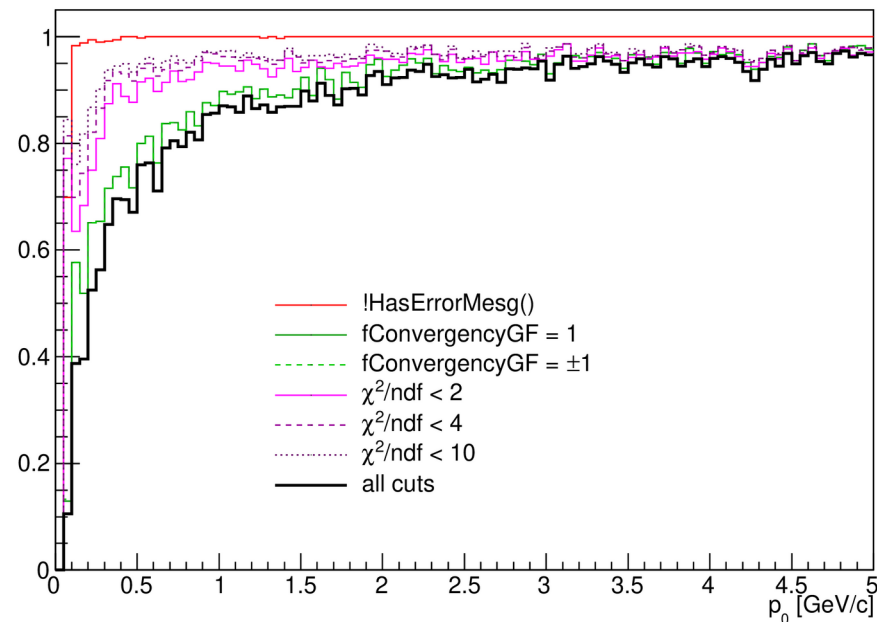
ignore active volume bounds
in R drift calculation

Efficiency of track quality cuts: $13^\circ < \theta < 36^\circ$

$13^\circ < \theta < 36^\circ$



$13^\circ < \theta < 36^\circ$



ignore active volume bounds
in R drift calculation

Material effects

- To confirm that smaller efficiency of the track fit quality cuts at low momenta is due to material effects the following changes to simulation are applied:
 - Pipe is removed.
 - Material of the top volume is set to **vacuum**.
 - Materials of the inner tracker and the straw tracker are set to **vacuum**.

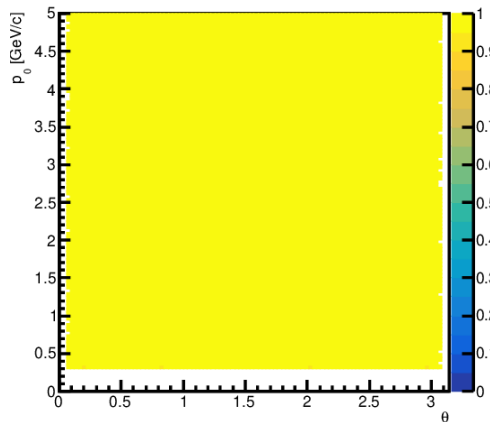
Efficiency of track quality cuts. No material.

initial values
from MC

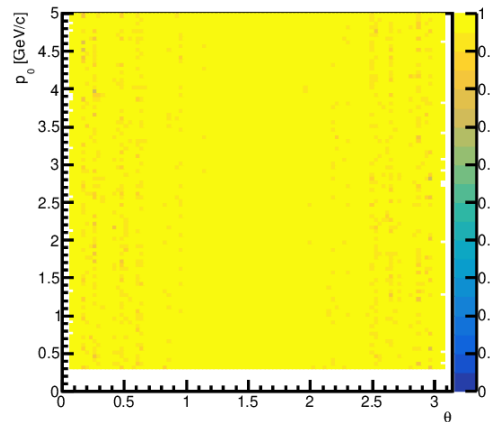
"ideal" Rdrift

no material

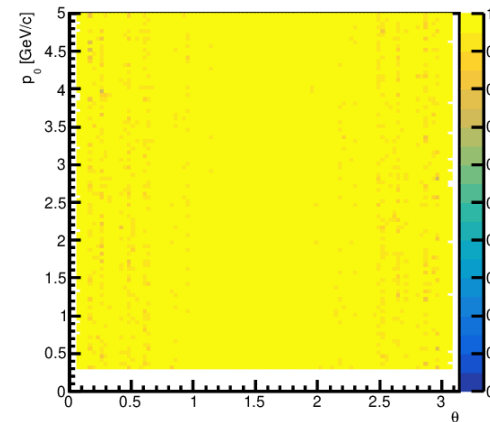
efficiency [!HasErrorMesg()]



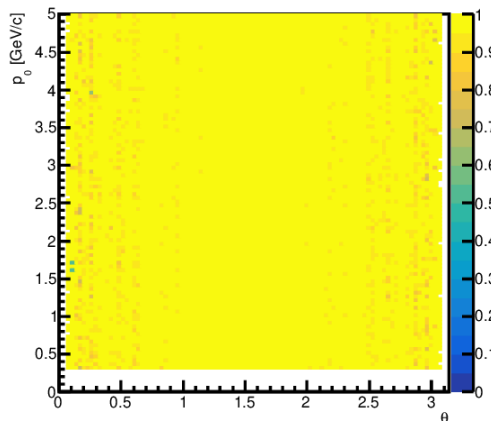
efficiency [fConvergencyGF = 1]



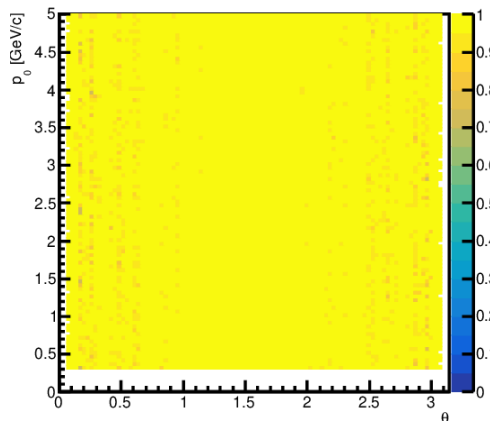
efficiency [fConvergencyGF = ±1]



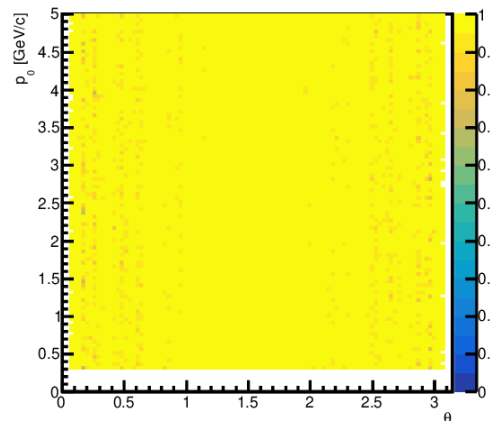
efficiency [$\chi^2/\text{ndf} < 2$]



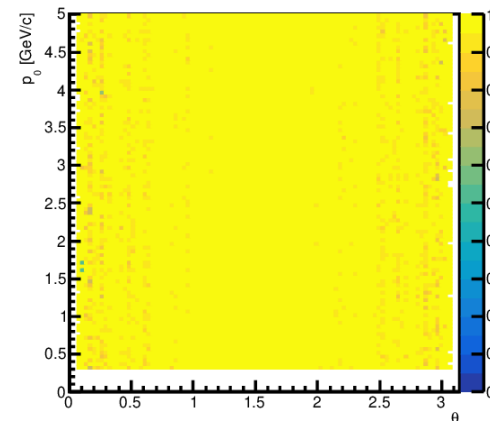
efficiency [$\chi^2/\text{ndf} < 4$]



efficiency [$\chi^2/\text{ndf} < 10$]

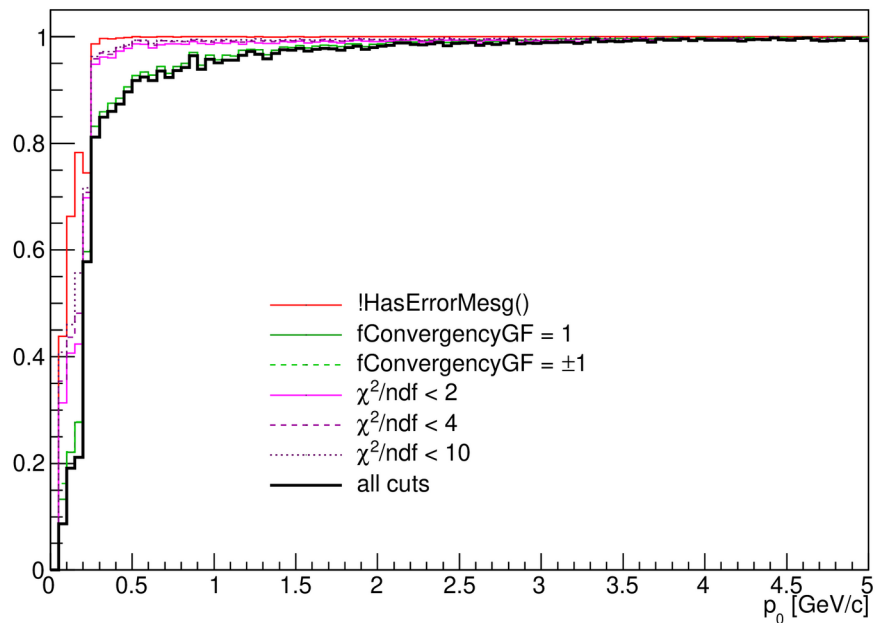


efficiency [all cuts]

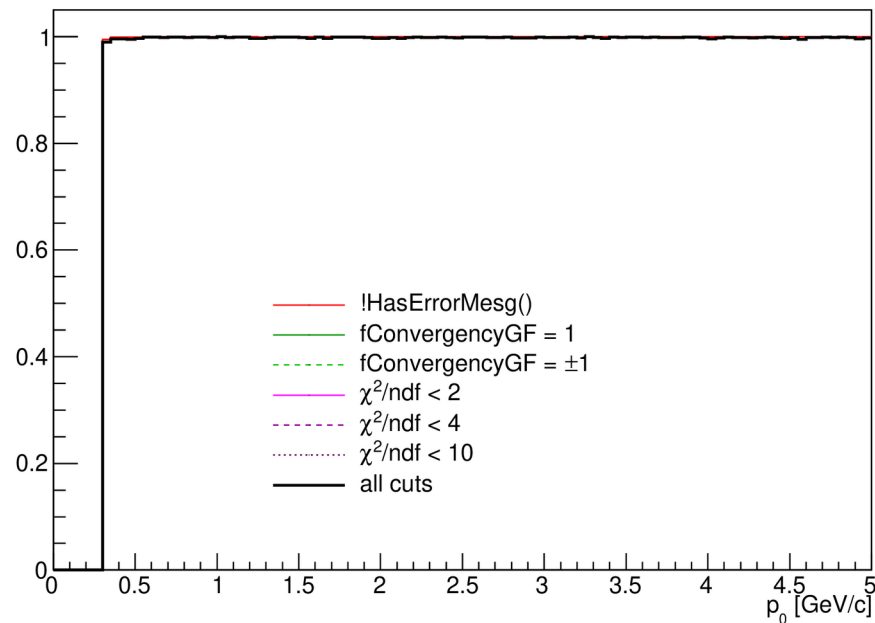


Efficiency of track quality cuts: $60^\circ < \theta < 120^\circ$

$60^\circ < \theta < 120^\circ$



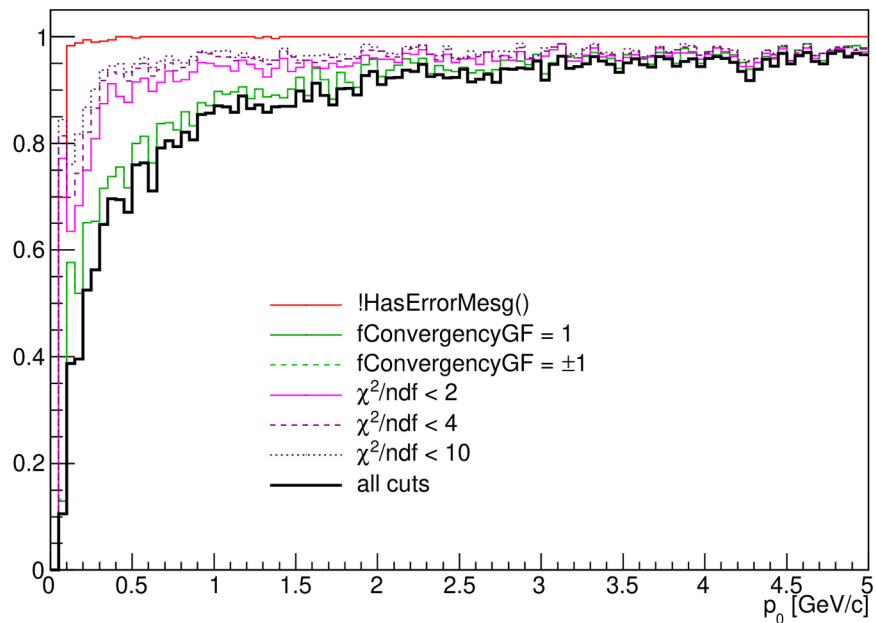
$60^\circ < \theta < 120^\circ$



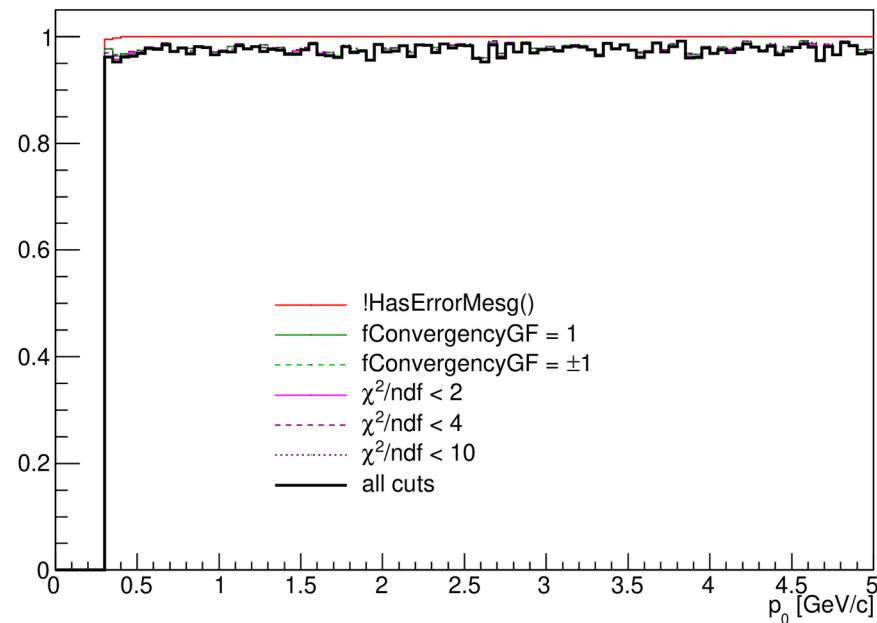
no material

Efficiency of track quality cuts: $13^\circ < \theta < 36^\circ$

$13^\circ < \theta < 36^\circ$



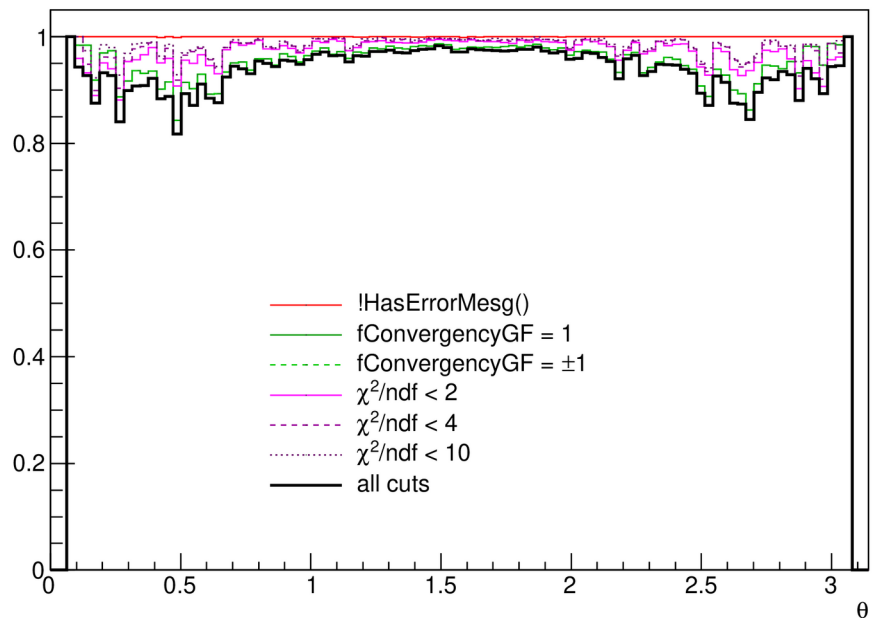
$13^\circ < \theta < 36^\circ$



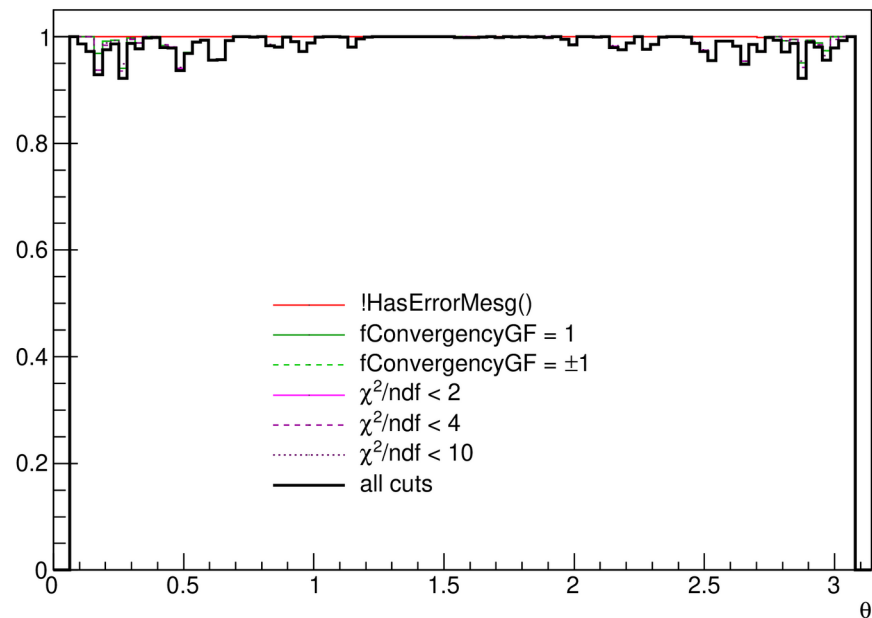
no material

Efficiency of track quality cuts: $1 < p_0 < 2$ GeV/c

$1 < p_0 < 2$



$1 < p_0 < 2$



no material

Conclusions

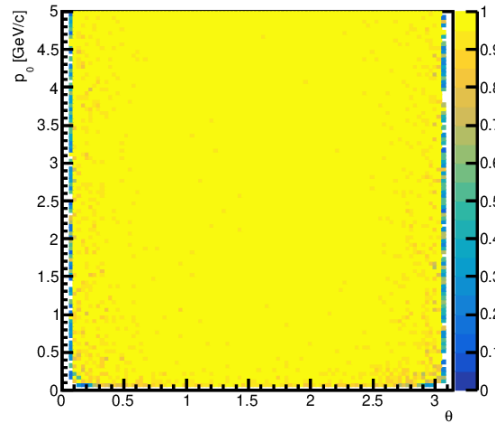
- Track fitting performance in SpdRoot is understood almost completely.
- Problem with convergency at high momenta was caused by a bad initialisation procedure of fit parameters.
- We need to rewrite the initialisation procedure!
- Tracks with $0.22 < \theta < 0.63$ have big χ^2/ndf values due to hits formed when the track crosses the end of the tube.
- Decreased efficiency of the cut on convergency at low momenta ($p \lesssim 1.5 \text{ GeV}/c$) is explained by material effects.

Thanks to my colleagues I. Denisenko, V. Andreev, A. Korzenev, A. Ivanov, and E. Zemlyanichkina for fruitful discussions!

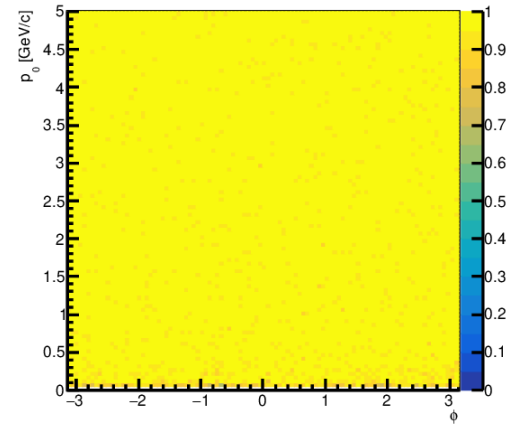
backup slides

Acceptance

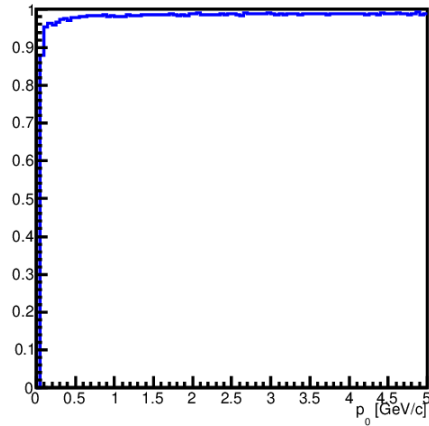
acceptance



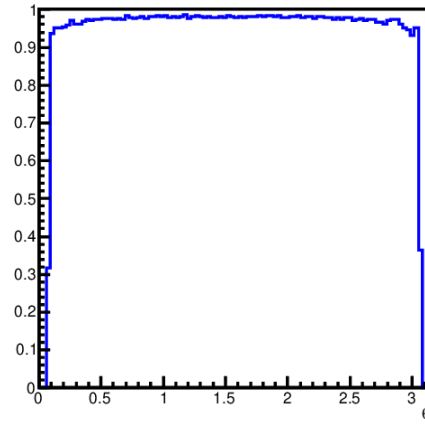
acceptance



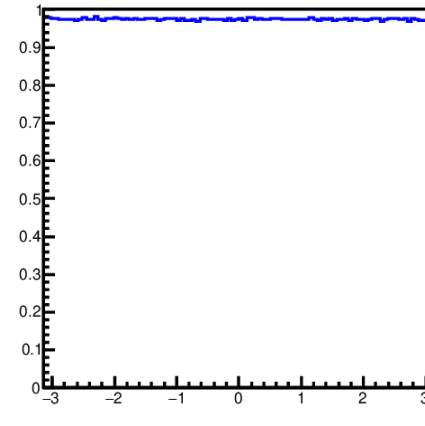
acceptance p_0



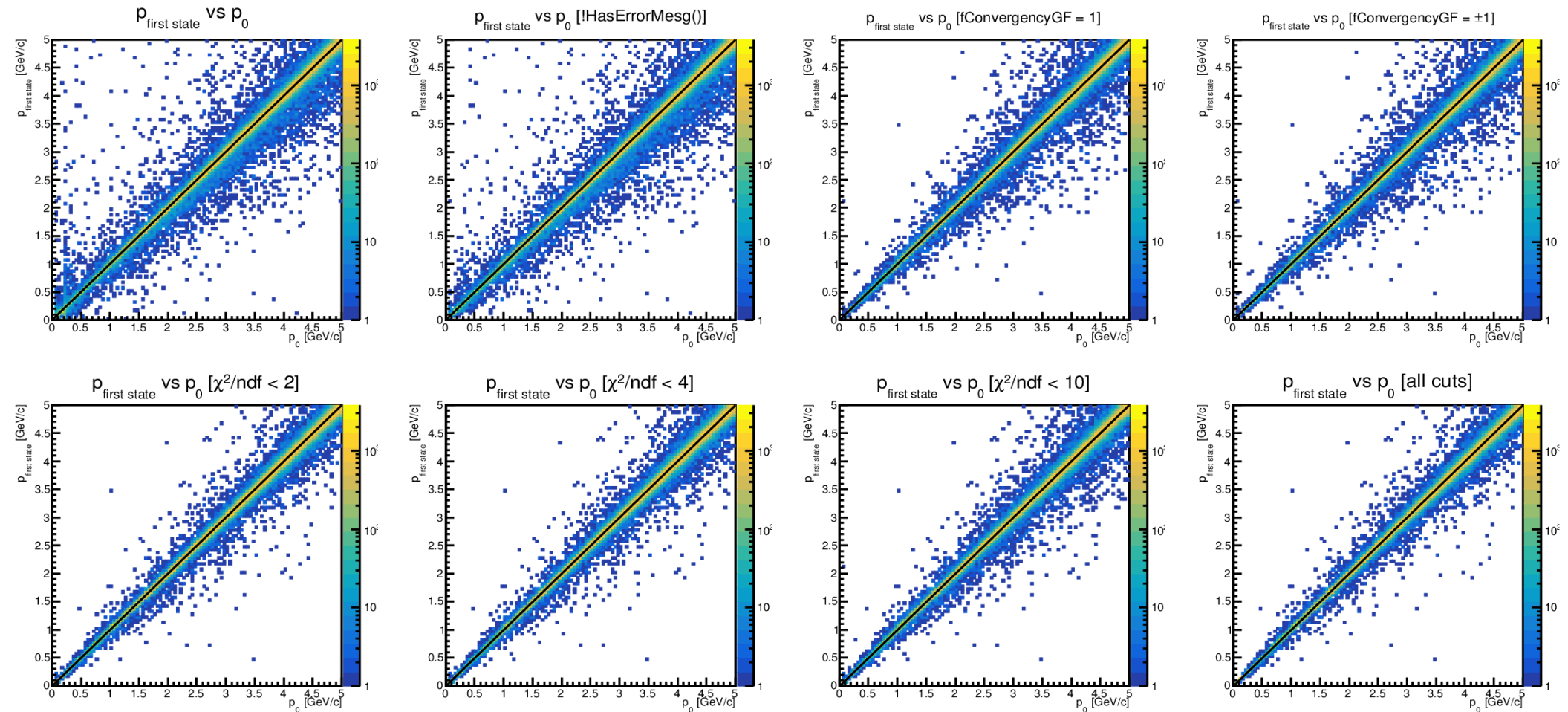
acceptance θ



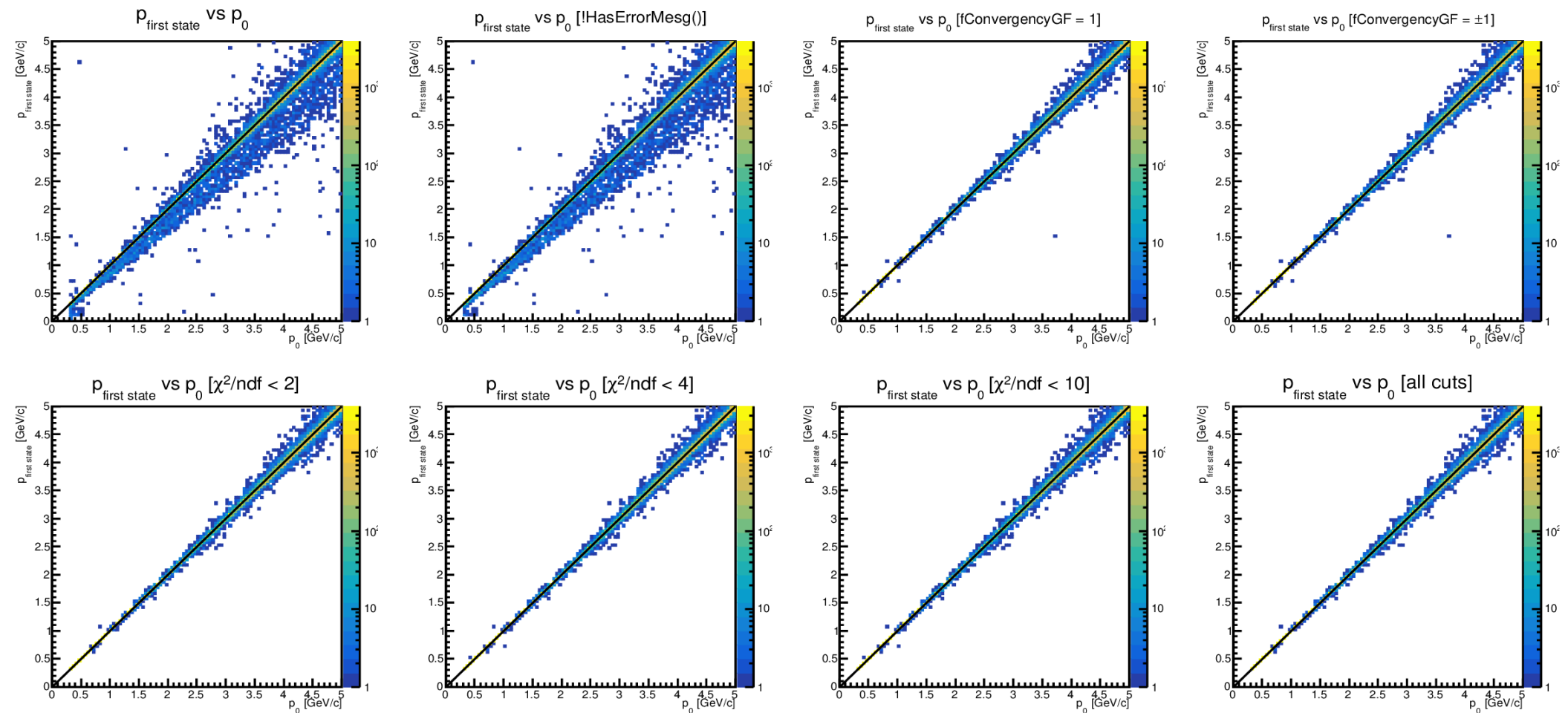
acceptance ϕ



Reco momentum vs true momentum. "Ideal" Rdrift



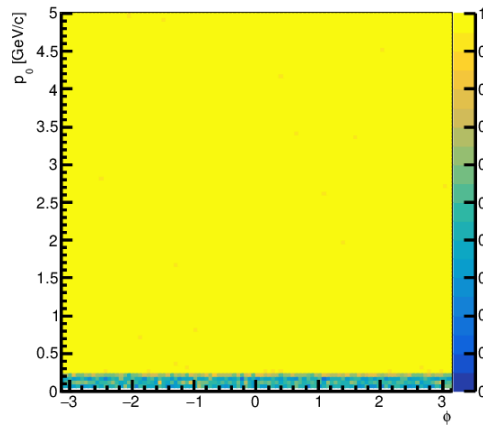
Reco momentum vs true momentum. No material



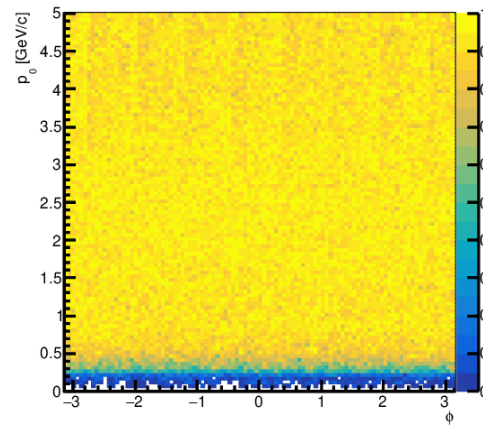
Efficiency of track quality cuts

current
initialisation
procedure

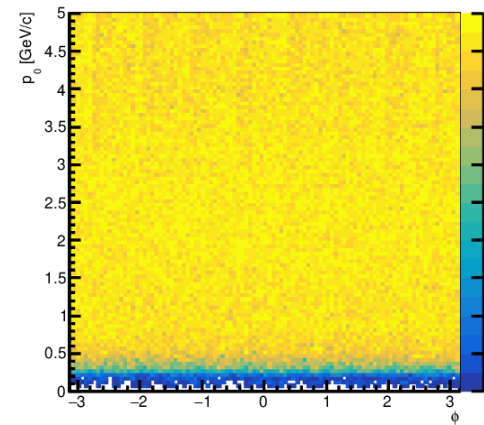
efficiency [`!HasErrorMesg()`]



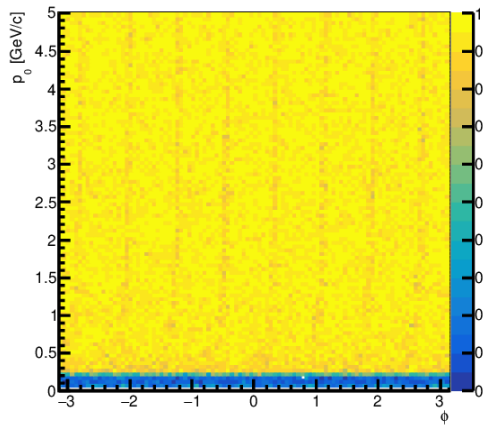
efficiency [`fConvergenceGF = 1`]



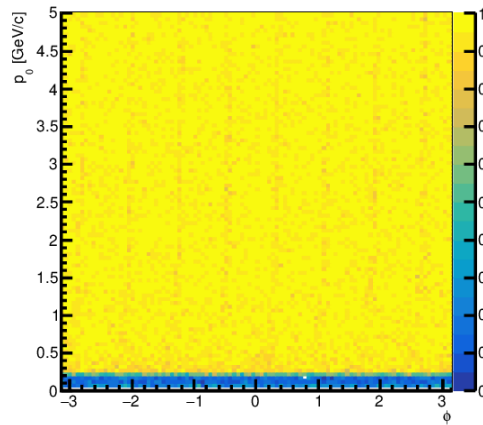
efficiency [`fConvergenceGF = ±1`]



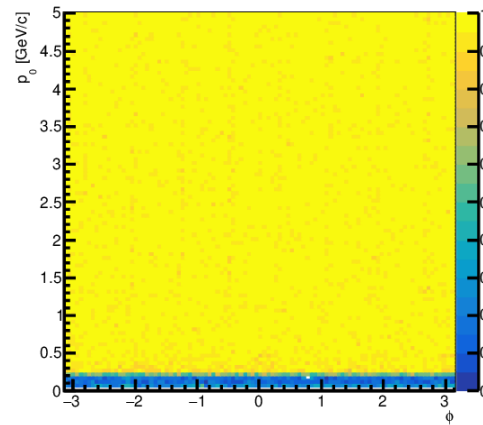
efficiency [$\chi^2/\text{ndf} < 2$]



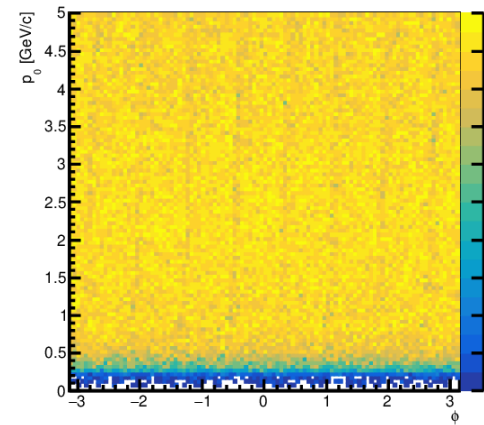
efficiency [$\chi^2/\text{ndf} < 4$]



efficiency [$\chi^2/\text{ndf} < 10$]



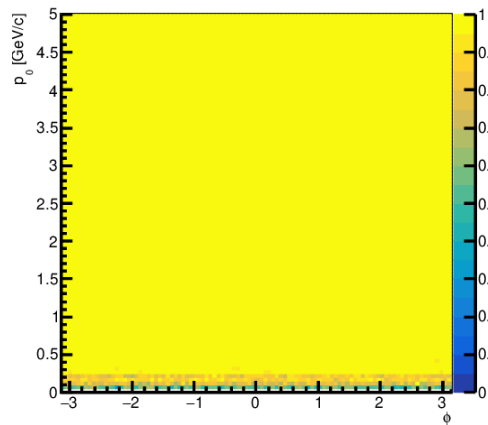
efficiency [all cuts]



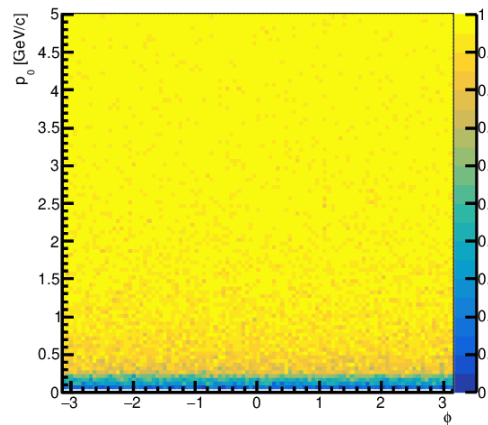
Efficiency of track quality cuts. Init. values = MC

initial values
from MC

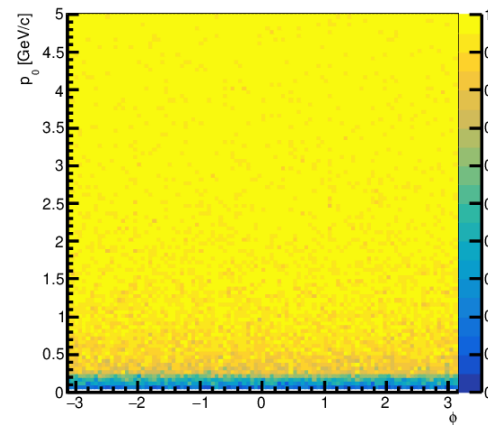
efficiency [!HasErrorMesg()]



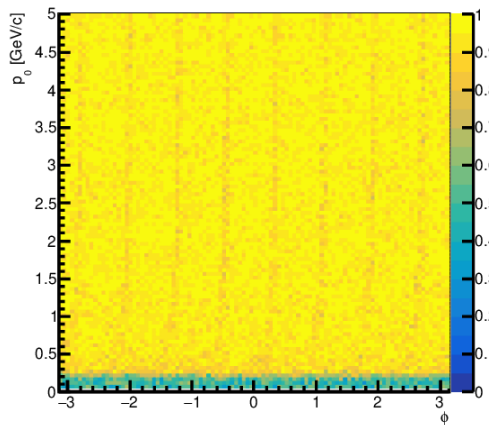
efficiency [fConvergencyGF = 1]



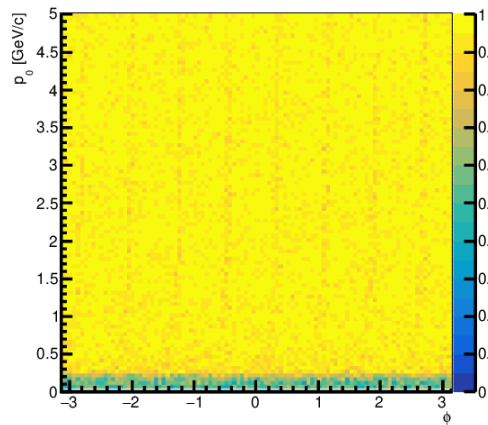
efficiency [fConvergencyGF = ±1]



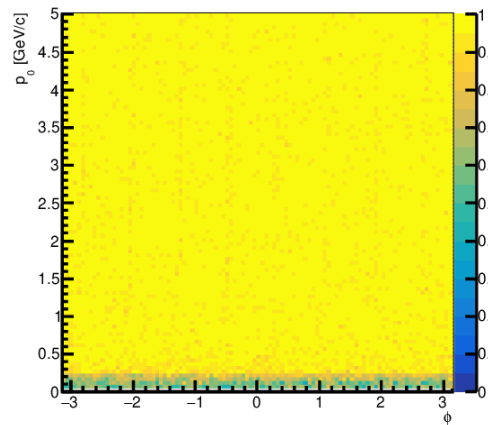
efficiency [$\chi^2/\text{ndf} < 2$]



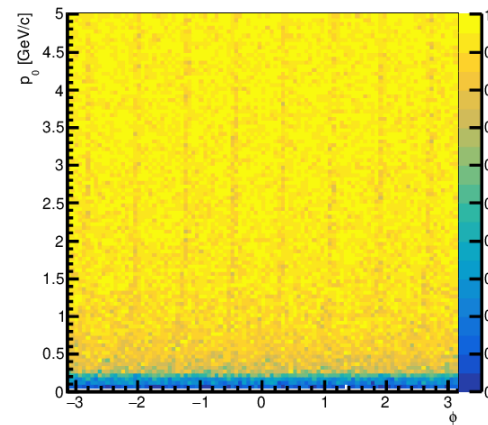
efficiency [$\chi^2/\text{ndf} < 4$]



efficiency [$\chi^2/\text{ndf} < 10$]



efficiency [all cuts]

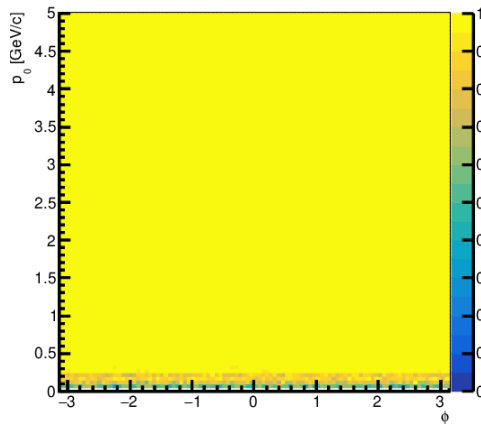


Efficiency of track quality cuts. "Ideal" Rdrift

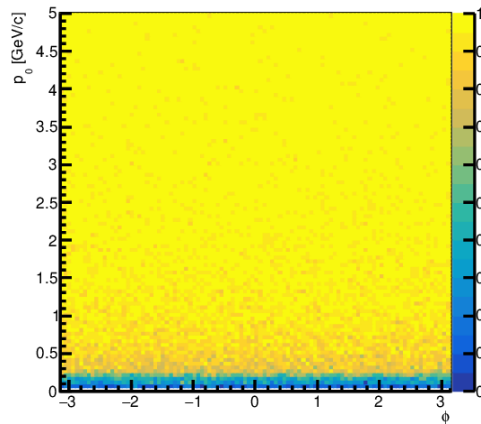
initial values
from MC

"ideal" Rdrift

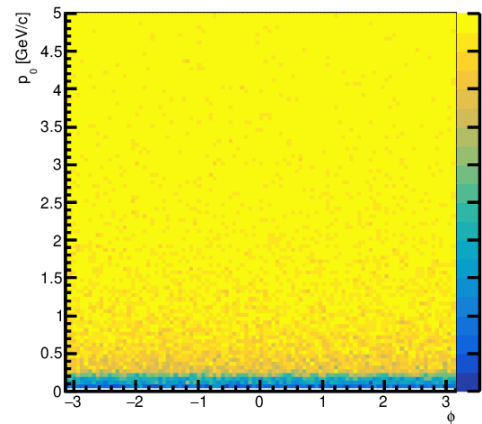
efficiency [`!HasErrorMesg()`]



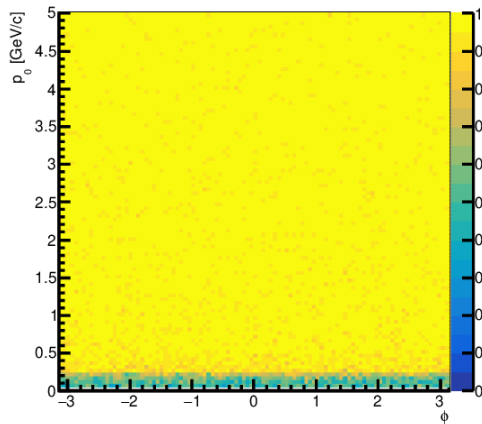
efficiency [`fConvergencyGF = 1`]



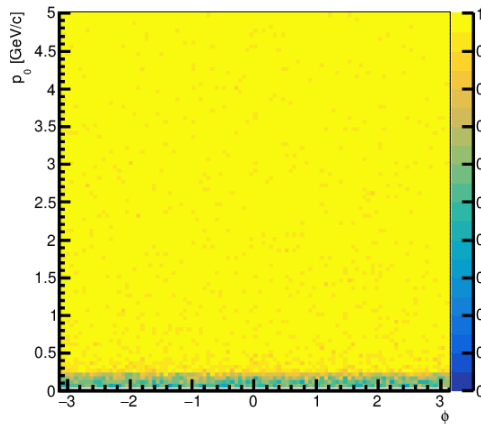
efficiency [`fConvergencyGF = ±1`]



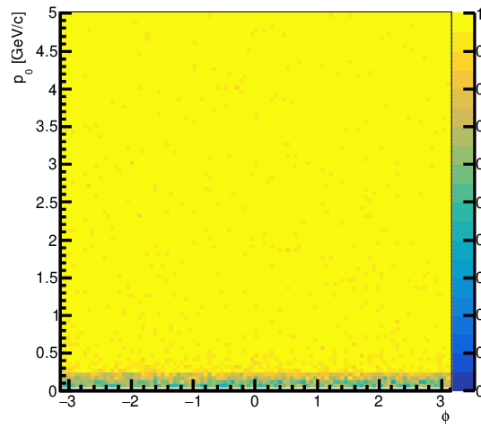
efficiency [$\chi^2/\text{ndf} < 2$]



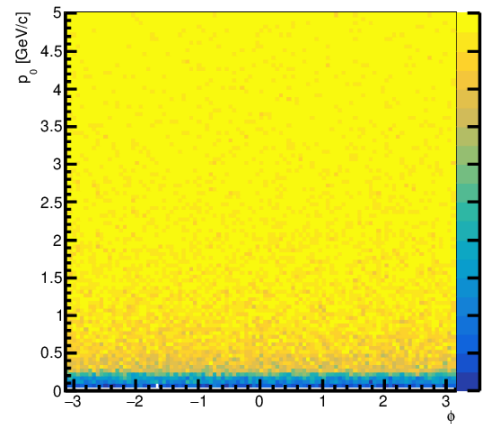
efficiency [$\chi^2/\text{ndf} < 4$]



efficiency [$\chi^2/\text{ndf} < 10$]



efficiency [all cuts]



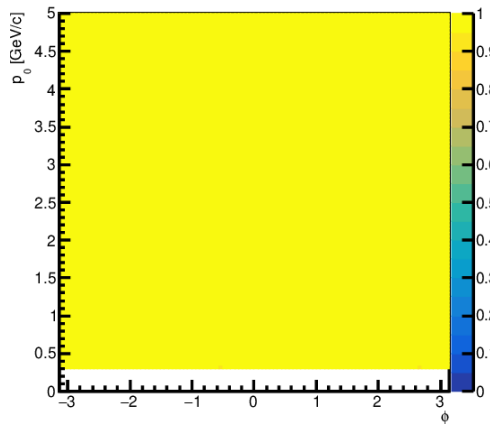
Efficiency of track quality cuts. No material

initial values
from MC

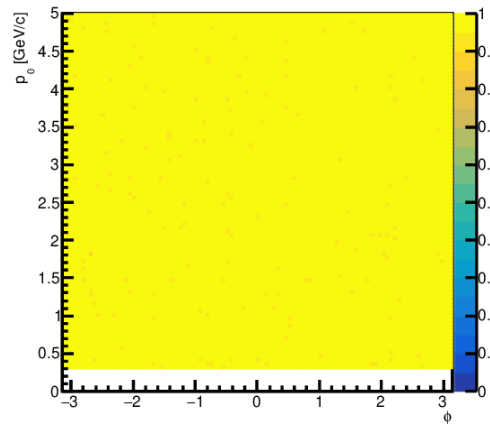
"ideal" Rdrift

no material

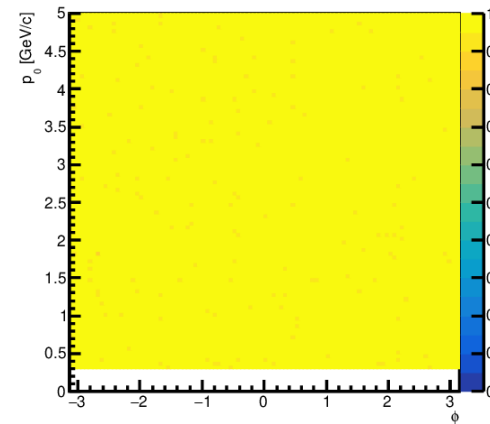
efficiency [!HasErrorMesg()]



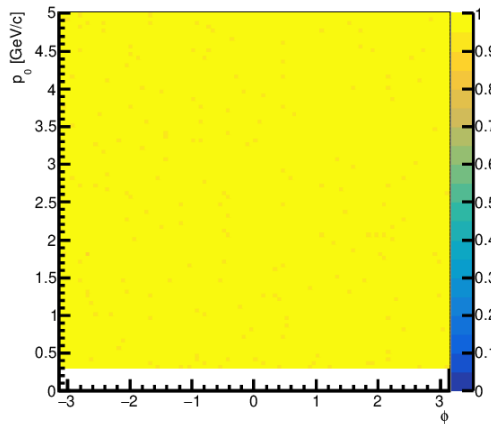
efficiency [fConvergencyGF = 1]



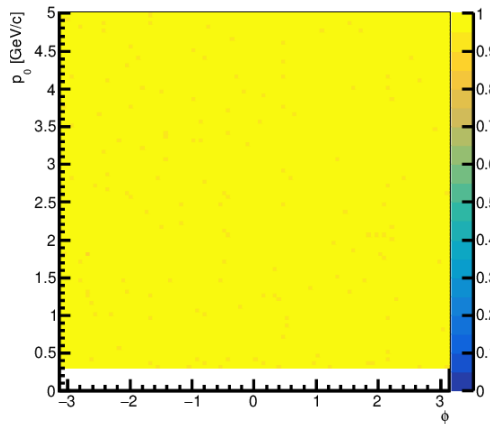
efficiency [fConvergencyGF = ±1]



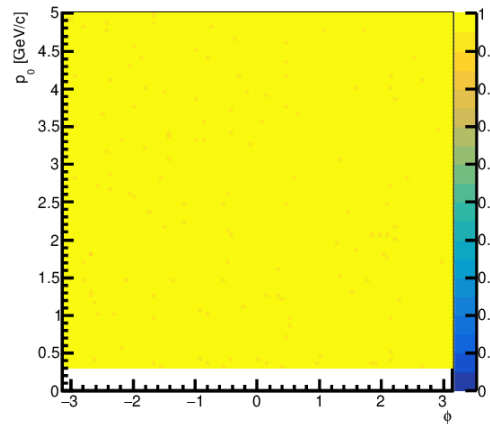
efficiency [$\chi^2/\text{ndf} < 2$]



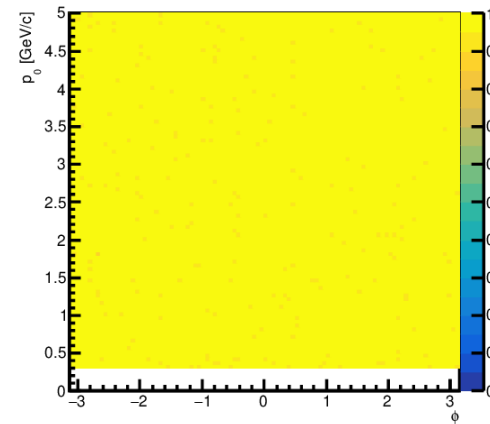
efficiency [$\chi^2/\text{ndf} < 4$]



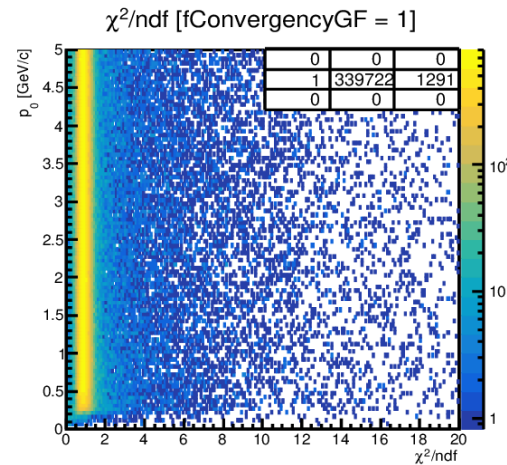
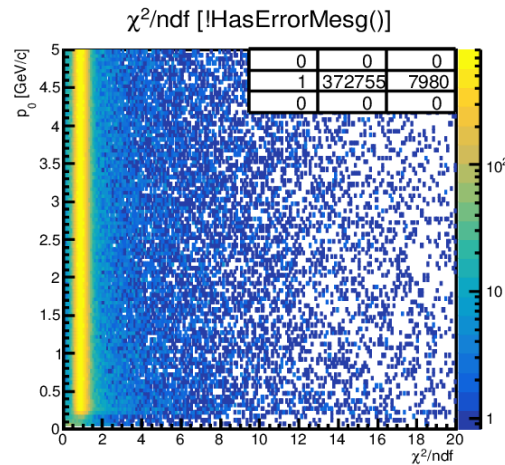
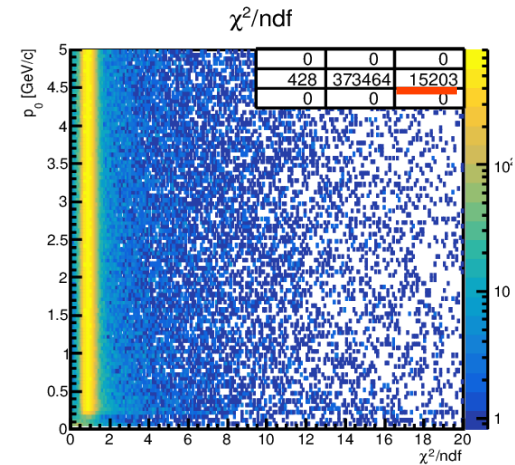
efficiency [$\chi^2/\text{ndf} < 10$]



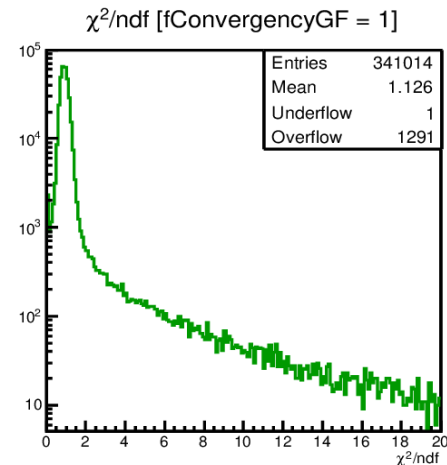
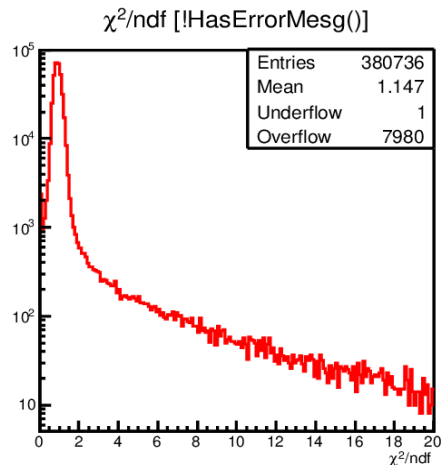
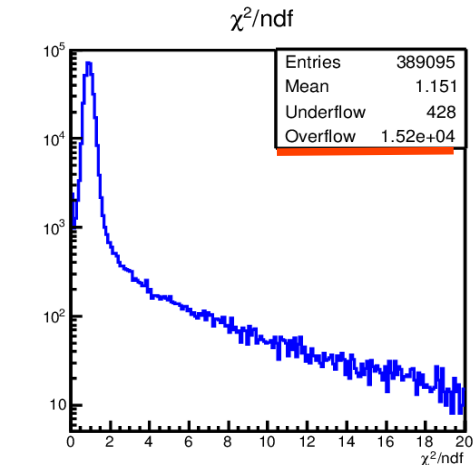
efficiency [all cuts]



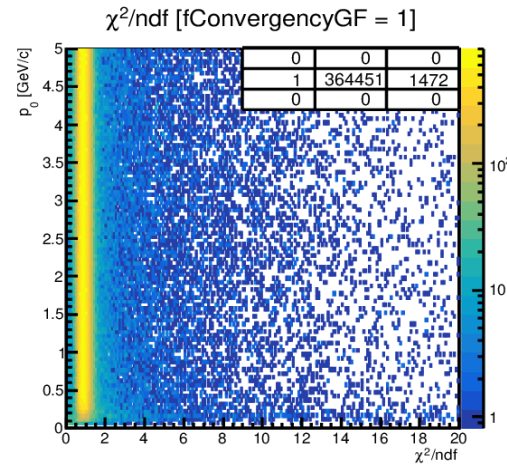
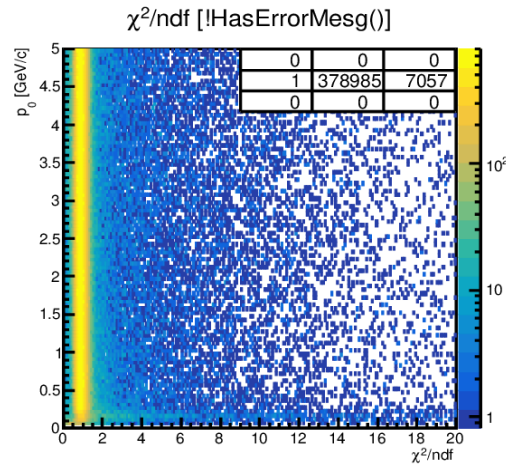
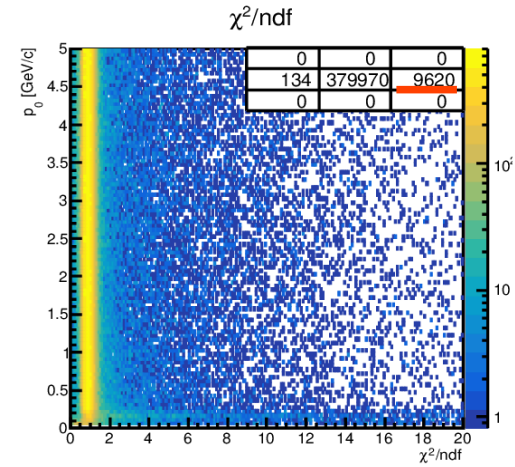
χ^2/ndf distribution



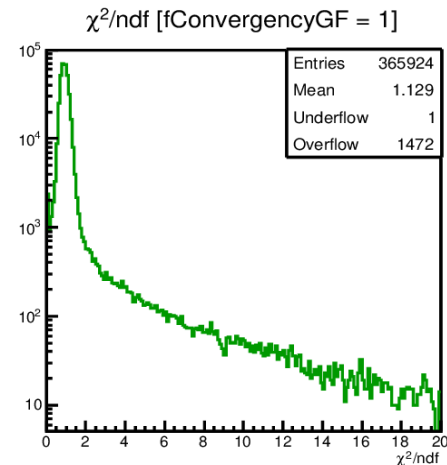
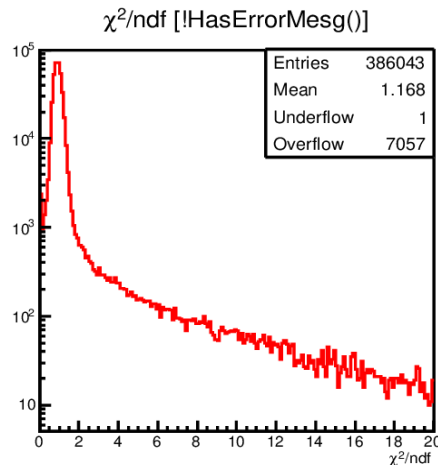
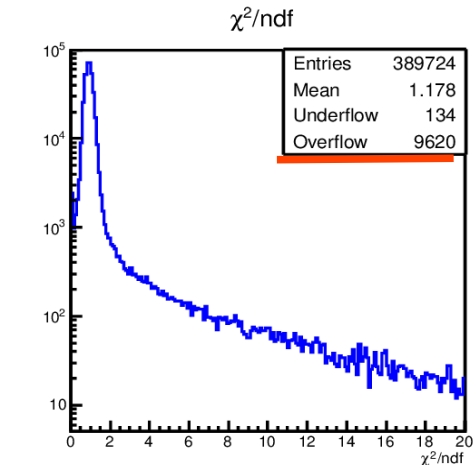
current
initialisation
procedure



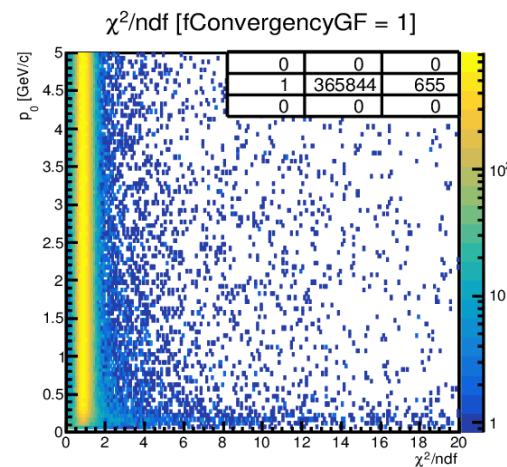
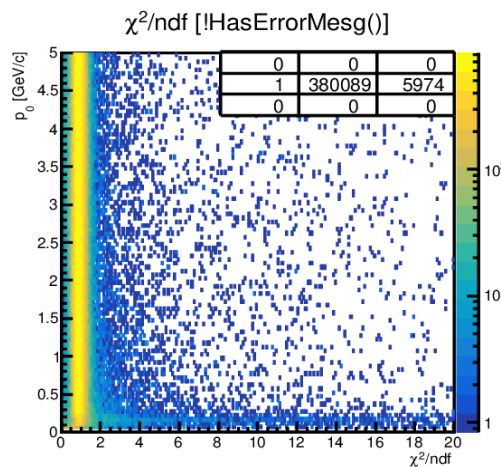
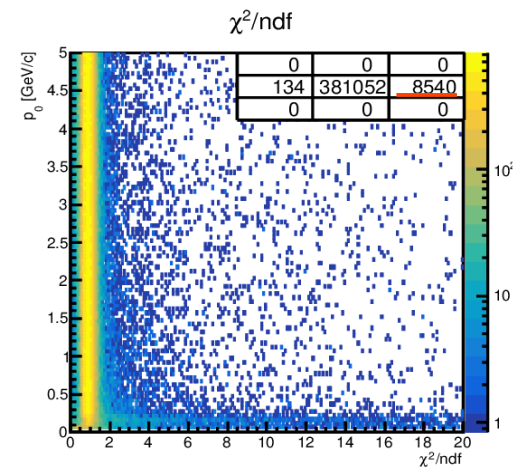
χ^2/ndf distribution. Initial values = MC.



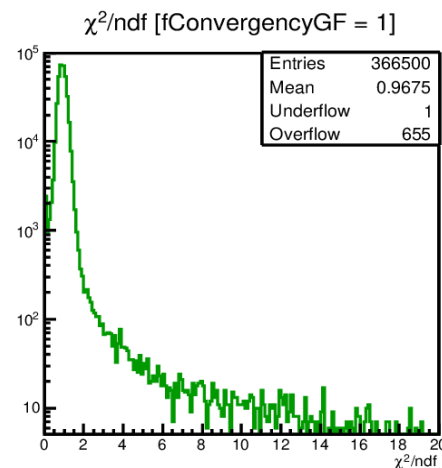
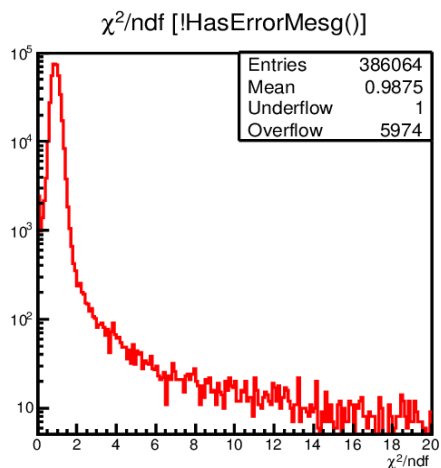
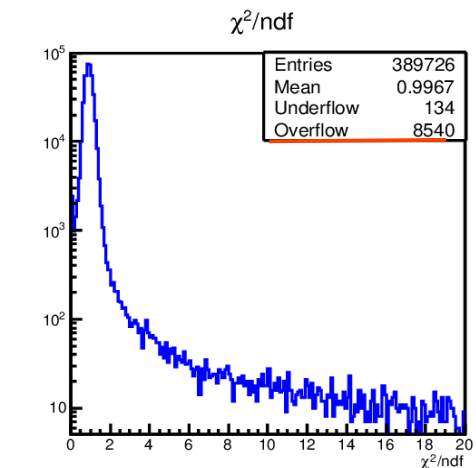
initial values
from MC



χ^2/ndf distribution. "Ideal" R drift.

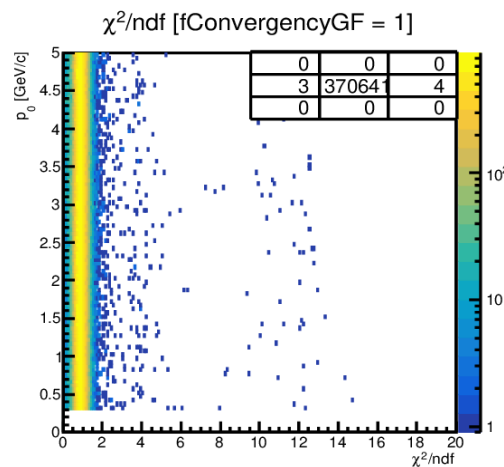
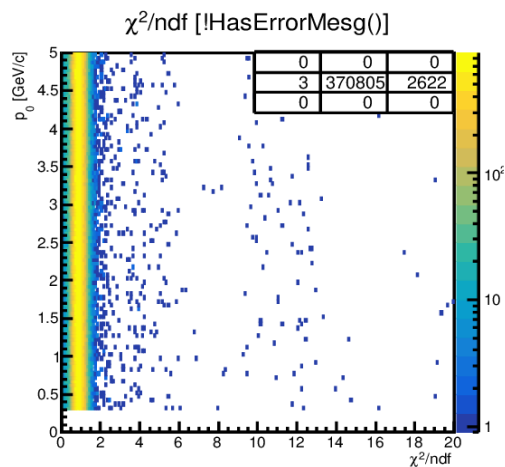
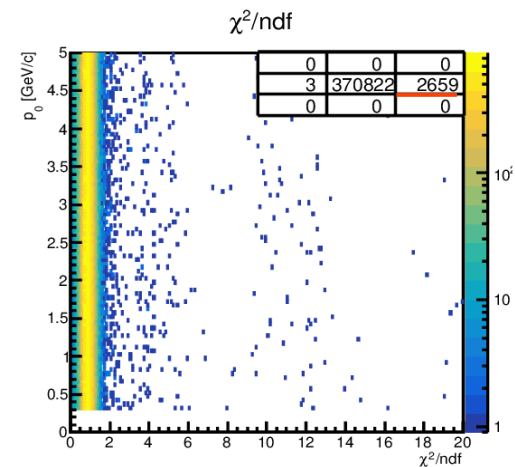


initial values
from MC

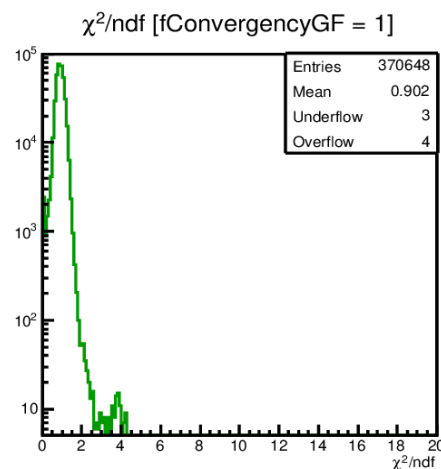
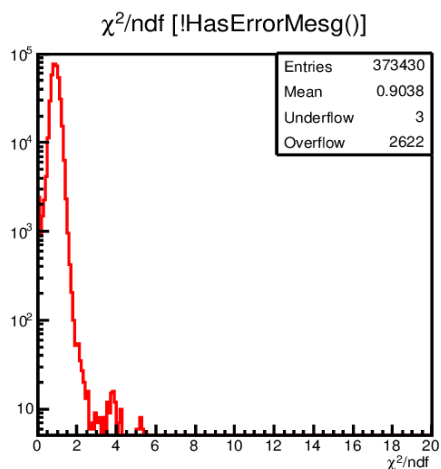
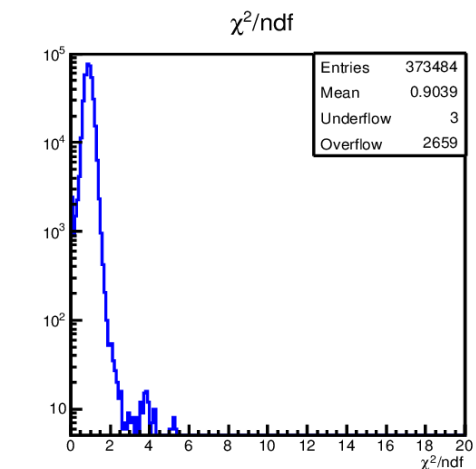


"ideal" Rdrift

χ^2/ndf distribution. No material.



initial values
from MC



"ideal" Rdrift

no material