

# Associated $J/\psi + \gamma$ production in the high-energy limit of QCD

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# Outline

- Introduction
- PRA
- ICEM
- NRQCD
- Models testing
- Results

# Introduction

## Motivation:

- ▶ "... clean probe of the gluon distribution ..."
- ▶ No  $J/\psi + \gamma$  measurements.
- ▶ Need predictions in different approaches.

## PRA introduction

### ⇒ Lipatov's Effective Field Theory

Reggeized gluons and quarks ⇒ Feynman rules

L. N. Lipatov (1995); L. N. Lipatov and M. I. Vyazovsky (2001).

Required matrix element  $|\bar{M}|_{pra}^2(R + R \rightarrow c\bar{c}[{}^3S_1^{(1)}] + \gamma)$  was calculate by using FeynArt's model file **ReggeQCD** by **Maxim Nefedov**

# PRA PDFs

## Kimber, Martin, Ryskin and Watt (KMRW) PDF

DGLAP ( $\sim \log(\mu^2)$ ) and BFKL ( $\sim \log(1/x)$ ) are taken into account

M. A. Kimber, A. D. Martin, and M. G. Ryskin (2001); G. Watt, A. D. Martin, and M. G. Ryskin (2003).

## MMRK modification

Exact normalization :

$$\left[ \int_0^{\mu^2} dt \Phi_i(x, t, \mu^2) = x f_i(x, \mu^2) \right] \equiv \left[ \Phi_i(x, t, \mu^2) = \frac{d}{dt} [T_i(t, \mu^2, x) x f_i(x, t)] \right]$$

From the equivalence requirement between normalization equation and KMRW prescription

## PRA factorization formula

$$\sigma = \int \frac{dx_1}{x_1} \frac{d^2 q_{1T}}{\pi} \int \frac{dx_2}{x_2} \frac{d^2 q_{2T}}{\pi} \Phi(x_1, t_1, \mu^2) \times \\ \Phi(x_2, t_2, \mu^2) \hat{\sigma}(R + R \rightarrow J/\psi + \gamma)$$

$$\hat{\sigma} = \frac{(2\pi)^4}{(2\pi)^{3n}} \delta^{(4)}(q_1 + q_2 - \sum p_i) \frac{|\bar{M}|_{pra}^2}{2x_1 x_2 s} \prod \frac{d^3 p_i}{2p_i^0}$$

$$q_{1,2}^\mu = x_{1,2} P_{1,2}^\mu + q_{1,2T}^\mu, \quad q_{1,2T} \neq 0 \quad q_{1,2}^2 = q_{1,2T}^2 = -\vec{q}_{1,2T}^2$$

For additional about MMRK and general about PRA see

M.A. Nefedov, V.A. Saleev (2020)

# Improved color evaporation model

## Processes

$R + R \rightarrow c + \bar{c} + \gamma, Q + \bar{Q} \rightarrow c + \bar{c} + \gamma$ , where  $Q = s, u, d$

## ICEM phenomenological cross-section

$$\sigma = F_{J/\psi} \times \int_{m_{J/\psi}^2}^{4m_D^2} \frac{d\sigma}{dM^2} dM^2, p_{T J/\psi} = \frac{m_{J/\psi}}{M} p_T c \bar{c}$$

Color evaporation model (CEM): H. Fritzsch (1977); F. Halzen (1977)

Improved CEM: Cheung V., Vogt R. (2017)

A. A. Chernyshev, V. A. Saleev (2022)

Fit  $pp \rightarrow J/\psi X$ :  $F_{J/\psi}(\sqrt{s}) = 0.012 + 0.952\sqrt{s}^{-0.525}$

# NRQCD

$$d\hat{\sigma}(a + b \rightarrow C + X) = \sum_n d\hat{\sigma}(a + b \rightarrow c\bar{c}[n] + X) \langle O^c \rangle$$

where n - color, spin, orbital and angular momentum quantum number.

## Colorless leaden order of NRQCD series named CSM

$$d\hat{\sigma}(g + g \rightarrow {}^3S_1^{(1)} + \gamma) = \langle O^{J/\psi} [{}^3S_1^{(1)}] \rangle d\hat{\sigma}(g + g \rightarrow c\bar{c} [{}^3S_1^{(1)}] + \gamma)$$

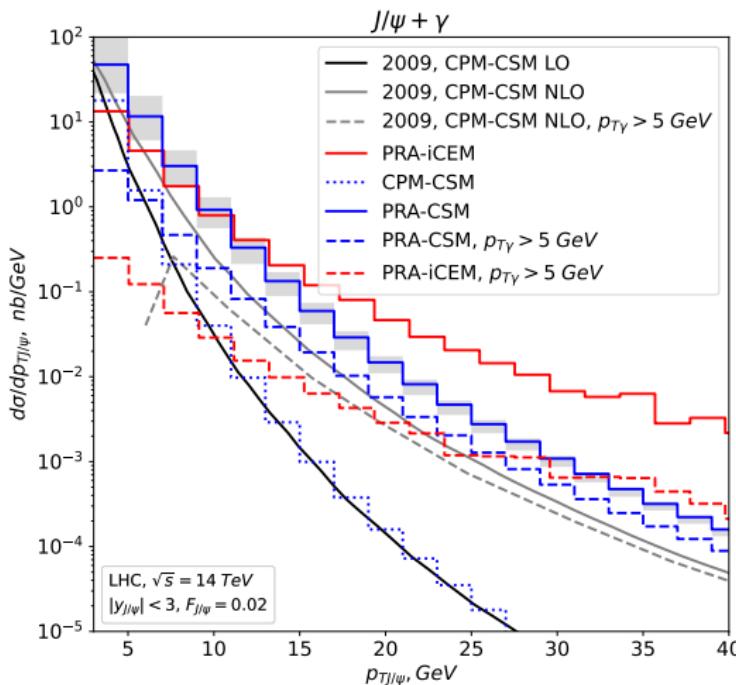
where  $\langle O^{J/\psi} [{}^3S_1^{(1)}] \rangle = 1.3 \text{ GeV}^3$  is singlet long distance matrix element.

In the leading order, the singlet contribution prevails over the prompt contribution.  
M. A. Doncheski, C. S. Kim (1993)

## So leading order in parton reggeization approach

$$d\hat{\sigma}(R + R \rightarrow {}^3S_1^{(1)} + \gamma) = \langle O^{J/\psi} [{}^3S_1^{(1)}] \rangle d\hat{\sigma}(R + R \rightarrow c\bar{c} [{}^3S_1^{(1)}] + \gamma)$$

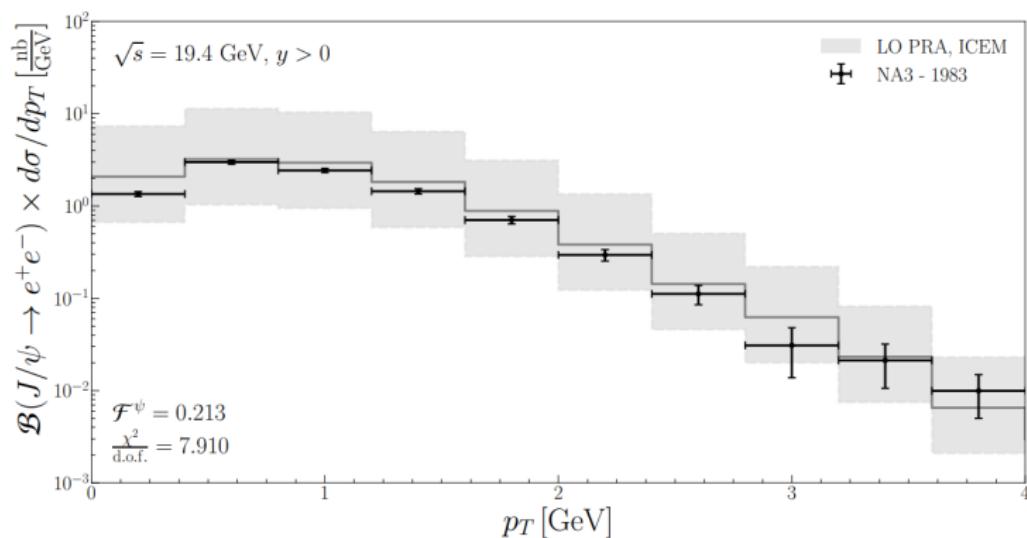
## At high energies



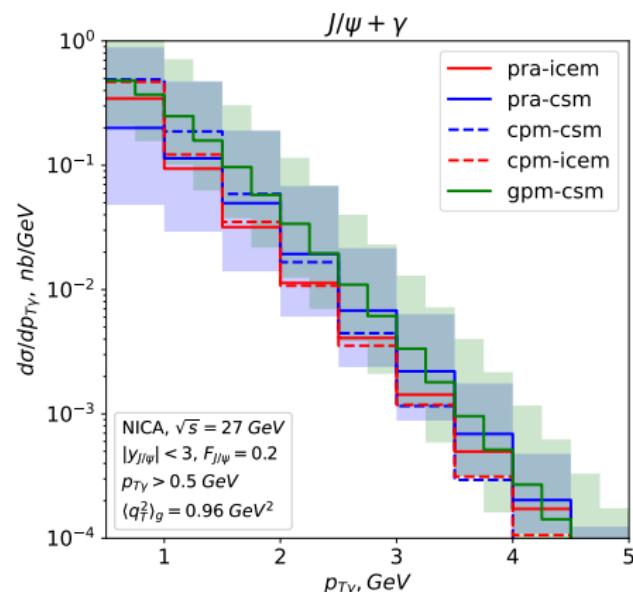
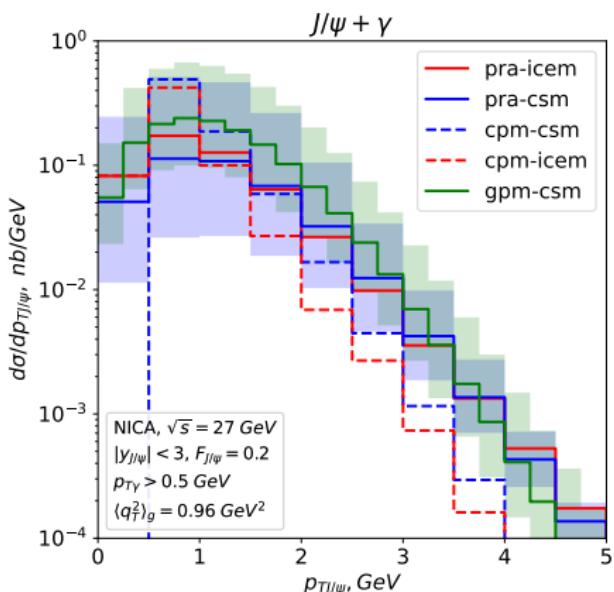
**PRA-CSM  $\simeq$  NLO CPM-CSM**  
[previous calculations by R. Li, J.X. Wang (2009)]

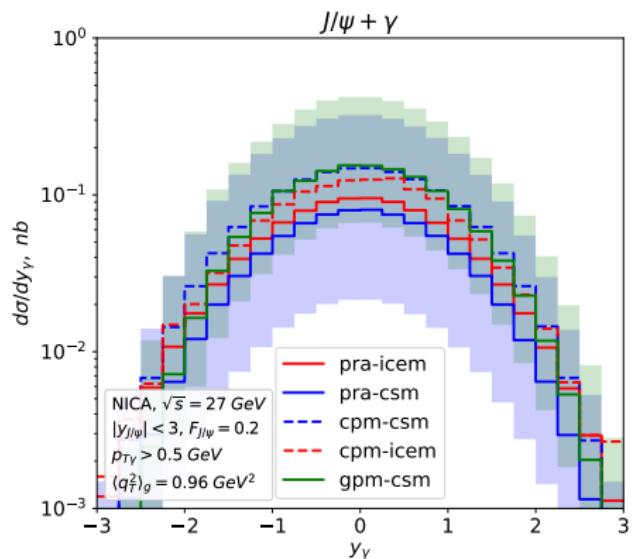
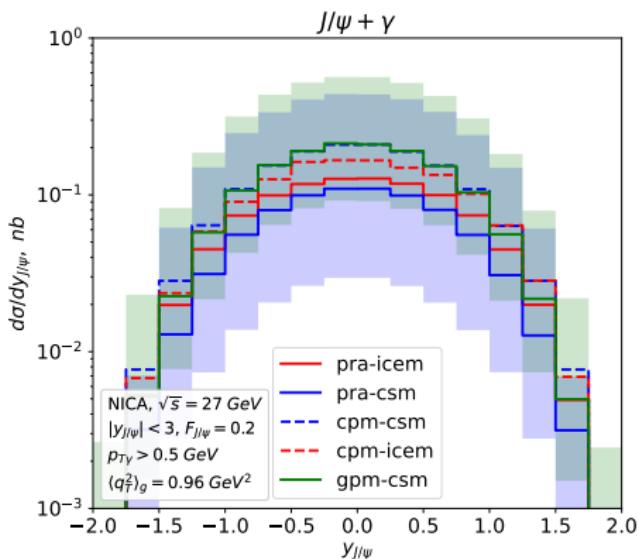
$$\begin{aligned}\sigma_{CPM-NLO} &= 61 \text{ nb} \\ \sigma_{PRA-CSM} &= 128 \text{ nb} \\ \sigma_{PRA-iCEM} &= 43 \text{ nb} \\ p_{T\gamma} > 5 : \\ \sigma_{CPM-NLO} &= 1.1 \text{ nb} \\ \sigma_{PRA-CSM} &= 9.4 \text{ nb} \\ \sigma_{PRA-iCEM} &= 1 \text{ nb}\end{aligned}$$

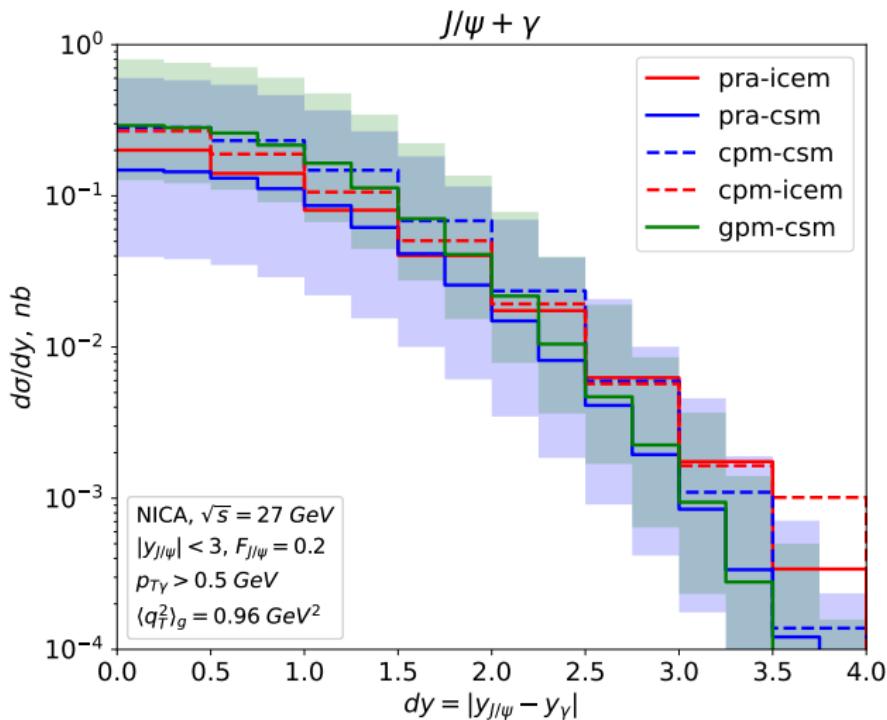
# Inclusive $J/\psi$ at low energies



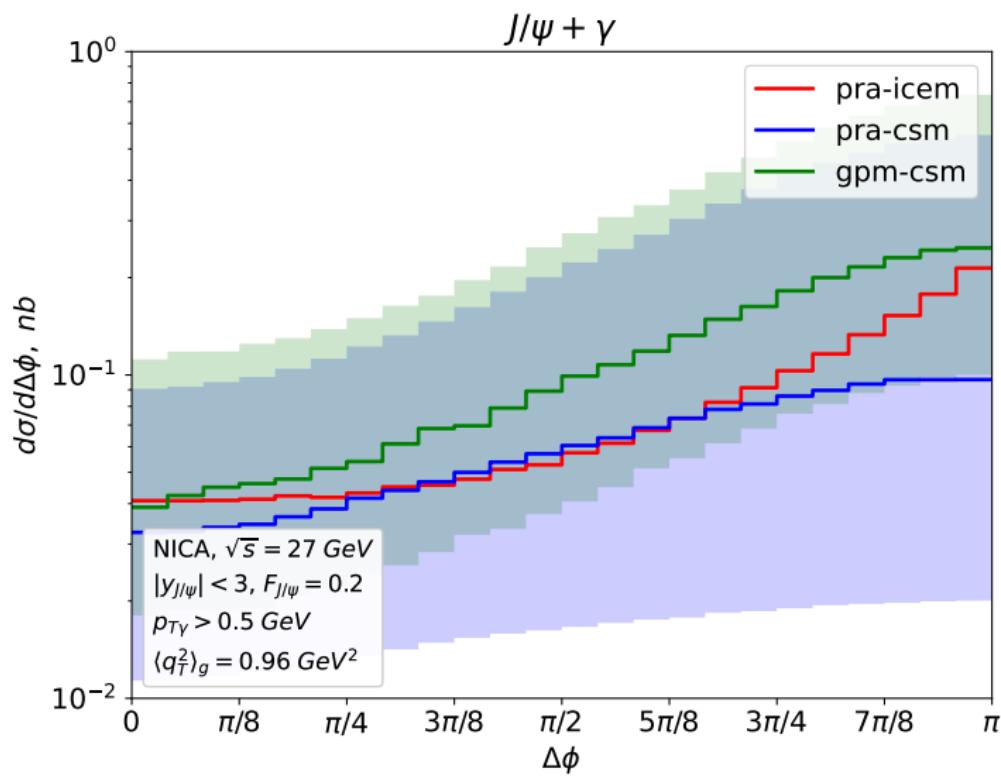
A. A. Chernyshev, V. A. Saleev (2022)

NICA,  $\sqrt{s} = 27 \text{ GeV}$ , transverse momentum cross sections

NICA,  $\sqrt{s} = 27$  GeV, rapidity cross sections

NICA,  $\sqrt{s} = 27$  GeV, rapidity difference cross-section

$$\sigma_{GPM-CSM} = 0.37 \text{ nb}$$
$$\sigma_{PRA-CSM} = 0.2 \text{ nb}$$
$$\sigma_{PRA-iCEM} = 0.24 \text{ nb}$$

NICA,  $\sqrt{s} = 27$  GeV, azimuthal correlations

## Conclusions

- ▶ Our PRA-CSM result for LHC ( $\sqrt{s} = 14 \text{ TeV}$ ) have good comparison with NEXT to leading order CPM-CSM computation. The implementation of this standard condition guarantees the correctness of the approach.
- ▶ A good description of the inclusive production data at low energies allows us to talk about the extensibility of the PRA. The extensibility argument of the PRA was used to predict differential cross sections at the energy of the NICA  $\sqrt{s} = 27 \text{ GeV}$ .
- ▶ At low energies, we show that the predictions in different models are in good agreement with each other, but the behavior of the cross sections is different according to the difference of azimuthal angles. So it seems possible to test, to discriminate models.

**Thank you for your attention!**