

Double longitudinal spin asymmetries in P-wave charmonium production at the NICA

A. V. Karpishkov^{1,2} and V. A. Saleev^{1,2}

¹ Joint Institute for Nuclear Research

² Samara National Research University

24.05.2024

VII SPD collaboration meeting

Outline

- NRQCD model
- Definition of the A_{LL}
- x_F -distribution of the A_{LL} at NICA
- Summary

A sketch of NRQCD formalism

The NRQCD framework [G. T. Bodwin, E. Braaten, and G. P. Lepage, *Phys. Rev. D* **51**, 1125 (1995)] describes heavy quarkonia in terms of Fock state decompositions. In case of orthoquarkonium state the wave function can be written as power series expansion in the velocity parameter $v \sim 1/\ln M_Q$:

$$|\mathcal{H}\rangle = \mathcal{O}(v^0)|Q\bar{Q}[{}^3S_1^{(1)}]\rangle + \mathcal{O}(v)|Q\bar{Q}[{}^3P_J^{(8)}]g\rangle + \mathcal{O}(v^2)|Q\bar{Q}[{}^1S_0^{(8)}]g\rangle \quad (1)$$

$$+\mathcal{O}(v^2)|Q\bar{Q}[{}^3S_1^{(1,8)}]gg\rangle + \dots \quad (2)$$

In the NRQCD effects of short and long distances are separated, and then the cross-section of heavy-quarkonium production via a partonic subprocess $a + b \rightarrow \mathcal{H} + X$ can be presented in a factorized form:

$$d\hat{\sigma}(a + b \rightarrow \mathcal{H} + X) = \sum_n d\hat{\sigma}(a + b \rightarrow Q\bar{Q}[n] + X) \times \langle \mathcal{O}^{\mathcal{H}}[n] \rangle, \quad (3)$$

where n denotes the set of quantum numbers of the $Q\bar{Q}$ pair, and its nonperturbative transitions into \mathcal{H} is described by the NMEs $\langle \mathcal{O}^{\mathcal{H}}[n] \rangle$.

In the general case, the partonic cross-section of quarkonium production from the $Q\bar{Q}$ Fock state $n = {}^{2S+1}L_J^{(1,8)}$ has the form:

$$d\hat{\sigma}(a + b \rightarrow Q\bar{Q}[{}^{2S+1}L_J^{(1,8)}] \rightarrow \mathcal{H}) = d\hat{\sigma}(a + b \rightarrow Q\bar{Q}[{}^{2S+1}L_J^{(1,8)}]) \times \frac{\langle \mathcal{O}^{\mathcal{H}}[{}^{2S+1}L_J^{(1,8)}] \rangle}{N_{col}N_{pol}},$$

where $N_{col} = 2N_c$ for color-singlet state, $N_{col} = N_c^2 - 1$ for color-octet state, and $N_{pol} = 2J + 1$.

Double-spin asymmetry

The double longitudinal-spin asymmetry is defined as

$$A_{LL} = \frac{\sigma_{++} - \sigma_{+-}}{\sigma_{++} + \sigma_{+-}} = \frac{\Delta\sigma}{\sigma},$$

LO Collinear Parton Model + LO NRQCD-factorization:

$$\Delta\sigma = \sum_{\mathbf{n}} \langle \mathcal{O}^X[\mathbf{n}] \rangle \sum_{i,j} \Delta f_i \otimes \Delta f_j \otimes \Delta \hat{\sigma}_{ij}[\mathbf{n}],$$

$$\sigma = \sum_{\mathbf{n}} \langle \mathcal{O}^X[\mathbf{n}] \rangle \sum_{i,j} f_i \otimes f_j \otimes \hat{\sigma}_{ij}[\mathbf{n}].$$

Un-polarized partonic cross-sections $\hat{\sigma}_{ij}[\mathbf{n}]$ are well-known at LO (e.g. [P.L. Cho, A.K. Leibovich (1996)] and [R. Gastmans, W. Troost and T. T. Wu, Phys. Lett. B **184**, 257-260 (1987)]).

Details on LO calculations of $\Delta \hat{\sigma}_{ij}[\mathbf{n}]$ can be found in [Klasen, Kniehl, Steinhauser, Phys.Rev.D **68** (2003) 034017, hep-ph/0306080]

PDFs and octet LDMEs

LO LDMEs from [Braaten, Kniehl, Lee, Phys.Rev.D**62** (2000) 094005] together with [NNPDF30_nlo_as_0119_nf_6](#) PDF set and [NNPDFpo111.100](#) polarized PDF set. Within NRQCD LO fits determine only linear combination of octet LDMEs:

$$\mathcal{M}_8 = \left\langle \mathcal{O}^{J/\psi} \left[{}^1S_0^{(8)} \right] \right\rangle + \frac{r}{m_c^2} \left\langle \mathcal{O}^{J/\psi} \left[{}^3P_0^{(8)} \right] \right\rangle, \quad r = 3.5, \quad m_c = 1.5$$

x_F -distributions of LO asymmetry of χ_{c1} meson at $\sqrt{s} = 27$ GeV

A_{LL} for a mean of all replicas of Δg , an orange band – scale-variation:

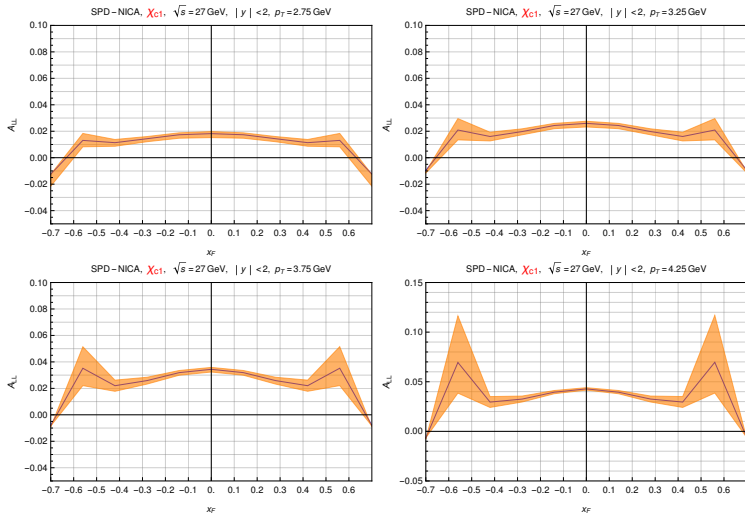


Figure 1: The A_{LL} for χ_{c1} production at $\sqrt{s} = 27$ GeV, $|y| \leq 2$ at different p_T -values: 2.75, 3.25, 3.75 and 4.25 GeV. $gg + qq$ contributions are taken into account.

x_F -distributions of LO asymmetry of χ_{c2} meson at $\sqrt{s} = 27$ GeV

A_{LL} for a mean of all replicas of Δg , an orange band – scale-variation:

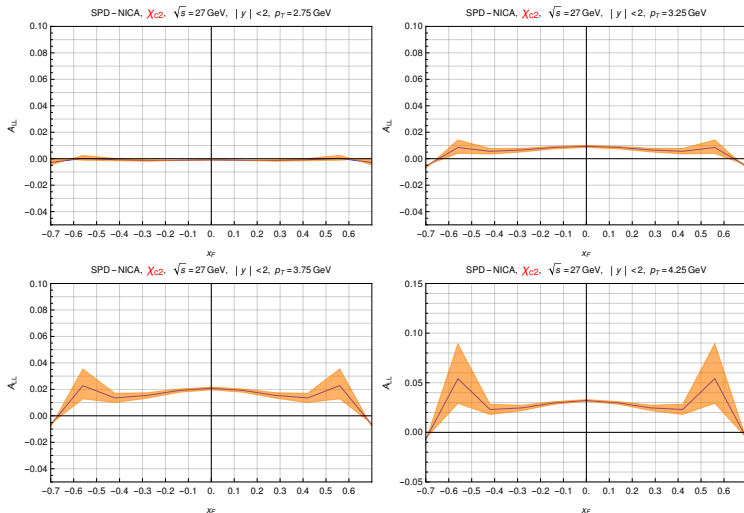
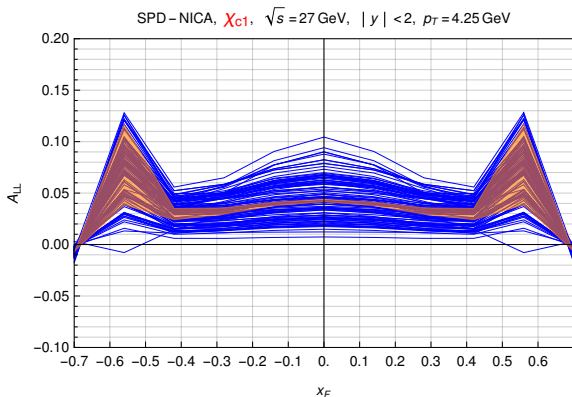


Figure 2: The A_{LL} for χ_{c2} production at $\sqrt{s} = 27$ GeV, $|y| \leq 2$ at different p_T -values: 2.75, 3.25, 3.75 and 4.25 GeV. $gg + qq$ contributions are taken into account.

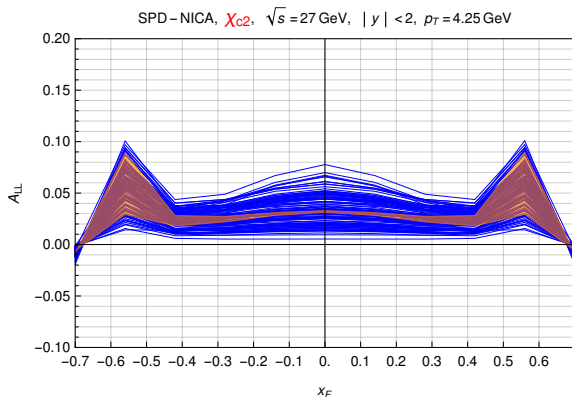
x_F -distribution of LO asymmetry of χ_{c1} meson at $\sqrt{s} = 27$ GeV and $p_T = 4.25$ GeV

The x_F -distribution of the LO A_{LL} for a hundred replicas of Δg , band – scale-variation:



x_F -distribution of LO asymmetry of χ_{c2} meson at $\sqrt{s} = 27$ GeV and $p_T = 4.25$ GeV

The x_F -distribution of the LO A_{LL} for a hundred replicas of Δg , band – scale-variation:



Summary

- At $\sqrt{s} = 27$ GeV within the NRQCD the A_{LL} is nearly zero and does not exceed the value of 13% for the $p_T \in [2.75, 4.25]$ GeV.
- We clearly see, that double longitudinal asymmetry decreases from χ_{c1} to χ_{c2} by approximately $1.3 \div 2$ times.

Thank you for your attention!