Mathematical Problems in Quantum Information Technologies



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Dense Quantum Hashing

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In [1] we have proposed a cryptographic quantum hash function and later in [2] provided its generalized version for arbitrary finite abelian groups based on the notion of -biased sets. However, the physical implementation of such functions nowadays poses a great challenge for the engineers since the proposed constructions of quantum hashing require completely entangled quantum states, which are hard to create and maintain. Therefore, in [3] we have proposed a simplified version of the quantum hash function that minimizes quantum state engineering and experimentally verified the collision resistance of such function. In this research we improve this approach by introducing a dense encoding of the classical information by the quantum states. Let $S=s_1,...,s_m$ Z_q be the set of numeric parameters. We propose a quantum hash function $\psi(x,y)$ that encodes classical information by the following superposition:

$$|\psi_j(x,y)| = \cos \frac{\pi s_j x}{2q} |0| + e^{i2\pi s_j y/q} \sin \frac{\pi s_j x}{2q} |1|, |\psi(x,y)| = |\psi_1(x,y)| |\psi_2(x,y)| |\psi_m(x,y)|.$$

That is, the quantum hash $|\psi(x,y)|$ of the classical input (x,y) is composed of m independent hashes $|\psi_j(x,y)|$ of smaller size. The only difference between them is the value of the numeric parameter s_j . The pair of arguments (x,y) can be interpreted as the split of a larger input, or as a pair of an input and a key. In any case this means that we can double the amount of information encoded in the same number of qubits as compared to [3]. The main idea behind quantum hashing is to provide the minimal fidelity of different quantum hash codes (collision resistance) with the minimal possible number of qubits (that affects the one-way property) [4]. The fidelity in our case can be expressed by the following formula:

$$\prod_{j=1}^{m} \cos^2 \frac{\pi s_j(x_2 - x_1)}{2q} - \sin \frac{\pi s_j x_1}{2q} \sin \frac{\pi s_j x_2}{2q} \sin^2 \frac{\pi s_j(y_2 - y_1)}{q} .$$

The formula above gives the probability of considering hashes $|\psi(x_1,y_1)|$ and $|\psi(x_2,y_2)|$ to be equal, and the set of parameters $S=s_1,...,s_m$ should be computed as the result of minimization of this formula over all pairs of unequal inputs.

References

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