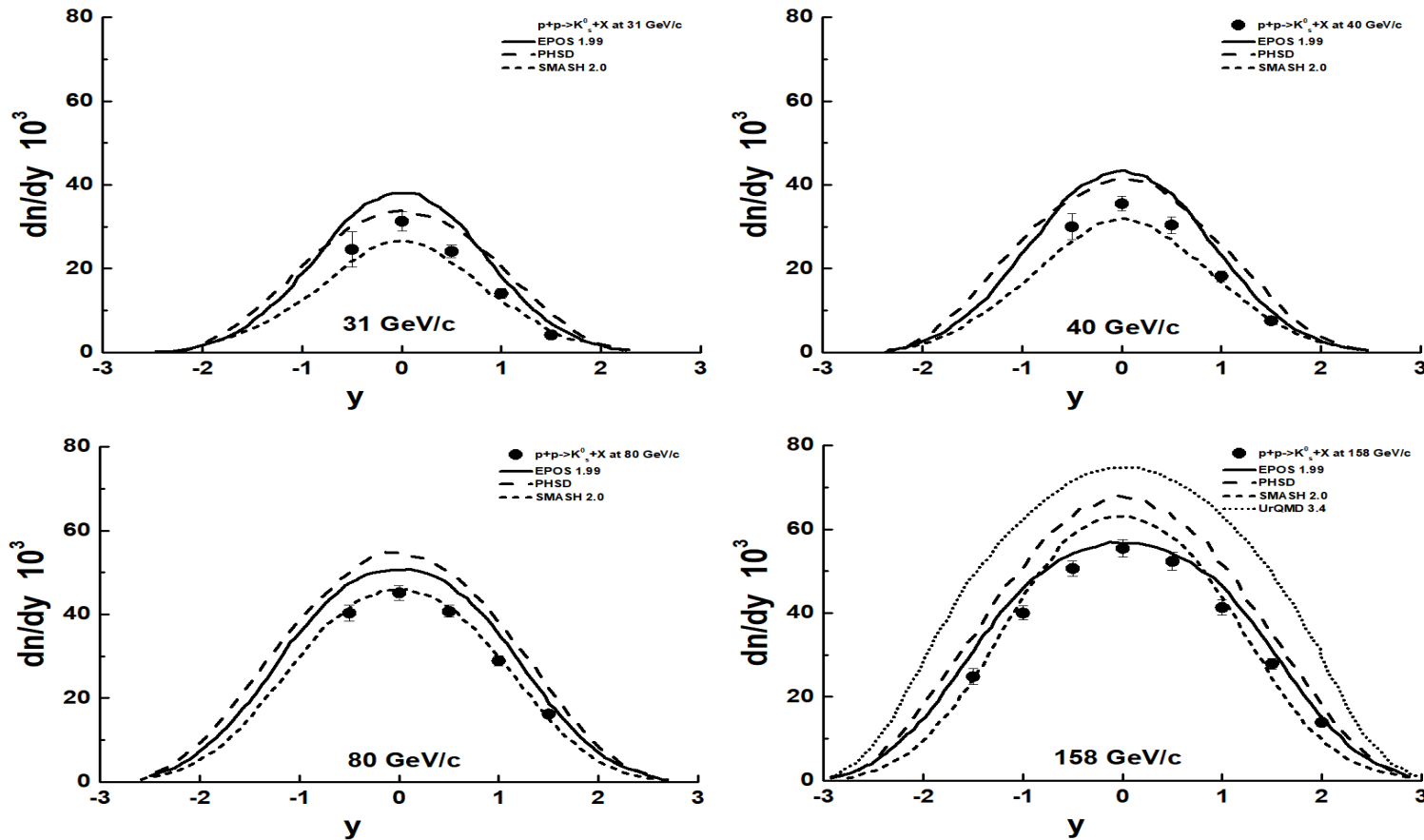


Towards understanding of K^0_s meson production in hadronic interactions

A. Galoyan, A. Ribon, V. Uzhinsky 05.2024

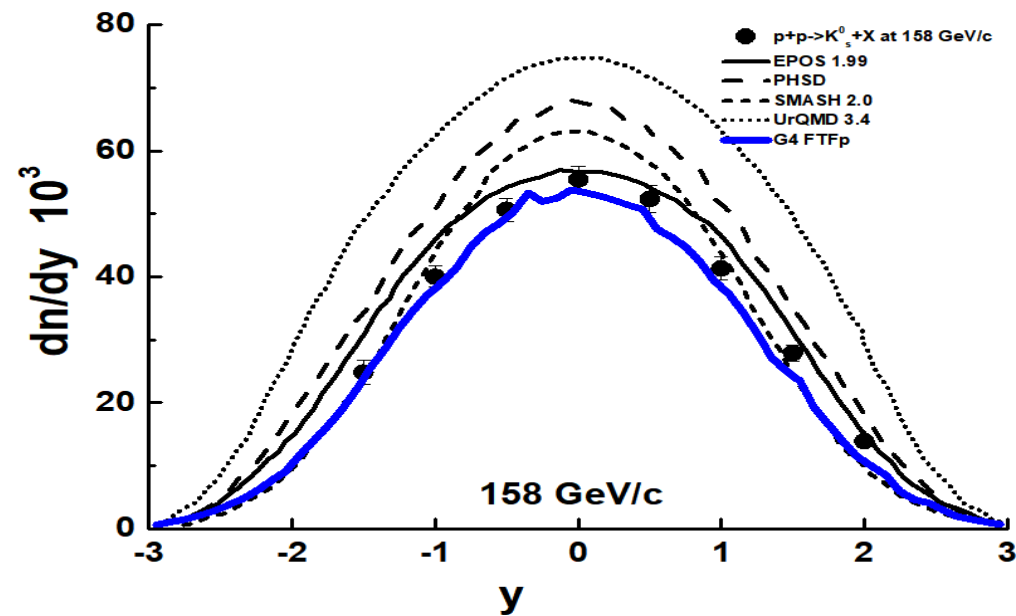
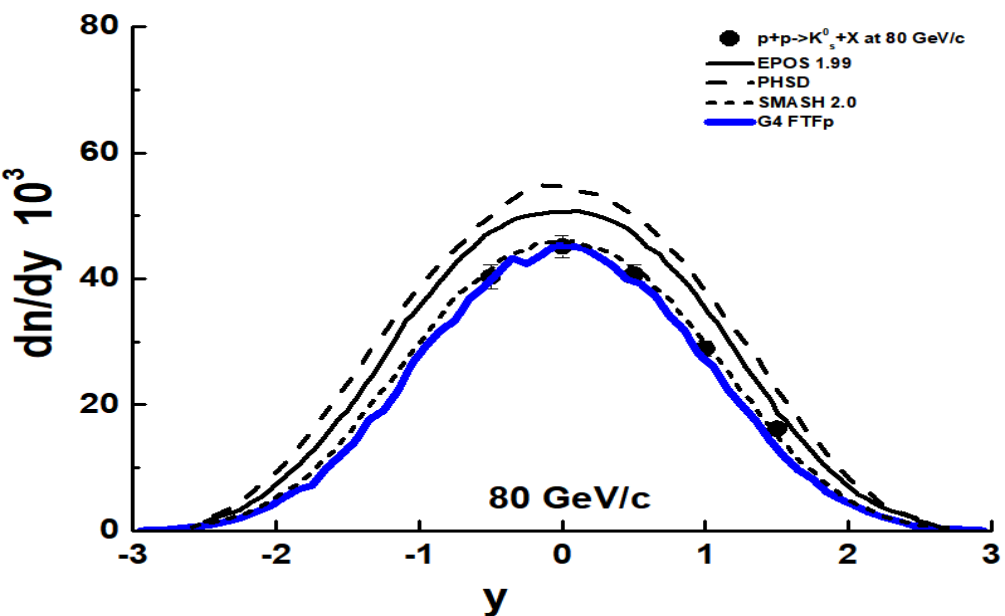
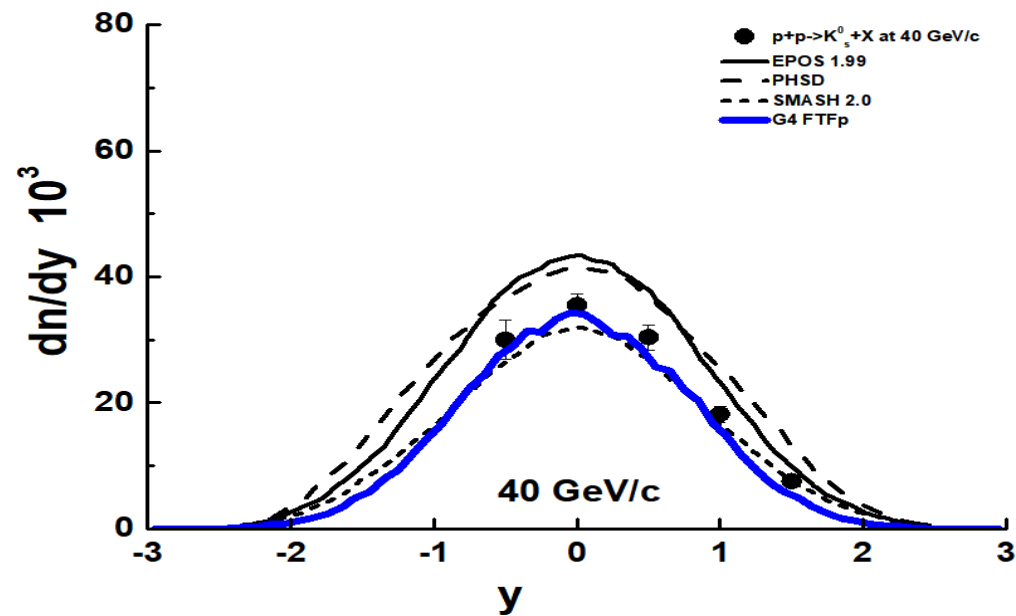
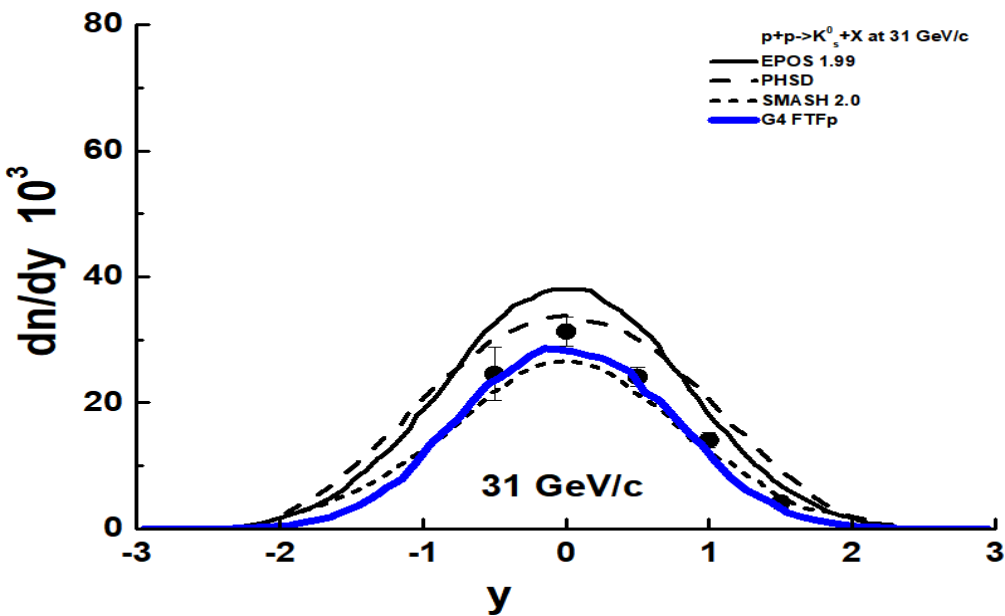
NA61/SHINE Collaboration arXiv:2402.17025v1 [hep-ex] 26 Feb 2024

K^0_s meson production in inelastic p+p interactions at 31, 40 and 80 GeV/c beam momentum measured by NA61/SHINE at the CERN SPS



SMASH ~ O.K., EPOS O.K. at 158 GeV/c, PHSD - ???

Experimental data and models + FTF



SMASH ~ O.K., EPOS O.K. at 158 GeV/c, PHSD - ?, FTF is the best!

Study of 2-particles transverse momentum correlations of Ks0-mesons in proton-proton interactions

V.Abramov et al, Possible studies at the first stage of the NICA collider operation with polarized and unpolarized proton and deuteron beams, arXiv:2102.08477

Phys.Part.Nucl. 52 (2021) 6, 1044-1119

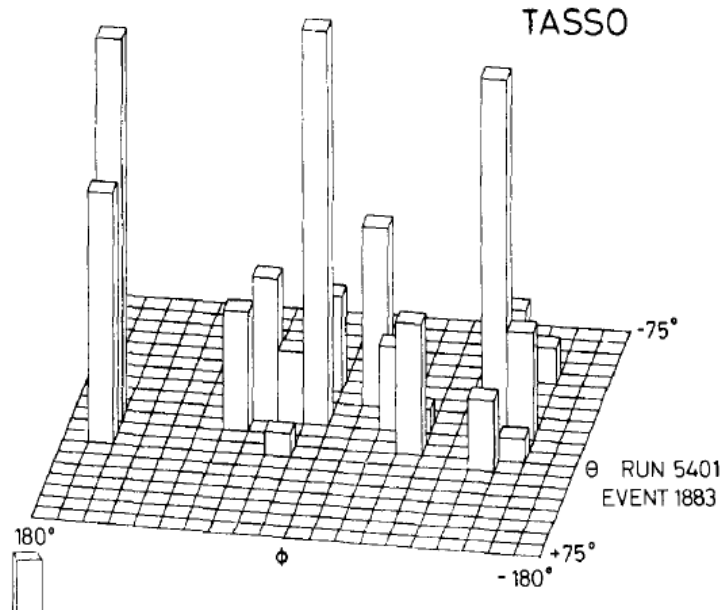
SPD collabotation

Spin effects in elastic scattering and hyperon production, study of multiquark correlation, dibaryon resonances, exclusive reactions, open charm and charmonia near threshold. Minimal bias interactions will be studied also at SPD. *2-particles transverse momentum correlations of Λ –hyperons in PP and DD interactions can be studied at SPD.*

A. Galoyan, A. Ribon, V. Uzhinsky
MDPI Physics 5 (2023) 3, 823-831

1. The method of study of 2-particle Pt-correlations
2. 2-particle Pt correlations of Ks0-mesons in PP-interactions in Geant4/FTF model
3. The Pt correlations of in Ks0-mesons PP-interactions in Pythia model and comparison with FTF ones.

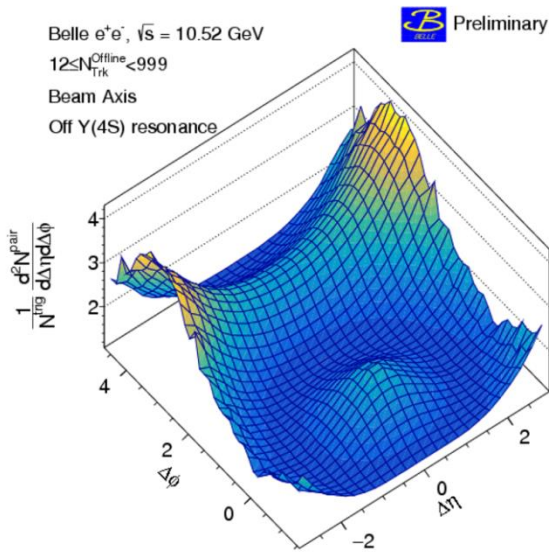
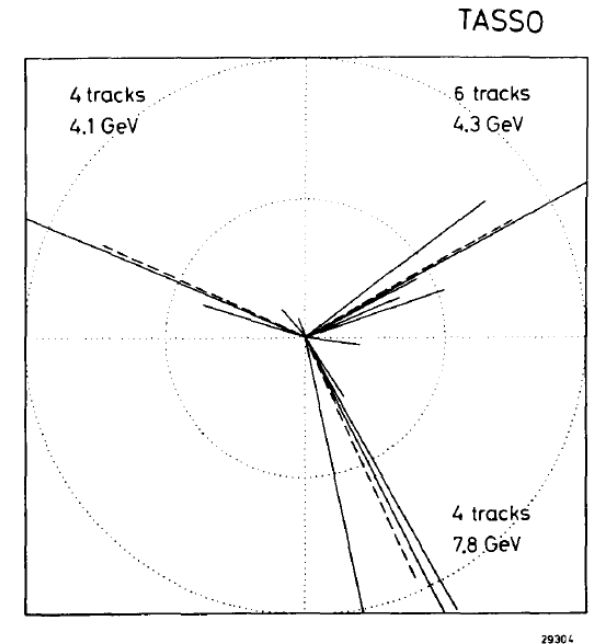
Towards Study of 2-Particle Pt Correlations



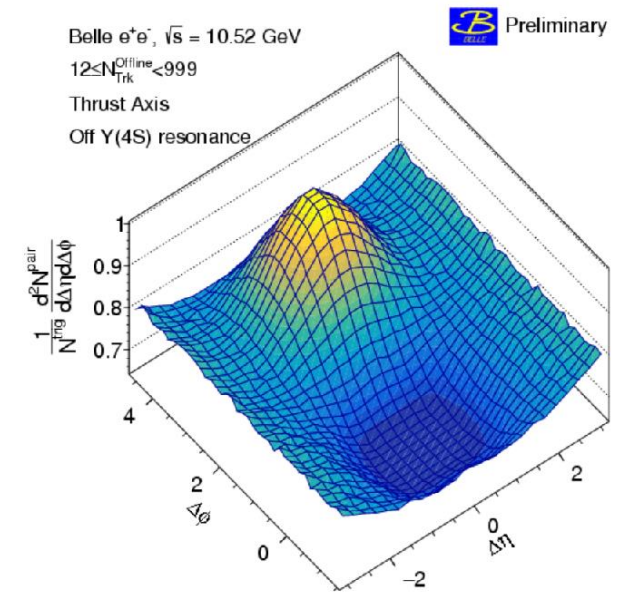
PHYSICS REPORTS 107 (1984) 59

**e+e- PHYSICS AT PETRA –
THE FIRST FIVE YEARS,**
Sau Lan WU and *DESY*.

Jets in High Energy Physics



Two-particle correlation functions
for beam (left) and thrust (right)
axis analyses with offline
multiplicity $N_{\text{offline Trk}} \geq 12$.



What to do at lower energies when jets are not produced?

K_S^0 - (Λ or anti- Λ)- hadron correlations in pp collisions at $\sqrt{s} = 13$ TeV
ALICE Collaboration

$$\frac{d^2 N_{\text{pair}}}{d\Delta\varphi d\Delta\eta}(\Delta\varphi, \Delta\eta) = \frac{1}{N_{\text{trigg}}} \frac{1}{\varepsilon_{\text{trigg}}} \frac{1}{\varepsilon_{\text{assoc}}} \frac{d^2 N_{\text{pair}}^{\text{raw}}}{d\Delta\varphi d\Delta\eta}(\Delta\varphi, \Delta\eta) \frac{1}{\varepsilon_{\text{pair}}}$$

$$Y_{\Delta\varphi} = \int_{\Delta\varphi_1}^{\Delta\varphi_2} \frac{dN}{d\Delta\varphi} d\Delta\varphi$$

ALICE
pp, $\sqrt{s}=13$ TeV
 K_S^0 -h correlations

$3 < p_T^{\text{trigg}} < 4$ GeV/c
 $1 \text{ GeV}/c < p_T^{\text{assoc}} < p_T^{\text{trigg}}$

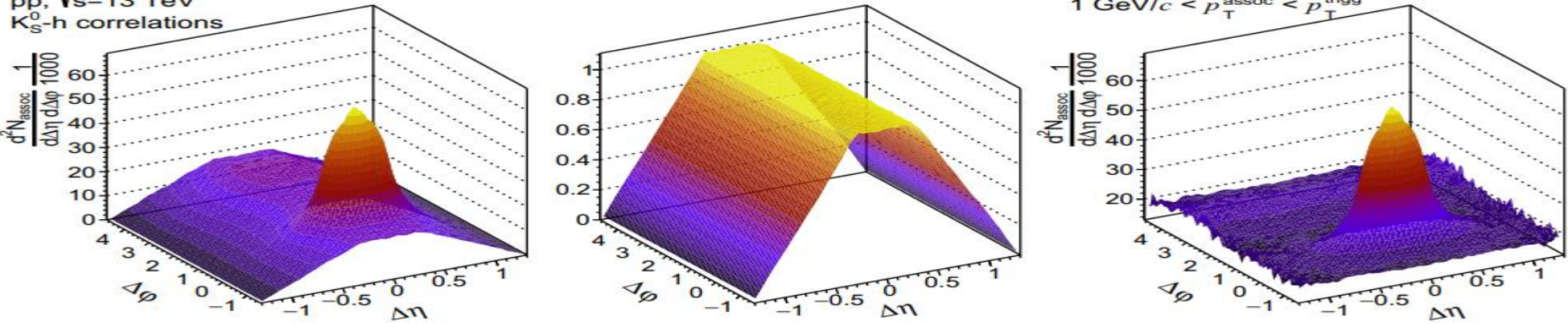
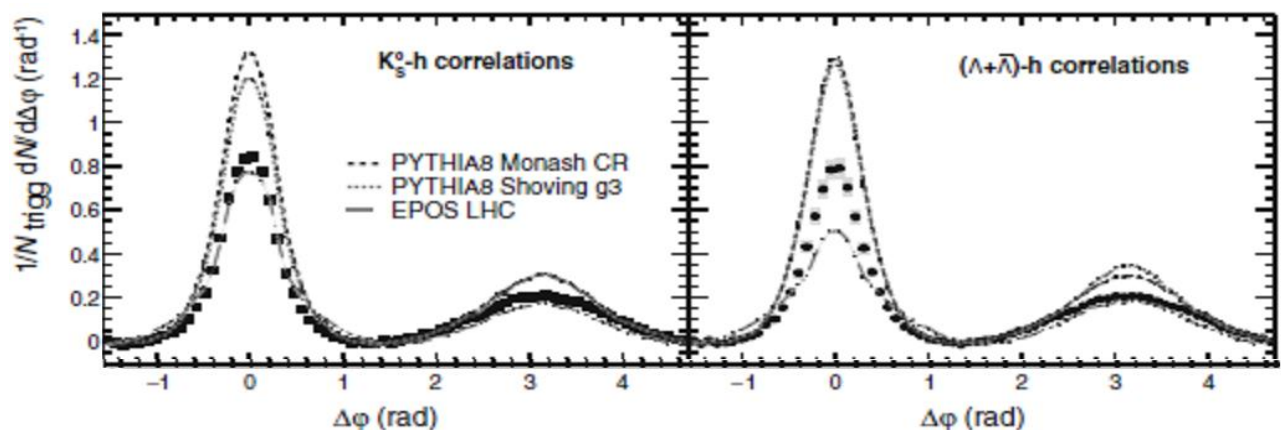


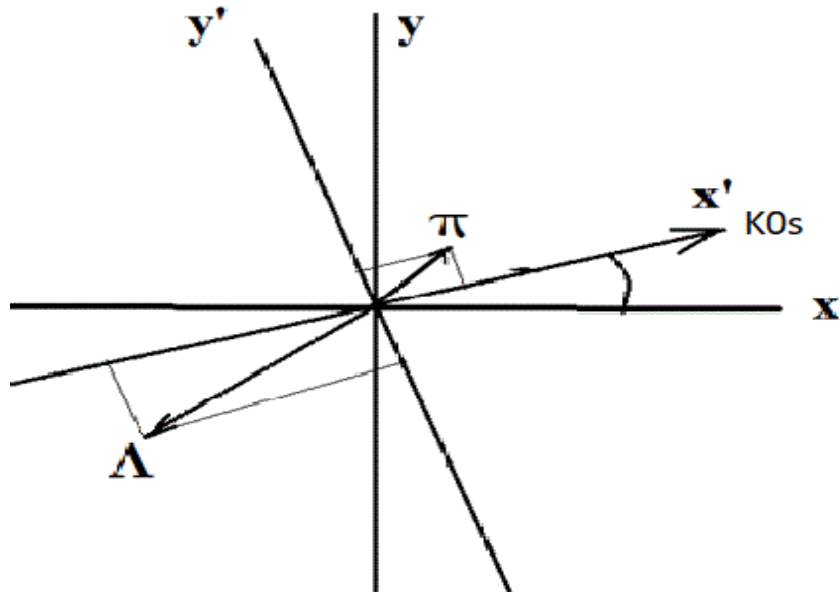
Fig. 1 An example of the raw same-event (left), mixed-event (middle) and final (mixed-event scaled, right) two-dimensional correlation function for K_S^0 -hadrons. The correlation functions were scaled with

1/1000 for better visibility. The plateau in the left and middle plot is caused by non-equal selection in η of the trigger and associated particle



Exp. data on K_S^0 - and (Λ anti- Λ)- hadron correlations were compared with predictions of Pythia, EPOS models.

2-Particle Pt Correlations



$$C(\vec{P}_{T,triger}, \vec{P}_{T,track}) = \frac{1}{N_{triger}} \frac{dN_{triger, track}}{d^2 P_{T,triger} d^2 P_{T,track}}$$

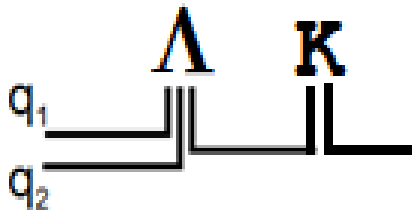
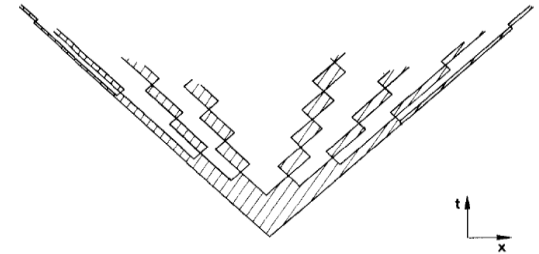
4 independent variables: $\vec{P}_{T,triger}$ and $\vec{P}_{T,track}$.

There are 3 independent variables with accounting the azimuthal symmetry –

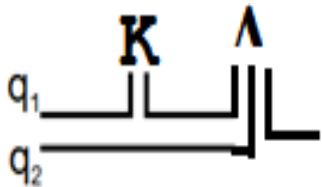
$|\vec{P}_{T,triger}|$, $P_{x,track}$ and $P_{y, track}$

$$\exp\left(-\frac{\pi m_{\perp}^2}{\kappa}\right) = \exp\left(-\frac{\pi m^2}{\kappa}\right) \exp\left(-\frac{\pi p_{\perp}^2}{\kappa}\right)$$

The correlations are connected with Schwinger mechanism of particle production



$$\vec{P}_{T,\Lambda} = \vec{P}_{T,qq} + \vec{P}_{T,S}, \quad \vec{P}_{T,K} = -\vec{P}_{T,\bar{S}} + \vec{P}_{T,q}$$



$$\begin{aligned} \vec{P}_{T,\Lambda} \cdot \vec{P}_{T,K} &= -\vec{P}_{T,qq} \cdot \vec{P}_{T,\bar{S}} + \vec{P}_{T,qq} \cdot \vec{P}_{T,q} - |\vec{P}_{T,S}|^2 + \vec{P}_{T,S} \cdot \vec{P}_{T,q} \\ \langle \vec{P}_{T,\Lambda} \cdot \vec{P}_{T,K} \rangle &= 0 \qquad \qquad \qquad 0 \qquad \qquad \qquad -|\vec{P}_{T,S}|^2 \qquad \qquad \qquad 0 \end{aligned}$$

Method of study 2 particle's Pt-correlations

1. We calculated 1000000 proton-proton interactions at $\sqrt{S}=10$ GeV using **FTF** and **Pythia** generators in **SPDRoot** version 4.1.6.1

2. We selected events with production of K_s^0 -mesons, and calculated:

$$\cos(\varphi_{K_s^0}) = P_{x_{K_s^0}} / P_{t_{K_s^0}}$$

$$\sin(\varphi_{K_s^0}) = P_{y_{K_s^0}} / P_{t_{K_s^0}}$$

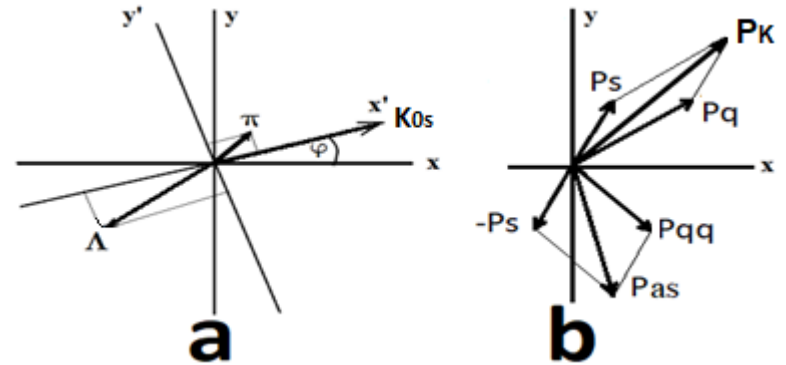
3. For these events we transformed P_x and P_y momenta of particles associated with Λ -hyperon in the new rotated coordinate system:

$$P_{x'} = P_x \cdot \cos(\varphi_{K_s^0}) + P_y \cdot \sin(\varphi_{K_s^0})$$

$$P_{y'} = -P_x \cdot \sin(\varphi_{K_s^0}) + P_y \cdot \cos(\varphi_{K_s^0})$$

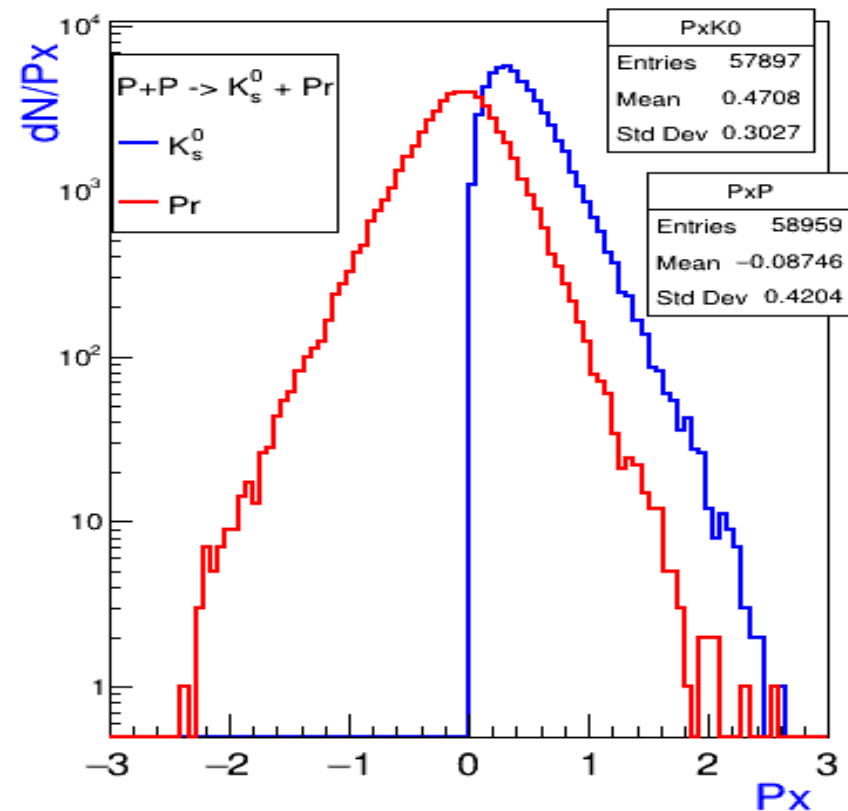
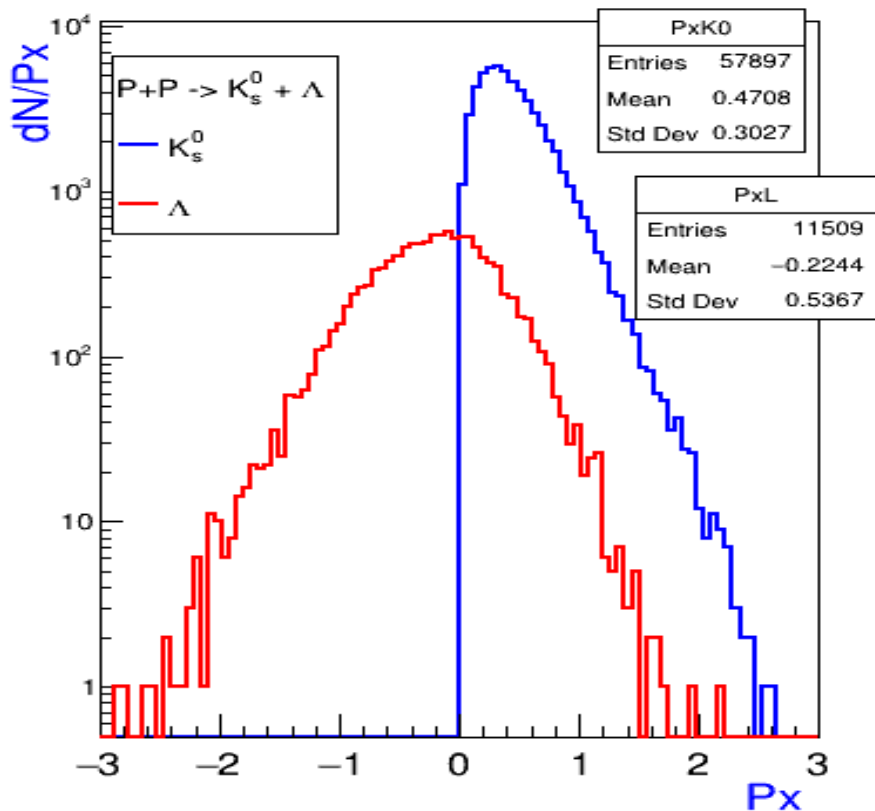
(It is obviously, that for K_s^0 $P_{x'}=P_t$; $P_{y'}=0$)

4. We performed analysis of transformed $P_{x'}$ and $P_{y'}^2$ of particles produced with K_s^0 - mesons.



Comparison of P_x' of Λ -hyperons and protons associated with K_s^0 - mesons in PP- events calculated by **FTF**

$$\langle P_x'_{K_s^0} \rangle = 470.8 \text{ MeV/c}, \quad N_{K_s^0} = 57897$$

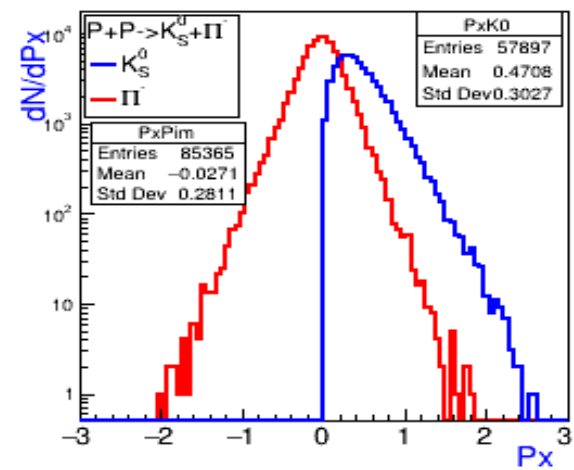
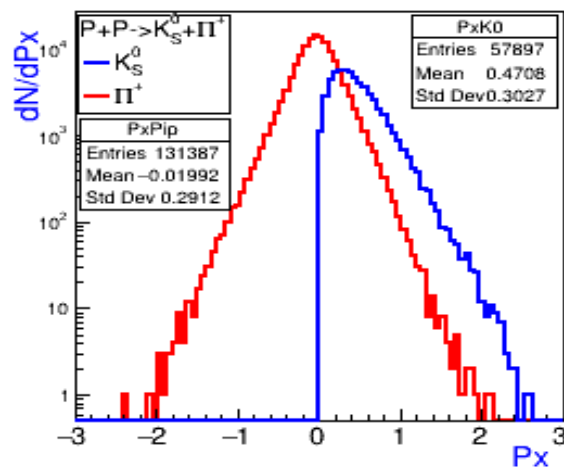
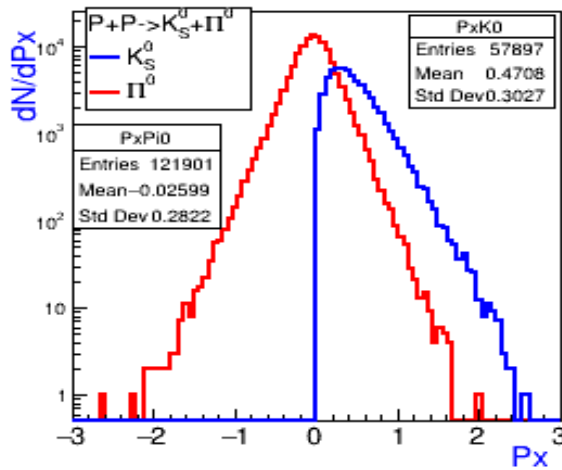
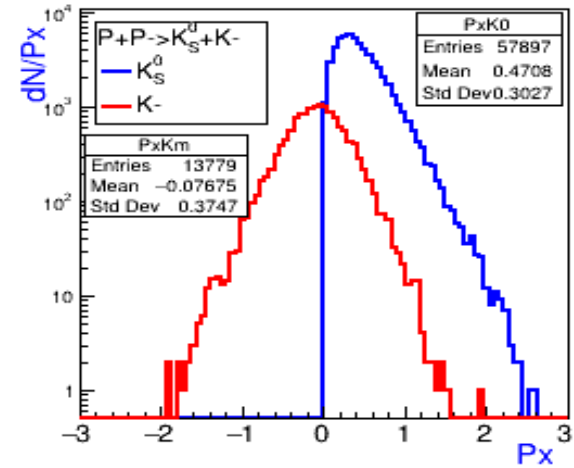
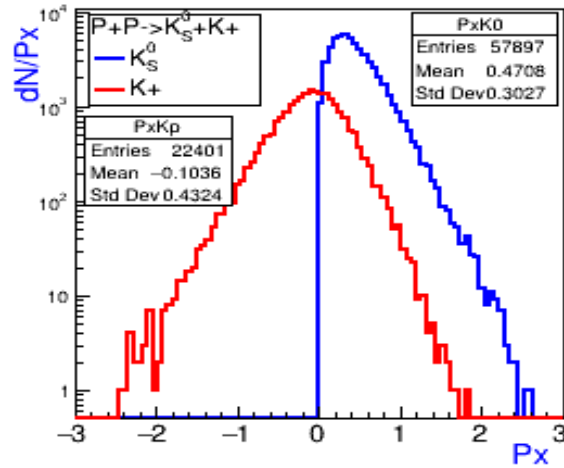
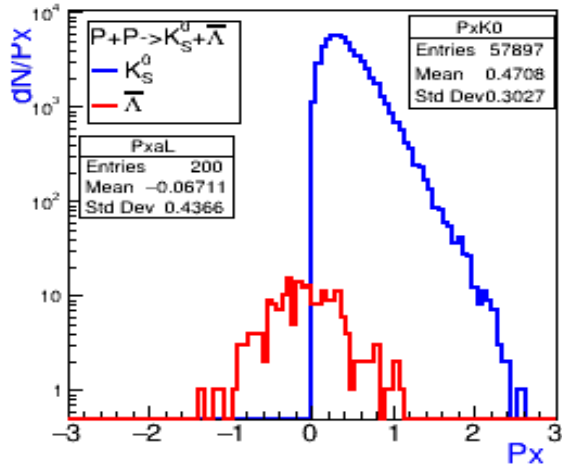


$$\langle P_x'_{\Lambda} \rangle = -224 \text{ MeV/c}, \quad N_{\Lambda} = 11509$$

$$\langle P_x'_{Pr} \rangle = -87.5 \text{ MeV/c}, \quad N_{Pr} = 58959$$

Px' of particles associated with K_S^0 – meson in PP-events calculated by **FTF** generator

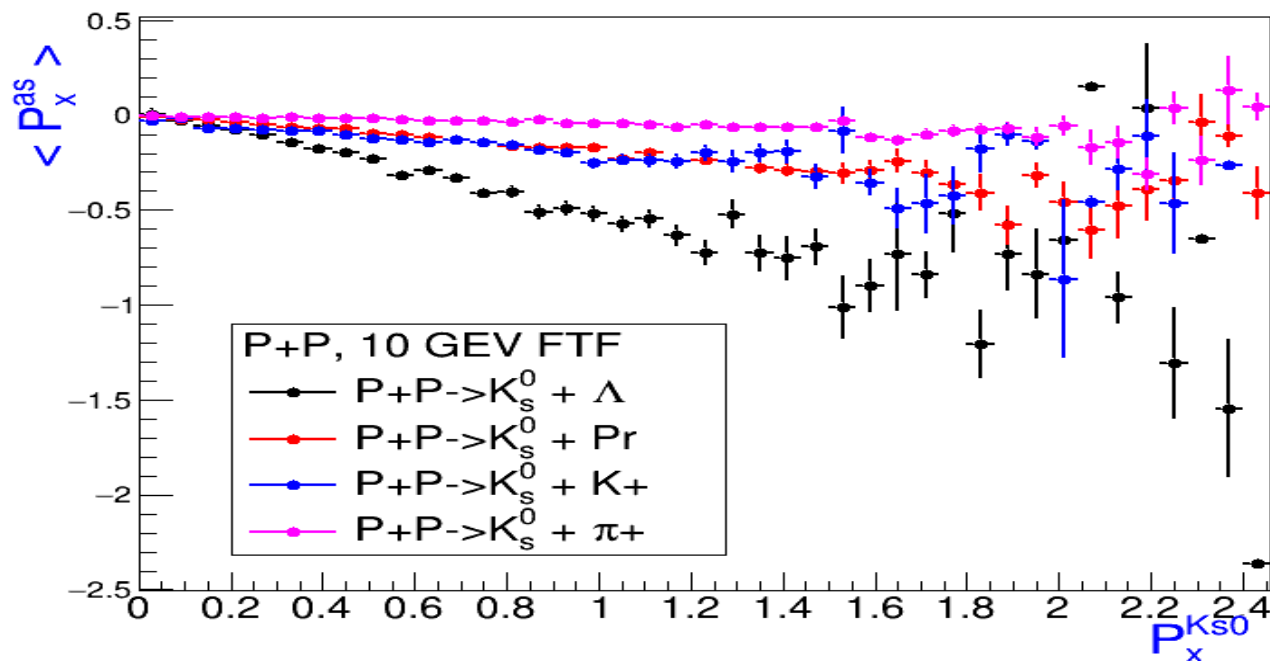
$$\langle Px' K_S^0 \rangle = 470.8 \text{ MeV/c}$$



$$\langle Px'_{\Lambda\text{bar}} \rangle = -67.1 \text{ MeV/c}, \quad \langle Px'_{K^+} \rangle = -103.6 \text{ MeV/c}, \quad \langle Px'_{K^-} \rangle = -78.8 \text{ MeV/c}$$

$$\langle Px'_{\pi^0} \rangle = -26 \text{ MeV/c}, \quad \langle Px'_{\pi^+} \rangle = -20 \text{ MeV/c}, \quad \langle Px'_{\pi^-} \rangle = -27 \text{ MeV/c}$$

Correlations of mean P_x' of Λ -hyperons, K^+ , protons and π -mesons with K_s^0 – meson P_x' in PP-events calculated by **FTF** and **PyTHIA**



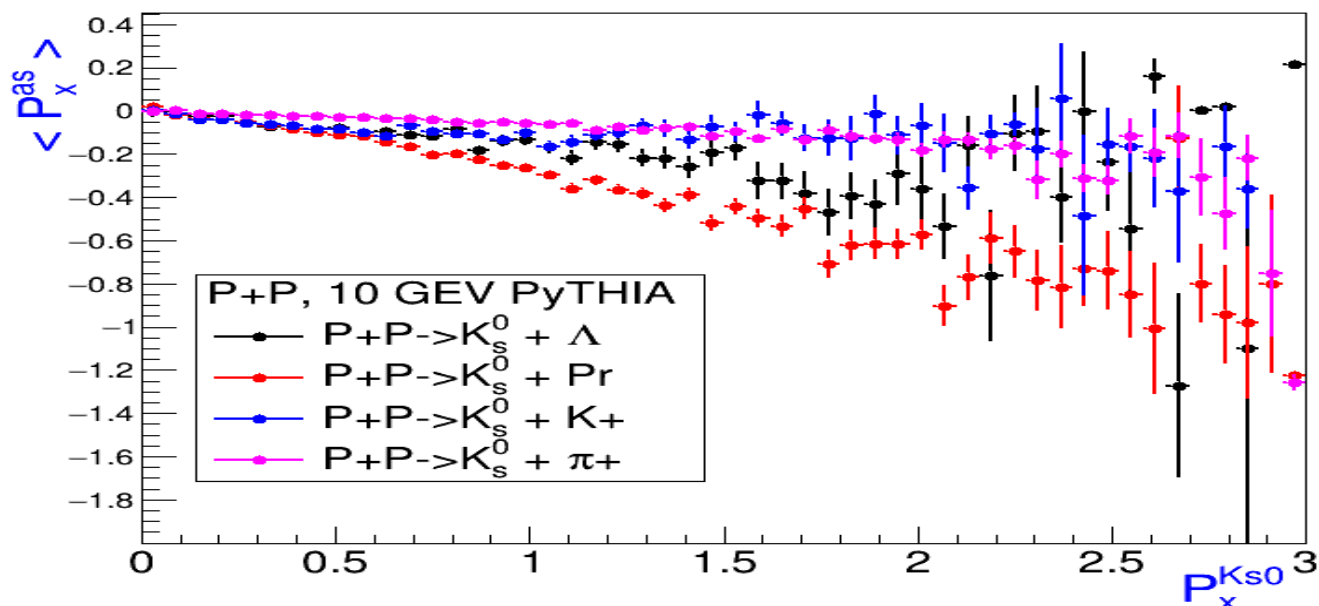
FTF

$$\langle P_x'_{\Lambda} \rangle = -224 \text{ MeV}/c$$

$$\langle P_x'_{K^+} \rangle = -103.6 \text{ MeV}/c$$

$$\langle P_x'_{Pr} \rangle = -87.5 \text{ MeV}/c$$

$$\langle P_x'_{\pi^+} \rangle = -20 \text{ MeV}/c$$



PyTHIA

$$\langle P_x'_{Pr} \rangle = -128 \text{ MeV}/c$$

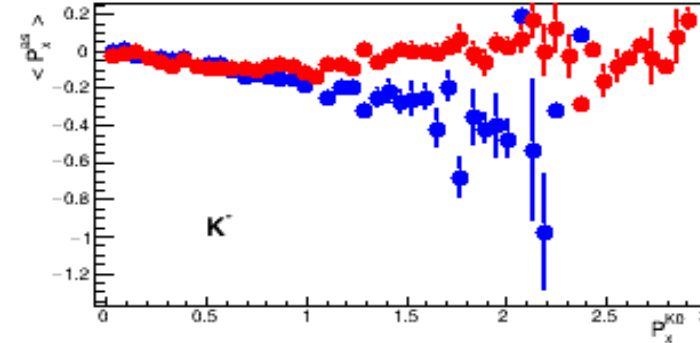
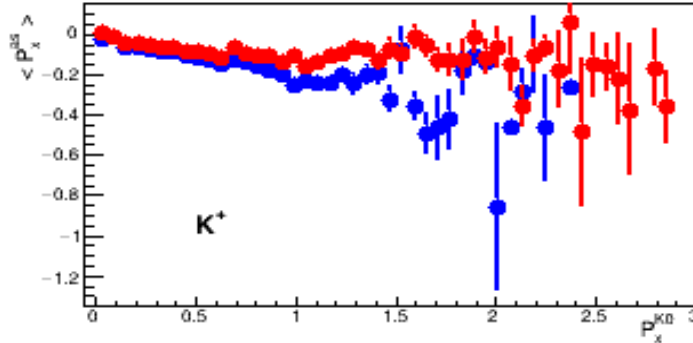
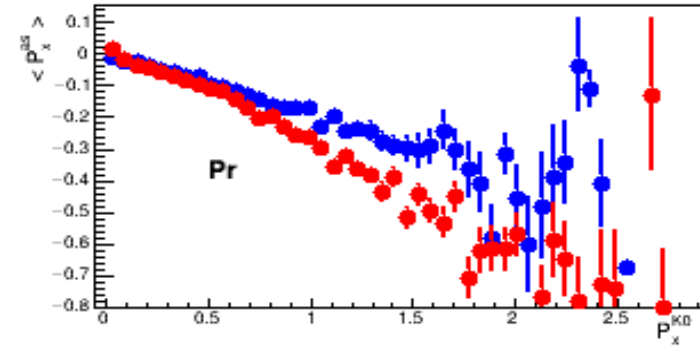
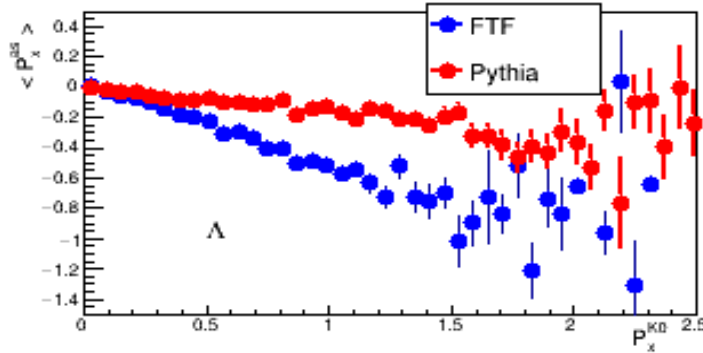
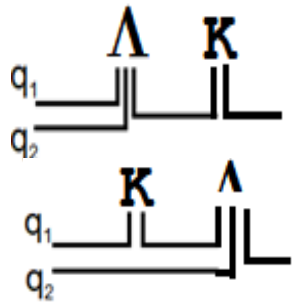
$$\langle P_x'_{\Lambda} \rangle = -87.8 \text{ MeV}/c$$

$$\langle P_x'_{K^+} \rangle = -74.8 \text{ MeV}/c$$

$$\langle P_x'_{\pi^+} \rangle = -31 \text{ MeV}/c$$

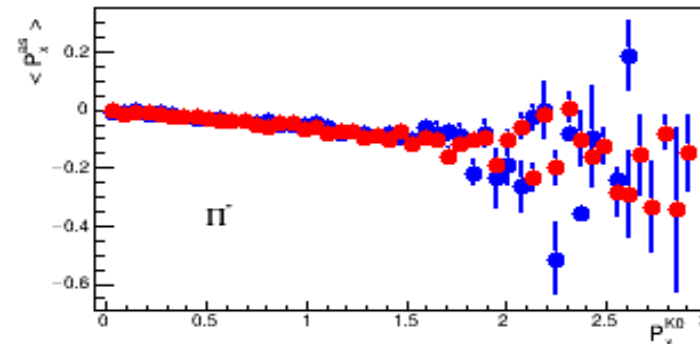
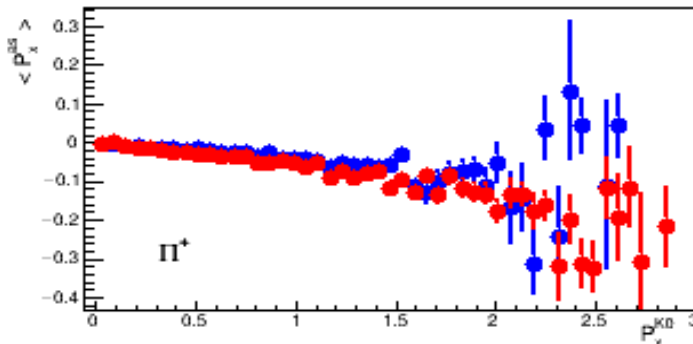
Comparison of correlations of mean P_x' of Λ hyperons, protons, K-mesons and π -mesons with K_s^0 – meson P_x' in events calculated by **PYTHIA** and **FTF**

FTF

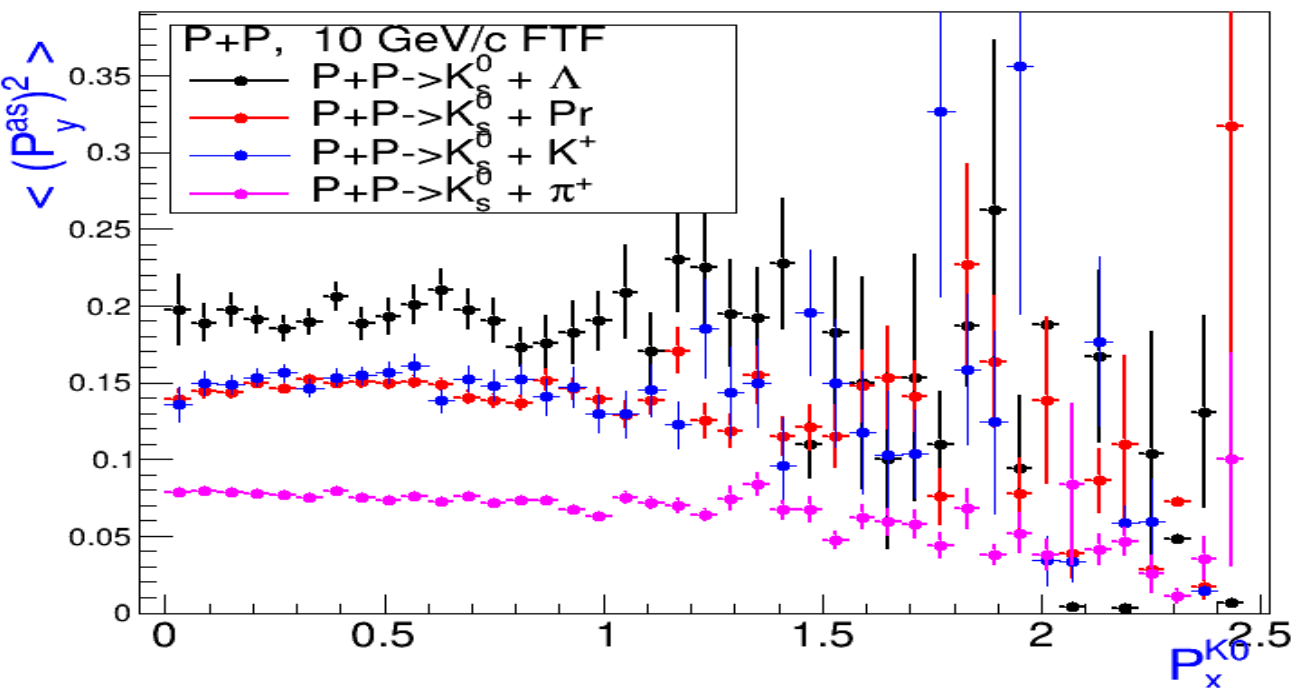


PyTHIA
Beam remnant
fragmentation

Where is
truth?



Correlations of mean $P_y'^2$ of Λ - hyperons, protons K and π mesons with K_s^0 – meson P_x' in PP-events calculated by **FTF and PyTHIA**



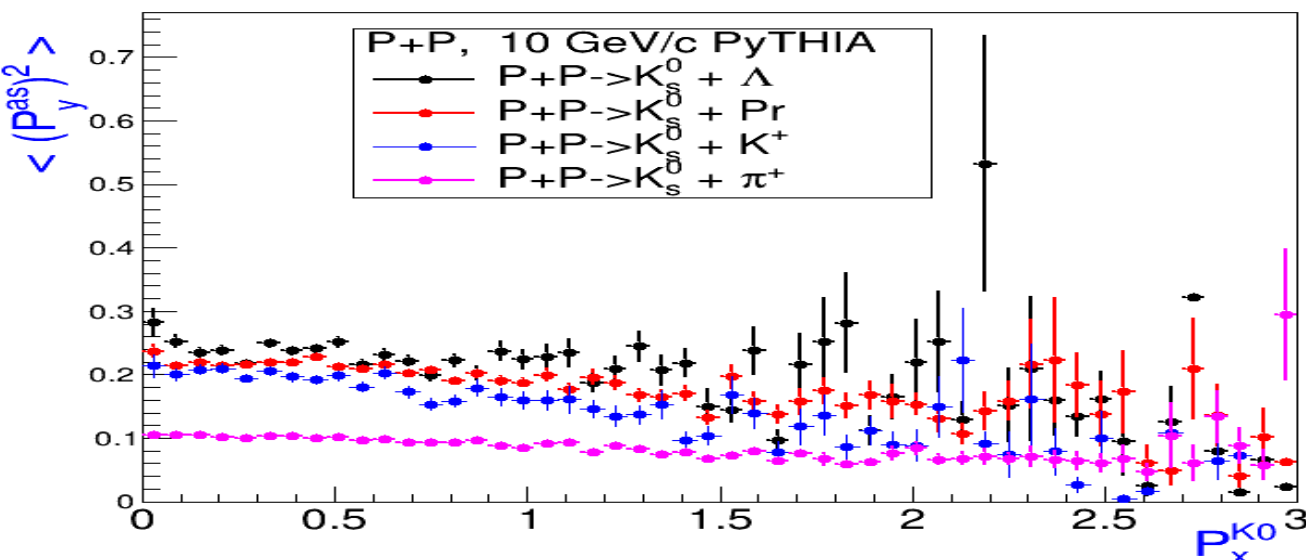
FTF

$$\langle P_y'^2 \Lambda \rangle = 193 \text{ (MeV/c)}^2$$

$$\langle P_y'^2 K^+ \rangle = 151 \text{ (MeV/c)}^2$$

$$\langle P_y'^2 Pr \rangle = 147 \text{ (MeV/c)}^2$$

$$\langle P_y'^2 \pi^+ \rangle = 75 \text{ (MeV/c)}^2$$



PyTHIA

$$\langle P_y'^2 \Lambda \rangle = 232 \text{ (MeV/c)}^2$$

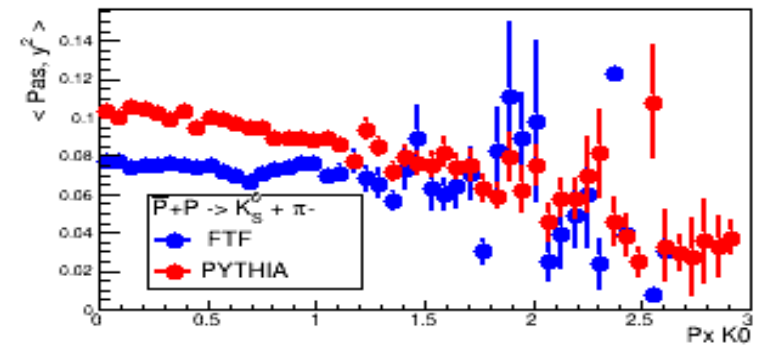
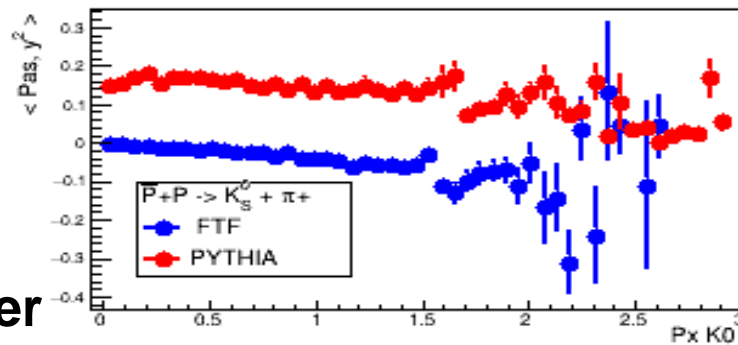
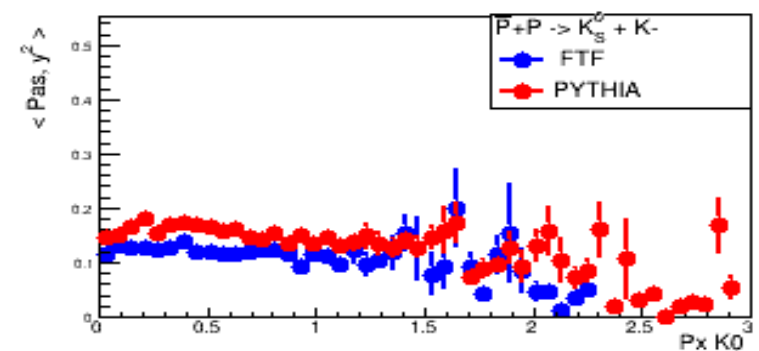
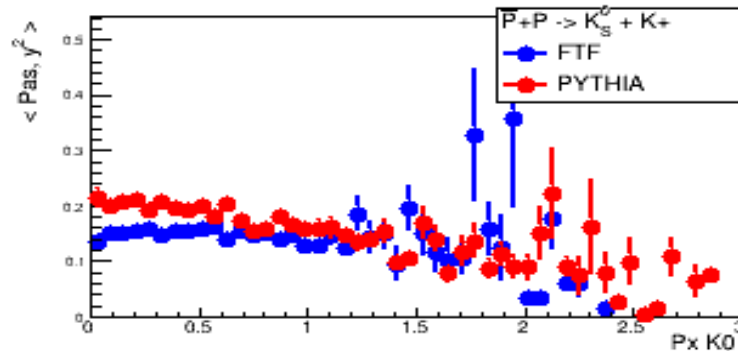
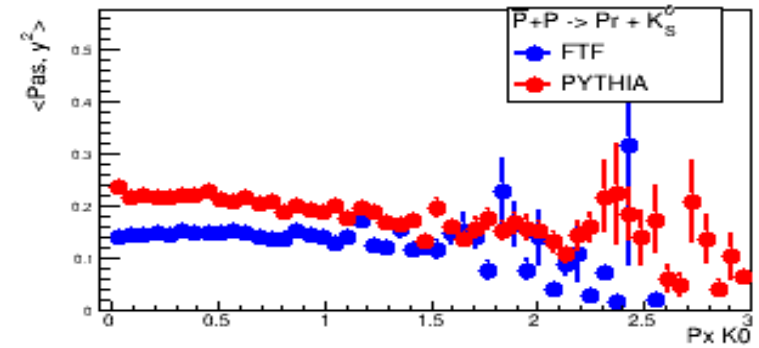
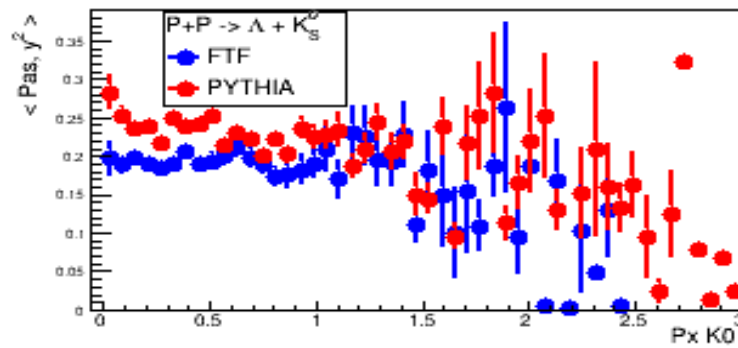
$$\langle P_y'^2 Pr \rangle = 211 \text{ (MeV/c)}^2$$

$$\langle P_y'^2 K^+ \rangle = 188 \text{ (MeV/c)}^2$$

$$\langle P_y'^2 \pi^+ \rangle = 98 \text{ (MeV/c)}^2$$

Comparison of correlations of mean P_T^2 of Λ hyperons, protons, K^- and π^- mesons with K_S^0 – meson P_T in events calculated by FTF and **PYTHIA**

Mt scaling



Nadine Fischer

Torbjörn Sjöstrand

Thermodynamical String Fragmentation

JHEP 1701 (2017) 140

Table of Numbers and mean values of P_x and P_y^2 of particles associated with K_s^0 – meson in PP-events at $\sqrt{S} = 10$ GeV

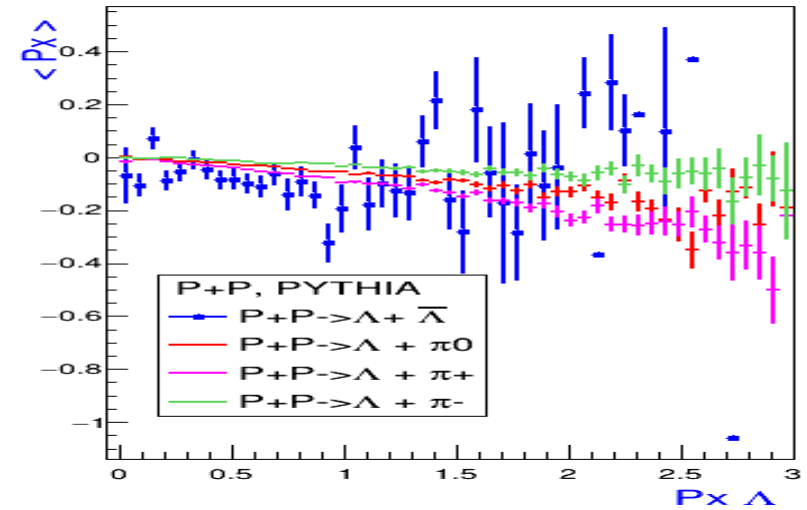
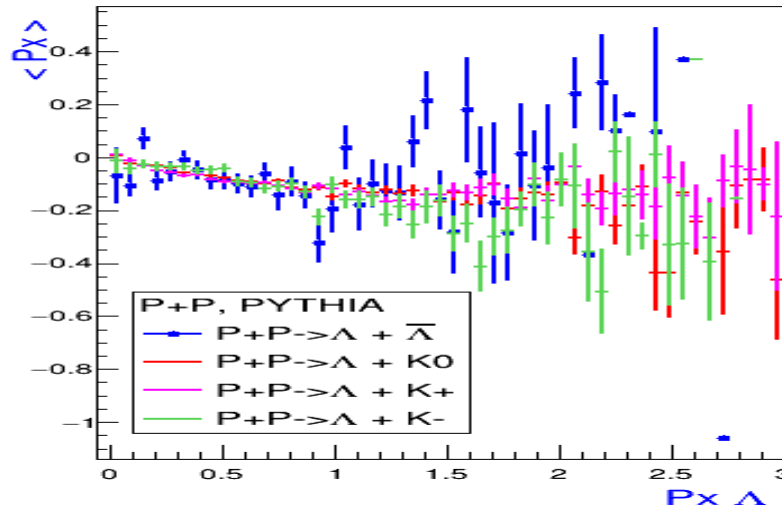
Generator	K_s^0	Λ	K^+	K^-	Λ bar	Proton	π^+	π^-	π^0
FTF	N 57897	N 11509	N 22401	N 13779	N 200	N 58959	N 131387	N 85365	N 121901
Pythia	N 78850	N 28219	N 29466	N 20857	N 573	N 74571	N 201812	N 129411	N 182025
FTF	$\langle P_x \rangle$ 471	$\langle P_x \rangle$ -224	$\langle P_x \rangle$ -104	$\langle P_x \rangle$ -77	$\langle P_x \rangle$ -67	$\langle P_x \rangle$ -87	$\langle P_x \rangle$ -30	$\langle P_x \rangle$ -27	$\langle P_x \rangle$ -26
Pythia	$\langle P_x \rangle$ 523	$\langle P_x \rangle$ -88	$\langle P_x \rangle$ -75	$\langle P_x \rangle$ -63	$\langle P_x \rangle$ -77	$\langle P_x \rangle$ -128	$\langle P_x \rangle$ -31	$\langle P_x \rangle$ -33	$\langle P_x \rangle$ -34
FTF	$\langle P_y^2 \rangle$ 0	$\langle P_y^2 \rangle$ 193	$\langle P_y^2 \rangle$ 151	$\langle P_y^2 \rangle$ 122	$\langle P_y^2 \rangle$ 202	$\langle P_y^2 \rangle$ 147	$\langle P_y^2 \rangle$ 75	$\langle P_y^2 \rangle$ 73	$\langle P_y^2 \rangle$ 72
Pythia	$\langle P_y^2 \rangle$ 0	$\langle P_y^2 \rangle$ 232	$\langle P_y^2 \rangle$ 188	$\langle P_y^2 \rangle$ 158	$\langle P_y^2 \rangle$ 222	$\langle P_y^2 \rangle$ 211	$\langle P_y^2 \rangle$ 98	$\langle P_y^2 \rangle$ 97	$\langle P_y^2 \rangle$ 91

Summary

1. We observe strong **2-particle Pt correlations** between K_s^0 mesons and strange particles in **PP interactions** according to Geant4 FTF model.
2. Event generators – **Pythia** and **Geant4 FTF** give different predictions for these correlations. **FTF** model predicts stronger correlations between strange particles than **Pythia** model.
3. According to **Pythia** generator, **2-particle Pt correlations** between K_s^0 mesons and protons stronger than in FTF generator.
4. **FTF** predicts lower values of mean P_T^2 of associated particles with K_s^0 mesons than **PyTHIA** generator.
5. The **Pt correlations** are connected with main assumptions of various **string models** used in **Pythia** and **Geant4 FTF** .

Study of correlations allows tuning and calibration of the main simulation generators -- Pythia and Geant4 in high energy physics!

Correlations of mean P_x' , $P_y'^2$ of Λ -bar hyperons, K and π mesons with Λ hyperon P_x' in PP-events calculated by **PYTHIA**



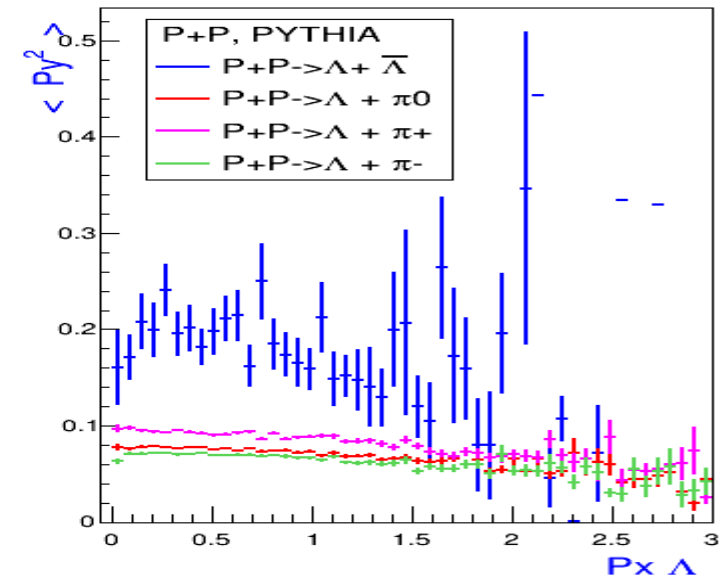
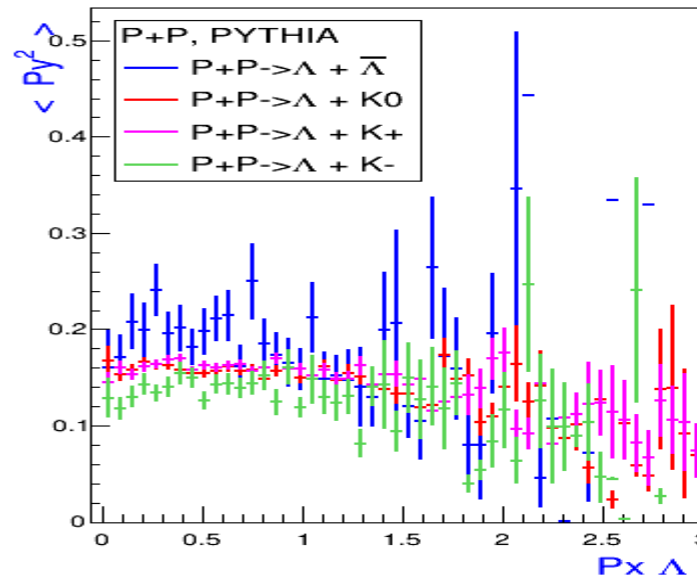
aLY%Lam

Mt scaling

Nadine Fischer and
Torbjörn Sjöstrand

Thermodynamical
String Fragmenta-
tion

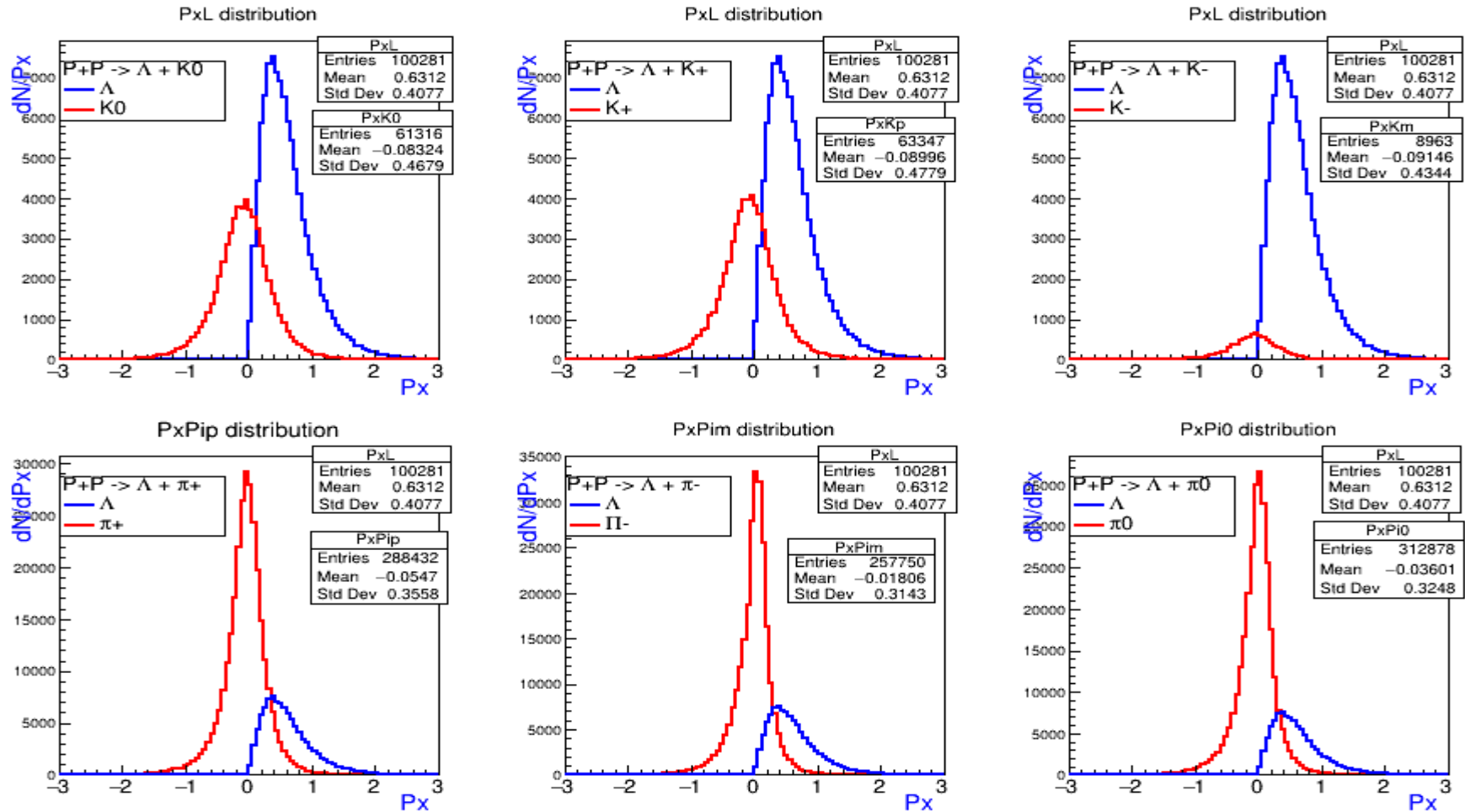
JHEP 1701 (2017) 140



$$\langle P_y'^2 \Lambda\text{bar} \rangle = 193 \text{ (MeV/c)}^2 \quad \langle P_y'^2 K^0 \rangle = 156 \text{ (MeV/c)}^2 \quad \langle P_y'^2 \pi^0 \rangle = 74 \text{ (MeV/c)}^2$$

Px' of particles associated with Λ hyperons in PP- events calculated by **Pythia**

We calculated 1000000 PP-events at $\sqrt{S}=10$ GeV using **Pythia** in SPDRoot

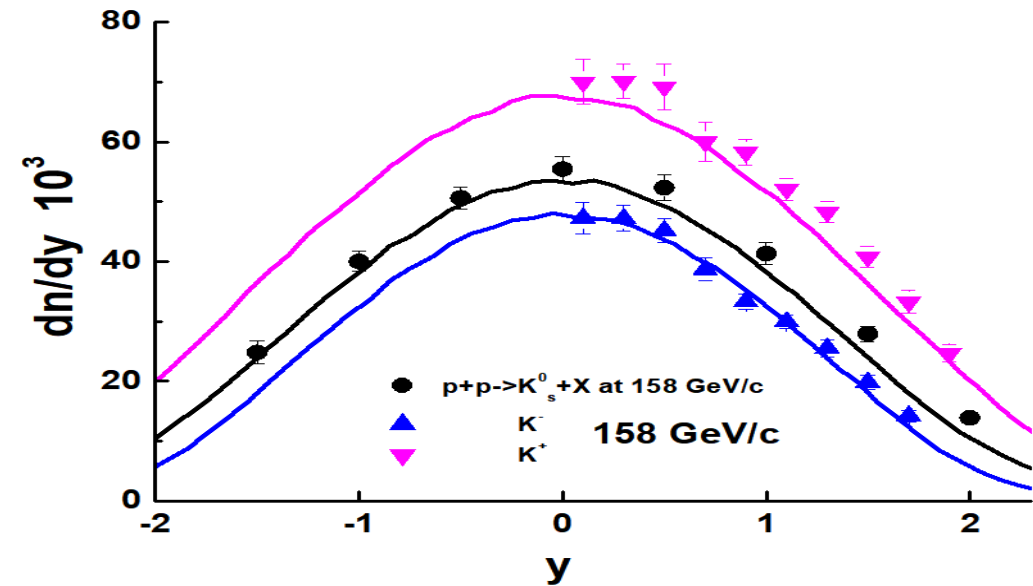
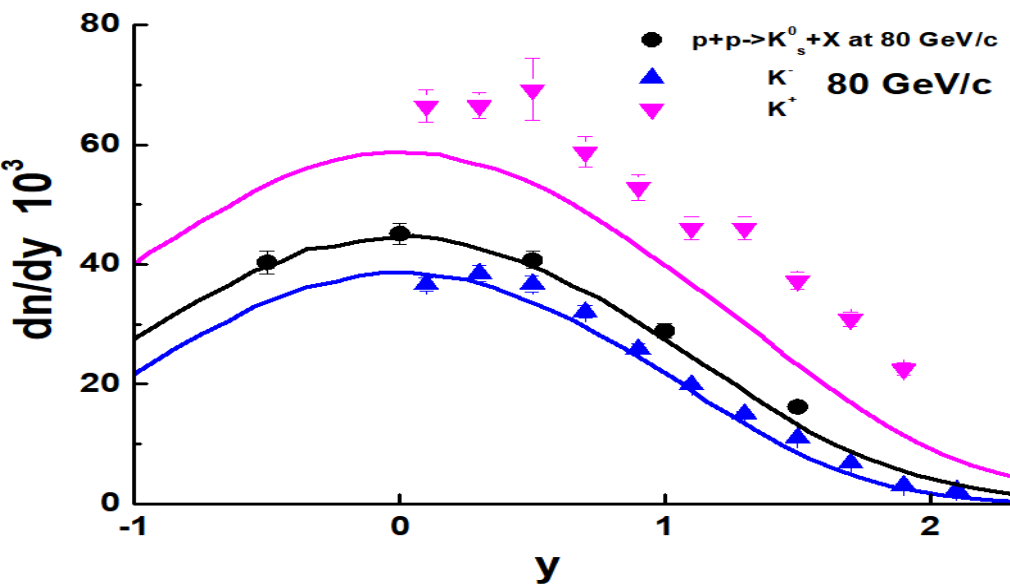
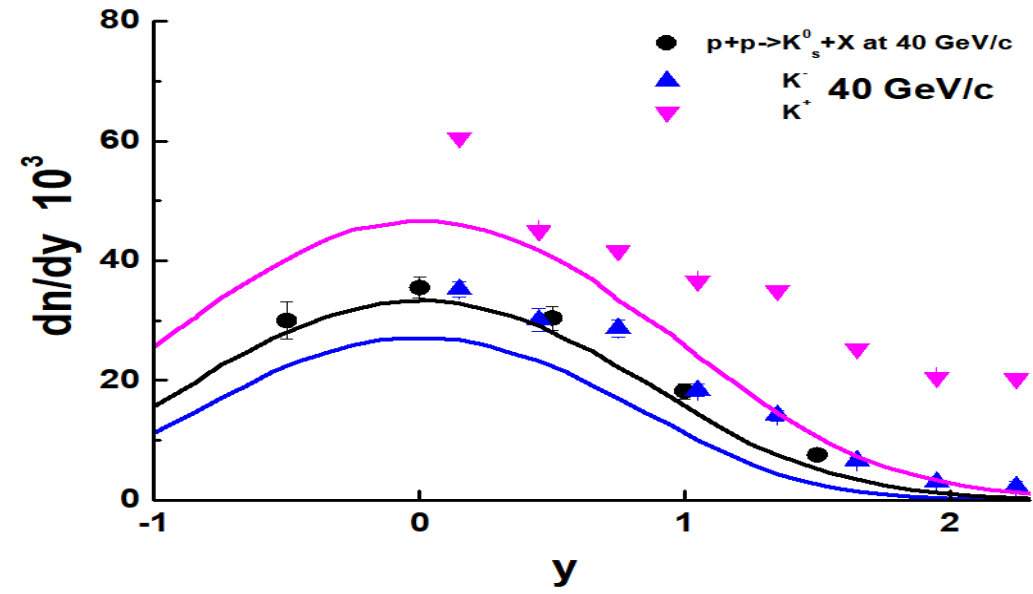
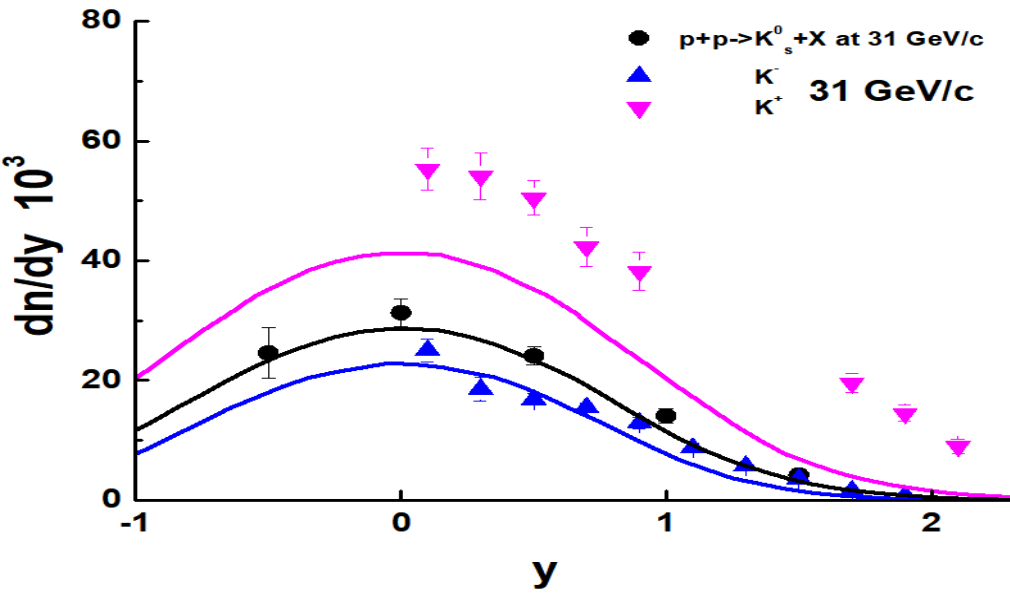


$\langle P_x'_{\Lambda} \rangle = 613$ MeV/c, $N_{\Lambda} = 100281$; $\langle P_x'_{\Lambda\bar{}} \rangle = -80$ MeV/c, $N_{\Lambda\bar{}} = 2731$

$\langle P_x'_{K0} \rangle = -83$ MeV/c, $\langle P_x'_{K+} \rangle = -90$ MeV/c, $\langle P_x'_{K-} \rangle = -91$ MeV/c

$\langle P_x'_{\pi^0} \rangle = -36$ MeV/c, $\langle P_x'_{\pi^+} \rangle = -55$ MeV/c, $\langle P_x'_{\pi^-} \rangle = -18$ MeV/c

K^+ , K^- and K^0 s in FTF model



All O.K. with K^0 s. K^- ~ O.K. There is exp. problem with K^+ !