

## Analysis of $\Lambda$ -hyperon production in carbon-nucleus run



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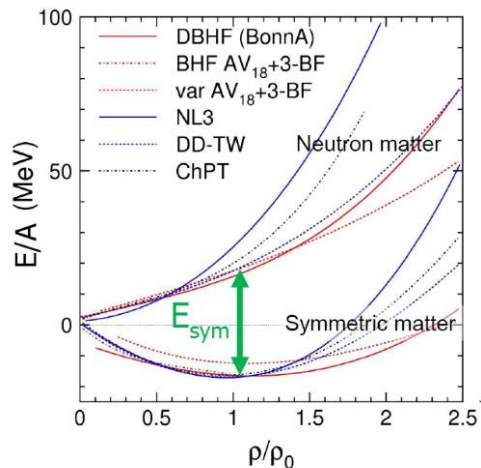
**Scientific adviser:** Yu. Stepanenko

**Scientific supervisor:** M. Zavertyaev

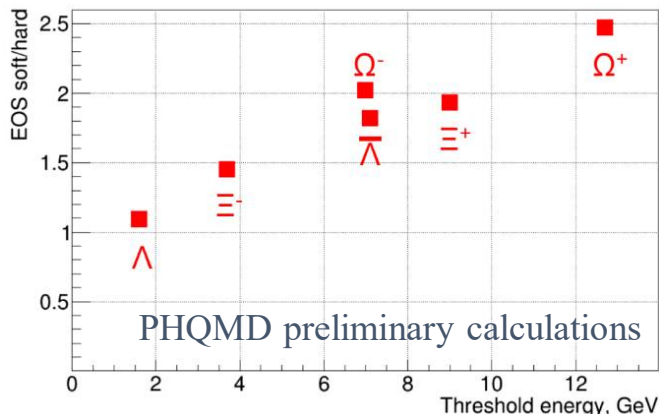
**08.10.2024**

# Physical motivation BM@N experiment

Ch.Fuchs, EPJA 30 (2006) 5

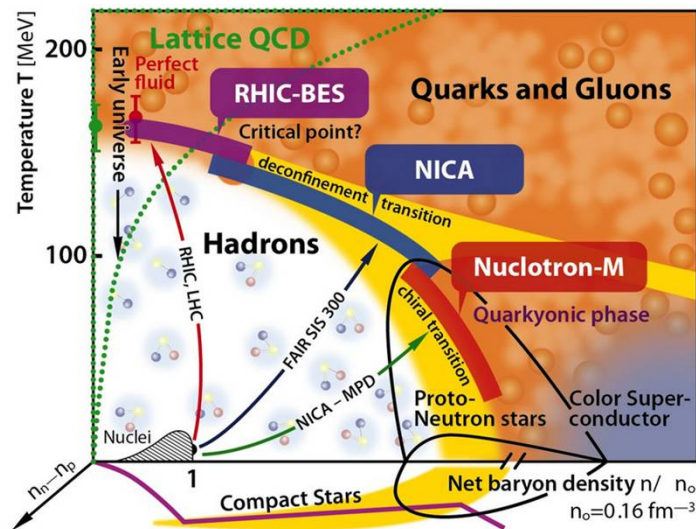
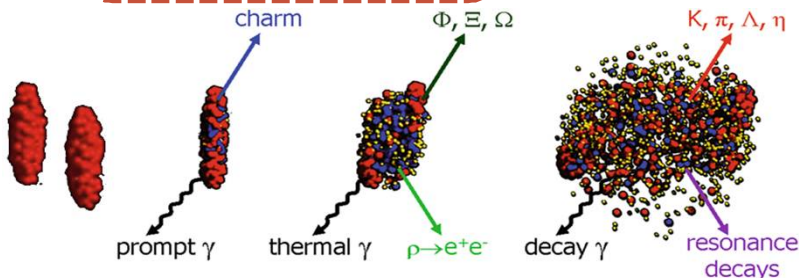
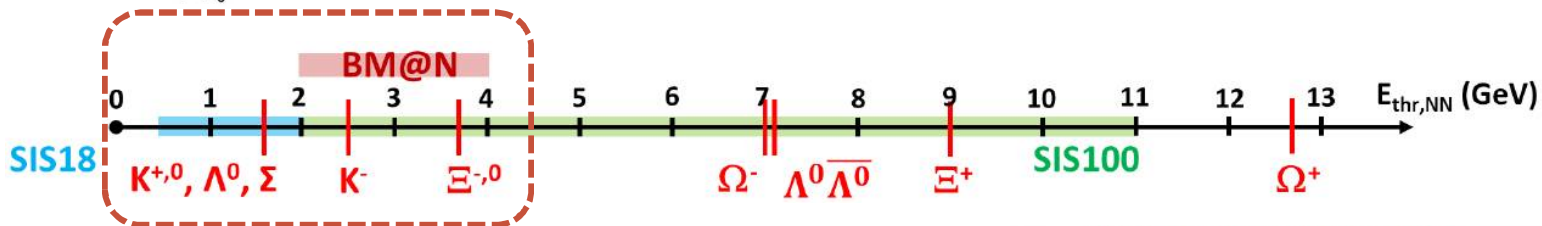


Hyperon yield in 4A GeV Au+Au:  
soft EOS (K=240 MeV) / hard EOS (K=350) MeV



**EoS study for symmetric matter at  $\rho/\rho_0 = 3 - 5$ ,  $\rho_0 = 0.16\text{fm}^{-3}$ :**

- Elliptical flow of protons, mesons and hyperons;
- Sub-threshold production of strange mesons and hyperons extract nuclear;
- Incompressibility ( $K_{mn}$ ) from the modeled data;



**EoS:** The relation between density, pressure, temperature, energy and isospin asymmetry:

$$E_A(\rho, \delta) = E_A(\rho, 0) + E_A(\rho) \delta^2$$

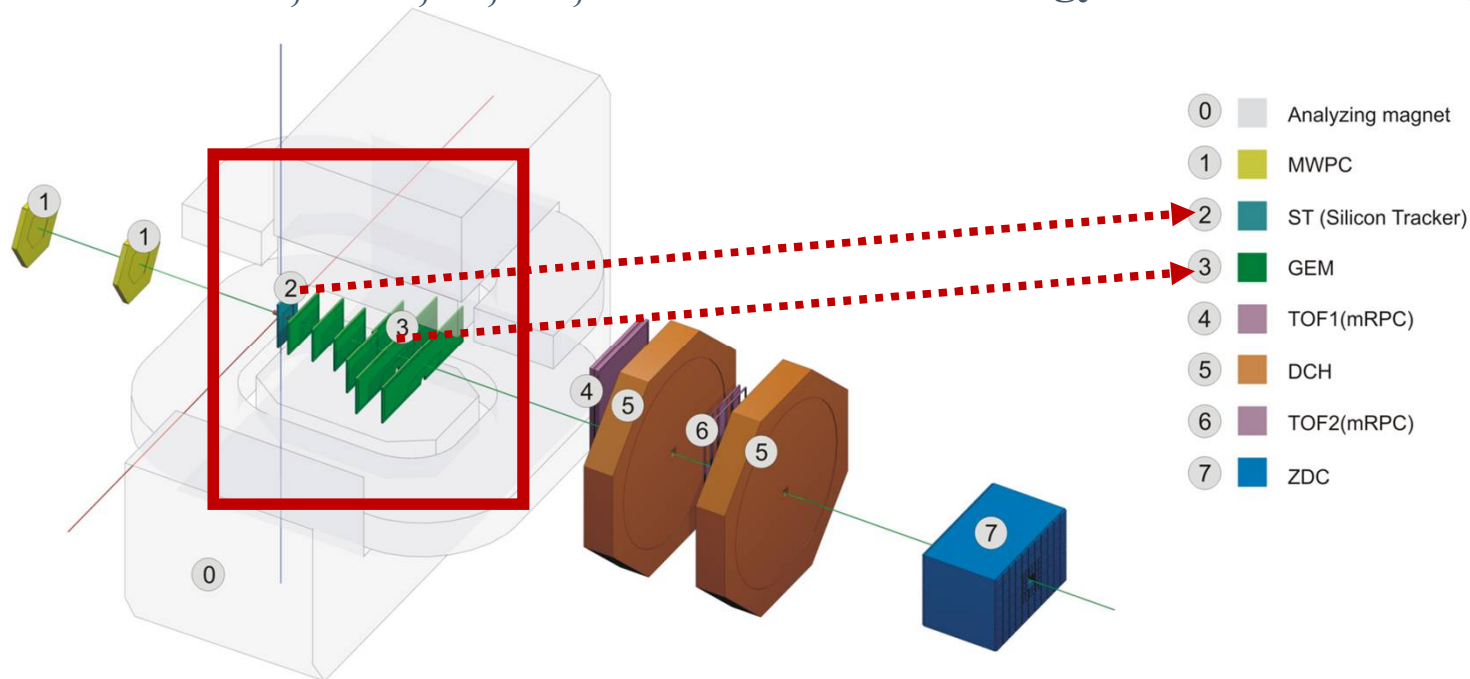
$$\delta = (\rho_n - \rho_p) / \rho$$

Incompressibility of the nucleus:  $K_{mn} = 9\rho^2 \frac{\partial^2}{\partial \rho^2} (E/A)|_{\rho=\rho_0}$

# Setup scheme

$C + A \rightarrow X$ ,  $A : C, Al, Cu, Pb$

Energy beam = 4.0 AGeV, 4.5 AGeV



## Central tracker:

- One plane of a forward Si detector;
- 6 GEM stations:
  - o 5 GEM detectors ( $66 \times 41 \text{ cm}^2$ );
  - o 2 GEM detectors ( $163 \times 45 \text{ cm}^2$ );

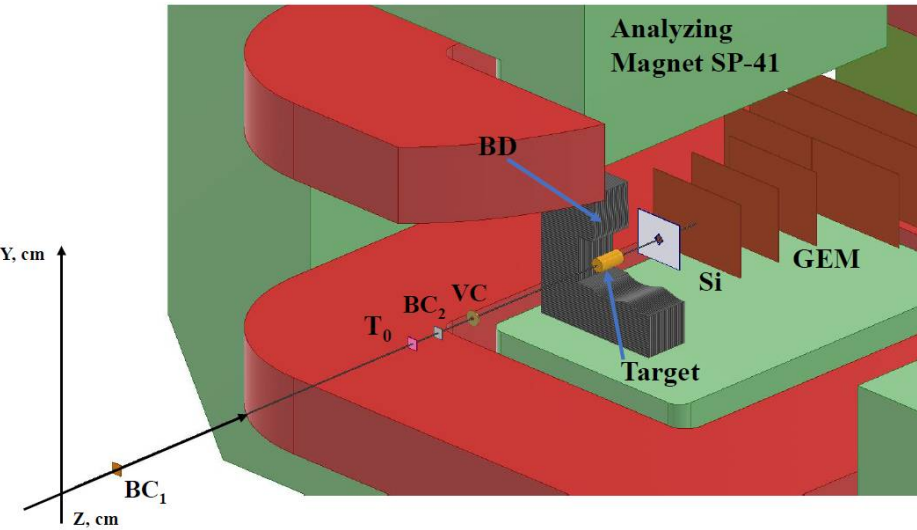
## Gas Electron Multiplier (GEM) system:

To measure momenta of a charged particle;

Event reconstruction in GEM in C+A interaction;

Triggers: BD, BC<sub>1</sub>, BC<sub>2</sub>, T<sub>0</sub>, VETO

# Event selection criteria



- 1 | Number of tracks in selected events:  
positive $\geq$ 1, negative $\geq$ 1
- 2 | Number of signals in the start detector:  $T_0=1$
- 3 | Number of signals in the beam counter:  
 $BC_2=1$
- 4 | Number of signals in the veto counter around  
the beam: Veto=0
- 5 | Trigger condition in the barrel detector: number  
of signals  $BD\geq 2$  or  $BD\geq 3$  (run dependent)

# Trigger efficiency

The trigger efficiency was evaluated by a convolution of the **GEANT simulation** of the trigger BD detector response to DCM-QGSM events with reconstructed  $\Lambda$  hyperons and the GEANT simulation of delta electrons.

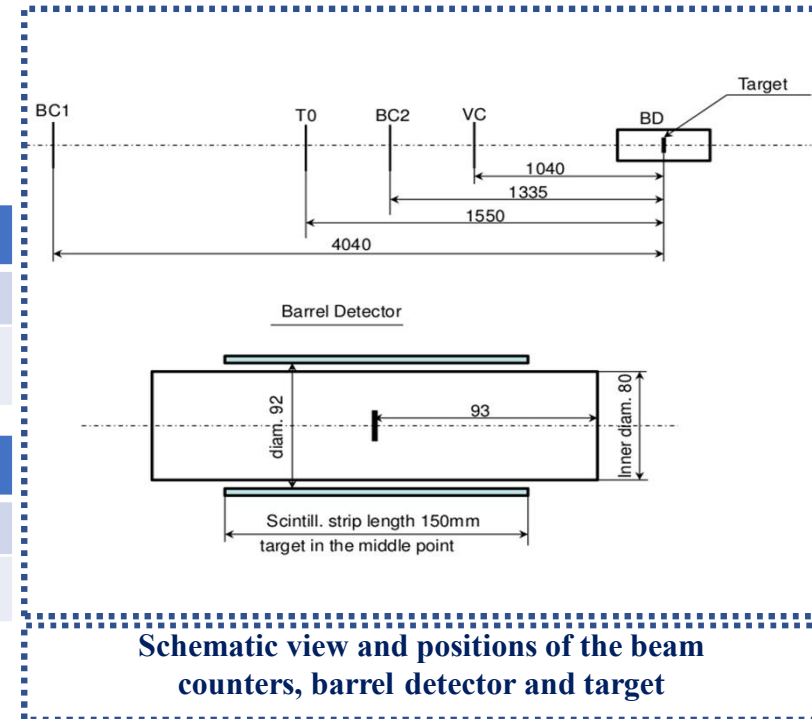
$$\epsilon_{trig} = N_{sim_{\Lambda}}(BD \geq n) / N_{sim_{all\Lambda}}$$

The **systematic** errors in **Table 1** cover:

- 1) Contribution of delta electrons;
- 2) The spread of the trigger efficiencies calculated for different  $y$  and  $p_T$  bins of the reconstructed  $\Lambda$ -hyperons;
- 3) Change in the trigger efficiency after correction of the simulated track multiplicity in agreement with the experimental data.

**Table 1. Trigger efficiency  $\epsilon_{trig}$**

4 AGeV	C	Al	Cu	Pb
$\epsilon_{trig}(BD \geq 2)$	$0.80 \pm 0.02$	-	-	-
$\epsilon_{trig}(BD \geq 3)$	-	$0.87 \pm 0.02$	$0.92 \pm 0.02$	$0.95 \pm 0.02$
4.5 AGeV	C	Al	Cu	Pb
$\epsilon_{trig}(BD \geq 2)$	$0.80 \pm 0.02$	-	-	-
$\epsilon_{trig}(BD \geq 3)$	-	$0.83 \pm 0.02$	$0.91 \pm 0.02$	$0.94 \pm 0.02$



$\epsilon_{trig}$  is used for evaluation of production cross section;

**1** | Gem's Efficiency(**next slide**, example C+C);

**2** | Track hits residual corrections\*;

**3** | Track hit position error corrections;

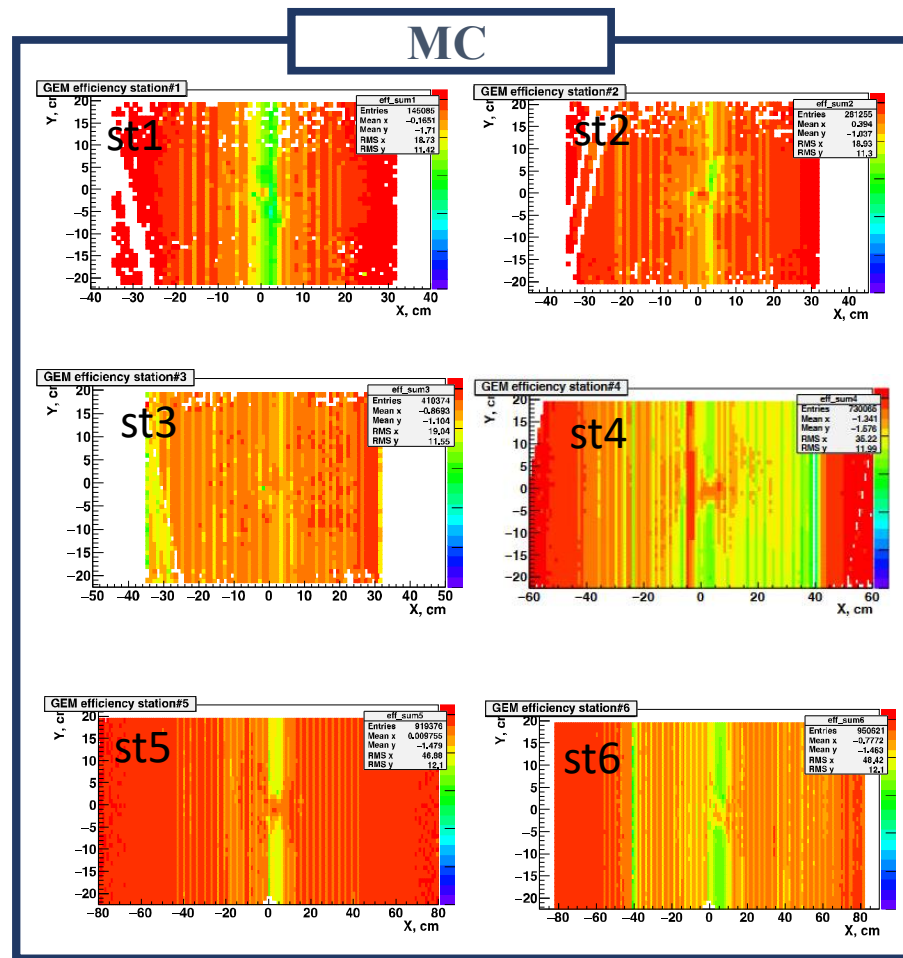
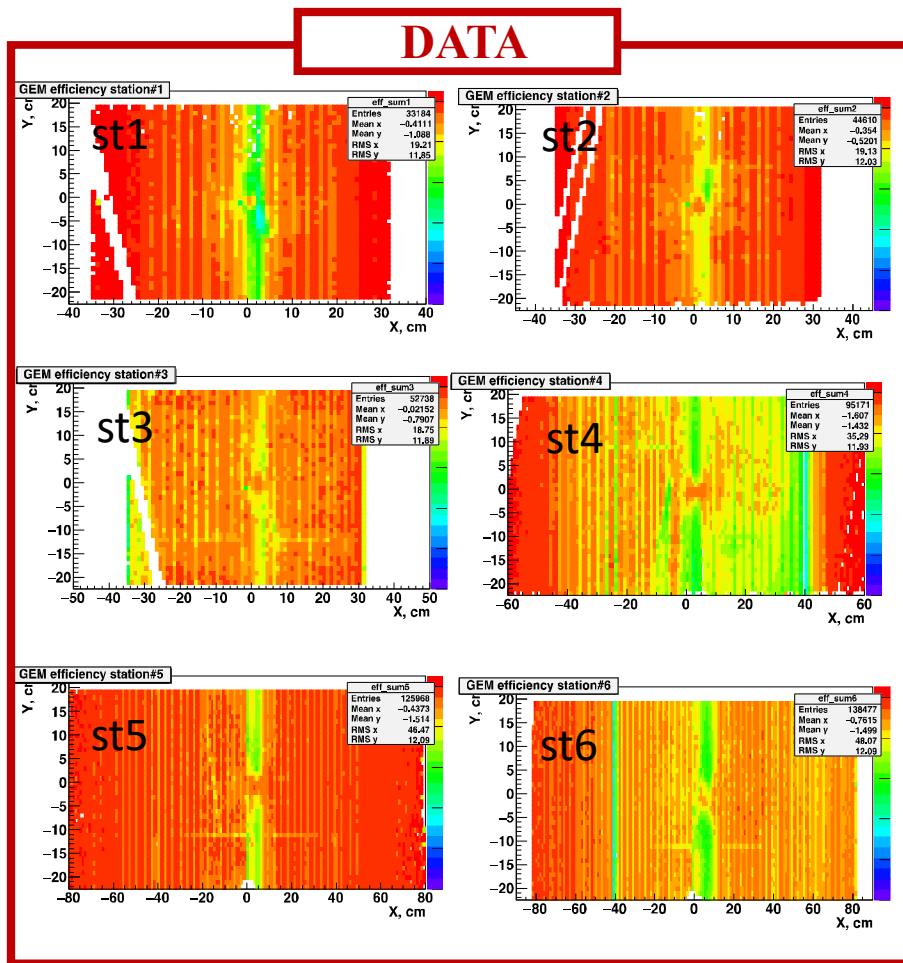
**4** | Residuals width vs. momentum corrections;

Yury Stepanenko

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\*K. A. Alishina, Yu. Yu. Stepanenko, A.Y Khukhaeva” Gem residuals corrections in monte-carlo simulation for the run 6 at the BM@N experiment”, PEPAN letters – volume 19, part 5, 2022

# GEM efficiencies comparison Data/MC (4.0GeV C+C) after applying effs to MC

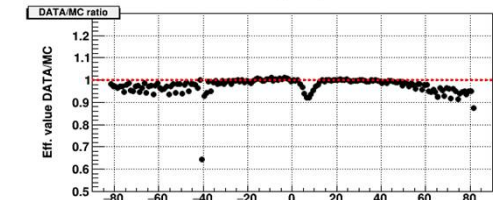
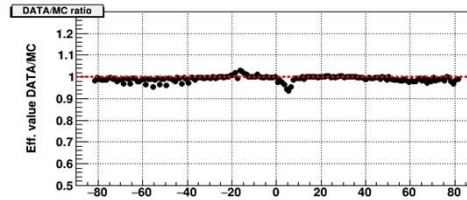
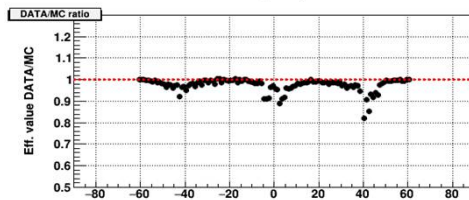
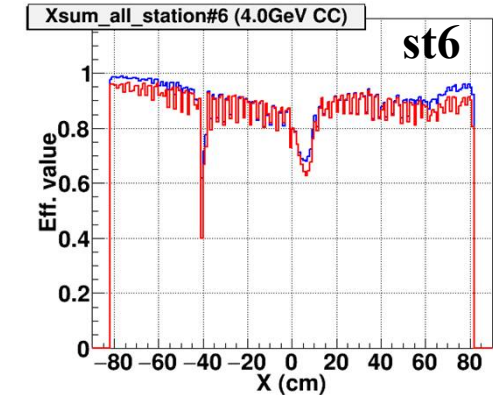
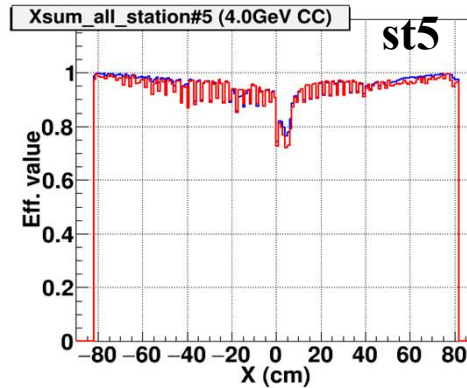
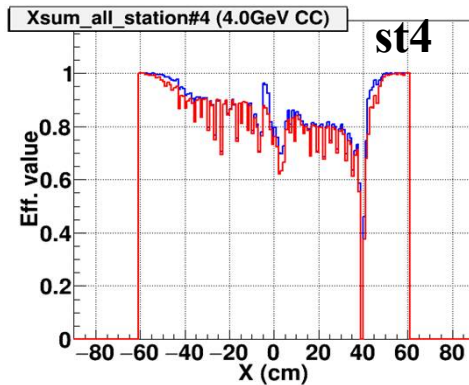
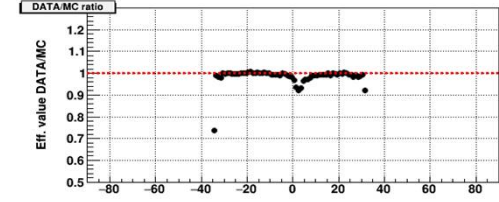
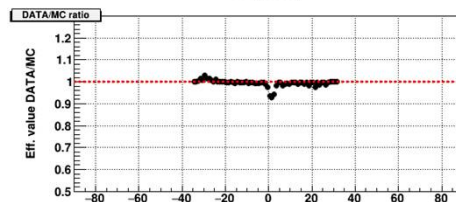
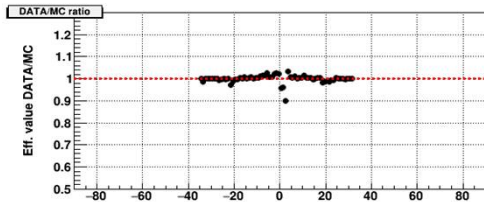
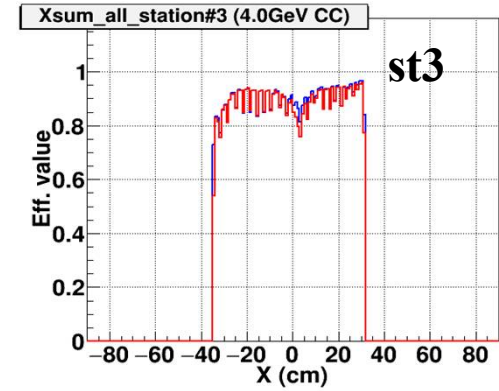
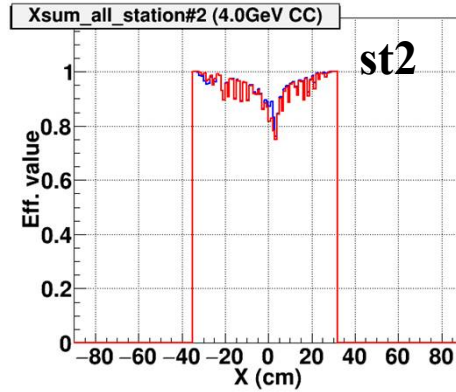
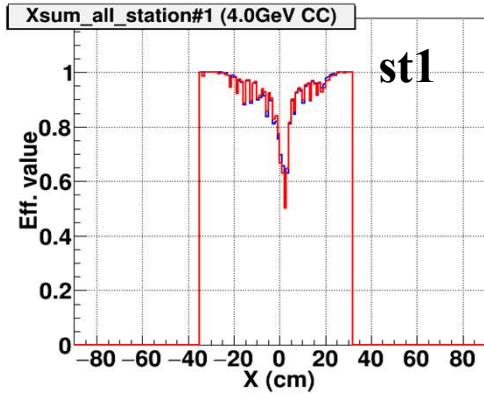


For each GEM station they were estimated using the following approach:

1. Select good quality tracks with the number of hits per track (excluding the station under study) not less than N;
2. Check that track crosses the detector area, if yes, add one track to the denominator;
3. If there is a hit in the detector, which belongs to the track, add one track to the numerator;
4. **GEM** efficiency = sum of tracks in numerator / sum of tracks in denominator.

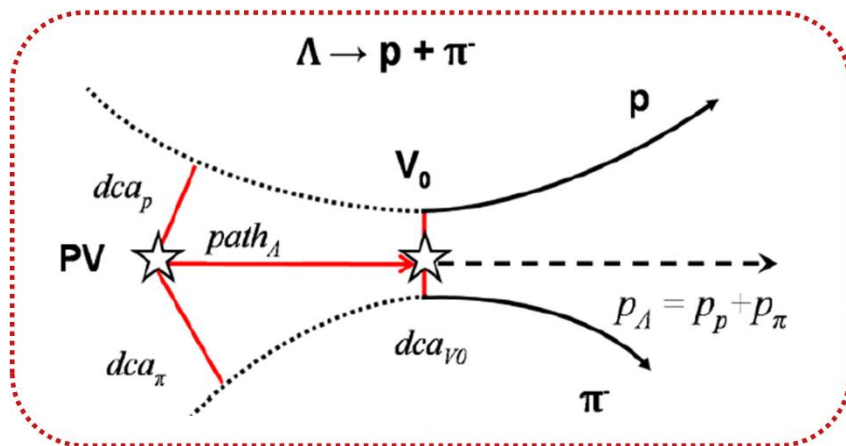
# 1D GEM efficiency comparison between the experimental data and MC (4.0GeV C+C)

Data—red line, MC—blue line;





# Selection of events with $\Lambda$ hyperon



**Event topology:**

**PV** – primary vertex

**V0** – vertex of hyperon decay

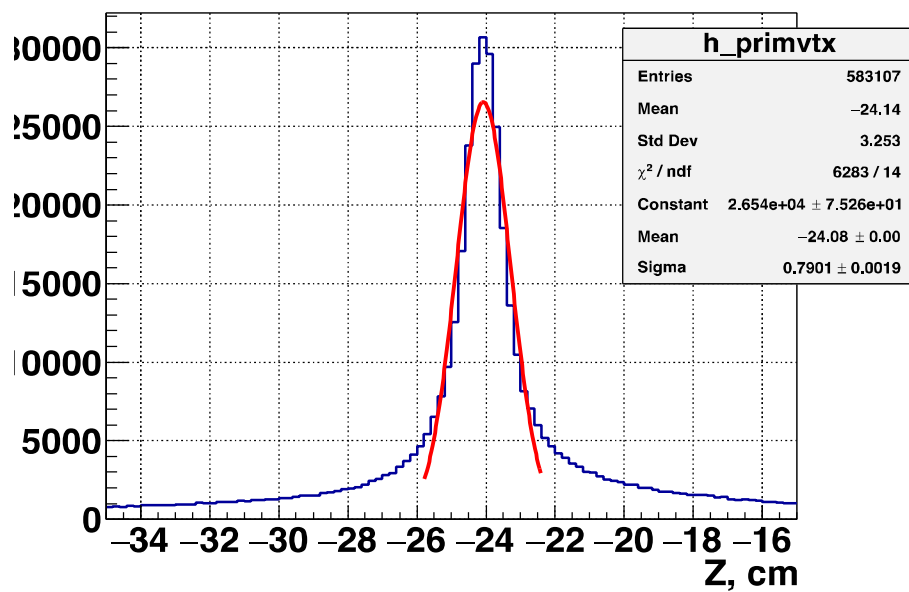
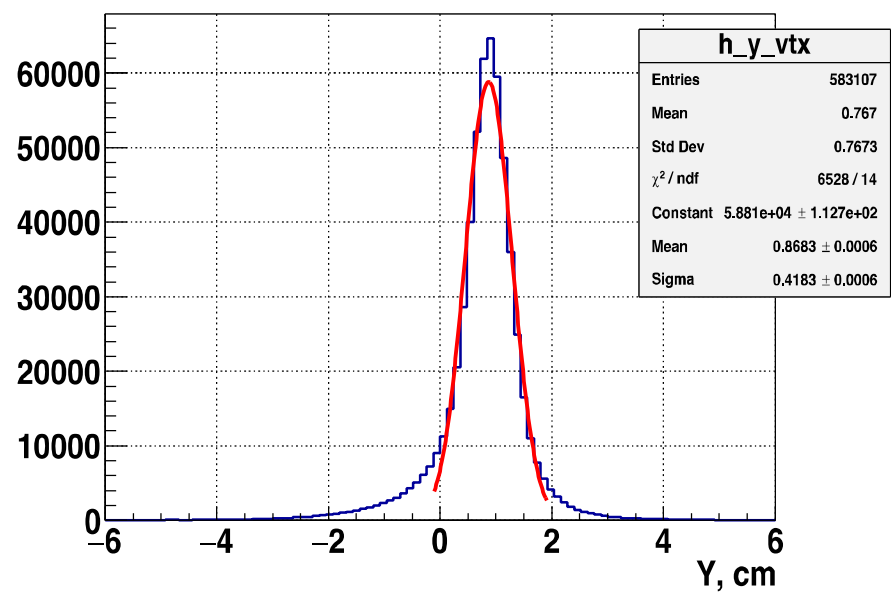
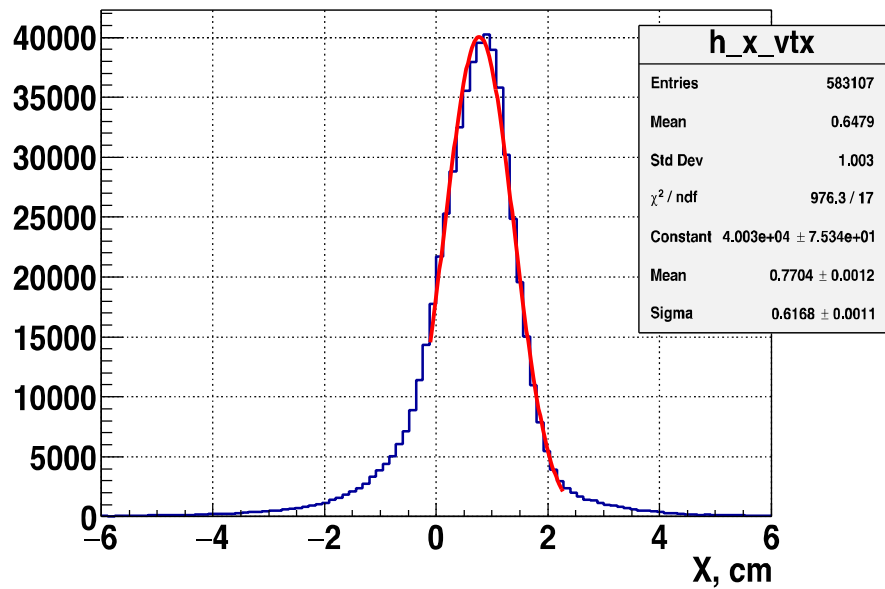
**dca** – distance of the closest approach

**path** – decay length

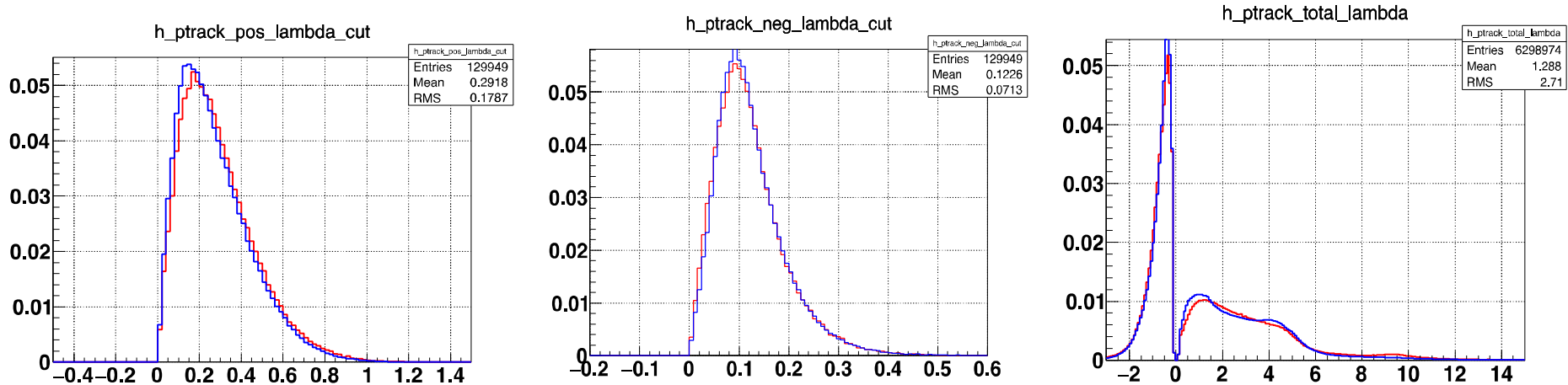
## Criteria for the selection of $\Lambda$ - hyperons :

- 1 Each track has at least 4 of the 6 hits in (Si+GEM);
- 2  $p_{\text{pos}} < 3.9(4.4)$  GeV/c for a beam energy of 4 (4.5) AGeV;
- 3  $p_{\text{neg}} > 0.3$  GeV/c;
- 4  $dca < 1$  cm;
- 5 Distance between the decay vertex  $V_0$  and the primary vertex:  $\text{path} > 2.5$  cm;

# X, Y, Z distributions of the experimental primary vertex

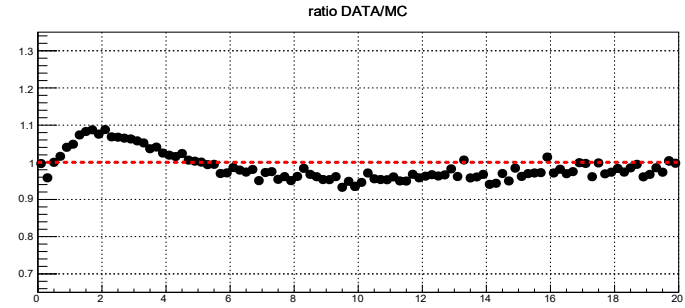
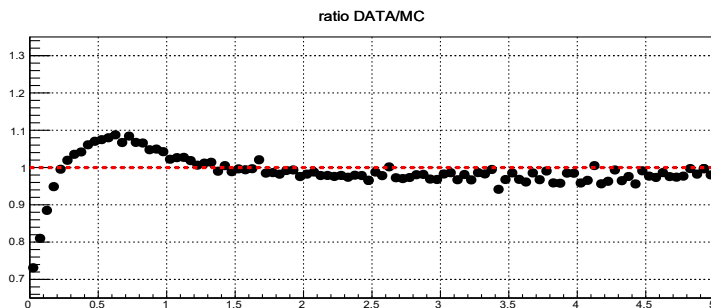
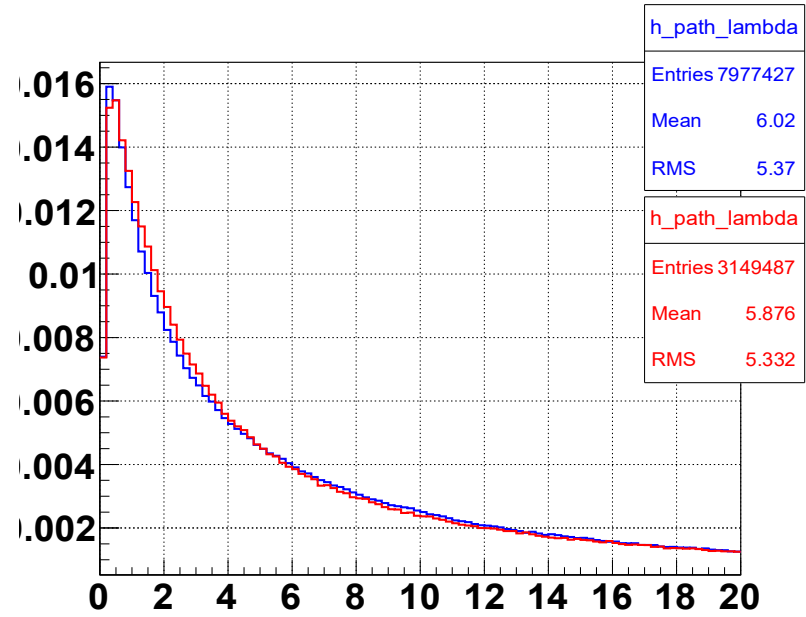
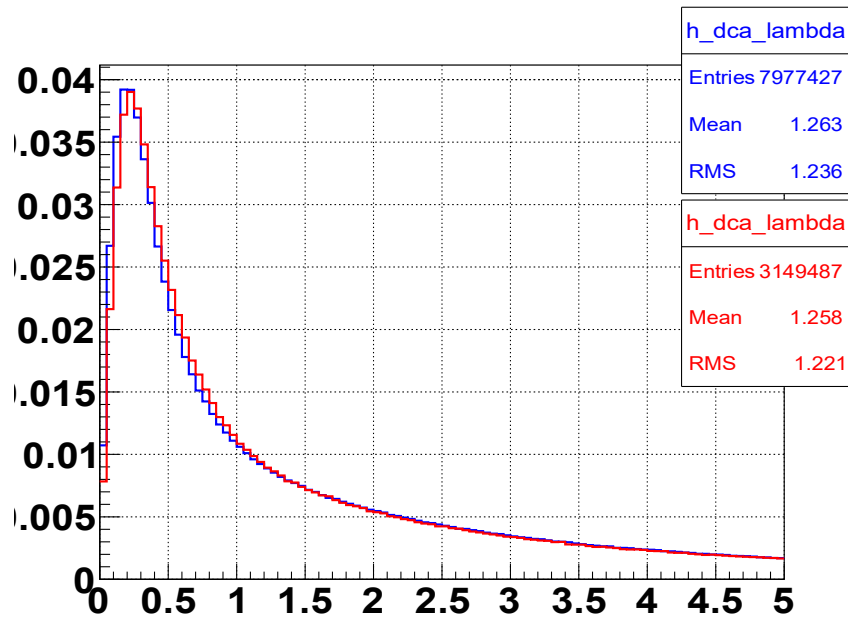


# Data and Monte - Carlo comparison



$C+Cu$  interactions at **4.0 AGeV** carbon beam energy: transverse momentum of positive particles (left); transverse momentum of negative particles (center); total momentum of negative ( $p/q < 0$ ) and positive particles ( $p/q > 0$ ) (right). **Blue line** - MC, **red line** - data.

# Data and Monte-Carlo comparison



**Distance of the closest approach** of  $V0$  decay tracks ( $dca$ ), distance between the primary vertex and  $V0$  (path). Ratio of the data/MC presented on bottom pictures. Cuts were applied as follow:  $dca < 1.0$ ,  $path > 2.5$ . Reaction  $C+Cu$ , energy **4.0 GeV**

- 1** | The experiment accumulated data, but the statistics from the reconstructed selected  $\Lambda$  candidates are not very rich.  
( $N_{\text{data}} \sim 5.9 \times 10^5$ ).
- 2** | The high statistic MC data set was generated: ( $N_{\text{MC}} \sim 3.8 \times 10^7$ ).  
MC were tuned to data and acceptance was evaluated in ( $y, p_T$ ) cells with high precision.
- 3** | Each event was weighted with the acceptance for each cell.
- 4** | 1D distributions in  $y$  or  $p_T$  were evaluated as the projections of 2D distributions to the corresponding kinematic variable.

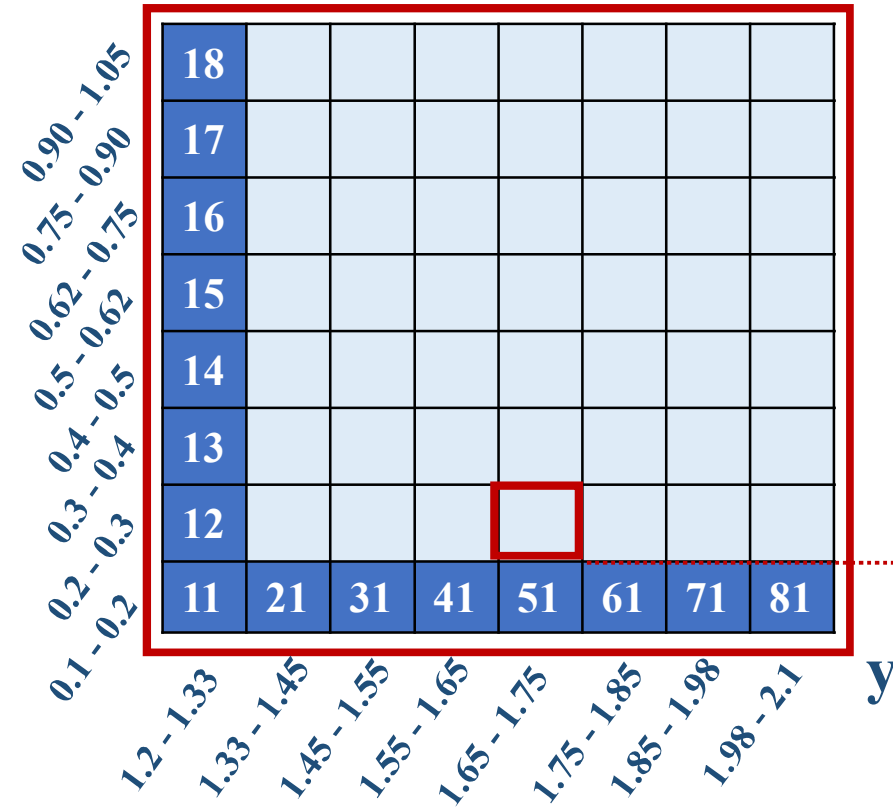
# Acceptance evaluation procedure (DCM - QGSM)

**Kinematic measuring range (4, 4.5 AGeV):**

$$0.1 < p_T < 1.05 \text{ GeV}/c$$

$$1.2 < y_{\text{lab}} < 2.1$$

$p_T, \text{ GeV}/c$



**1**

Divide the kinematic measuring range by  $y, p_T$  into (8×8) cells in the MC simulation.

**2**

To get the number of events generated by the MC.

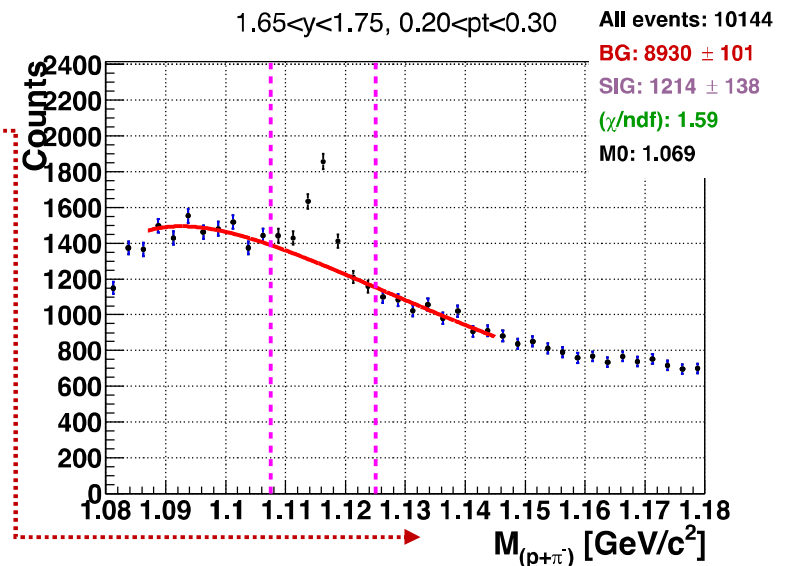
**3**

In each cells the invariant mass distribution fit with

$$f_{bg} = N \cdot (m - M_0)^A \cdot e^{-B \cdot (m - M_0)}$$

$N, A, B$  are free parameters,

$M_0 = 1.078 \text{ GeV}/c^2$  is the threshold limit,  $m$  is the mass value.

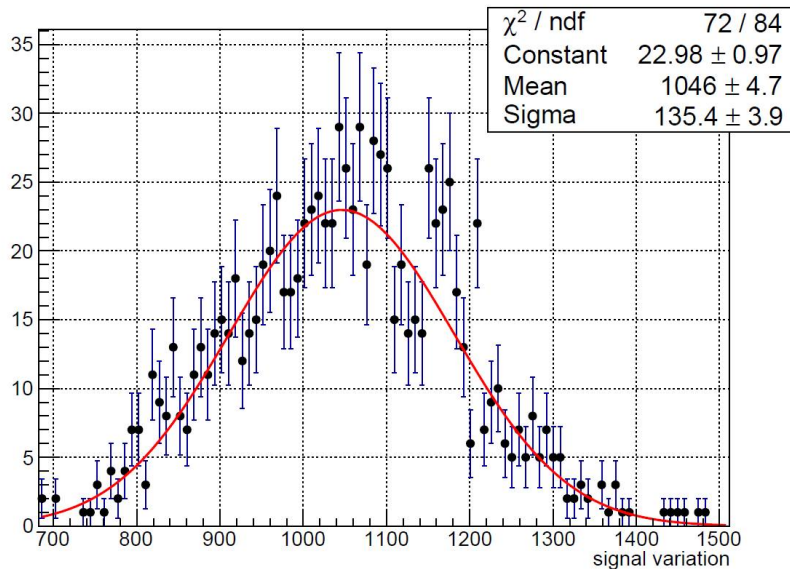


## Pseudo-experiment

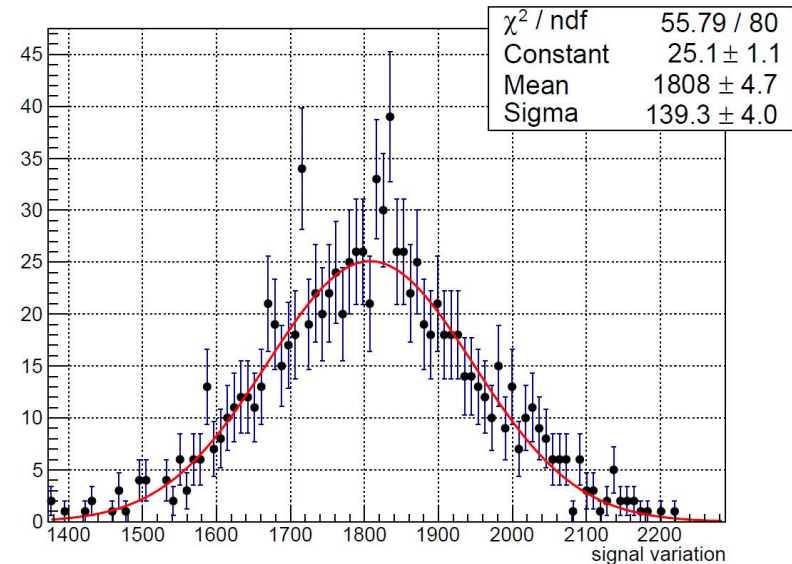
In each bin the bin content was modified by gaussian distribution with the widths equal to the bin error.

The “new” histogram was fit and the new signal was evaluated.

Procedure was repeated 1000 times and the **signal variation** are presented in a **bottom histogram**.



$$1.2 < y_{\text{lab}} < 1.33, 0.1 < p_{\text{T}} < 0.2$$



$$1.33 < y_{\text{lab}} < 1.45, 0.2 < p_{\text{T}} < 0.3$$

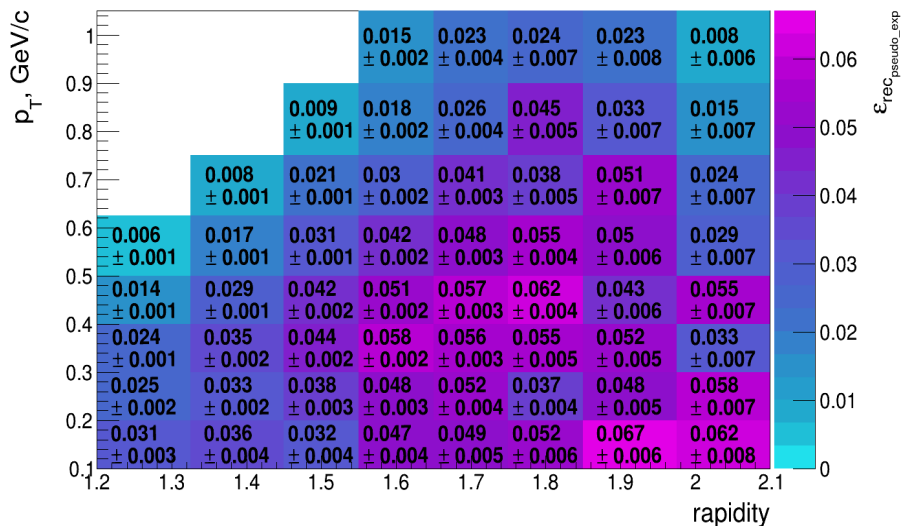
Red Line – Fit function  $\text{Gauss}(\langle N_{\text{recMC}}^\Lambda \rangle, \sigma_{N_{\text{recMC}}^\Lambda})$

4

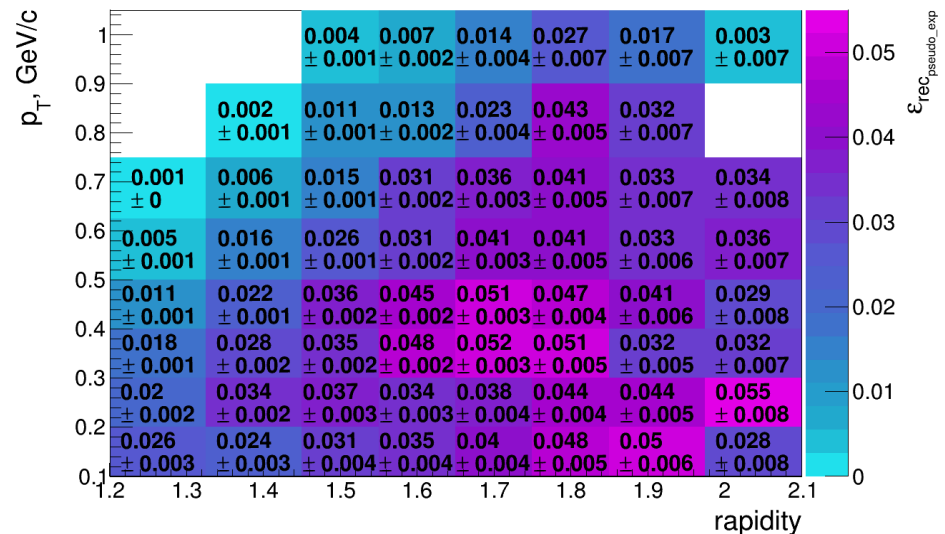
Each event is weighted with  $\varepsilon_i = \langle N_{\text{recMC}}^\Lambda \rangle_i / N_{\text{gen}_i}^\Lambda$  is evaluated number of  $\Lambda$ ,  $N_{\text{gen}_i}^\Lambda$  is the number of  $\Lambda$  generated;  $\Delta\varepsilon_i = \sigma_{N_{\text{recMC}_i}^\Lambda} / N_{\text{gen}_i}^\Lambda$  is evaluated error.

# Spectrometer acceptance ( $\varepsilon_i \pm \Delta\varepsilon_i$ ) for $\Delta$ in (y, p<sub>T</sub>) cells

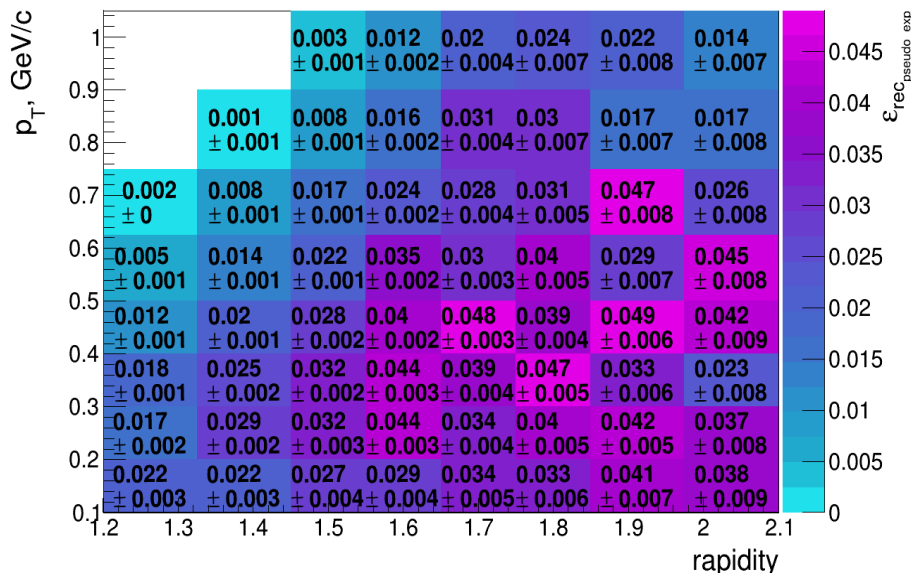
## C+C, E<sub>kin</sub> = 4 AGeV



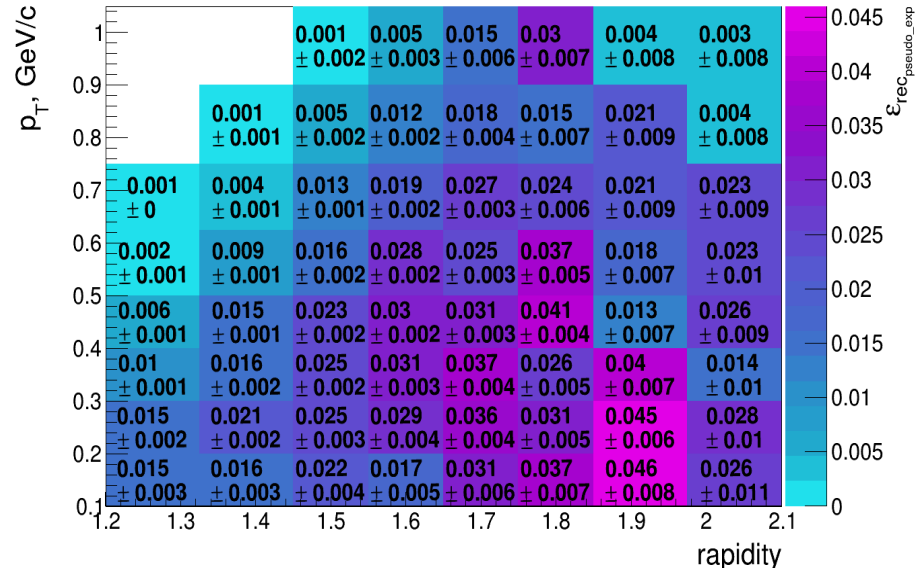
## C+Al, E<sub>kin</sub> = 4 AGeV



## C+Cu, E<sub>kin</sub> = 4 AGeV



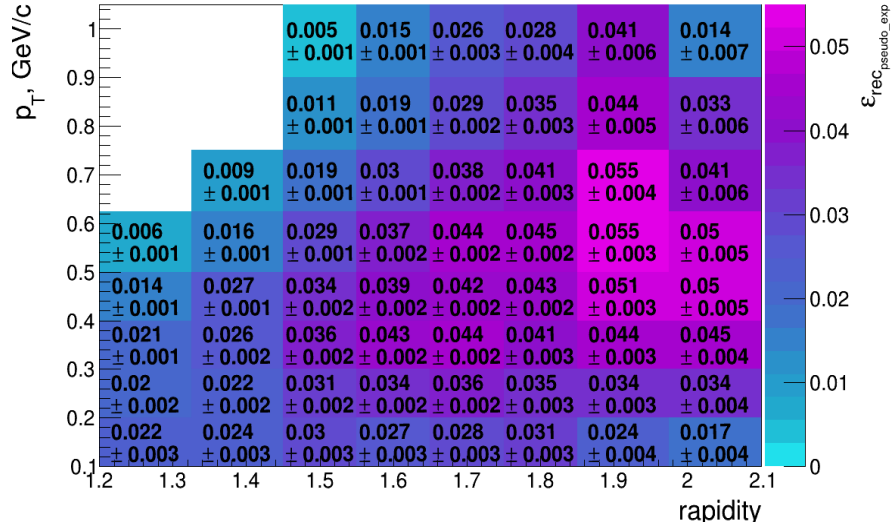
## C+Pb, E<sub>kin</sub> = 4 AGeV



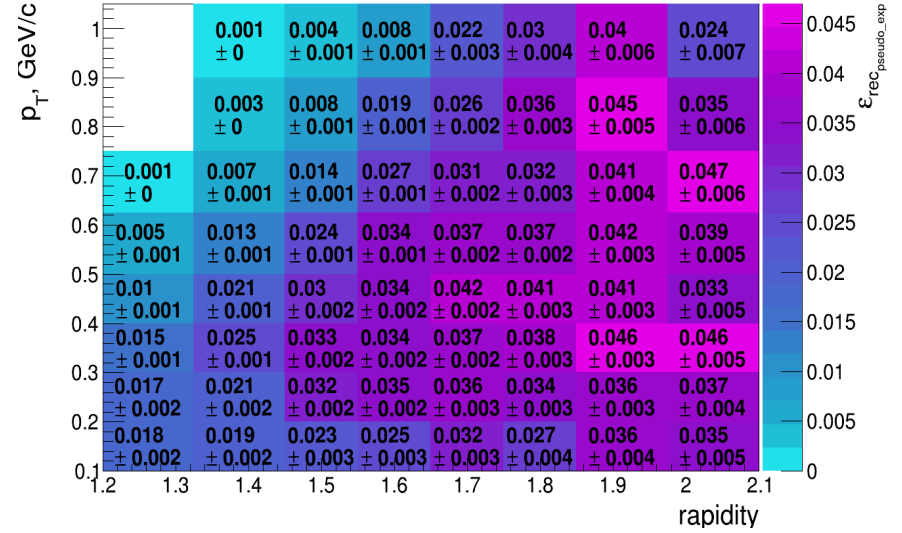


# Spectrometer acceptance ( $\varepsilon_i \pm \Delta\varepsilon_i$ ) for $\Lambda$ in (y, p<sub>T</sub>) cells

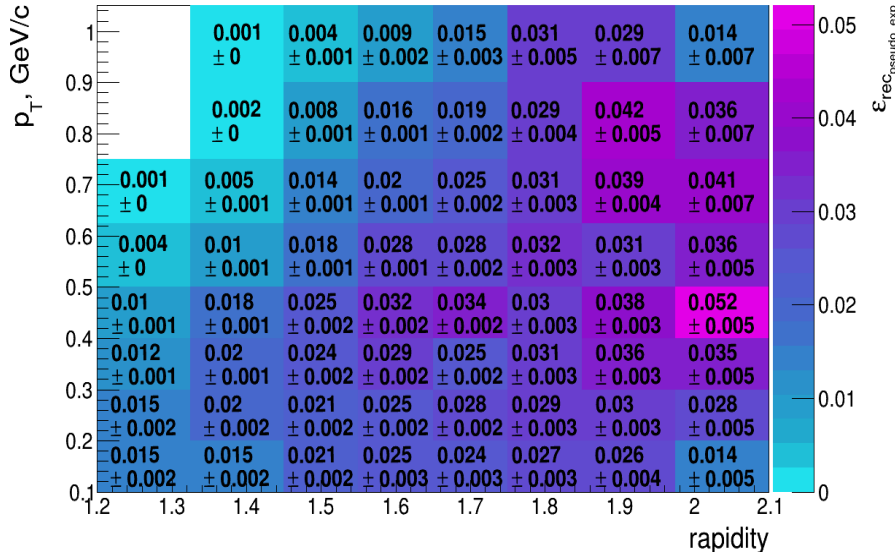
## C+C, E<sub>kin</sub> = 4.5 AGeV



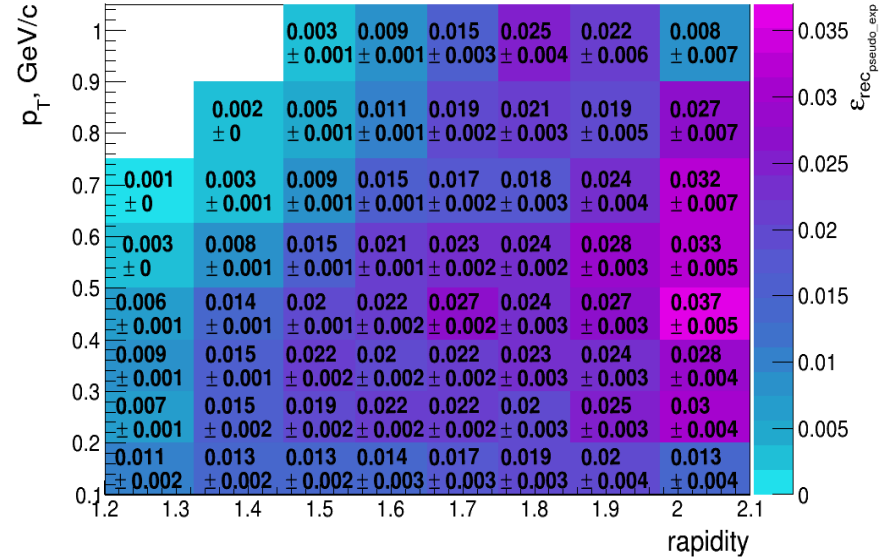
## C+Al, E<sub>kin</sub> = 4.5 AGeV



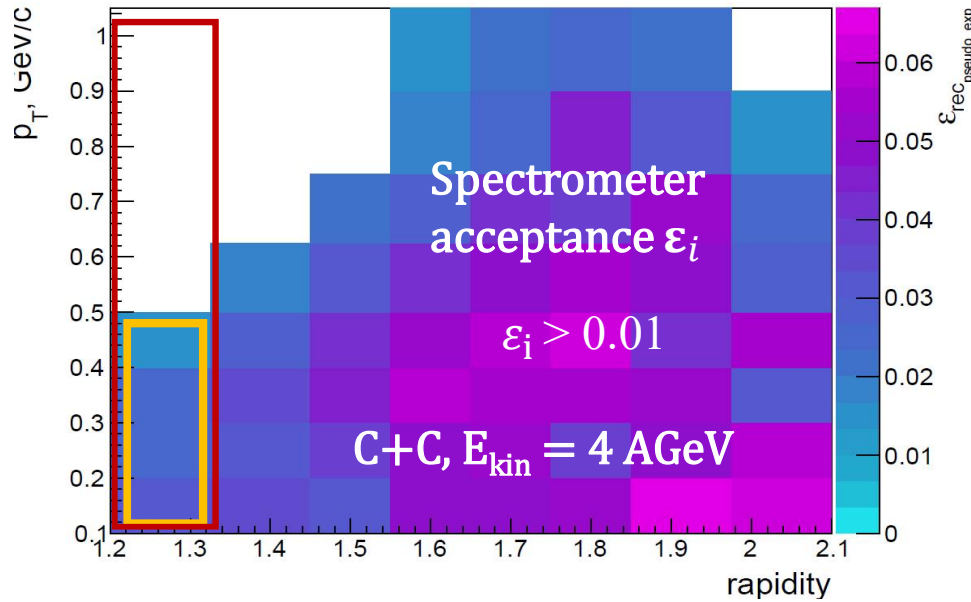
## C+Cu, E<sub>kin</sub> = 4.5 AGeV



## C+Pb, E<sub>kin</sub> = 4.5 AGeV

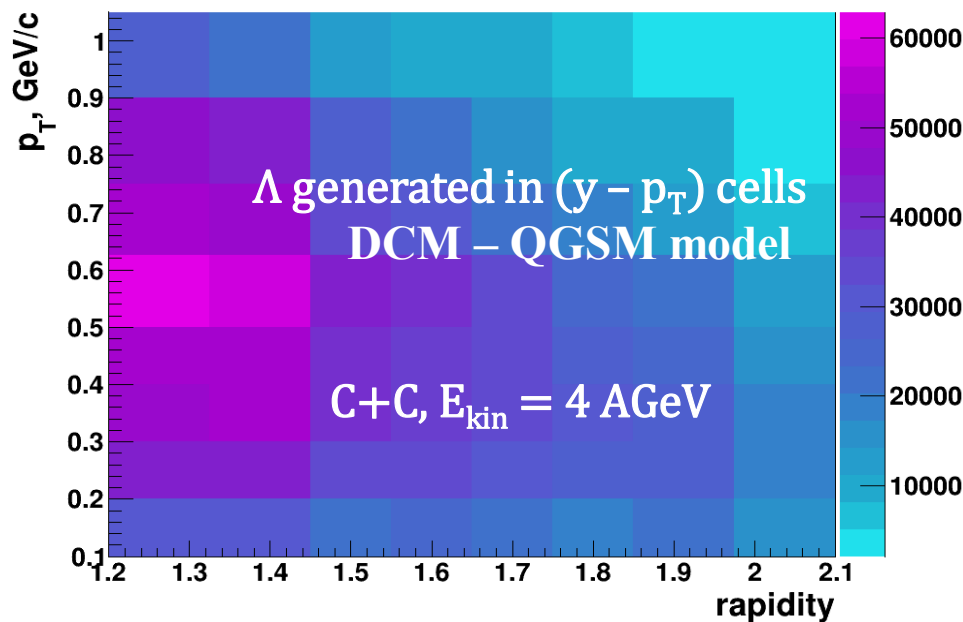


# Extrapolation to low acceptance ( $y, p_T$ ) cells

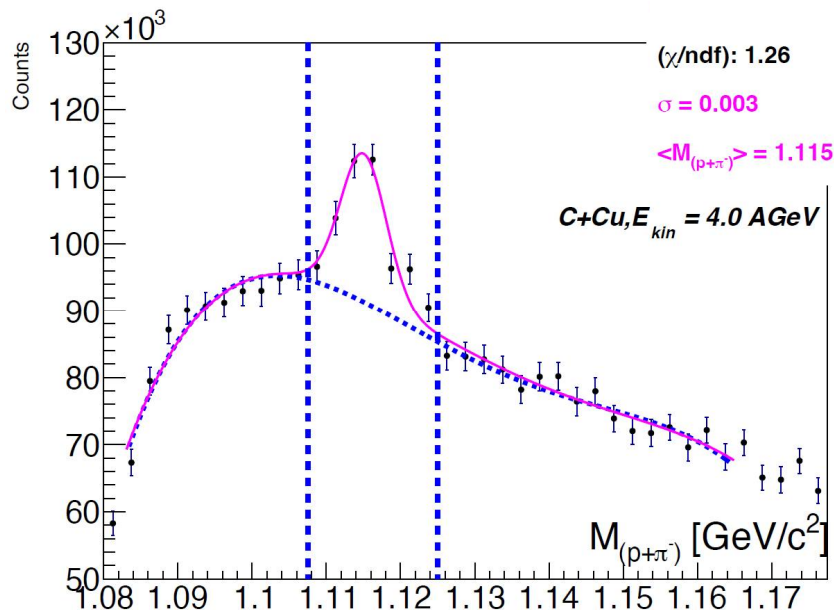
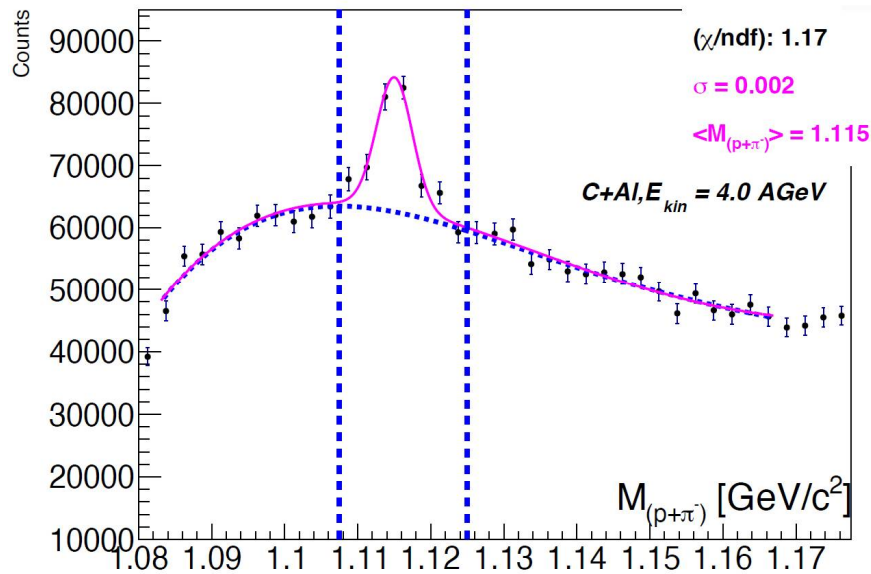


## Extrapolation steps:

- 1 Extrapolation based on the DCM – QGSM model;
- 2 Extrapolation factor is calculated  $f_{\text{extr}} = N_{\text{all}}/N_{\text{con}}$ ,  $N_{\text{all}}$  – sum of all generated events;  $N_{\text{con}}$  – sum of generated events in cells with high acceptance;
- 3  $f_{\text{extr}}$  - is used for evaluation of production cross section in full kinematic range;



# Mass distribution of the $\Lambda$ (BM@N DATA)



## Procedure in DATA $C+A \rightarrow X$

- 1) Split  $(y, p_T)$  area in small cells for MC/DATA (8x8);
- 2) **To each event assigned the weight  $\epsilon_i$** ;
- 3) Sum the cells by  $\sum_{ij} y_{ij}$  and by  $\sum_{ij} pT_{ij}$

$0.1 < p_T < 1.05$   
and  
 $1.2 < y_{lab} < 2.1$

- $\Lambda$  signal width  $\sim 2.0 - 4 \text{ MeV}$ ;
- **Signal** = hist – Background in **1107.5 - 1125  $\text{MeV}/c^2$** ;

# The suppression factors

- The suppression factors of reconstructed events  $\epsilon_{pileup}$  due to selection **criteria 2** applied to eliminate beam halo and pile-up events in interactions of the 4.0 and 4.5 AGeV carbon beam with the C, Al, Cu, Pb targets.

Number of signals in the start detector:  $T_0=1$

Table 2.  $\epsilon_{pileup}$  suppression factors

Selection	4 AGeV	4.5 AGeV
$T_0=1$	+	+
$BC2=1$	+	+
$Veto=0$	+	+
C	$0.674 \pm 0.034$	$0.529 \pm 0.026$
Al	$0.740 \pm 0.037$	$0.618 \pm 0.031$
Cu	$0.779 \pm 0.039$	$0.621 \pm 0.031$
Pb	$0.784 \pm 0.039$	$0.686 \pm 0.034$

Preliminary systematics evaluation:

$$\delta\epsilon_{pileup_{SYS}} = \epsilon_{pileup} \cdot \delta\epsilon_{pileup};$$

$$\text{where } \delta\epsilon_{pileup} = 5\%$$

- $\epsilon_{pileup}$  is used for evaluation of production cross section;

# Cross sections $\sigma_{\Lambda}(y/p_T)$ of the $\Lambda$

The inclusive cross section  $\sigma_{\Lambda}$  and  $Y_{\Lambda}$  of  $\Lambda$  hyperon in C+A interactions are calculated in bins of  $(y - p_T)$  according to the formula:

$$\sigma_{\Lambda}(p_T) = \frac{[\sum_y N_{rec}^{\Lambda}(y, p_T) / \epsilon_{rec}(y, p_T)]}{[\epsilon_{trig} \cdot \epsilon_{pileup} \cdot L]}$$

$$\sigma_{\Lambda}(y) = \frac{[\sum_{p_T} N_{rec}^{\Lambda}(y, p_T) / \epsilon_{rec}(y, p_T)]}{[\epsilon_{trig} \cdot \epsilon_{pileup} \cdot L]}$$

$L$  is the luminosity,  $N_{rec}^{\Lambda}$  is the number of recontacted  $\Lambda$ -hyperons,  $\epsilon_{rec}$  is the combined efficiency of the  $\Lambda$  - hyperon reconstruction,  $\epsilon_{trig}$  is the trigger efficiency,  $\epsilon_{pileup}$  is the suppression factors of reconstructed events.

**Table 3.** Integrated **luminosities** collected in interactions of the carbon beam of 4.0 and 4.5 AGeV with different targets.

Interactions, target thickness		Integrated luminosity/ $10^{30} \text{ cm}^{-2}$		Integrated luminosity/ $10^{30} \text{ cm}^{-2}$
C+C (9 mm)	4 AGeV	6.06	4.5 AGeV	4.69
C+Al (12 mm)		2.39		3.60
C+Cu (5 mm)		2.00		3.06
C+Pb (10 mm)		0.22		0.84

# Yields of the $\Lambda$

The  $Y_\Lambda$  of  $\Lambda$  hyperon in C+A interactions are calculated in bins of  $(y - p_T)$  cells according to the formula:

$$Y_\Lambda(y - p_T) = \sigma_\Lambda(y - p_T) / \sigma_{inel}$$

$\sigma_{inel}$  is the cross section for minimum bias inelastic C+A interactions(model).

The cross sections for inelastic C+Al, C+Cu, C+Pb interactions calculated by the formula (DCM-QGSM):

$$\sigma_{inel} = \pi R_0^2 (A_P^{1/3} + A_T^{1/3})^2$$

$R_0 = 1.2$  fm is an effective nucleon radius,  $A_P$  and  $A_T$  are atomic numbers of the beam and target nucleus [1]. The **uncertainties** for C+Al, C+Cu, C+Pb inelastic cross sections are estimated by formula:  $\sigma_{inel} = \pi R_0^2 (A_P^{1/3} + A_T^{1/3} - b)^2$  with  $R_0 = 1.46$  fm and  $b = 1.21$  [2].

**Table 4. Inelastic cross sections  $\sigma_{inel}$  for carbon-nucleus interactions**

Interaction	C+C	C+Al	C+Cu	C+Pb
Inelastic cross section, mb	830±50	1260±50	1790±50	3075±50

[1] Kalliopi Kanaki “Study of  $\Lambda$  hyperon production in C+C collisions at 2 AGeV beam energy with the HADES spectrometer”.

[2] H. Angelov et al., P1-80-473, JINR, Dubna.

# The results (Preliminary) of the integrated yields of the $\Lambda$

Target	Energy, AGeV	$Y_{\Lambda} \pm \Delta Y_{\text{stat}\Lambda} \pm \Delta Y_{\Lambda_{\text{sys}}}$	Energy, AGeV	$Y_{\Lambda} \pm \Delta Y_{\text{stat}\Lambda} \pm \Delta Y_{\Lambda_{\text{sys}}}$
<b><math>0.1 &lt; p_T &lt; 1.05</math> and <math>1.2 &lt; y_{\text{lab}} &lt; 2.1</math></b>				
C + C	4.0	$0.011 \pm 0.001 \pm 0.004$	4.5	$0.013 \pm 0.002 \pm 0.005$
C + Al		$0.032 \pm 0.004 \pm 0.006$		$0.025 \pm 0.003 \pm 0.005$
C + Cu		$0.030 \pm 0.003 \pm 0.005$		$0.037 \pm 0.004 \pm 0.006$
C + Pb		$0.039 \pm 0.008 \pm 0.009$		$0.033 \pm 0.010 \pm 0.010$

## 1 part

An approach in the estimation of systematic uncertainties related to the variation of selection criteria for events with  $\Lambda$ -hyperons.

The selection criteria considered are **path, dca**.

**Nominal Analysis:**  $dca < 1 \text{ cm}$ ,  $path > 2.5 \text{ cm}$ ;

**Cut variation 1:**

$path > 2.25 \text{ cm}$ , **fixed:**  $dca < 1 \text{ cm}$ ;

$path > 2.75 \text{ cm}$ ,

**Cut variation 2:**

$dca < 0.9 \text{ cm}$ ,

$dca < 1.1 \text{ cm}$ , **fixed:**  $path > 2.5 \text{ cm}$ ;

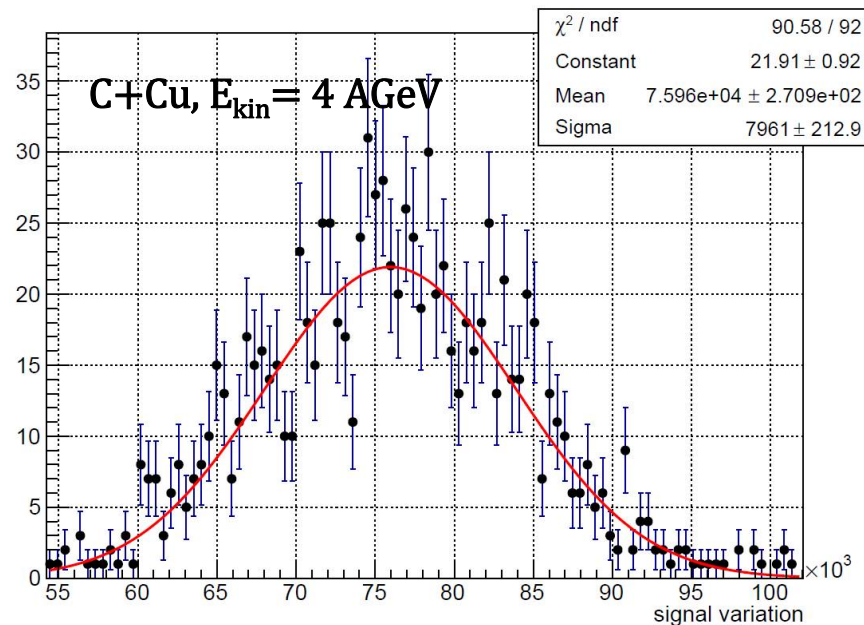
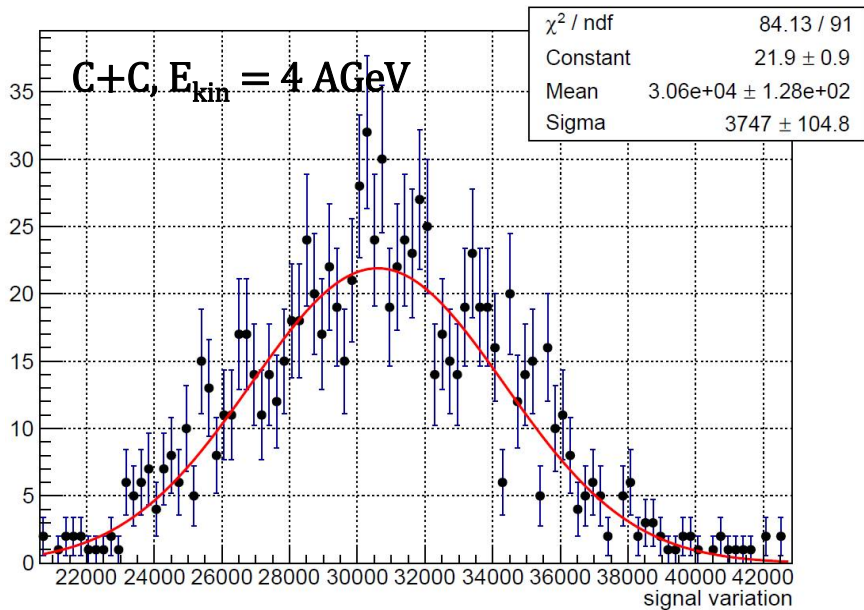


# Combined systematic uncertainties

C+Cu,  $E_{\text{kin}} = 4.5$  AGeV

dca	path	Yields (with cut variation)	Yields (nominal analysis)
Data statistic – II period			
<b>Fixed:</b> dca <1 cm	Path >2.25	0.043±0.004	0.035±0.009±0.007
	Path >2.75	0.042±0.004	
dca <0.9 cm	<b>Fixed:</b> Path >2.5	0.041±0.004	
dca <1.1 cm		0.042±0.004	
Data statistic – I period			
<b>Fixed:</b> dca <1 cm	Path >2.25	0.037±0.004	0.035±0.011±0.003
	Path >2.75	0.036±0.005	
dca <0.9 cm	<b>Fixed:</b> Path >2.5	0.038±0.004	
dca <1.1 cm		0.039±0.005	
Data statistic – (I + II) periods			
<b>Fixed:</b> dca <1 cm	Path >2.25	0.041±0.003	0.037±0.007±0.004
	Path >2.75	0.041±0.003	
dca <0.9 cm	<b>Fixed:</b> Path >2.5	0.041±0.003	
dca <1.1 cm		0.041±0.003	

# Uncertainties from signal variation (BM@N DATA)



**2 part**

Red Line – Fit function

$$\text{Gauss}(\langle N_{recDATA}^\Lambda \rangle, \sigma_{N_{recDATA}^\Lambda})$$

$$0.1 < p_T < 1.05$$

and

$$1.2 < y_{lab} < 2.1$$

$$\Delta\sigma_\Lambda = \sigma_{N_{recDATA}^\Lambda} / (\varepsilon_{trig} \times \varepsilon_{pileup} \times L)$$

$$\Delta Y_{stat\Lambda} = \Delta\sigma_\Lambda / \sigma_{inel}$$

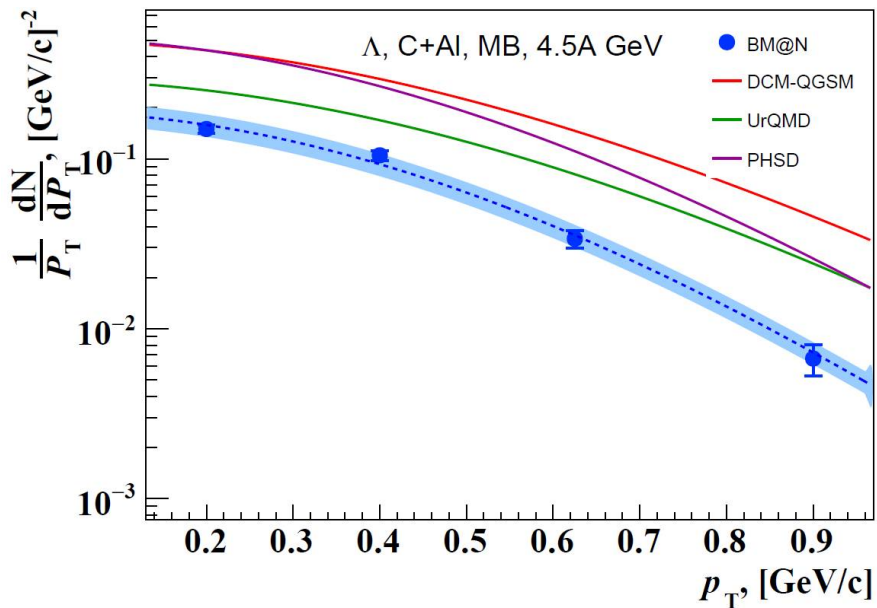
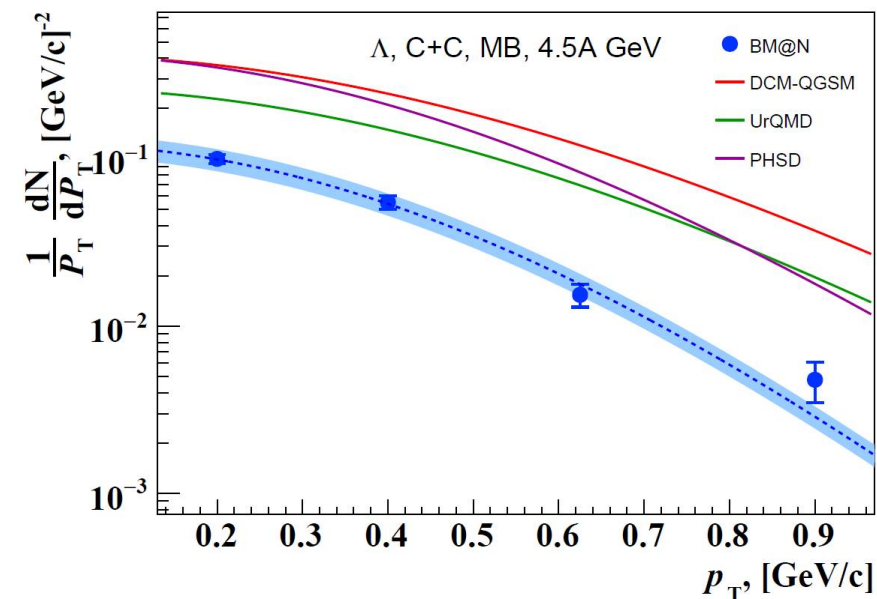
# Calculation of systematic uncertainties yields of the $\Lambda$

**1**  $\Delta Y_{\Lambda_{sys\_pseudo\_exp}}^2 = Y_{\Lambda}^2 (\sigma_{N_{recDATA}^{\Lambda}}^2 / \langle N_{recDATA}^{\Lambda} \rangle^2 + \sigma_{N_{recMC}^{\Lambda}}^2 / \langle N_{recMC}^{\Lambda} \rangle^2);$

**2**  $\Delta Y_{\Lambda_{syscut\_var}} = 0.004$  – from the variation of the  $\Lambda$ -hyperon selection criteria;

**3**  $\Delta Y_{\Lambda_{sys}} = \sqrt{\Delta Y_{\Lambda_{sys\_pseudo\_exp}}^2 + \Delta Y_{\Lambda_{syscut\_var}}^2}$  - total systematic uncertainty;

# Invariant $p_T$ spectra of $\Lambda$ hyperons vs models predictions(Preliminary)



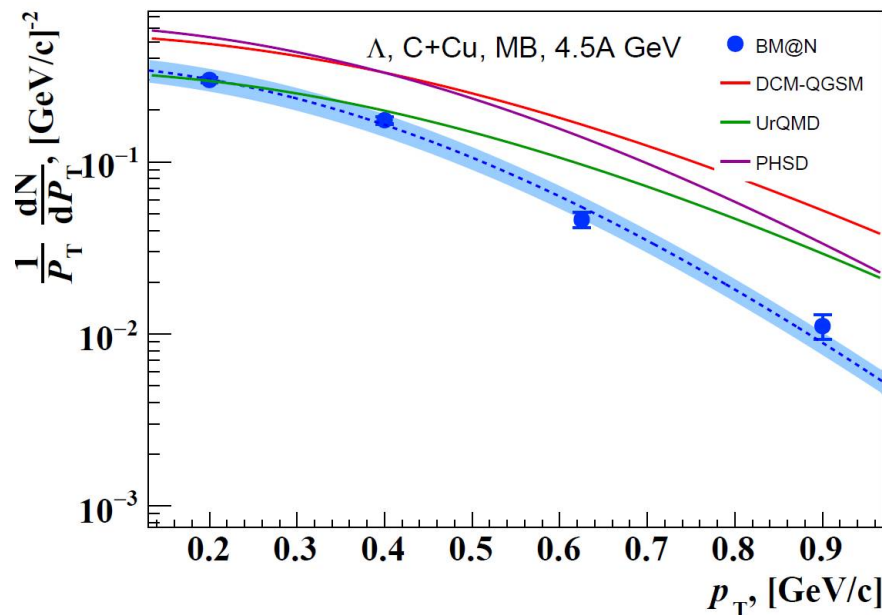
The measured spectra of the  $\Lambda$  yields in  $p_T$  are parameterized by the formula:

$$1/p_T d^2N/dp_T dy = N \cdot \exp(-(m_T - m_\Lambda)/T_0)$$

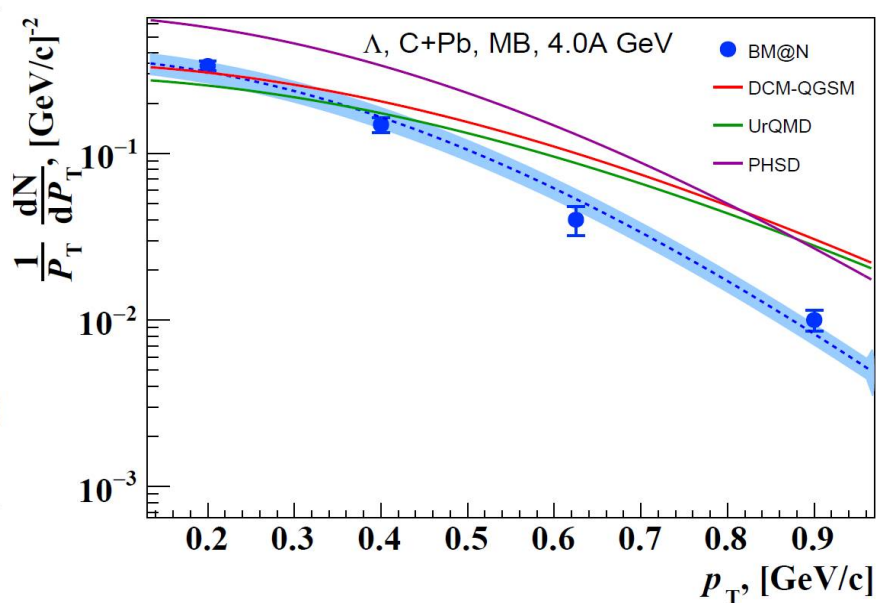
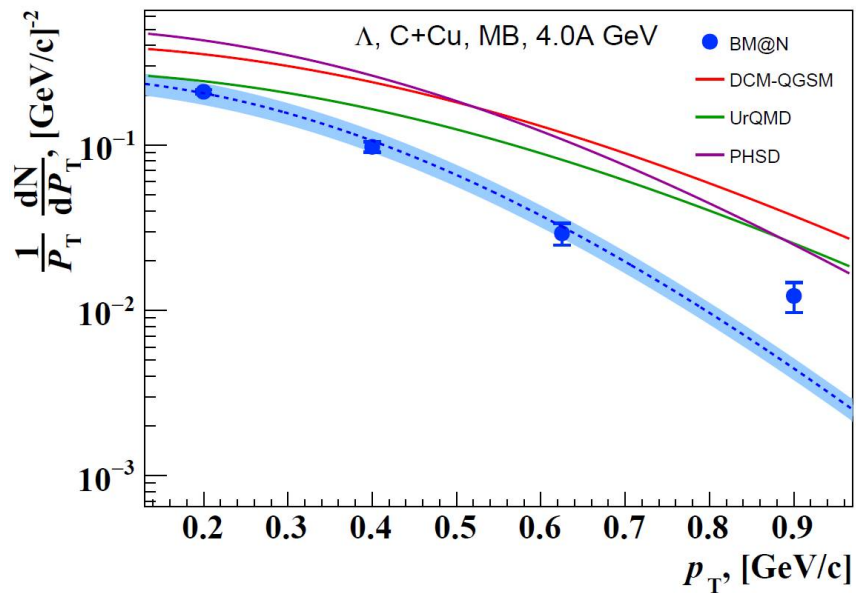
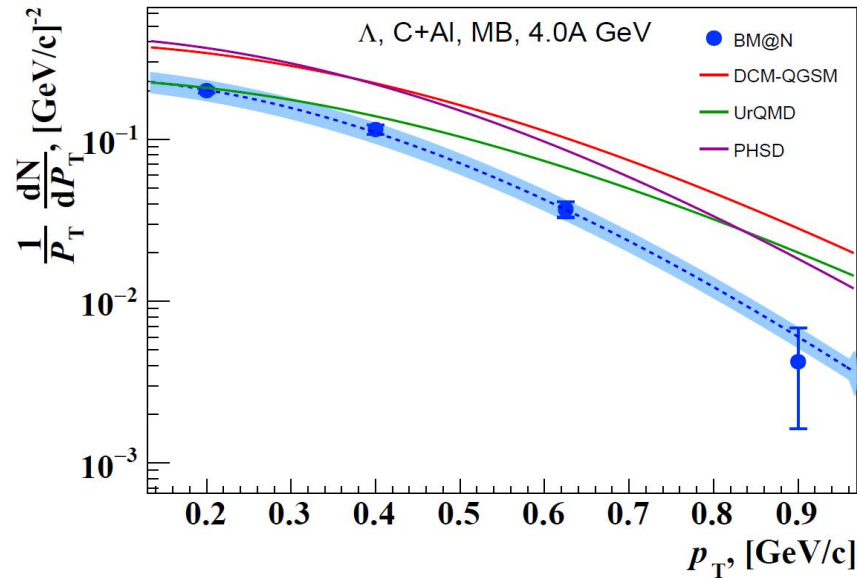
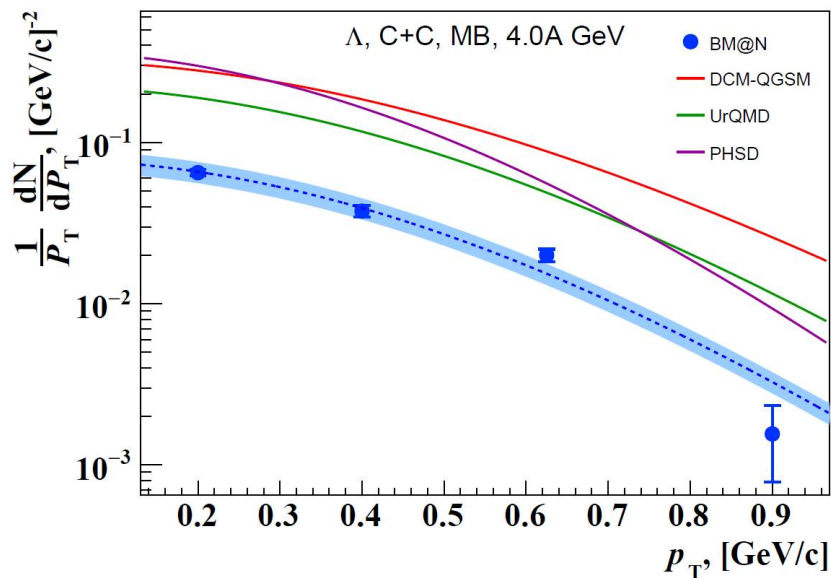
The transverse mass  $m_T = \sqrt{m_\Lambda^2 + p_T^2}$ ,

The  $N$  normalization,

The inverse slope parameter  $T_0$  are free parameters of the fit;



# Invariant $p_T$ spectra of $\Lambda$ hyperons vs models predictions(Preliminary)



# SLOPE RESULTS (Preliminary)

4.0 AGeV	$T_0$ , MeV, C+C	$T_0$ , MeV, C+Al	$T_0$ MeV, C+Cu	$T_0$ MeV, C+Pb
BM@N	$114 \pm 19 \pm 17$	$108 \pm 16 \pm 16$	$96 \pm 14 \pm 14$	$83 \pm 8 \pm 12$
DCM - QGSM	126	120	133	130
UrQMD	107	128	133	136
PHSD	87	100	105	98

4.5 AGeV	$T_0$ , MeV, C+C	$T_0$ , MeV, C+Al	$T_0$ , MeV, C+Cu	$T_0$ , MeV, C+Pb
BM@N	$116 \pm 24 \pm 17$	$115 \pm 7 \pm 17$	$101 \pm 3 \pm 15$	Due to low statistics
DCM - QGSM	132	133	135	142
UrQMD	122	128	130	134
PHSD	101	106	109	108

**Thank you for  
your attention**

