

Signal charge reconstruction and slewing correction using the ToT method for the Highly-Granular Neutron Detector of the BM@N

Nikolay Karpushkin
on behalf of the INR RAS team

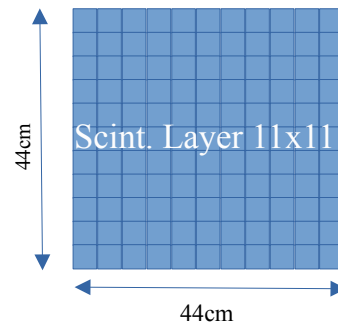
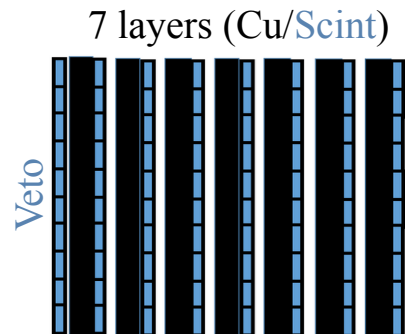
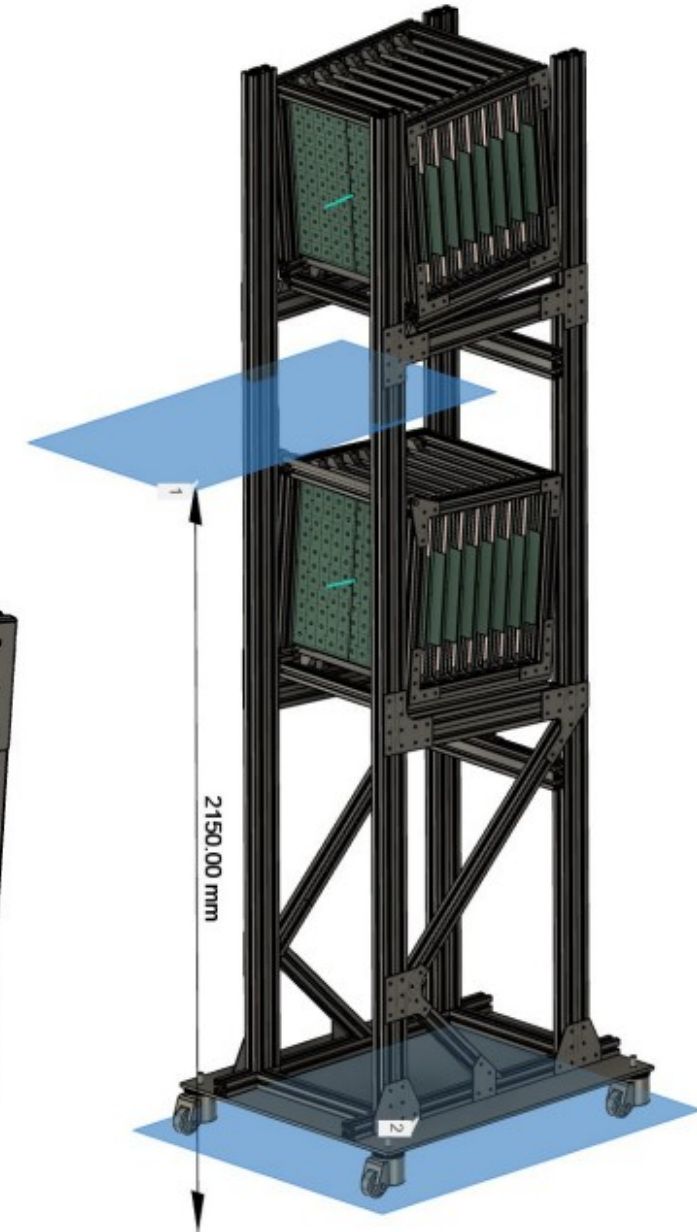
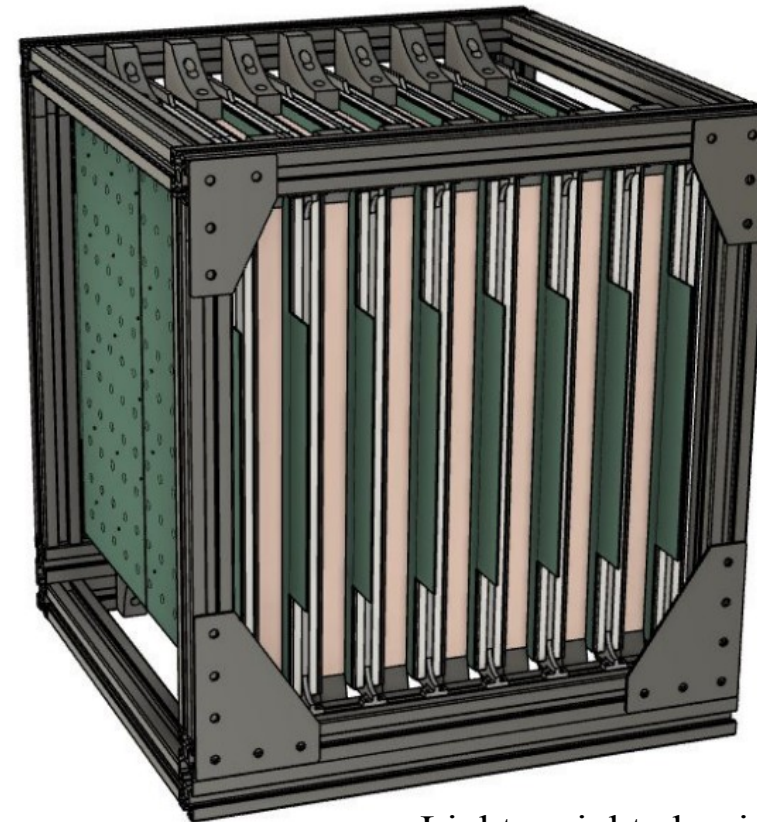
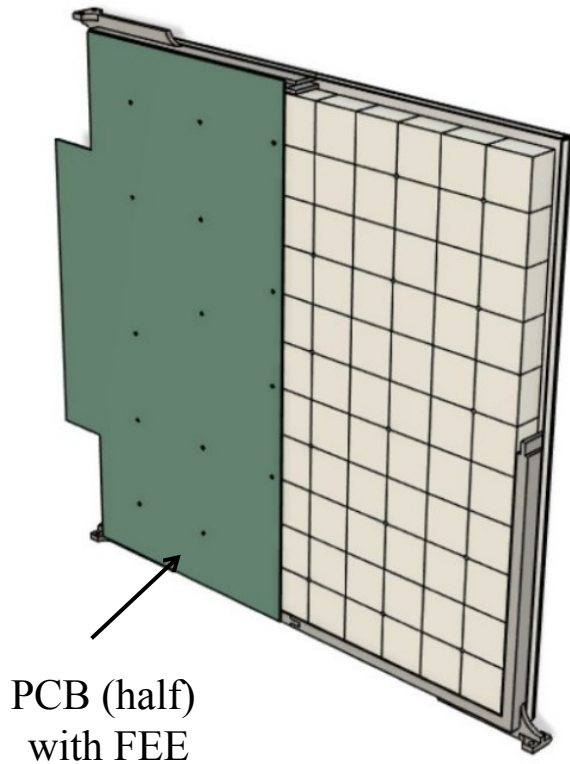


The 13th Collaboration Meeting of the BM@N Experiment at NICA
9 October 2024, JINR

Mechanical design

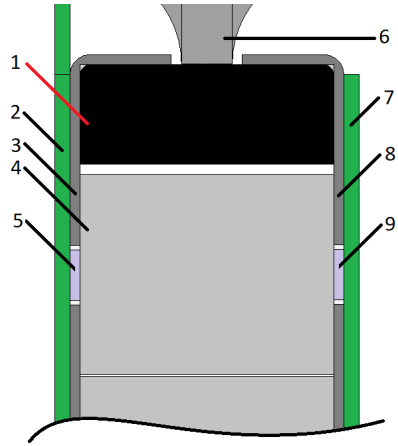
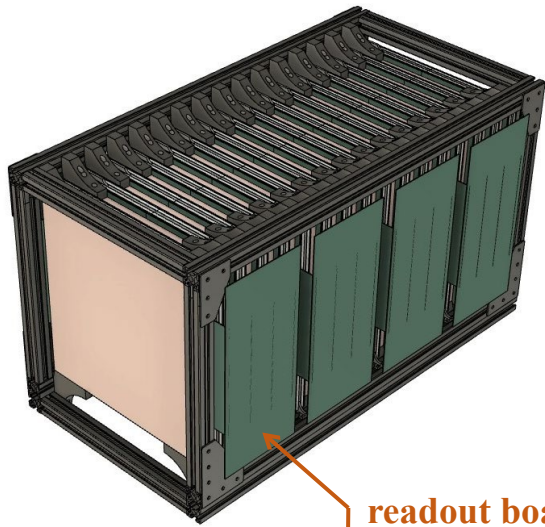
Light-tight and air-cooled assembly of 2 separate arms. Each arm:

- 1 veto-layer
- 7 Cu absorber layers (3 cm thick)
- 7 sensitive layers:
 - 11x11 matrix of scintillator detectors $4 \times 4 \times 2.5 \text{ cm}^3$
 - surrounded from both sides by PCBs
 - upstream board: LEDs for time calibration
 - downstream board: SiPMs and FEE



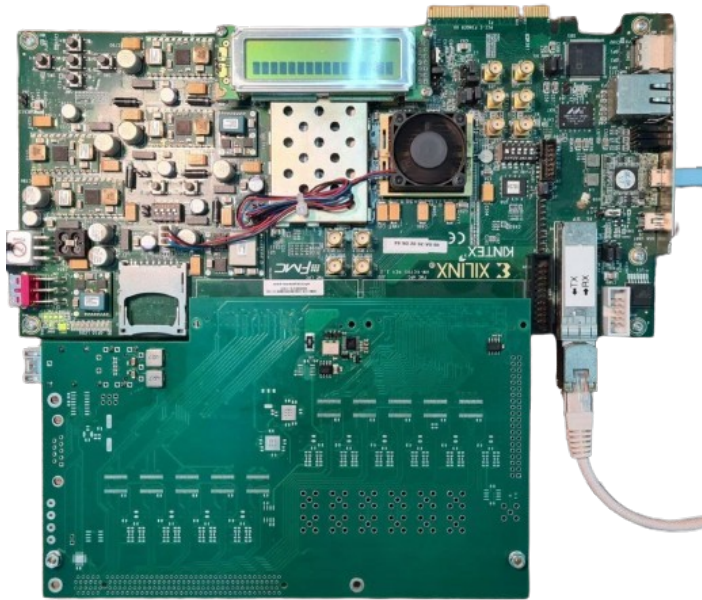
total length $\sim 48\text{cm}$ ($1.5 \lambda_{\text{in}}$)

Light-weight aluminum frame

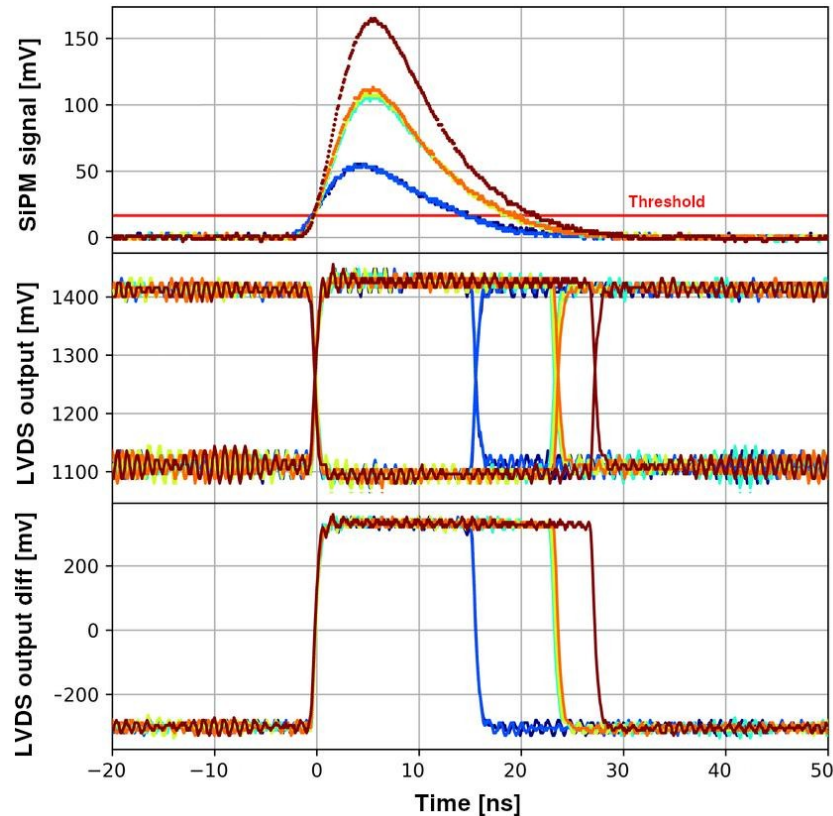


- 1 – the frame of layer case
- 2 – SiPM PCB
- 3&8 – aluminum plates for both sides of the frame case with cutouts for SiPMs and LEDs
- 4 – scintillator
- 5 – SiPM
- 6 – layer support bracket
- 7 – LED PCB
- 9 – LED

readout board



Readout board prototype based on Xilinx Kintex 7 Evaluation Board



Readout scheme

1. Plastic scintillator light flash
 2. SiPM EQR15 11-6060D-S
 3. High-speed comparator with differential LVDS output
 4. FPGA-based TDC
- = Response time + ToT

Per channel

- Dynamic range: 0.5-7 MIP
- Time resolution: 135 ps
- Amplitude resolution: < 20% (reconstructed from ToT)

F. Guber, et al., *Instrum. Exp. Tech.* 66 (2023) 4, 553-557.

D. Finogeev, et al., *Nucl. Instrum. Meth. A* 1059 (2024) 168952.

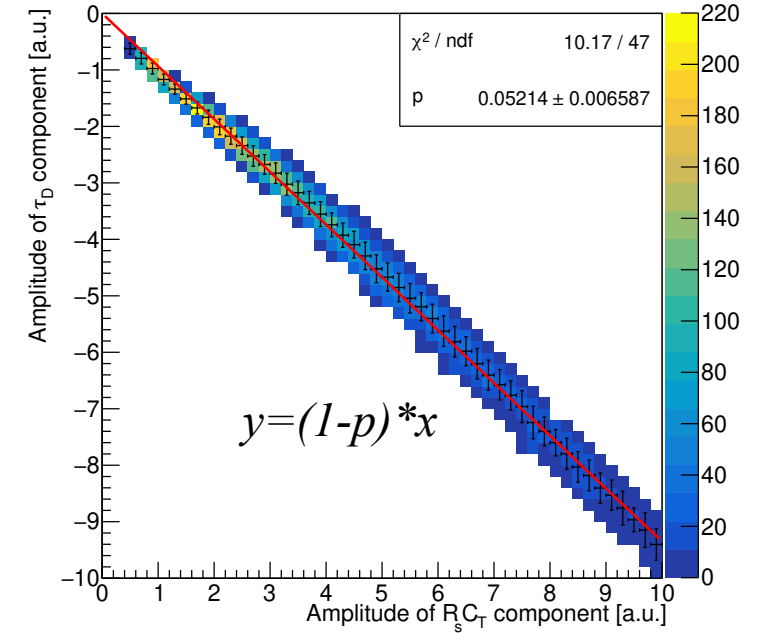
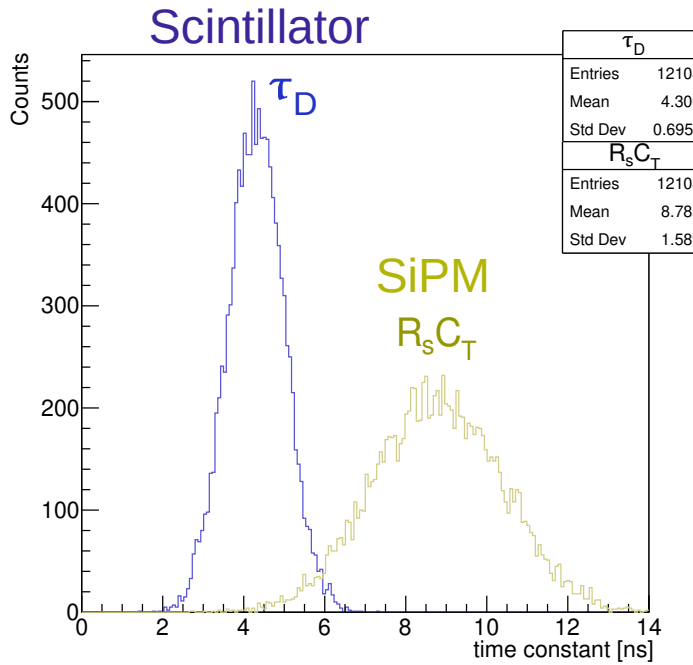
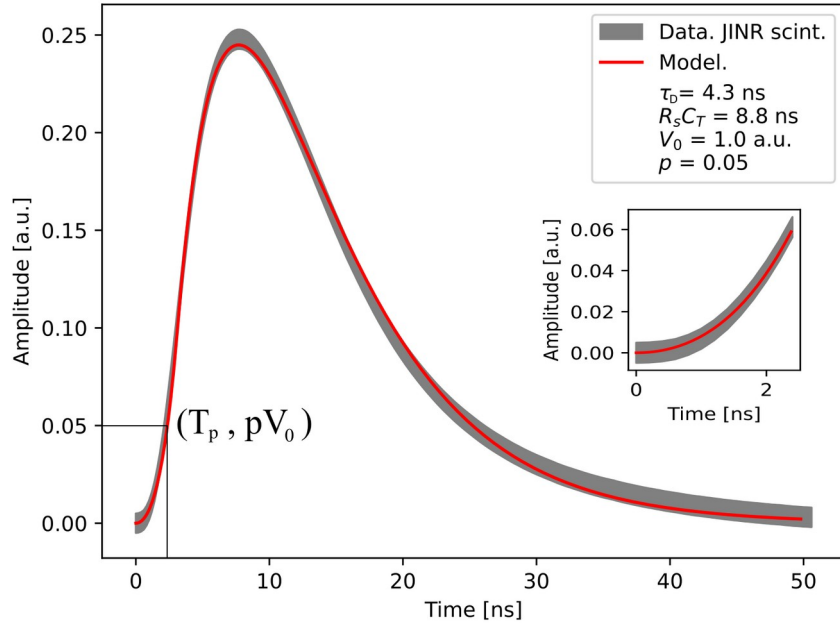
SiPM: Beijing NDL EQR15 11-6060D-S

- Active area $6 \times 6 \text{ mm}^2$
- Pixel size $15 \times 15 \text{ } \mu\text{m}^2$
- Total pixels: 160 000
- PDE: 45%
- Gain: $4 \cdot 10^5$



Analytical description of light signals captured by SiPM

CAEN DT5742 5GHz sampling rate



N. Karpushkin, et al., Nucl. Instrum. Meth. A 1068 (2024) 169739.

$$V_0 \equiv \frac{\eta q G N_{ph}^0 R_s}{R_s C_T - \tau_D} \quad T_p = \frac{2e - 1}{e - 1} \frac{p R_s C_T \tau_D}{R_s C_T (1 - p) - \tau_D}$$

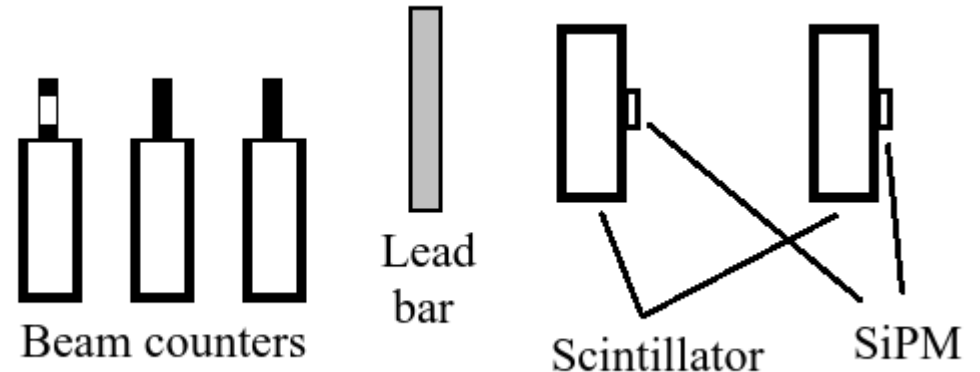
$$V(t) = \begin{cases} \frac{p V_0}{e - 1} \frac{t}{T_p} \left(e^{\frac{t}{T_p}} - 1 \right) & \text{if } 0 \leq t < T_p \\ V_0 \left(e^{-\frac{t - T_p}{R_s C_T}} - (1 - p) e^{-\frac{t - T_p}{\tau_D}} \right) & \text{if } t \geq T_p \end{cases}$$

free parameters: τ_D , $R_s C_T$, p

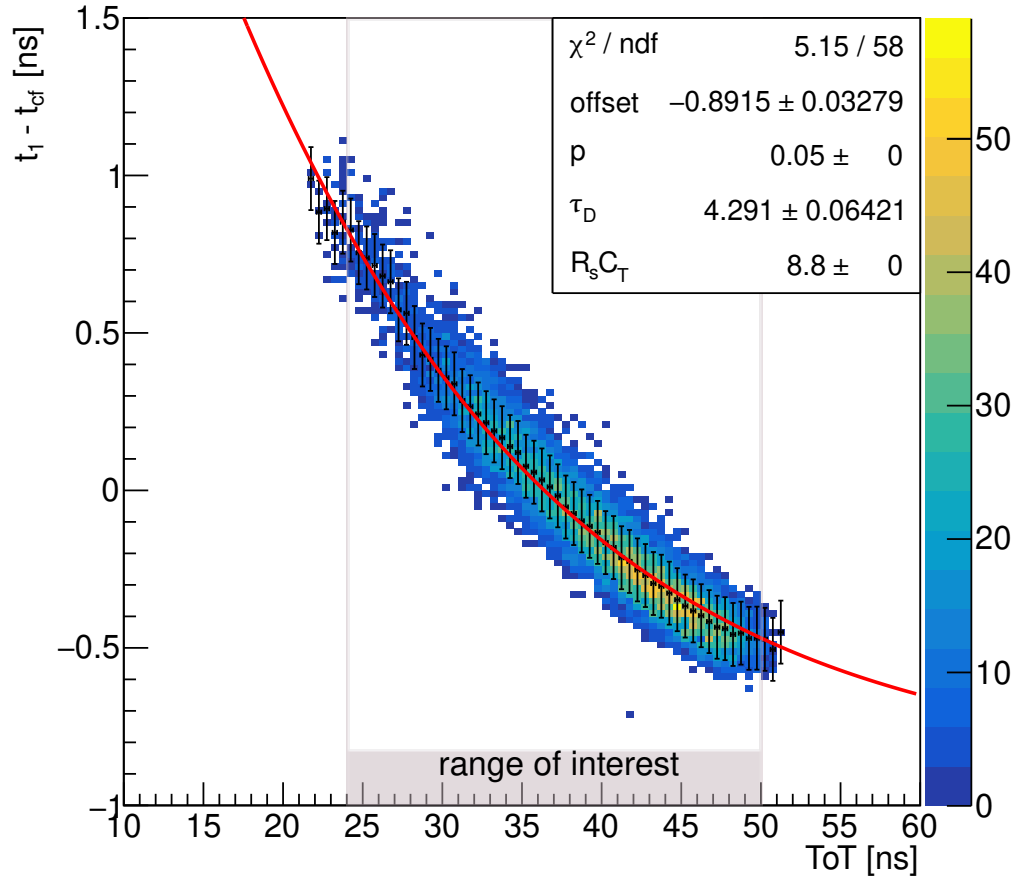
280 MeV

e^-

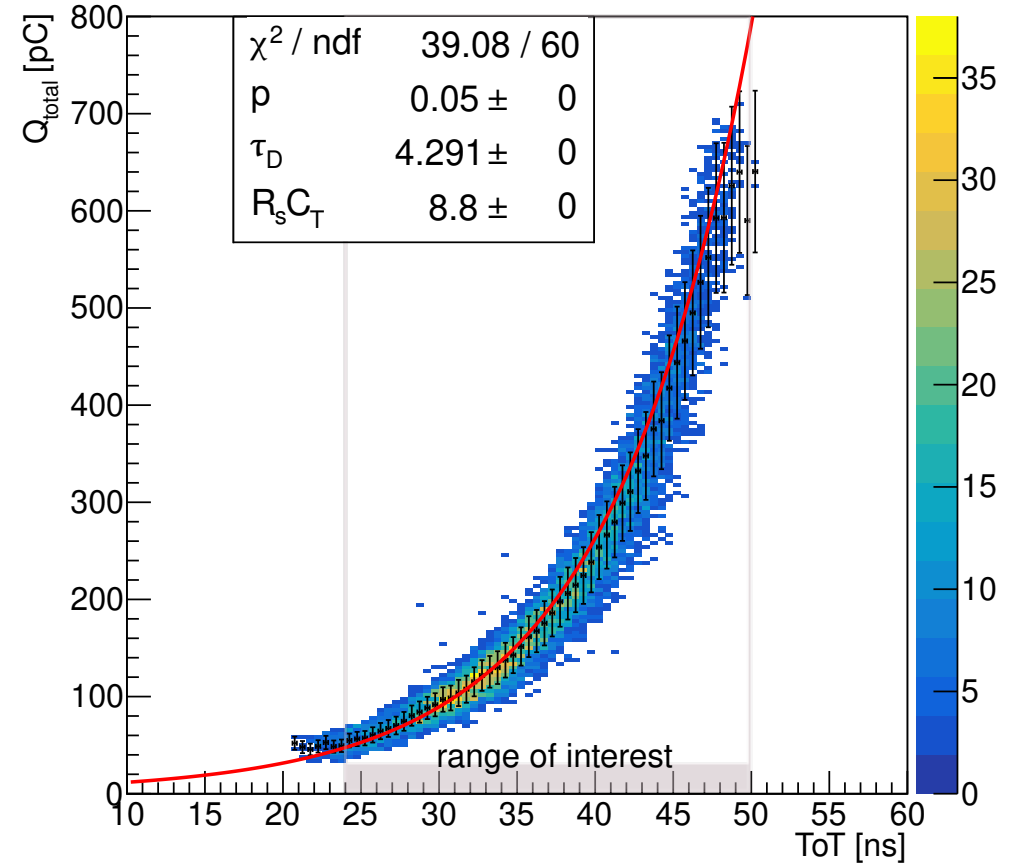
LPI setup



$$t_1 \approx 2R_s C_T W_0 \left(\frac{T_p}{2R_s C_T} \sqrt{\frac{e-1}{p}} e^{\frac{T_p - ToT}{2R_s C_T}} \right) \quad ToT \equiv t_2 - t_1$$



$$Q_{total} = \frac{\theta}{R_s} \left(\frac{pT_p}{2(e-1)} + R_s C_T - \tau_D(1-p) \right) e^{\frac{ToT + t_1 - T_p}{R_s C_T}}$$



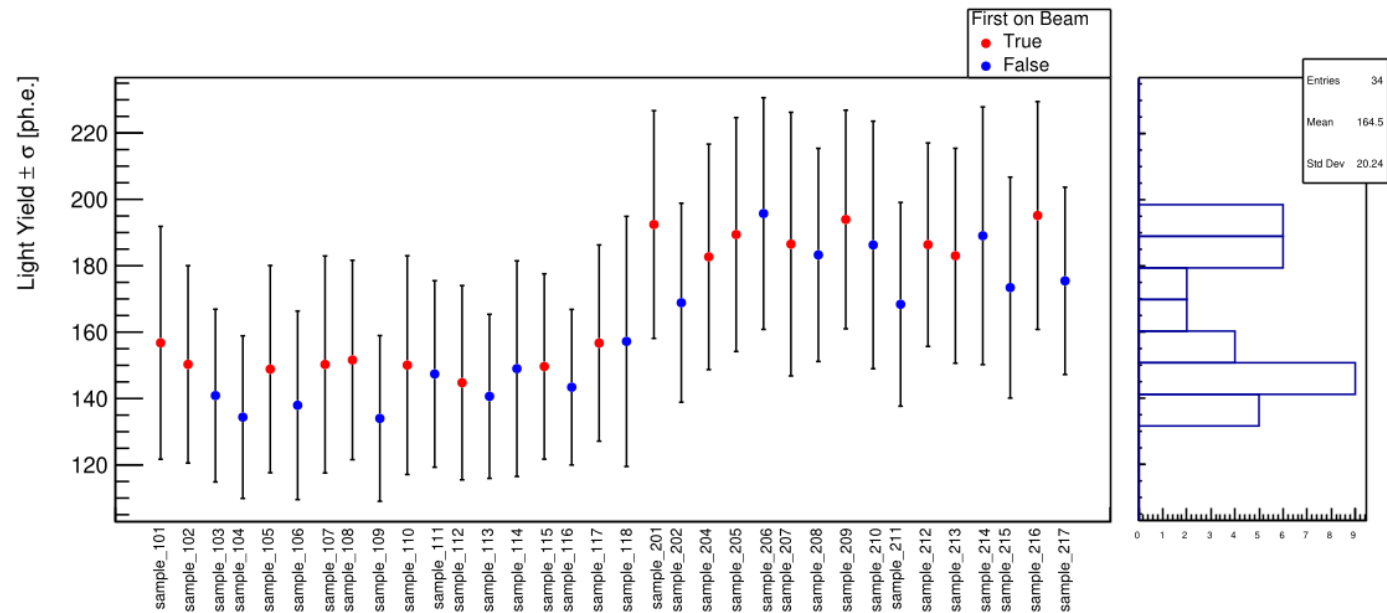
Purpose:

- Perform slewing correction based on physical principles

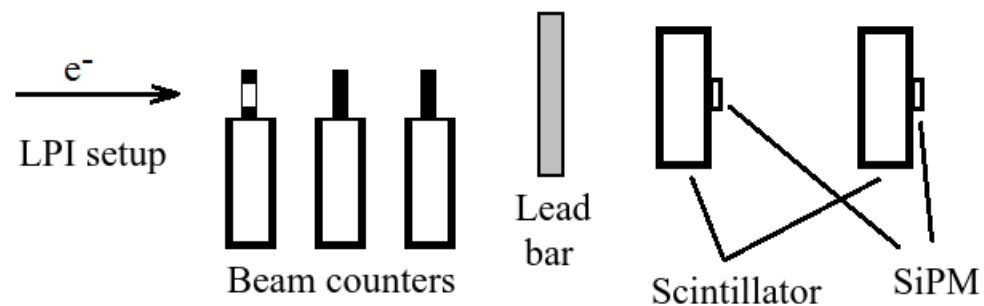
By-product:

- Ideal: obtain τ_D , $R_s C_T$, p from tdc:tot slewing correction fit and reconstruct signal charge
- Reality: tdc:tot correlation shows low sensitivity to p and $R_s C_T$, therefore these parameters are fixed at their average values

N. Karpushkin, et al., Nucl. Instrum. Meth. A 1068 (2024) 169739.

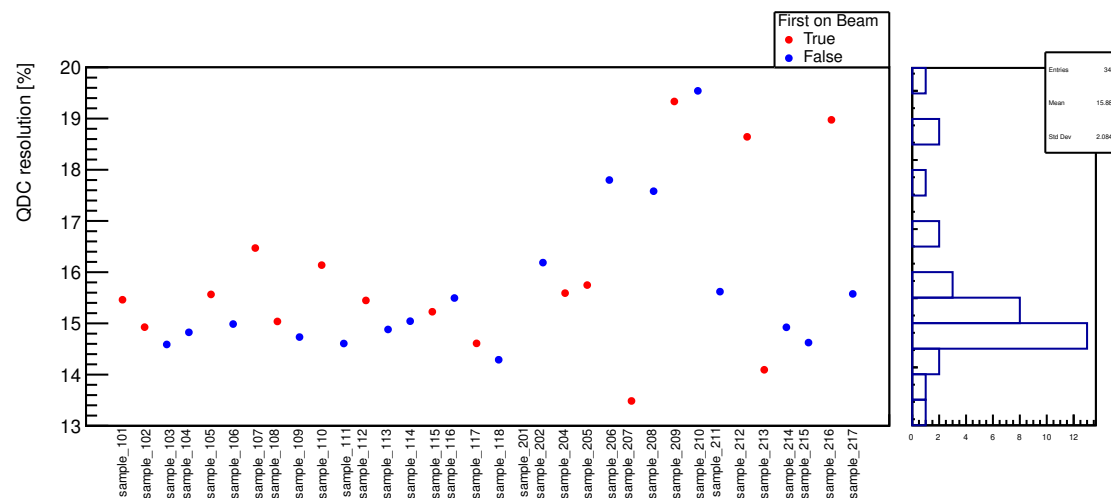
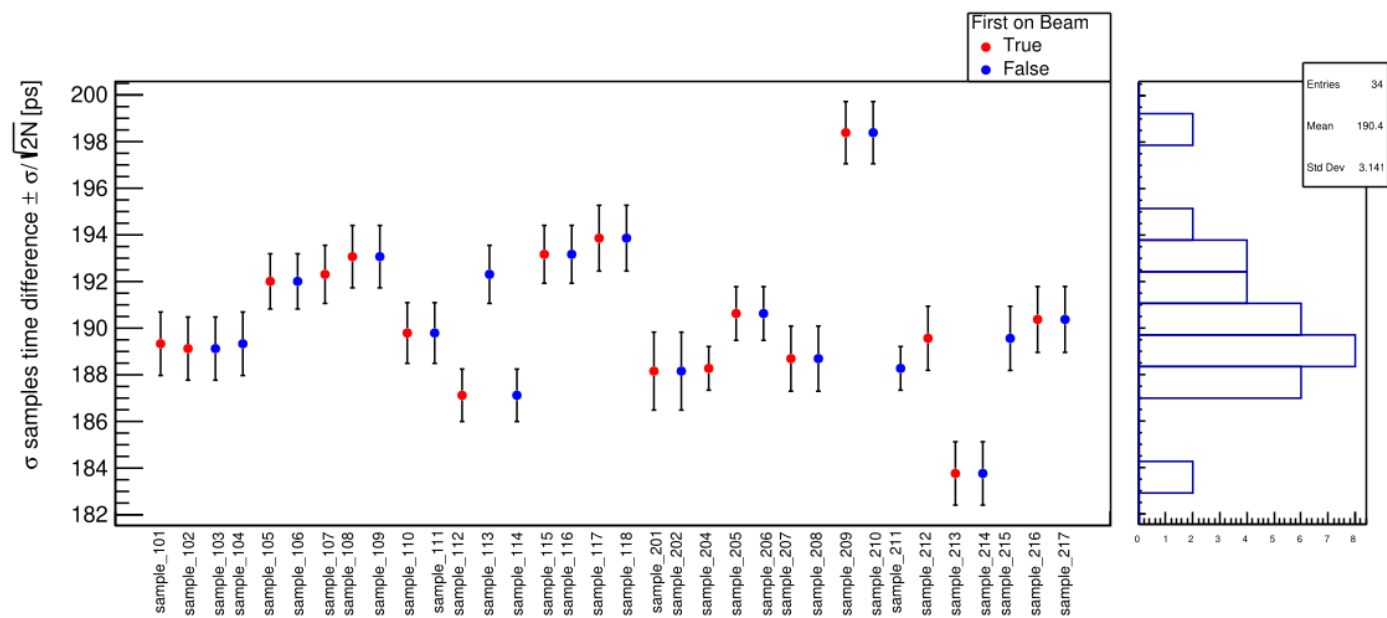


34 scintillator samples from 2 production series were tested at 280-MeV electron beam at LPI.



LPI test March 2024 averaged results

Measurement	Average in center	Gradient
Light Yield	151 or 179 p.e.	-43 p.e./cm
Time resolution	135 ps	+16 ps/cm
Charge resolution	<20 %	0 %/cm

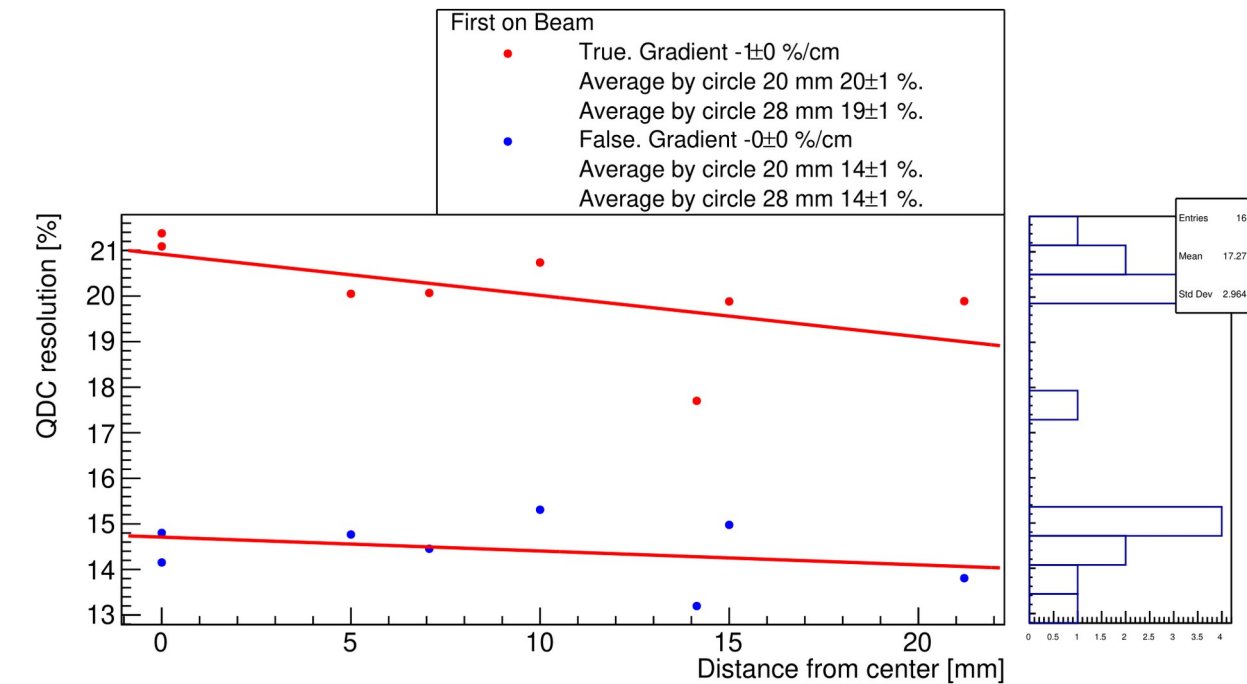
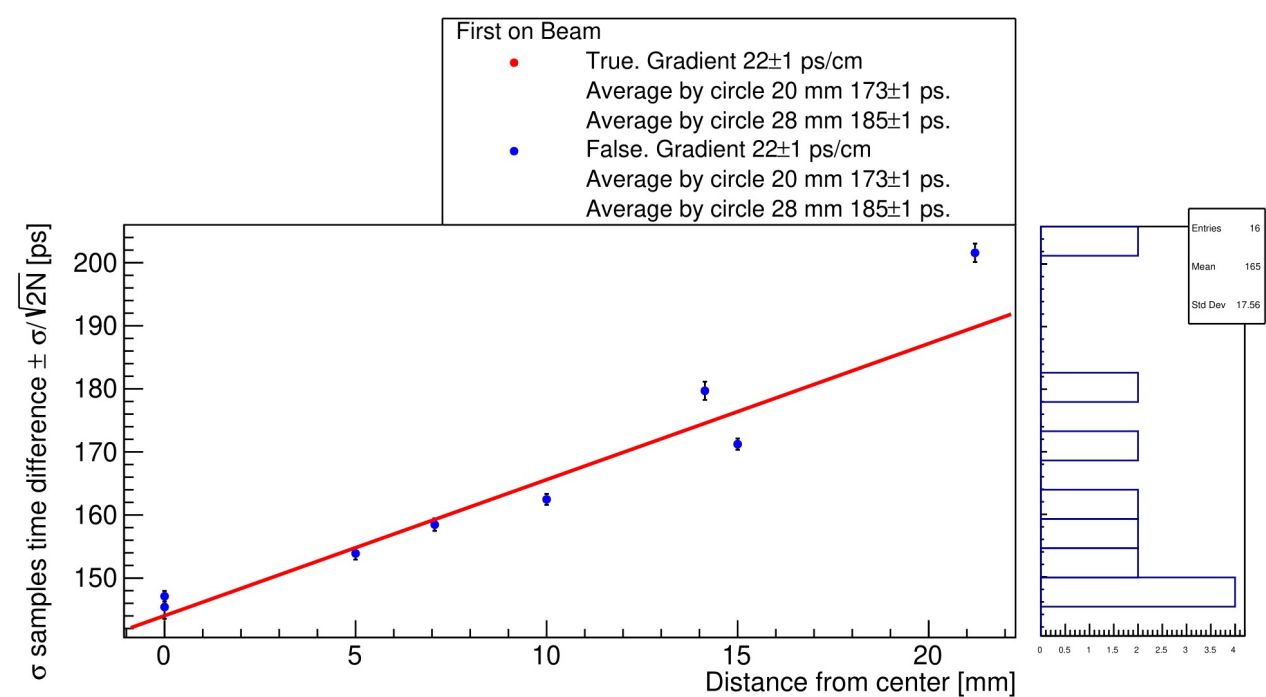
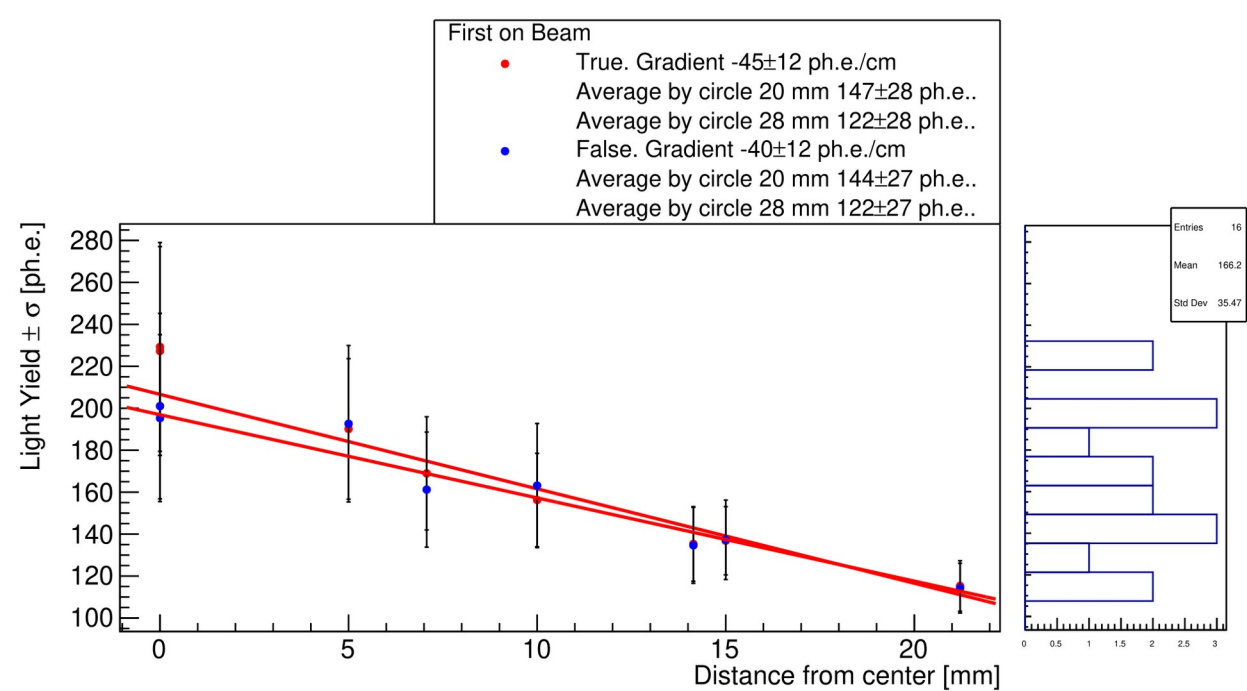


Conclusion and next steps

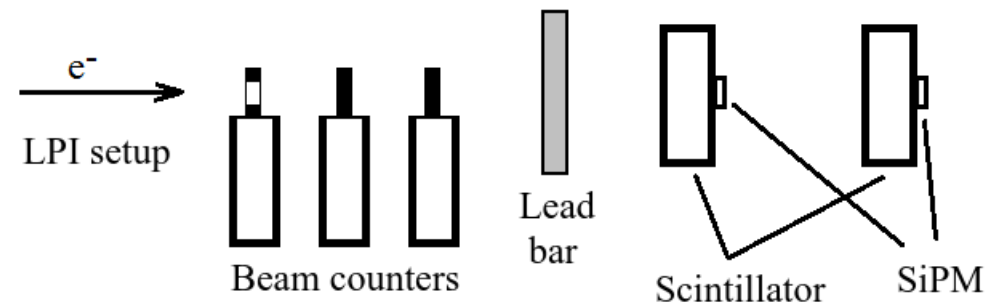
- 34 JINR-produced scintillator samples for HGND were tested at LPI on the 280 MeV electron beam.
- The electronics are tuned so as not to distort the smooth physical behavior.
- Analytical description of signal shape is developed,
allowing physically based description of tdc:ToT slewing correction and signal charge reconstruction
 - Average time resolution achieved: 135 ps
 - Average charge resolution achieved: <20%
- HGND performs the ToF measurement. Central trigger time corrected for slewing is required in bmnroot dst

Thank you for your attention!

BACKUP



LPI test March 2024 averaged results		
Measurement	Average in center	Gradient
Light Yield	151 or 179 p.e.	-43 p.e./cm
Time resolution	130 ps	+16 ps/cm
Charge resolution	<20 %	0 %/cm



EOS for high baryon density matter

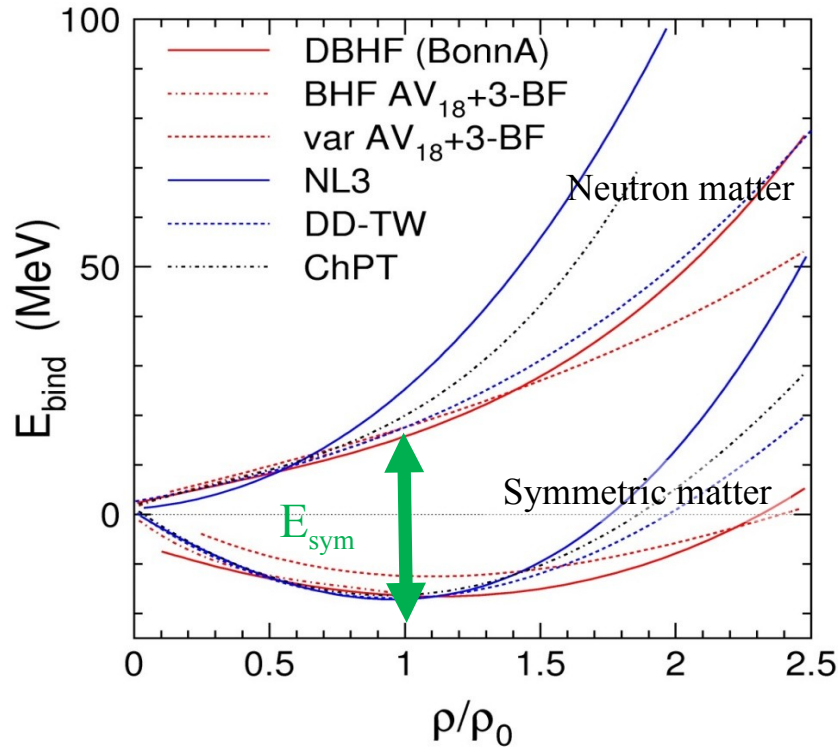
The binding energy per nucleon: $E_A(\rho, \delta) = E_A(\rho, 0) + E_{sym}(\rho)\delta^2 + O(\delta^4)$

Isospin asymmetry:

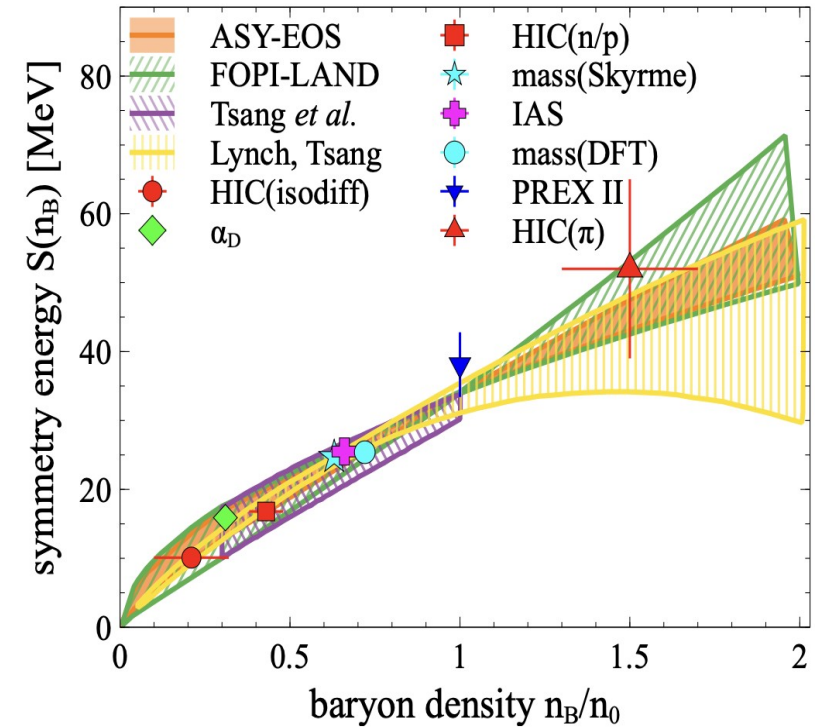
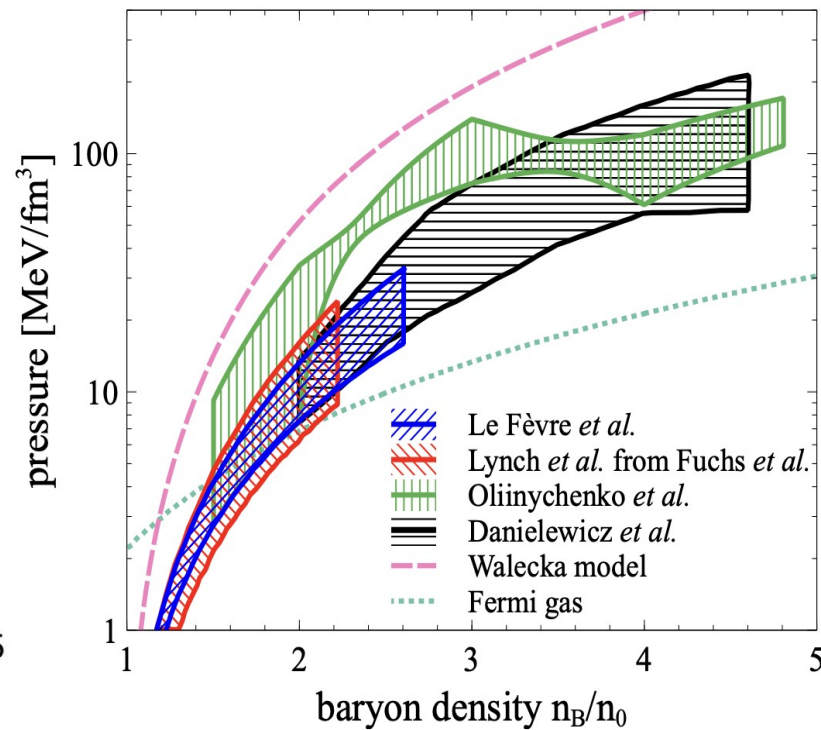
$$\delta = (\rho_n - \rho_p) / \rho$$

Symmetric matter

Symmetry energy



Ch. Fuchs and H.H. Wolter, EPJA 30 (2006) 5



A. Sorensen *et al.*, Prog.Part.Nucl.Phys. 134 (2024) 104080

EOS for high baryon density matter

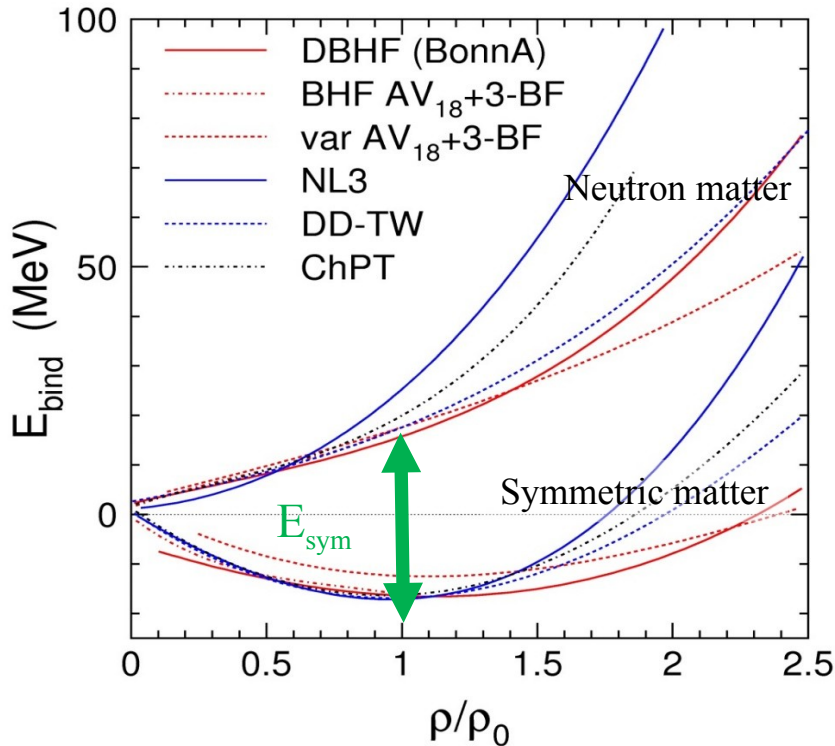
The binding energy per nucleon: $E_A(\rho, \delta) = \boxed{E_A(\rho, 0)} + \boxed{E_{sym}(\rho)}\delta^2 + O(\delta^4)$

Isospin asymmetry:

$$\delta = (\rho_n - \rho_p) / \rho$$

Symmetric matter

Symmetry energy



Ch. Fuchs and H.H. Wolter, EPJA 30 (2006) 5

- Being extensively studied nowadays using observables (flow, meson yields, etc) to explore incompressibility

$$K_0 = 9\rho^2 \frac{d^2 E_A}{d\rho^2}$$

- One of the main sources of uncertainty: discrepancy between experimental data

- One of the main parameters to study is the E_{sym} slope

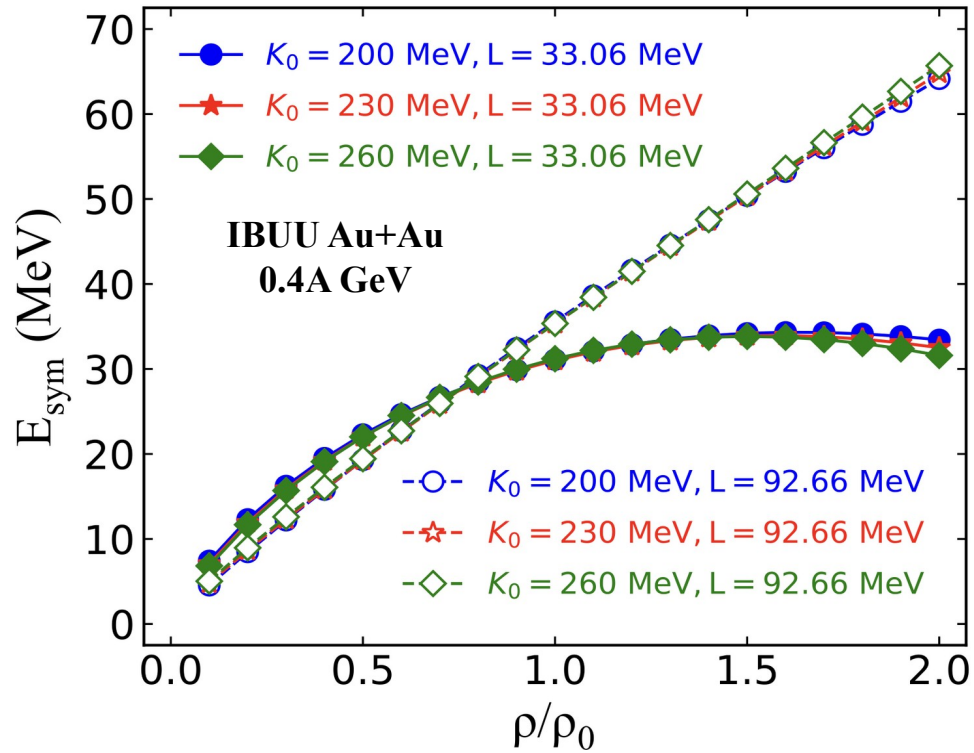
$$L = 3\rho \frac{dE_{\text{sym}}(\rho)}{d\rho}$$

- No experimental data for beam energies $E_{\text{kin}} > 0.4$ GeV
- One needs to establish observables sensitive to L and obtain new experimental data

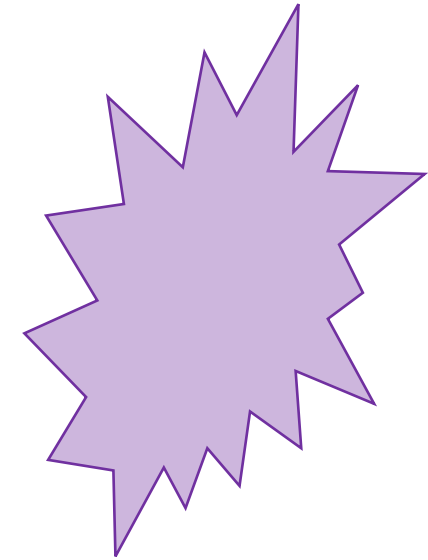
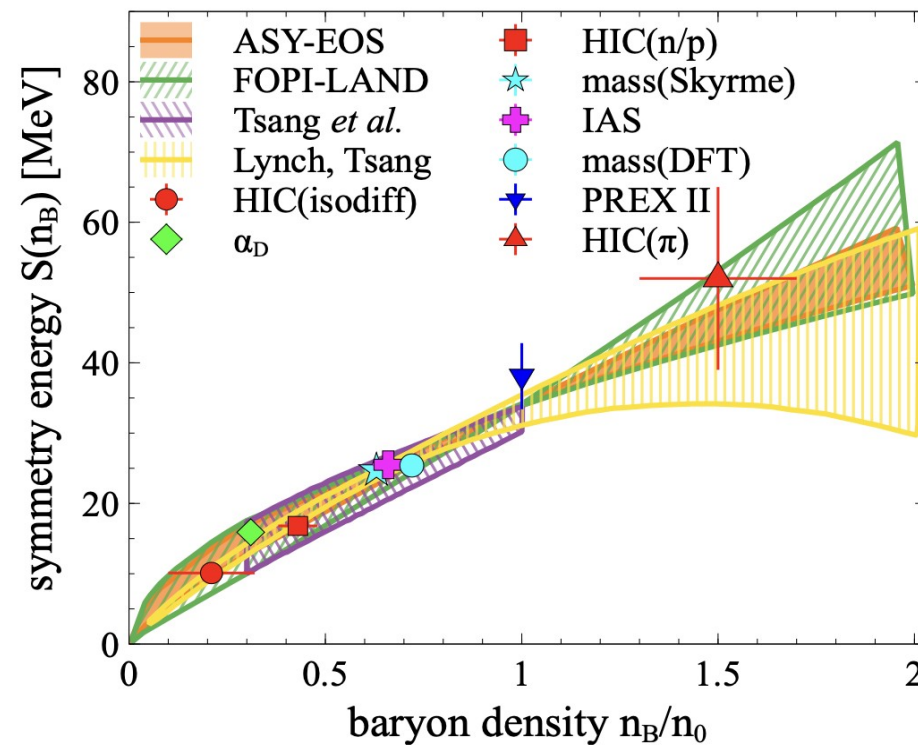
New data is needed to further constrain transport models with hadronic d.o.f.

Symmetry energy in high-density region

X.X. Long, G.F. Wei, Phys.Rev.C 109 (2024) 5, 054619



A. Sorensen et. al., Prog.Part.Nucl.Phys. 134 (2024) 104080



uncovered region
above $2 n_B/n_0$

- Nuclotron-NICA density region: $2 < n_B/n_0 < 8$
- Symmetry energy E_{sym} has strong density dependence and can be described with its slope

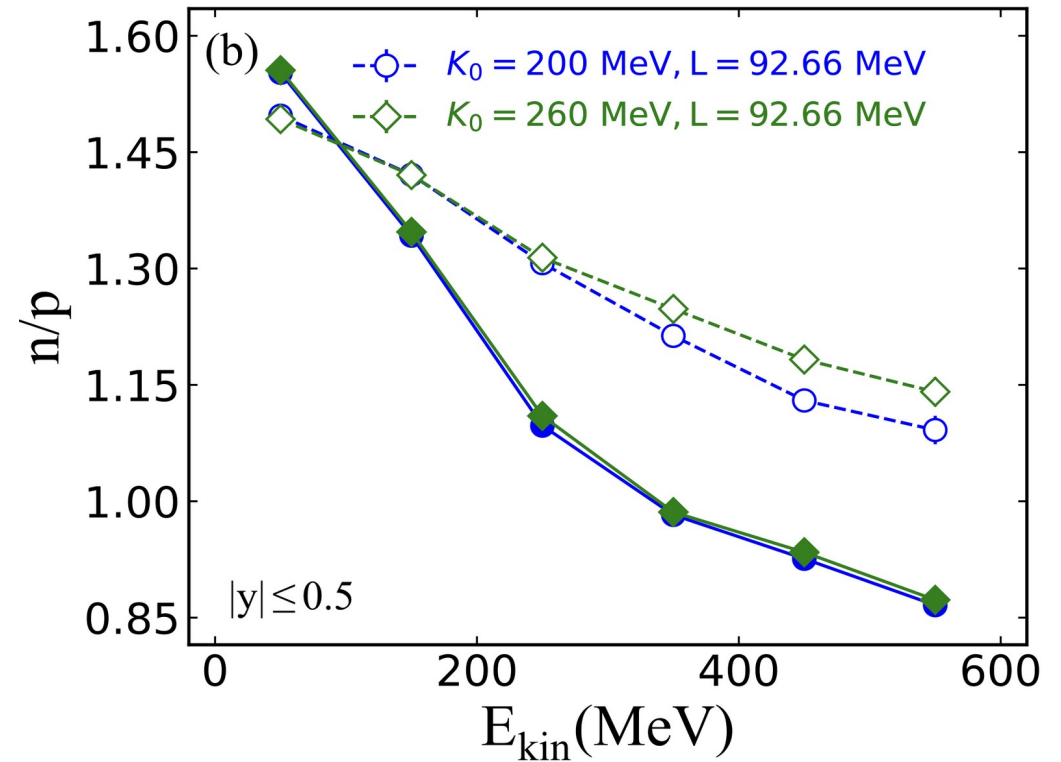
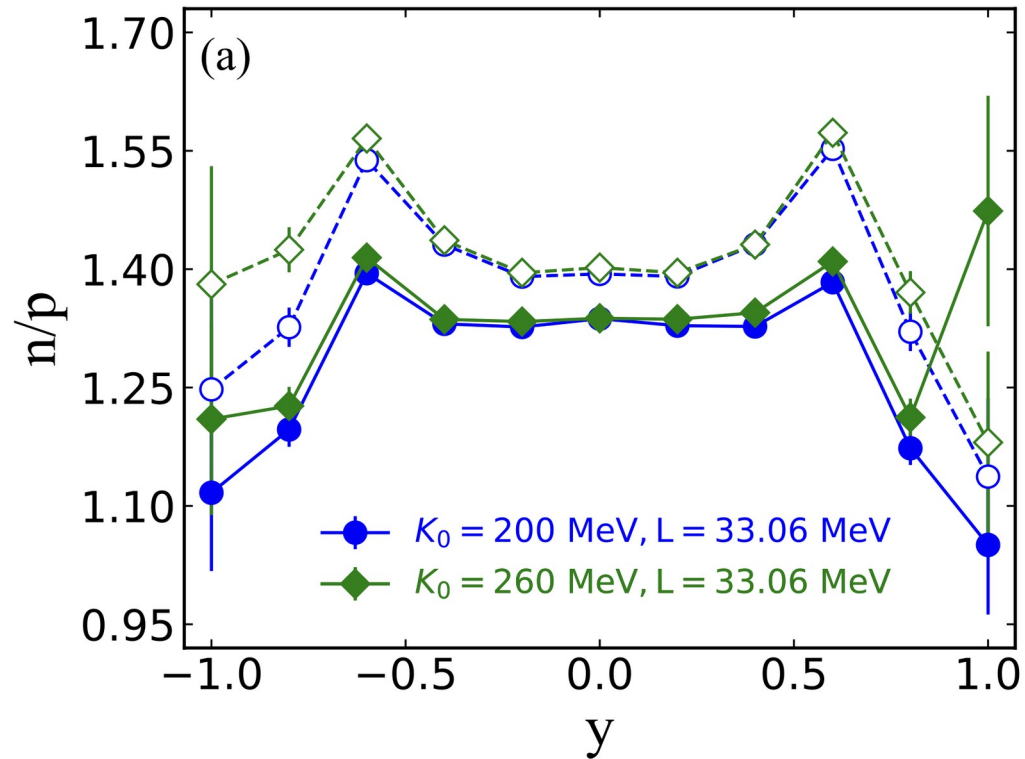
What observables can we use to extract information about L ?

Observables to study symmetry energy

Rapidity and kinetic energy distributions of n/p ratios show strong dependence on L and weak dependence on K_0

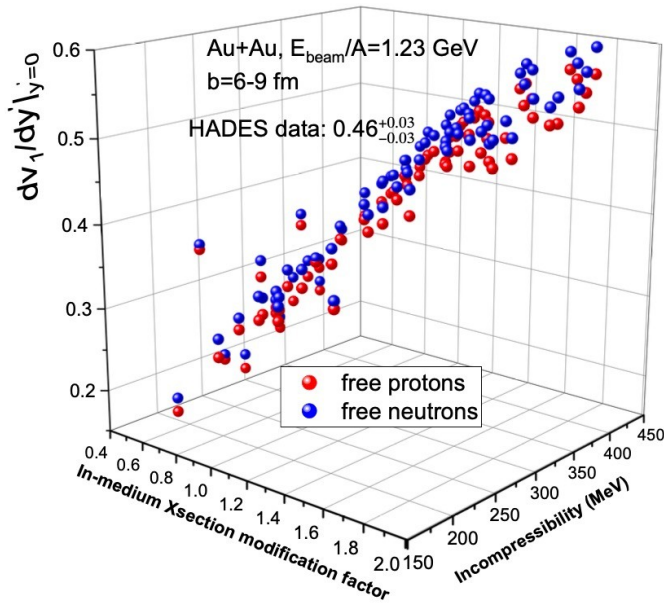
X.X. Long, G.F. Wei, Phys.Rev.C 109 (2024) 5, 054619

IBUU, Au+Au, 0.4A GeV



Neutron measurements are required to extract robust information about symmetry energy

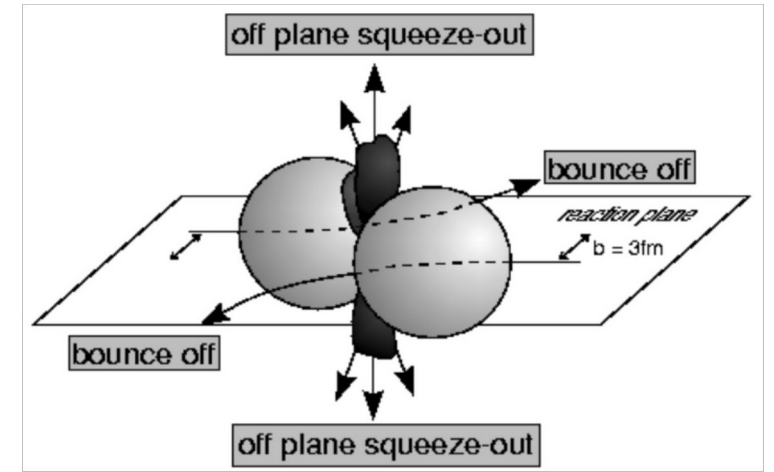
Collective flow as sensitive probe to the EOS



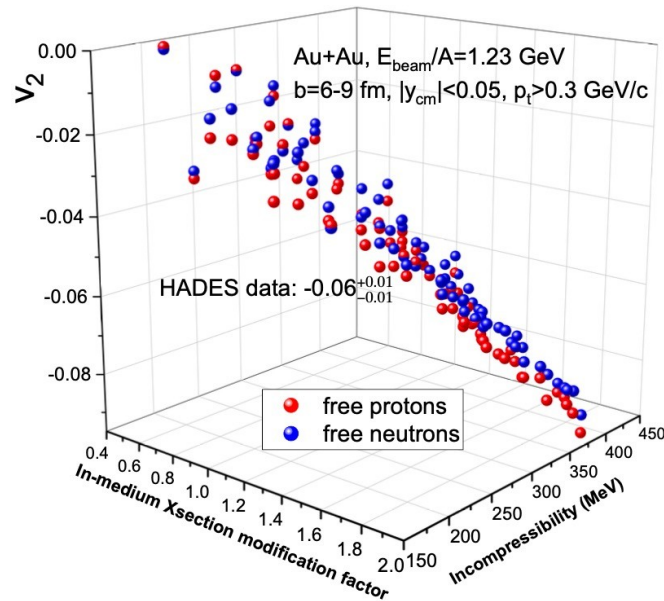
Incompressibility parameter $K_0(\rho)$:

Specifies the behavior of EOS in the given baryon densities

Models with flexible EOS for different (K_0, ρ) are required



$$\frac{dN}{d\varphi} \propto 1 + 2 \sum_{n=1} v_n \cos[n(\varphi - \Psi_{RP})], v_n = \langle \cos[n(\varphi - \Psi_{RP})] \rangle$$



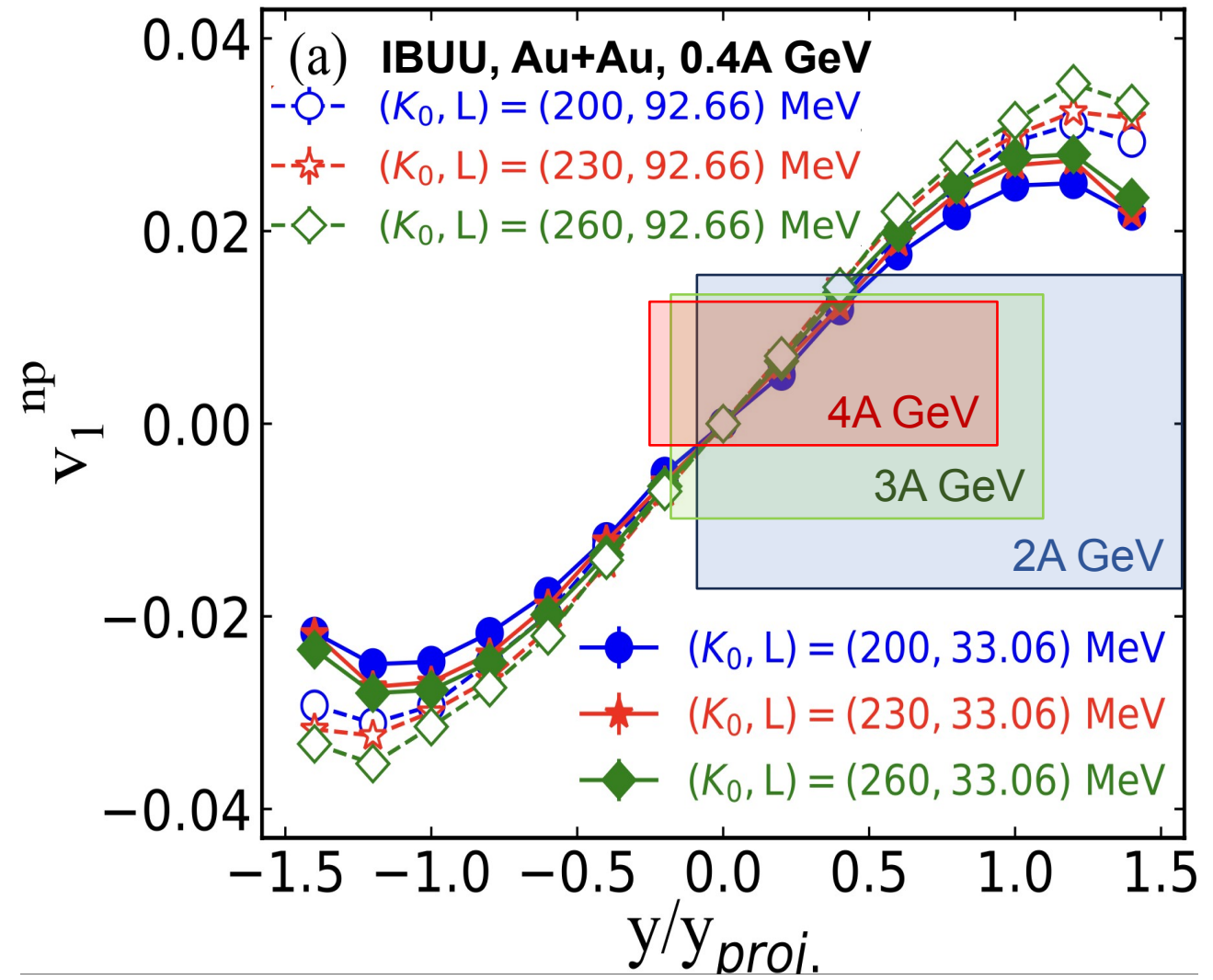
Collective flow is sensitive to:

- Compressibility of the created in the collision matter
- Time of the interaction between the matter within the overlap region and spectators

How to measure the collective flow?

Using v_1^{np} to study L

X.X. Long, G.F. Wei, Phys.Rev.C 109 (2024) 5, 054619



One can define free neutron-proton differential directed flow:

$$v_1^{np} = \frac{N_n(y)}{N(y)} \langle v_1^n(y) \rangle - \frac{N_p(y)}{N(y)} \langle v_1^p(y) \rangle$$

$N_n(y), N_p(y), N(y)$ - total number of neutrons, protons and nucleons respectively

$\langle v_1^n(y) \rangle, \langle v_1^p(y) \rangle$ - flow of neutrons and protons respectively

- v_1^{np} sensitive to both K_0 and L which may lead to ambiguous interpretation
 - More observables might be necessary for robust study of L

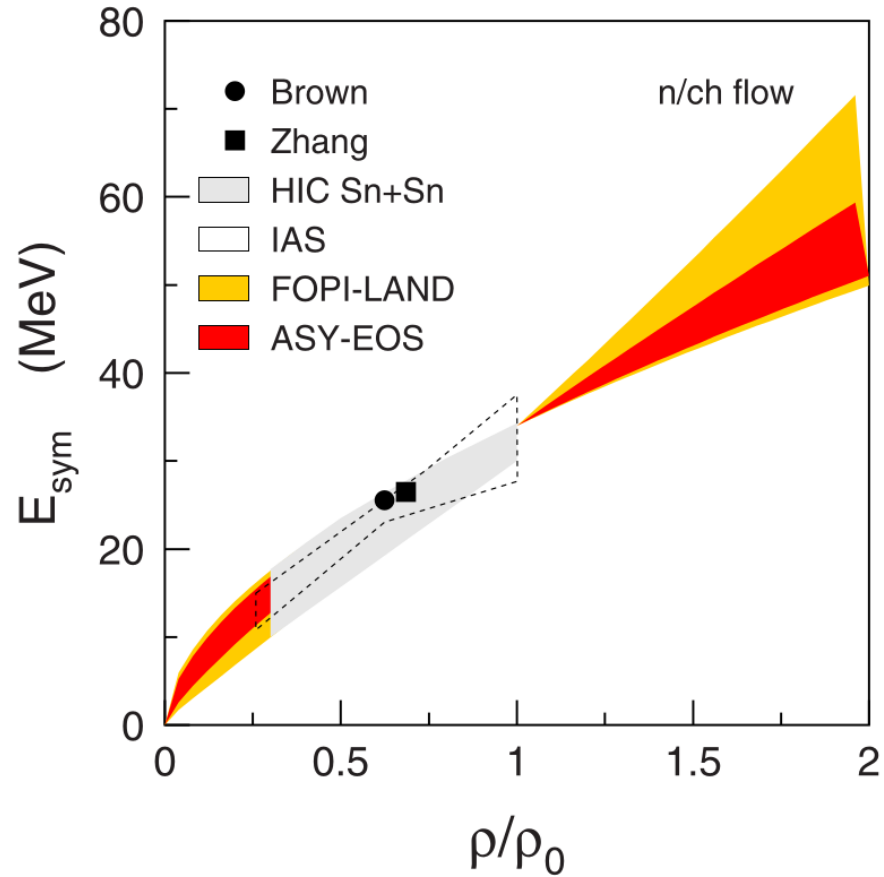
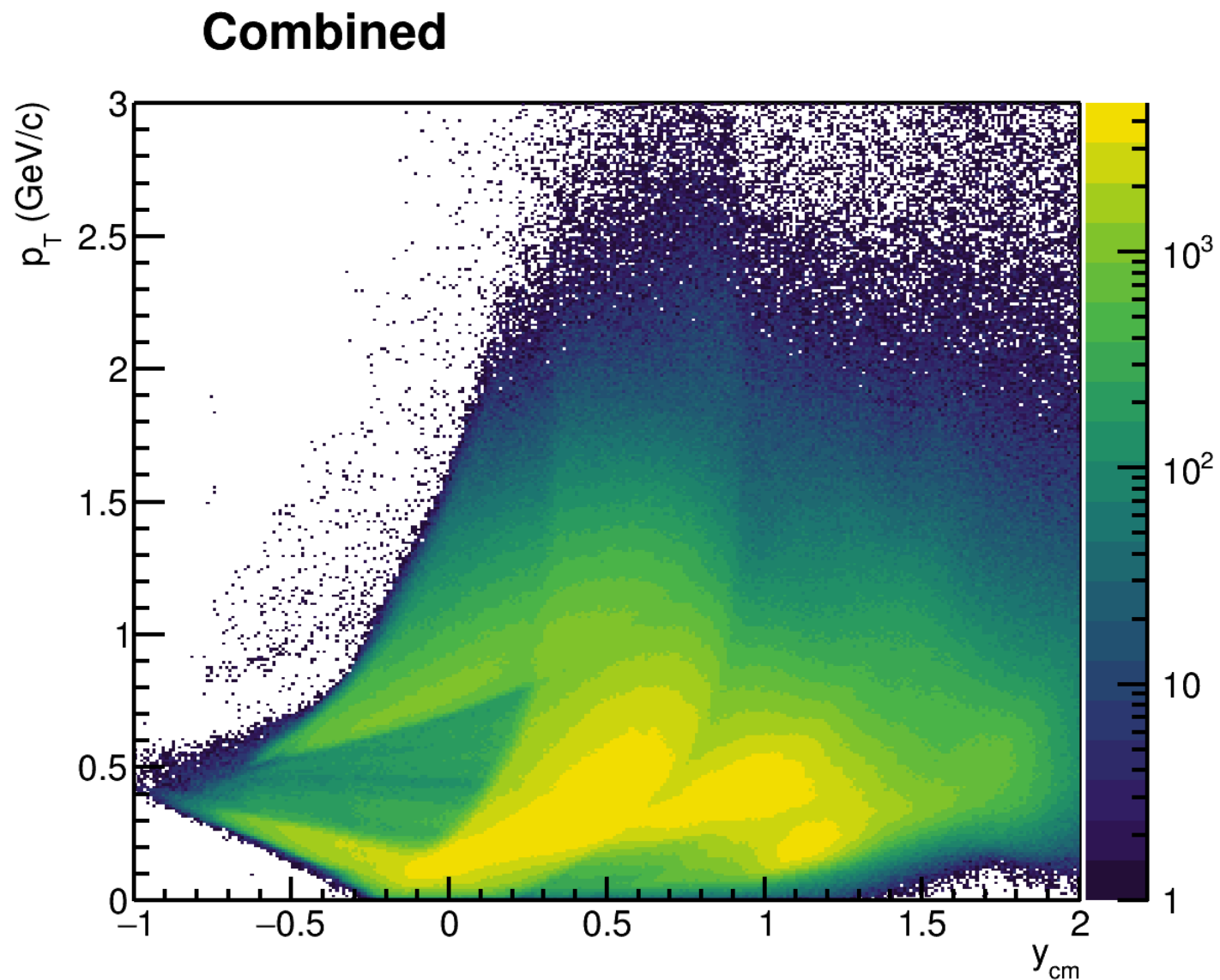
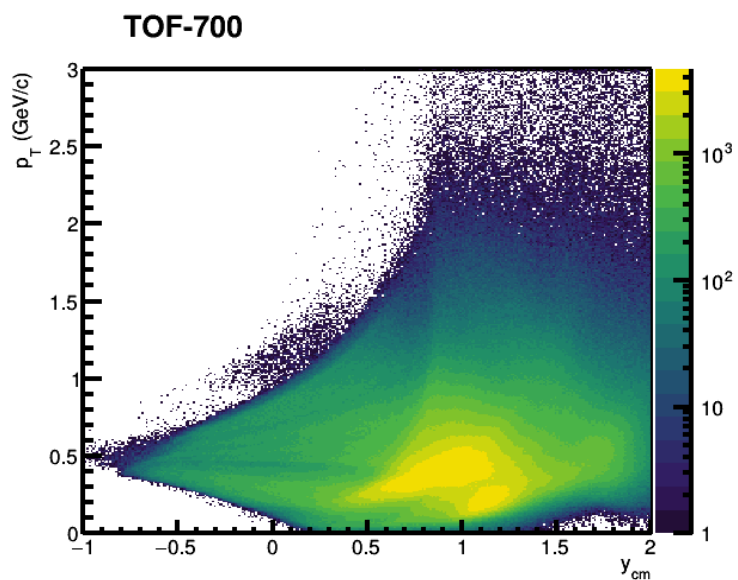
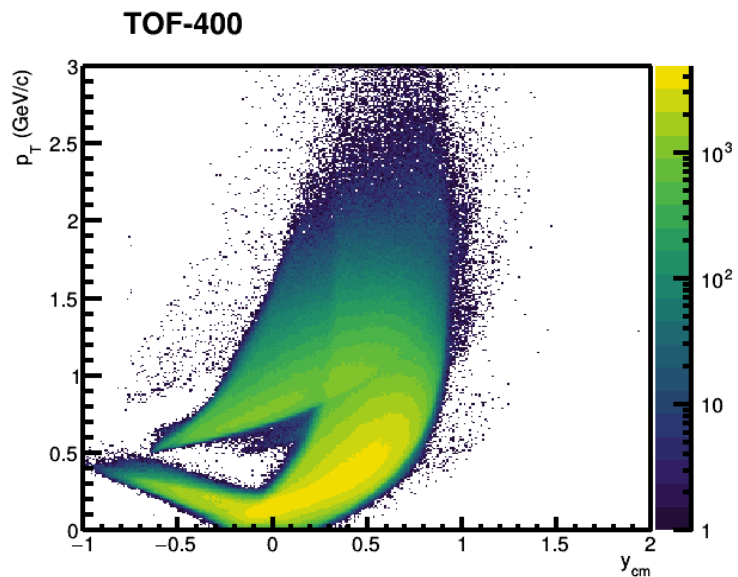


FIG. 18. Constraints deduced for the density dependence of the symmetry energy from the present data in comparison with the FOPI-LAND result of Ref. [5] as a function of the reduced density ρ/ρ_0 . The low-density results of Refs. [78–81] as reported in Ref. [82] are given by the symbols, the gray area (HIC), and the dashed contour (IAS). For clarity, the FOPI-LAND and ASY-EOS results are not displayed in the interval $0.3 < \rho/\rho_0 < 1.0$.

Proton p_T - y acceptance



Analytical description of light signals captured by SiPM: main behavior

$$N_{ph}^{scint}(t) \approx N_{ph}^0 e^{-t/\tau_D}$$

N_{ph}^0 – normalization factor, τ_D – light decay constant.

Solution 1 – Process as convolution of photoelectron current $I_{discharge}$ with SiPM impulse response function $g(t)$

$$I_{discharge} = -q\eta G \frac{dN_{ph}^{scint}}{dt} \quad g(t) = \frac{1}{R_s C_T} e^{-t/R_s C_T}$$

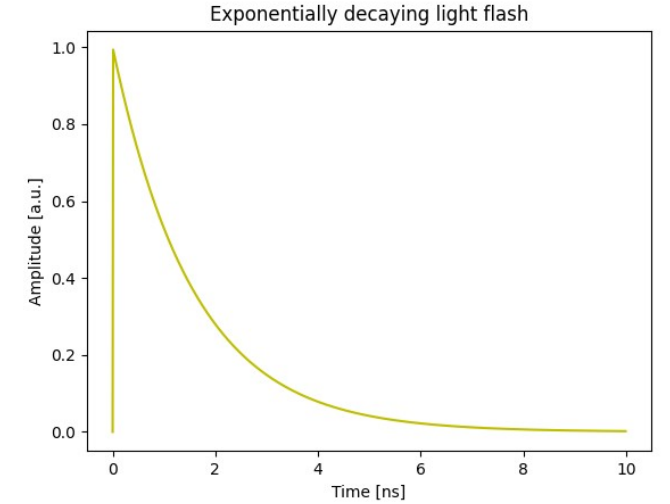
η – PDE, q – electron charge, G – SiPM gain, R_s – load resistance + low intrinsic SiPM resistance, C_T – total SiPM capacitance.

$$V(t) = R_s (I_{discharge} * g)(t) = \frac{\eta q G N_{ph}^0}{C_T \tau_D} \int_0^t e^{-\frac{x}{\tau_D}} e^{-\frac{t-x}{R_s C_T}} dx = \frac{\eta q G N_{ph}^0 R_s}{R_s C_T - \tau_D} \left(e^{-t/R_s C_T} - e^{-t/\tau_D} \right). \quad (1)$$

Solution 2 – Process as differential equation

$$\frac{dQ}{dt} = I_{recharge} - I_{discharge} \quad V_{bias} - R_s I_{recharge} = \frac{Q}{C_T}.$$

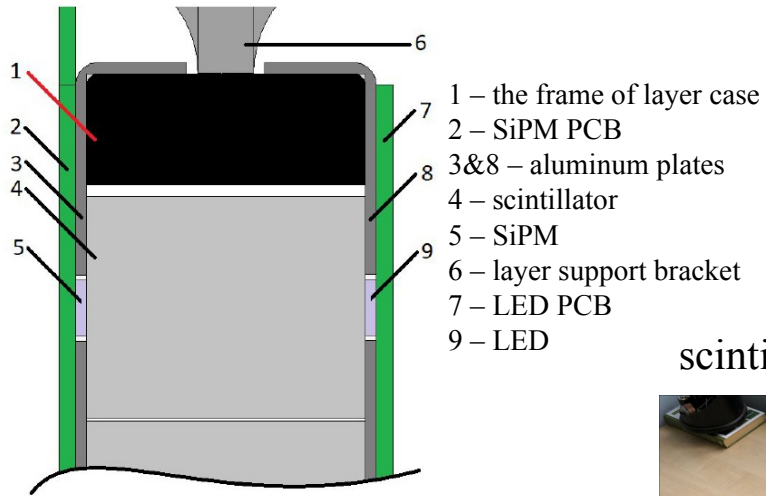
$$V(t) = R_s I_{recharge} = \frac{\eta q G N_{ph}^0 R_s}{R_s C_T - \tau_D} \left(e^{-t/R_s C_T} - e^{-t/\tau_D} \right). \quad (2)$$



Construction status

LPI test March 2024 averaged results	
Measurement	Average over 20mm circle
Light Yield	94 or 122 p.e.
Time resolution	156 ps = $\frac{\sqrt{(135+1.6*r)*2\pi \text{ rdr}}}{\pi r^2}$
Charge resolution	<20 %

Structure of active layer



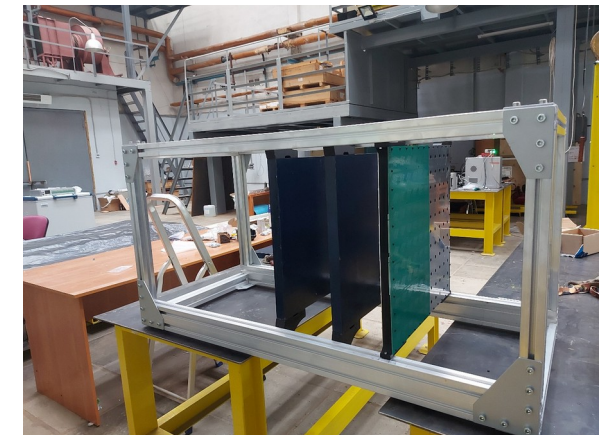
scintillator layer assembled



active layer PCB positioning



The HGND mock-up assembled at INR



- **Scintillator Cells:** All ~2,000 cells (40x40x25 mm³) have been built.
- **PCB:** Design is finalized and production is underway.
- **Readout board:** The FPGA-based TDC readout board is under active development.
- **Prototype:** First mock-up prototype with scintillator layer assembled; beam test preparations completed.
- **Timeframe:** To be commissioned by the end of 2025.