

# Pair production is a key tool to study TMD PDFs

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## Report on activity of Samara University group in 2024

- ▶ **People:** 3 principal researchers (Saleev V., Shipilova A., Karpishkov A.), PhD students (Alimov L., Shilyaev K.), students (Morosova S., Ospennikov N., Chernyshev A., Shapurin F., Pustobaeva A., Maloletnev G.)
- ▶ **New young researchers in the group:** Fedor Martynenko, Alexey Eskin
- ▶ **Tasks:** Theory ( $J/\psi$ ,  $D$ ,  $\gamma$  production in the TMD factorization, pair production at small  $p_T$  in the TMD factorization), MC modeling (S/B ratio study for hard probes with Pythia and KaTie, and timeslices simulation with Geant4)
- ▶ **Financial support in 2024:** total amount is 9360K rubles, two 128-core servers (3200K rubles)



# Report on activity of Samara University group in 2024

## ► Relevant publications in 2024:

1. A. V. Karpishkov, V. A. Saleev and K. K. Shilyaev, Production of Polarized  $J/\psi$  Mesons within Nonrelativistic QCD and Generalized Parton Model, Phys. Atom. Nucl. **87** (2024) no.4, 494-497
2. A. V. Anufriev and V. A. Saleev, High-Energy Production of  $\eta_c$  Mesons in Proton-Proton Collisions, Phys. Part. Nucl. **55** (2024) no.4, 836-840
3. V. Saleev, Challenges and Problems in Charmonium Production at the SPD NICA, Physics of Particles and Nuclei, 2024, Vol. 55, No. 6, pp. 1460-1466.
4. N. Y. Ospennikov and A. V. Shipilova, The Study of Backgrounds in Direct Photon Production at SPD NICA Energies, Phys. Part. Nucl. Lett. **21** (2024) no.4, 687-690
5. S. D. Morozova and A. V. Shipilova, The Simulation of Interactions in the Straw-Based SPD Track Detector and Primary Vertex Reconstruction, Phys. Part. Nucl. Lett. **21** (2024) no.4, 727-730

## ► Forthcoming publications in 2024-2025:

1. Small- $p_T$   $J/\psi$  production in the soft gluon resummation approach at NICA
2. DLSA in the charmonium production at NICA
3.  $D\bar{D}$  pair production at NICA
4. Relativistic correction in the charmonium production at NICA



# Outline

- ▶ CPM and TMD PM
- ▶ Hard probes at the SPD NICA
- ▶ Pair production at the small transverse momenta,  $p_T \ll M$
- ▶  $\mu^+ + \mu^-$  production
- ▶  $\gamma + \gamma$  production
- ▶  $D + \bar{D}$  production
- ▶  $J/\psi + J/\psi$  production
- ▶  $\gamma + J/\psi$  production



## CPM and TMD PM

- ▶ **Collinear Parton Model (CPM):**  $p_T \gg q_{1,2T} \sim 1 \text{ GeV}$ ,  $\mu = \mu_F \sim p_T$   
 $2 \rightarrow 2, 2 \rightarrow 3, \dots$  parton subprocesses

$$d\sigma^{CPM}(pp \rightarrow kX) = \sum_{i,j} \int dx_1 dx_2 f_i(x_1, \mu) f_j(x_2, \mu) d\hat{\sigma}(ij \rightarrow kl),$$

DGLAP evolution equations for collinear PDFs  $f_i(x, \mu)$

$$\frac{d\sigma^{CPM}(pp \rightarrow kX)}{dp_T} \sim \frac{d\hat{\sigma}(ij \rightarrow kl)}{dp_T}$$

## CPM and TMD PM

- ▶ **TMD Parton Model (TMD):**  $p_T \sim q_{1,2T} \sim 1 \text{ GeV}$ ,  $p_T \ll \mu$  and  $\mu$  is a hard scale independent on  $p_T$

$$d\sigma(pp \rightarrow kX) = \sum_{i,j} \int dx_1 dx_2 F_i(x_1, \mathbf{q}_{1T}) F_j(x_2, \mathbf{q}_{2T}) d\hat{\sigma}(ij \rightarrow k) + \mathcal{O}\left(\frac{p_T}{\mu}\right)^2,$$

2  $\rightarrow$  1 processes at the parton level

$$\tilde{F}(x, \mathbf{b}_T) = \int d^2 q_T e^{i\mathbf{b}_T \mathbf{q}_T} F(x, \mathbf{q}_T), \quad \text{two-scale Collins-Soper evolution}$$

$$\tilde{F}(x, \mathbf{b}_T) = \tilde{F}(x, \mathbf{b}_T, \mu, \zeta)$$

$$\frac{d\sigma(pp \rightarrow kX)}{dp_T} = \sum_{i,j} \sigma_{ij} \int d^2 b_T e^{i\mathbf{b}_T \mathbf{p}_T} \tilde{F}_i(x_1, \mathbf{b}_T) \tilde{F}_j(x_2, \mathbf{b}_T)$$

$$\sigma = \sigma_0 + \alpha_S \sigma_1 + \alpha_S^2 \sigma_2 + \dots$$

## Hard probes at the SPD NICA

- ▶ **Inclusive  $\gamma$  production:**  $pp \rightarrow \gamma X$  and  $p_{T\gamma} \gg 1$  GeV  
At the parton level LO subprocesses are

$$q + g \rightarrow q + \gamma, \quad q + \bar{q} \rightarrow g + \gamma, \quad \text{and } \mu \sim p_{T\gamma}$$

- ▶ The process of single  $\gamma$  production is not a subject of TMD PM



## Hard probes at the SPD NICA

► **Inclusive  $D$ -meson production:**  $pp \rightarrow DX$

1. At the large  $p_{TD} \gg m_D$ , the only Collinear Factorization and CPM can be applicable
2. At the small  $p_{TD} \ll m_D(2m_D)$  we may suggest that TMD PM can be used, but ...

At the parton level LO subprocesses are  $2 \rightarrow 2$

$$g + g \rightarrow c + \bar{c}, \quad q + \bar{q} \rightarrow c + \bar{c}$$

$$\frac{d\sigma}{dp_{TD}} \sim \int d^2 p_{T\bar{D}} \overline{|M(gg \rightarrow c\bar{c})|^2}, \quad p_{TD} \approx p_{T\bar{D}}$$

To control TMD PM conditions, we must know that  $p_{T\bar{D}} \sim p_{TD} \ll m_D$ , and, in fact, we study D-meson pair production,  $pp \rightarrow D\bar{D}X$ .

3. There is FSI  $c\bar{c}$ -pair with spectator partons and interference between FSI and ISI, which destroy TMD factorization. Formally, we can use TMD factorization formula but the gluon TMD PDF became process dependent.





## Hard probes at the SPD NICA

► **Inclusive  $J/\psi$ -meson production:**  $pp \rightarrow J/\psi X$

1. At the large  $p_{T\psi} \gg m_\psi$ , the only Collinear Factorization and CPM is used, and  $\mu \sim p_T$
2. At the small  $p_{T\psi} \ll m_\psi \sim \mu$  we can use TMD PM can be used, but the answer depends on hadronization model

► In the Color Singlet Model (CSM) the LO subprocess is  $2 \rightarrow 2$ ,  $g + g \rightarrow J/\psi + g$

► In the NRQCD and ICEM, the LO subprocess is  $2 \rightarrow 1$ ,  $g + g \rightarrow J/\psi$  with color-octet intermediate state  $[^1S_0^{(8)}, ^3P_{0,2}^{(8)}]$ . In this case **the soft FSI and ISI+FSI** destroy factorization formula and TMD PDFs became process dependent.

► *Theoretically sound* processes for gluon TMD PDF study at the NICA energy in the charmonium production are the following (CSM works !):

$$pp \rightarrow \eta_c X \quad (g + g \rightarrow \eta_c)$$

$$pp \rightarrow \chi_c X \quad (g + g \rightarrow \chi_c).$$



# Pair production at the small transverse momenta, $p_T \ll M$

## The short motivation list of theoretical publications on pair production

- ▶ C. Balazs, E. L. Berger, S. Mrenna and C. P. Yuan, Photon pair production with soft gluon resummation in hadronic interactions, Phys. Rev. D **57** (1998), 6934-6947
- ▶ C. Pisano, D. Boer, S. J. Brodsky, M. G. A. Buffing and P. J. Mulders, Linear polarization of gluons and photons in unpolarized collider experiments, JHEP **10** (2013), 024
- ▶ T. Altinoluk, C. Marquet and P. Taels, Low- $x$  improved TMD approach to the lepto- and hadroproduction of a heavy-quark pair, JHEP **06** (2021), 085
- ▶ R. F. del Castillo, M. G. Echevarria, Y. Makris and I. Scimemi, Transverse momentum dependent distributions in dijet and heavy hadron pair production at EIC, JHEP **03** (2022), 047 doi:10.1007/JHEP03(2022)047
- ▶ D. Boer, L. Maxia and C. Pisano, Azimuthal asymmetries in lepton and heavy-quark pair production in UPCs, [arXiv:2410.23924 [hep-ph]].
- ▶ A. C. Serri, J. Bor, D. Boer and J. P. Lansberg,  $J/\psi$ -pair production at NLL in TMD factorisation at the EIC, PoS(EPJ-HEP2023) (2024), 272 doi:10.22323/1.449.0272

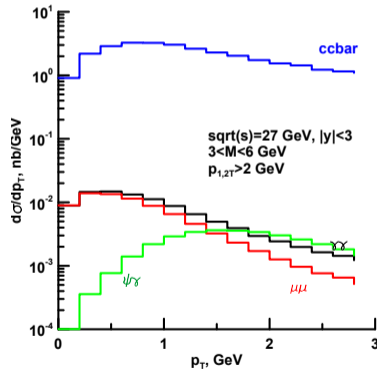


## Pair production at the small transverse momenta, $p_T \ll M$

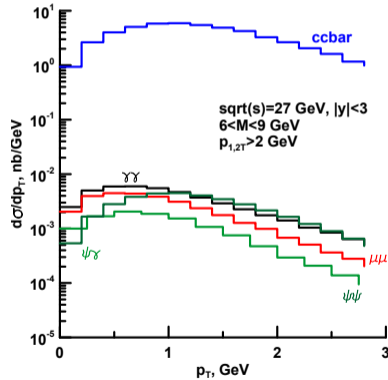
- ▶ **DY pair production**,  $pp \rightarrow \ell\bar{\ell}X$ , with  $p_T = |\mathbf{p}_{T\ell} + \mathbf{p}_{T\bar{\ell}}| \ll M = \sqrt{(p_\ell + p_{\bar{\ell}})^2}$ . The TMD factorization is OK.
- ▶ **Direct photon pair production**,  $pp \rightarrow \gamma\gamma X$ , with  $p_T \ll M = \sqrt{(p_{\gamma 1} + p_{\gamma 2})^2}$ . The TMD factorization is OK.
- ▶ **D-meson pair production**,  $pp \rightarrow D\bar{D}X$ , with  $p_T \ll M = \sqrt{(p_D + p_{\bar{D}})^2}$ . There is final state interaction, the TMD factorization is not OK.
- ▶  **$J/\psi + J/\psi$  pair production**. The TMD factorization is OK, if CSM is OK as hadronization model.
- ▶  **$J/\psi + \gamma$  pair production**. The TMD factorization is OK, if CSM is OK as hadronization model.



# Pair production at the small transverse momenta, $p_T \ll M$ , $KaTie$



# Pair production at the small transverse momenta, $p_T \ll M$ , $KaTie$



## Conclusions

▶ Single particle production processes to study gluon TMD PDFs

1.  $pp \rightarrow \eta_c X, pp \rightarrow \chi_c X$  (CSM !)
2.  $pp \rightarrow J/\psi X$  (COM !)

▶ Pair particle production processes to study TMD PDFs

1.  $pp \rightarrow l\bar{l}X$  and  $pp \rightarrow \gamma\gamma X$ , (quark TMD PDFs)
2.  $pp \rightarrow D\bar{D}X$  (FSI+ISI !)
3.  $pp \rightarrow J/\psi J/\psi X$  (CSM !)
4.  $pp \rightarrow J/\psi\gamma X$  (CSM !)



$$\sigma(pp \rightarrow D\bar{D}X) \approx 10 \text{ nb}, \quad \sigma(pp \rightarrow l\bar{l}X) \approx \sigma(pp \rightarrow \gamma\gamma X) \approx 10 \text{ pb}, \quad \sigma(pp \rightarrow J/\psi J/\psi X) \approx 1 \text{ pb}, \quad \text{here } p_{1,2T} > 2 \text{ GeV}$$

- ▶ The opportunity of pair production of D-mesons and charmonia at NICA should be study carefully, as from the theory side as in the MC modeling.



THANK YOU FOR YOUR ATTENTION!

