



Diquark role in production of baryons and exotic hadrons for the SPD NICA energies

Andrei V. Zelenov, Victor T. Kim
NRC «Kurchatov Institute» - PNPI, Gatchina

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- Large- p_T processes in QCD
- Diquark role in large- p_T hadron production
- Diquark role in large- p_T multi-quark exotic state production
- Ulysses
- Summary

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Introduction

The QCD parton model demonstrates a good description of mesons over a wide range of energies. But it can't describe an anomalously large yield of protons along with its strong scaling violation.

Taking into account the two-quark correlation (Diquark) allows us to describe the anomalous proton yield. [Laperashvili \(1982\)](#), [Ekelin et al \(1984\)](#), [Kim \(1988\)](#)

Being a higher-twist, the Diquark contribution can describe the strong scaling violation in deep inelastic scattering of nucleons observed in p/π^+ ratio. [Kim \(1988\)](#)



Large- p_T processes in QCD

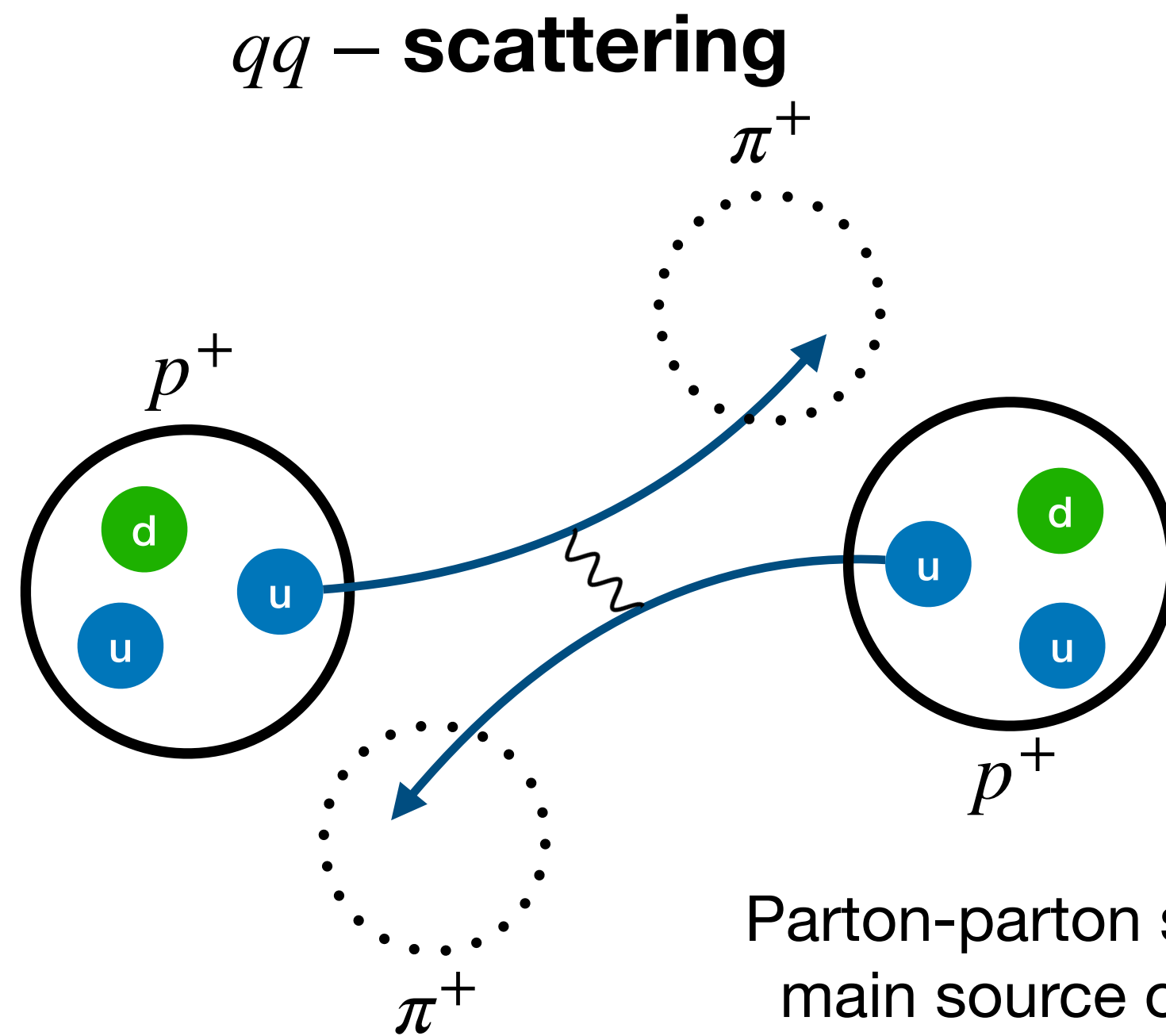
Collinear factorization

$$\frac{E d^3\sigma}{d^3p} = \int_{x_{min}}^1 dx \int_{y_{min}}^1 dy G_a^A(x, Q^2) G_b^B(y, Q^2) \left(\frac{d\sigma}{d\hat{t}} \right)_{ab} \frac{D_C^c(z, Q^2)}{\pi z}$$

$G_a^A(x, Q^2)$, $G_b^B(y, Q^2)$ & $D_C^c(z, Q^2)$ – scaling functions

IHEP, Serpukhov, $\sqrt{s} = 11.5$ GeV
FODS, V.V. Abramov et al. (1985)

FNAL, Batavia, $\sqrt{s} = 23.4$ GeV
D. Antreasyan et al. (1979)

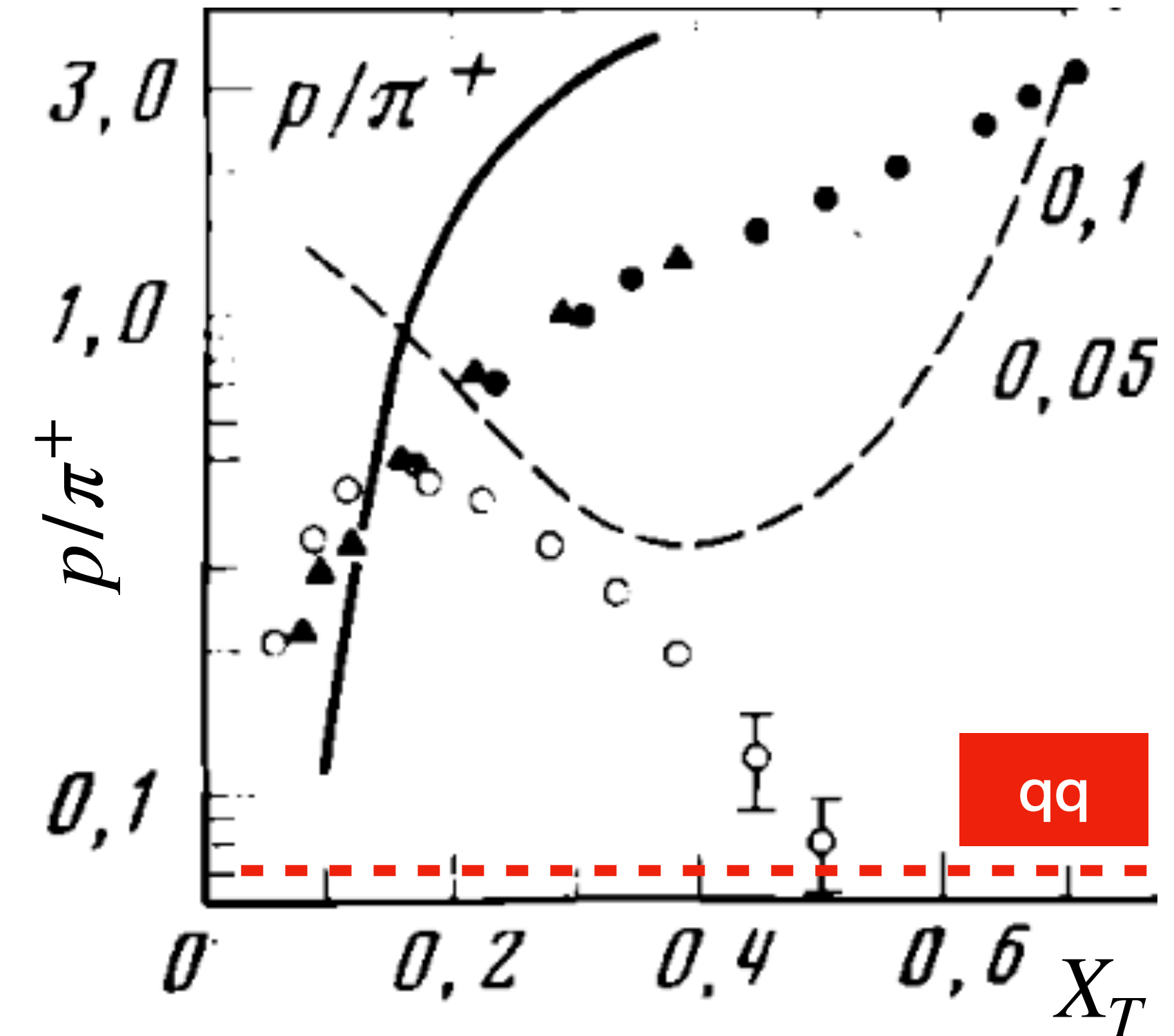


$$x_T = p_T / p_T^{max} = 2p_T / \sqrt{s}$$

$$\frac{E d^3\sigma}{d^3p} \sim \frac{c(x_T, \sqrt{s})}{p_T^4}$$

Weak dependence of $\sqrt{s} \rightarrow$ scaling

Parton-parton scattering is the main source of mesons with large p_T in pp collisions



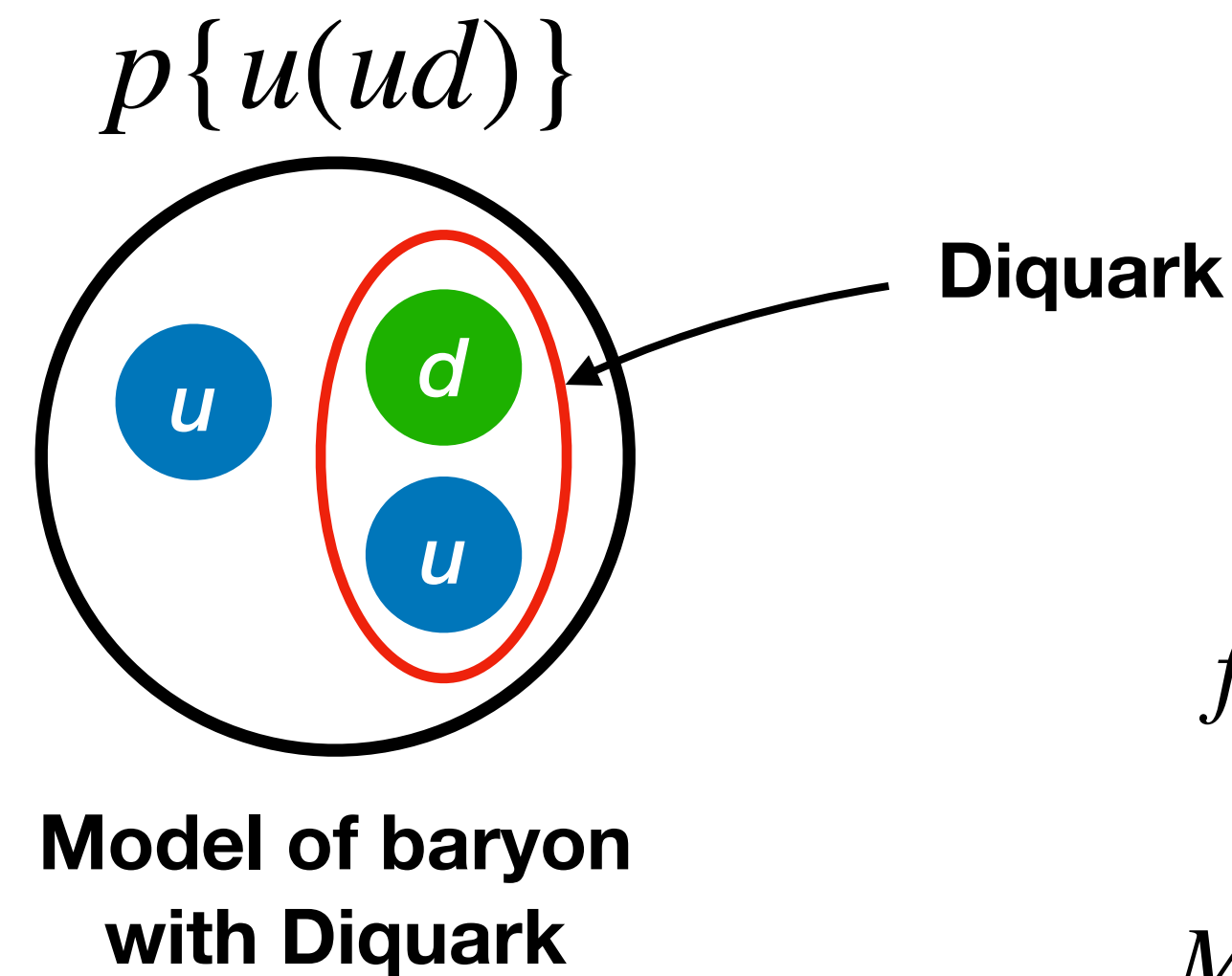
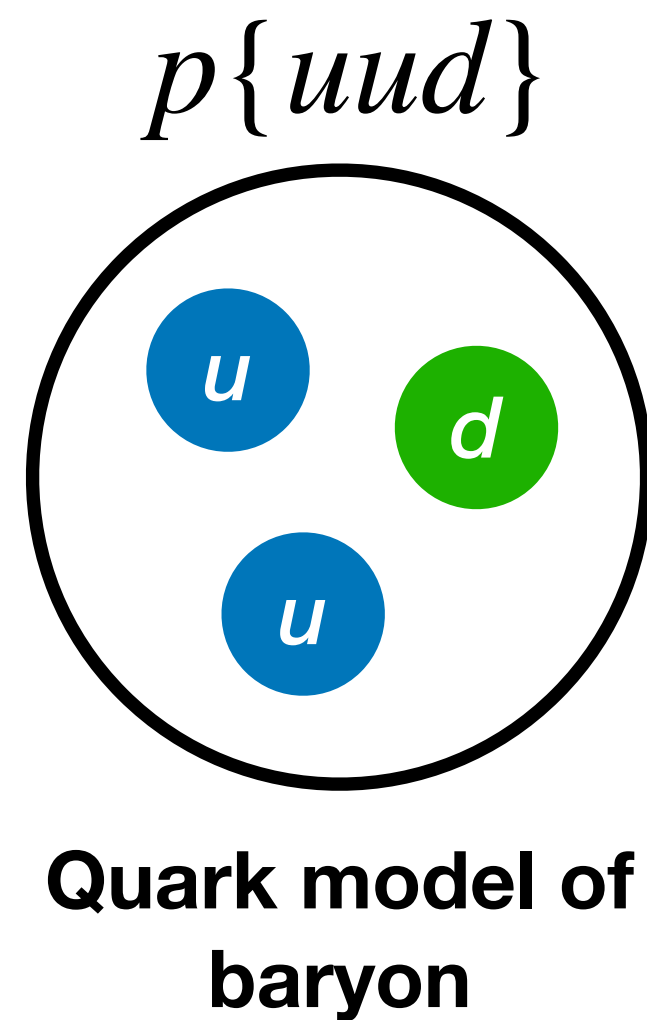
STRONG SCALING VIOLATION



Two-quark correlations: Diquarks

Diquark is a two-quark correlation in baryons.

Diquark is not a point-like object!



$$f(Q^2) = \frac{1}{1 + \frac{Q^2}{M^2}} \quad - \quad \text{Diquark form-factor}$$

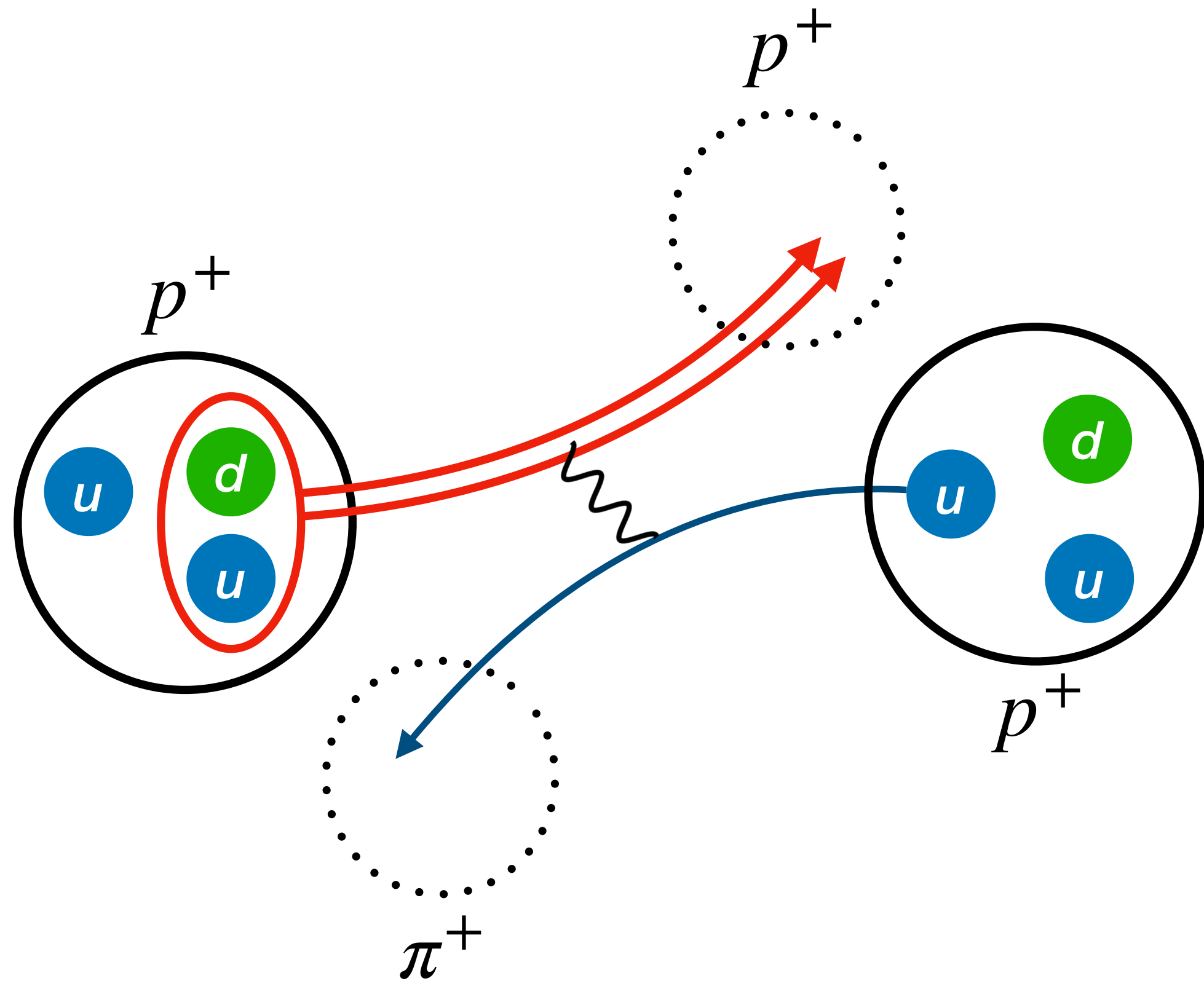
M^2 – Diquark size parameter

Baryon (proton) is in quark-Diquark state with probability W

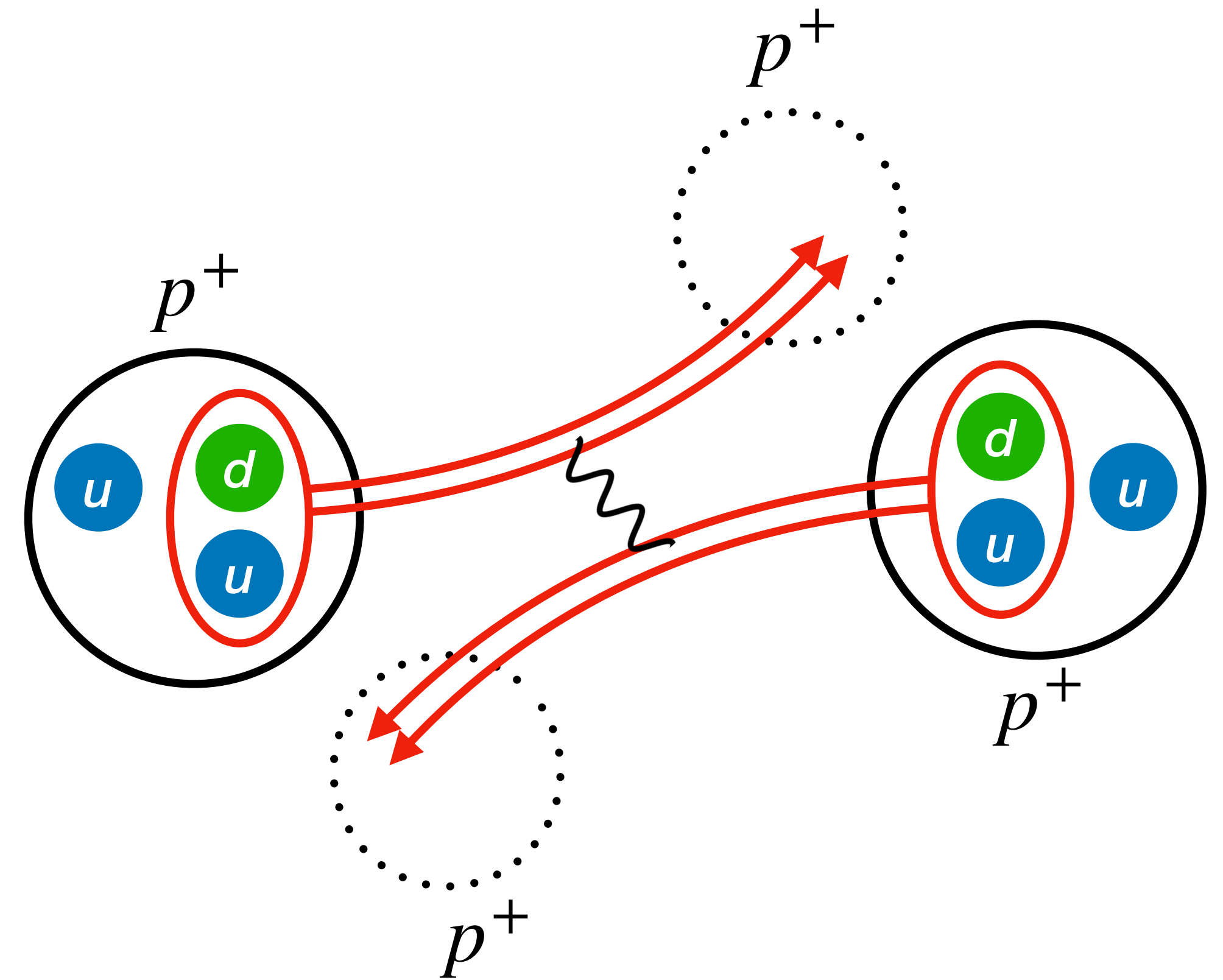


Two-quark correlations: Diquarks

(ud) Diquark scatters on u quark



(ud) Diquark scatters on (ud) Diquark



$$\left(\frac{d\hat{\sigma}}{d\hat{t}}\right)_{qD} = \left(\frac{d\hat{\sigma}}{d\hat{t}}\right)_{qq} \cdot f^2(Q^2)$$

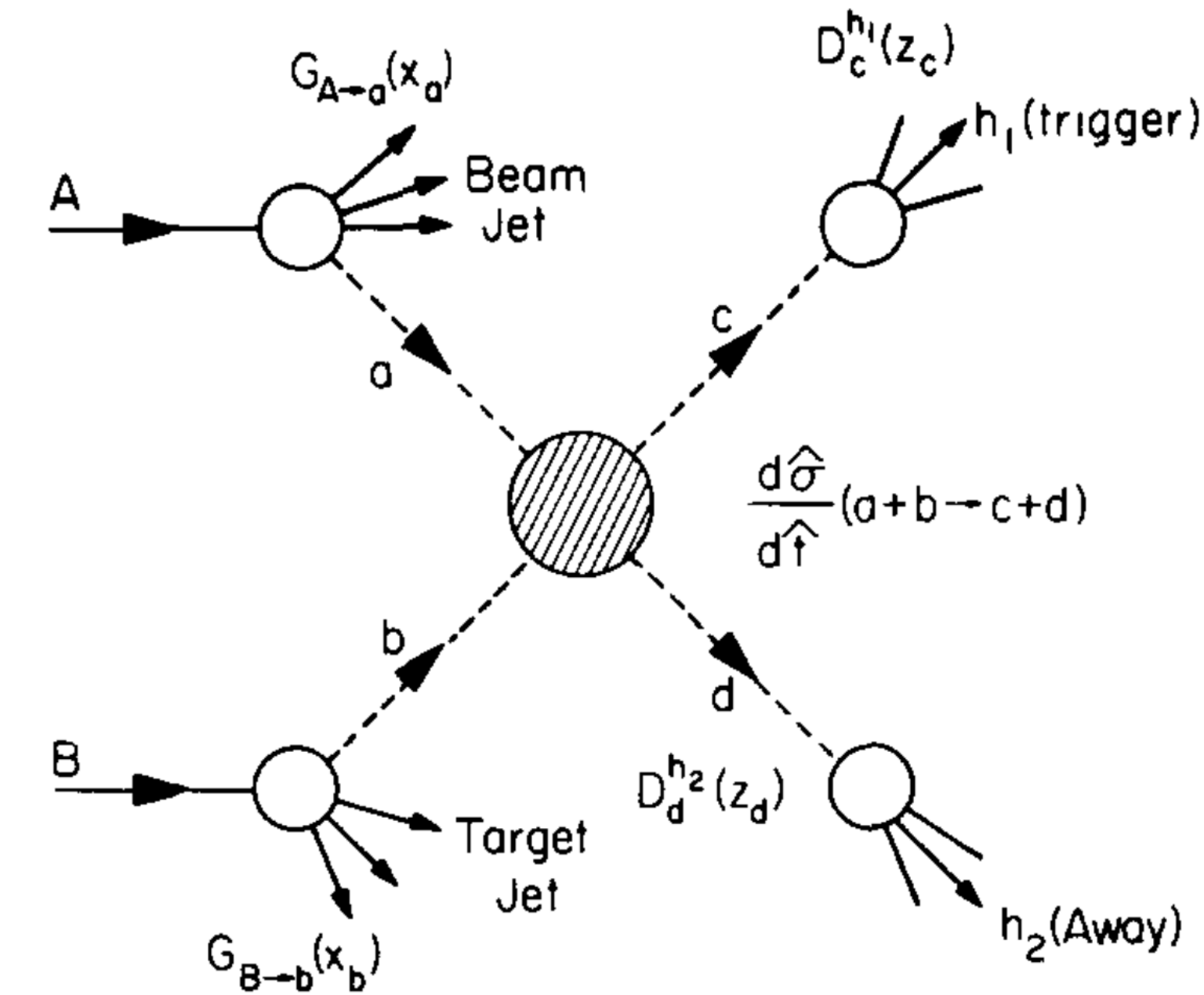
The main source of baryons with large p_T
in pp collisions at NICA energies

$$\left(\frac{d\hat{\sigma}}{d\hat{t}}\right)_{DD} = \left(\frac{d\hat{\sigma}}{d\hat{t}}\right)_{qq} \cdot f^4(Q^2)$$



Feynman approach: collinear factorization improved by k_T dependence

R.P. Feynman, R.D. Field and G.C. Fox
Phys. Rev. **D** 18 (1978) 3320



$$Ed^3\sigma/d^3p(s, t, u; A + B \rightarrow h + X) =$$

$$\int d^2k_{T_a} \int d^2k_{T_b} \int d^2k_{T_c} \int dx_a \int dx_b \boxed{G_{A \to a}(x_a, k_{T_a}, Q^2) G_{B \to b}(x_b, k_{T_b}, Q^2)}$$

$$\times \boxed{D_c^h(z_c, k_{T_c}, Q^2)} \frac{1}{z_c} \frac{1}{\pi} \frac{d\hat{\sigma}}{d\hat{t}}(\hat{s}, \hat{t}, \hat{u}; q_a + q_b \rightarrow qc + qd)$$

Parton Distribution Functions

Fragmentation Function

Subprocess cross section

$$F(x, y, k_T) = \hat{F}(x, y) \cdot \tilde{F}(k_T)$$

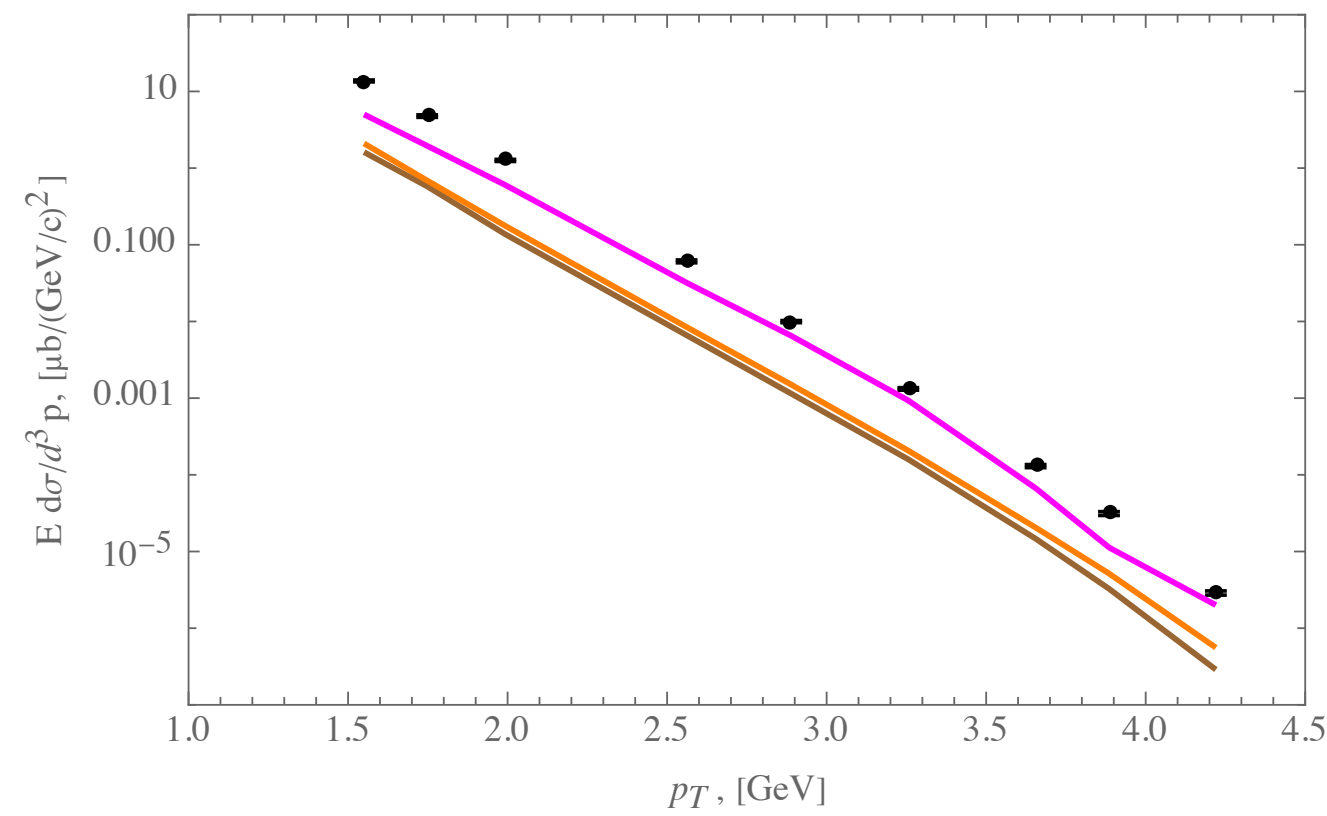
$$\tilde{F}(k_T) = J(k_T, Q^2) \sim e^{k_T^2/\sigma^2(Q^2)}, \text{ where } \sigma^2 = \langle k_T^2 \rangle$$



Large- p_T π^+ production

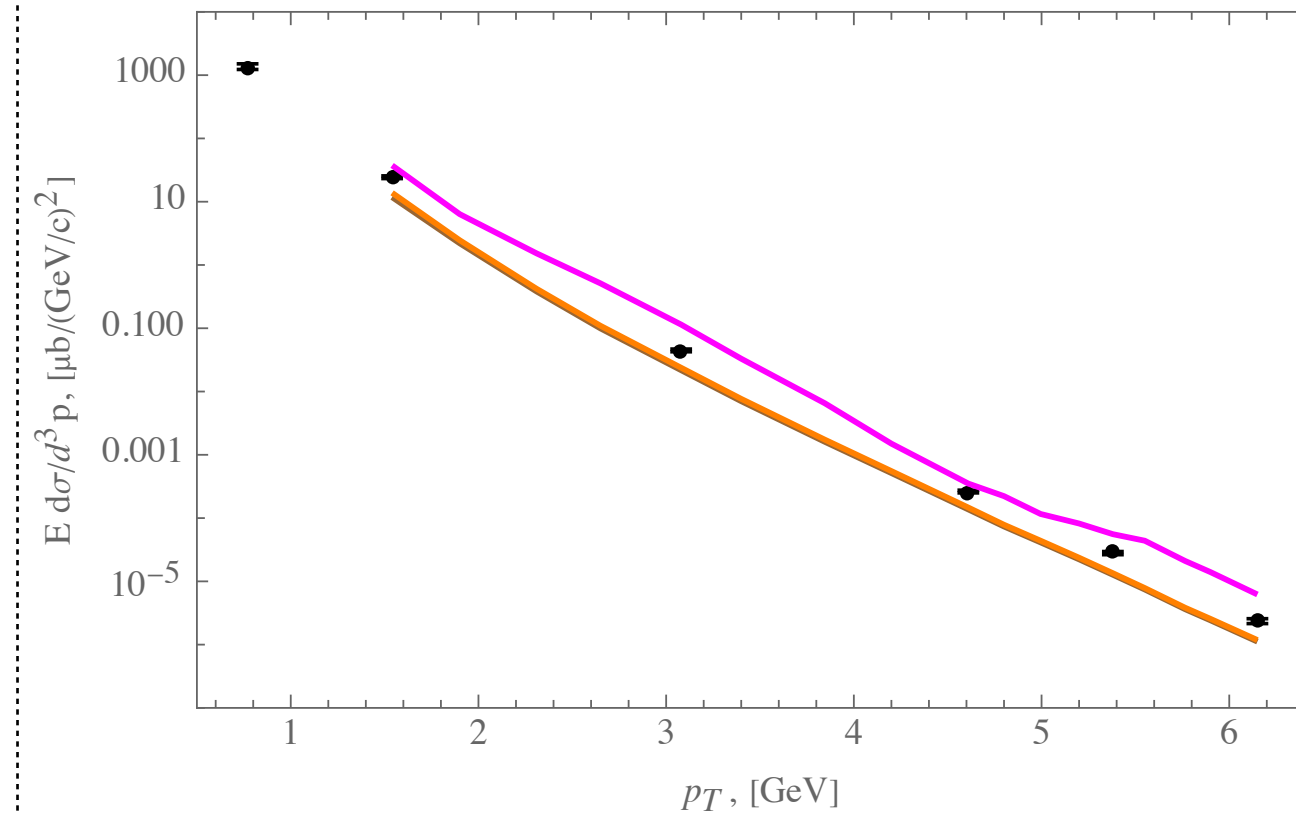


$\sqrt{s} = 11.5$ GeV



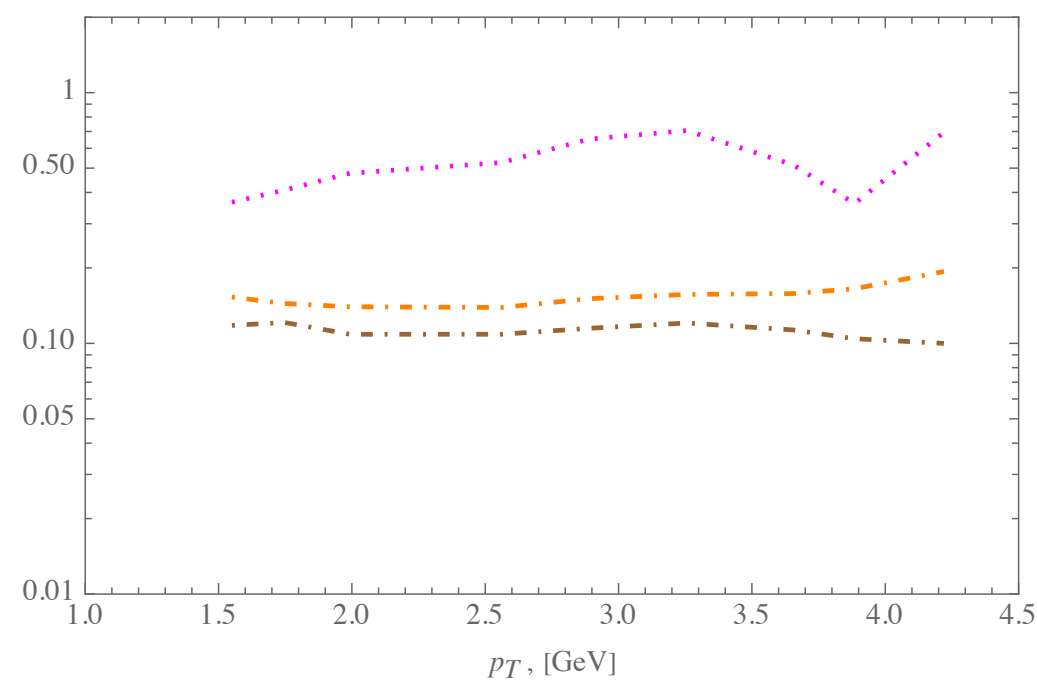
- Abramov, V.V., et al, π^+ ; $\sqrt{s} = 11.5$ GeV
- no Diquark; **FFHNKS**
- Diquark ($M_D^2 = 10, \nu_0 = 2, \lambda = 4.1$); **FFHNKS**
- PYTHIA 8.3, π^+ ; $\sqrt{s} = 11.5$ GeV

$\sqrt{s} = 23.4$ GeV



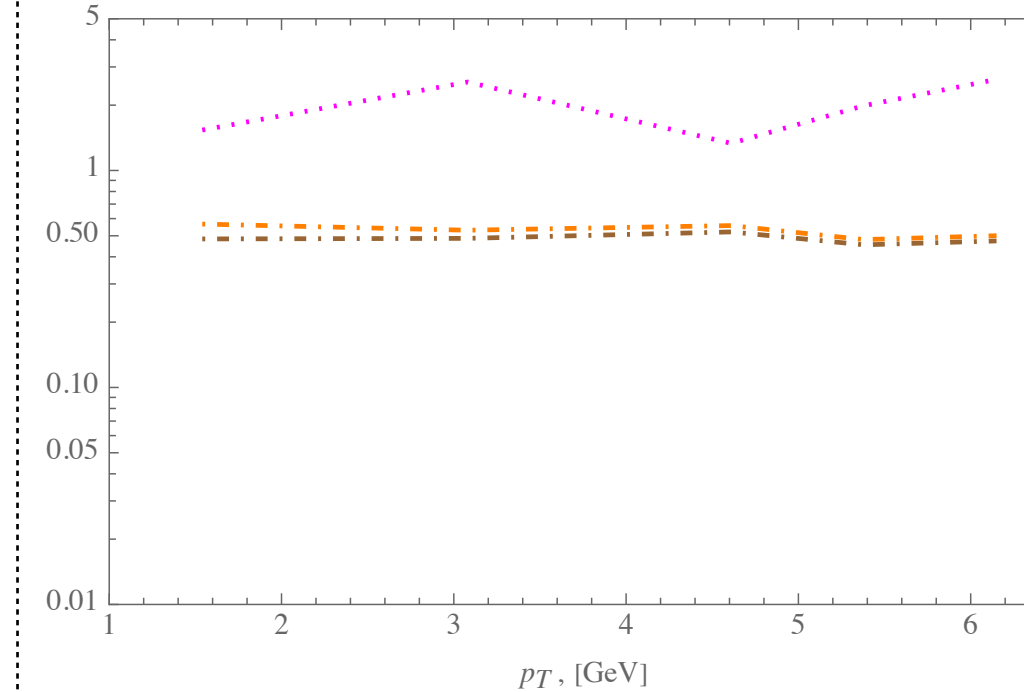
- Antreasyan, et al, π^+ ; $\sqrt{s} = 23.4$ GeV
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- PYTHIA 8.3, π^+ ; $\sqrt{s} = 23.4$ GeV

Theory/Data



- no Diquark; **FFHNKS** VS Data $\sqrt{s} = 11.5$ GeV
- Diquark ($M_D^2 = 10, \nu_0 = 2, \lambda = 4.1$); **FFHNKS** VS Data $\sqrt{s} = 11.5$ GeV
- PYTHIA 8.3 VS Data Ratio

Theory/Data



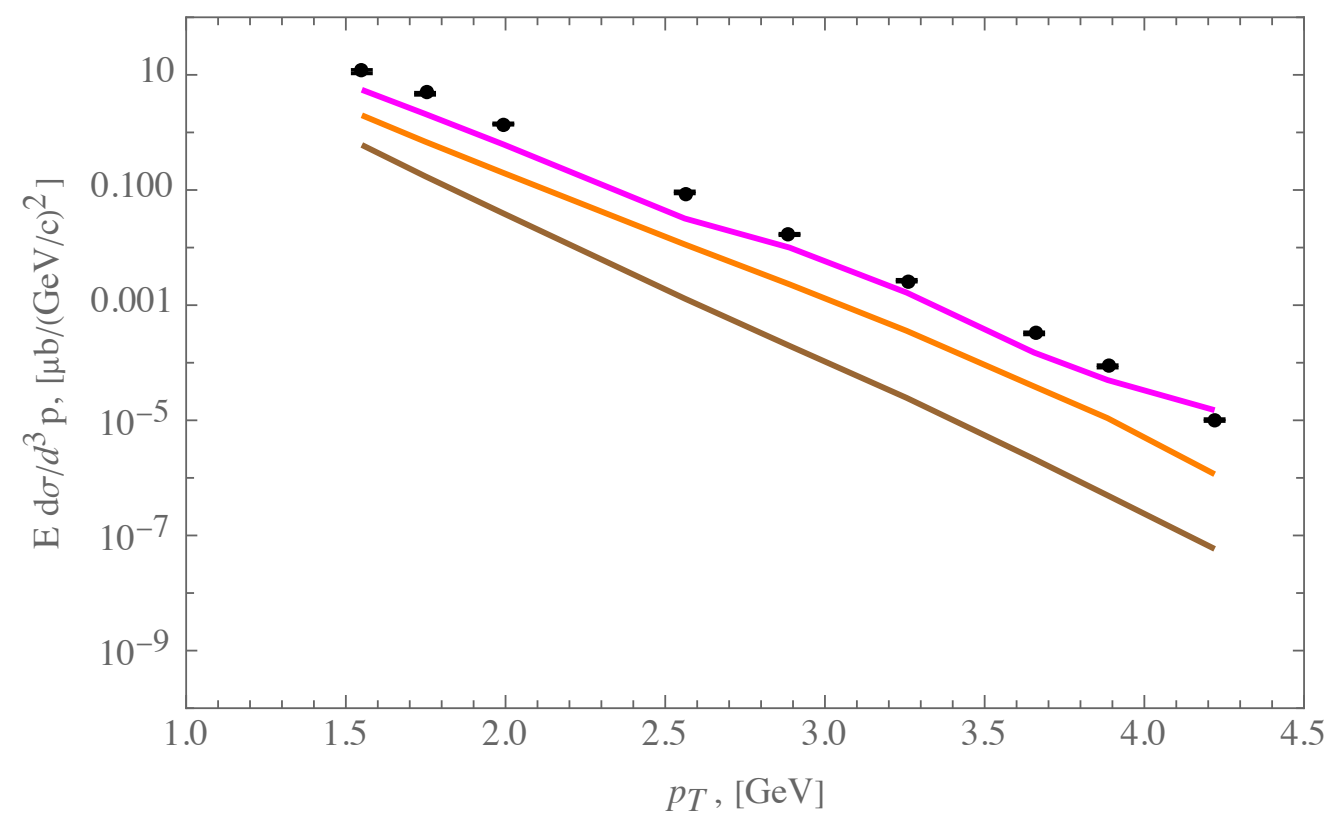
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Large- p_T p production

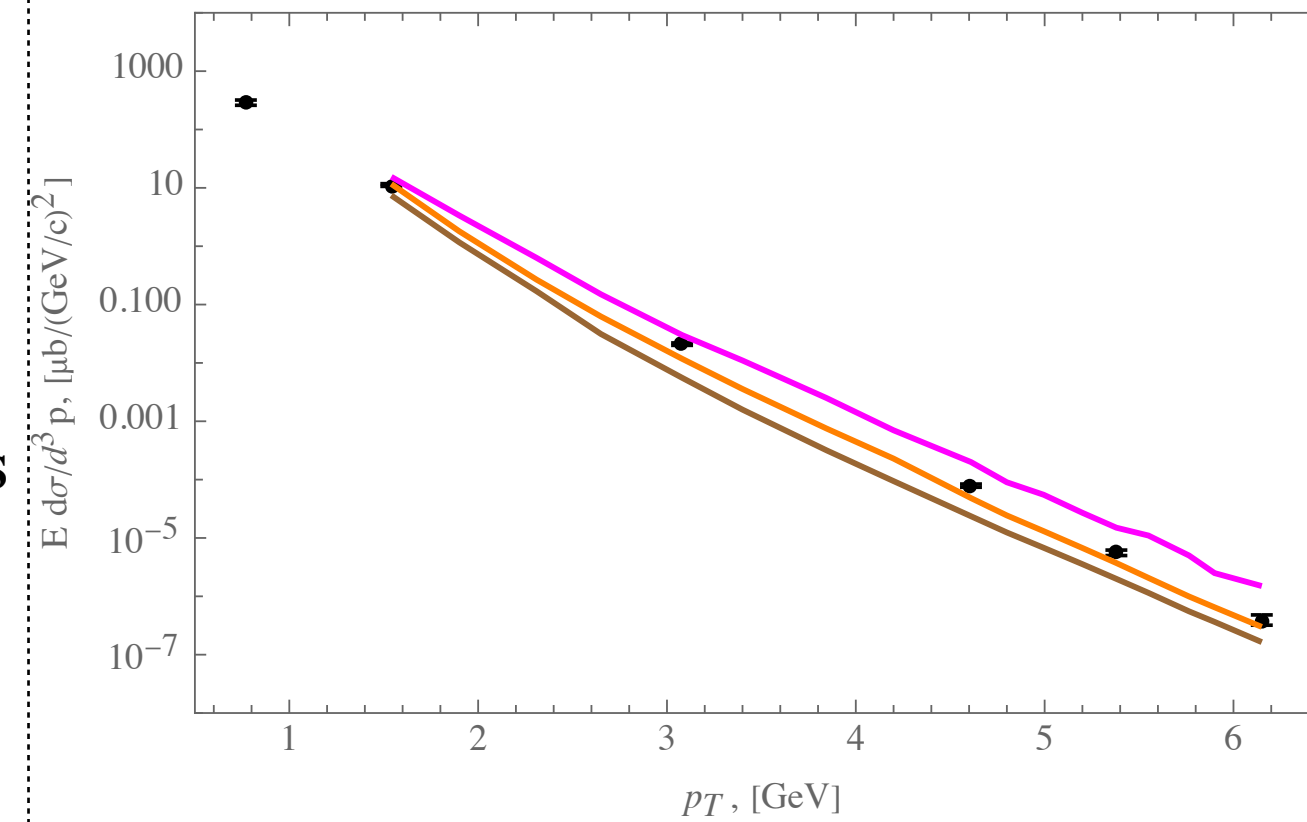


$\sqrt{s} = 11.5$ GeV



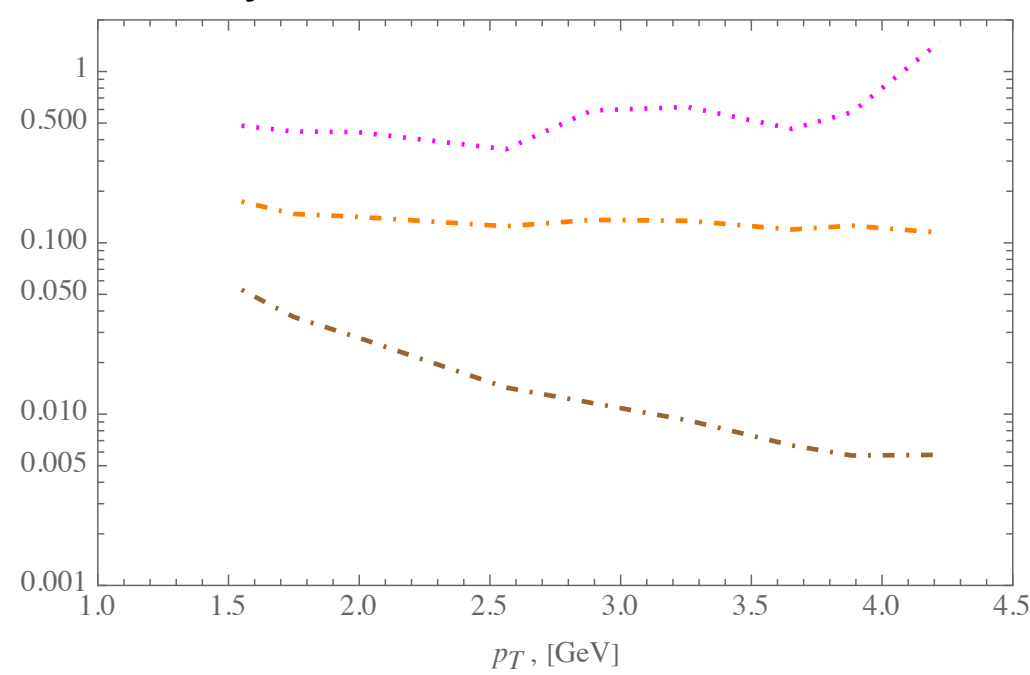
- Abramov, V.V., et al, p; $\sqrt{s} = 11.5$ GeV
- no Diquark; **FFHNKS**
- Diquark ($M_D^2 = 10, \nu_0 = 2, \lambda = 4.1$); **FFHNKS**
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$\sqrt{s} = 23.4$ GeV



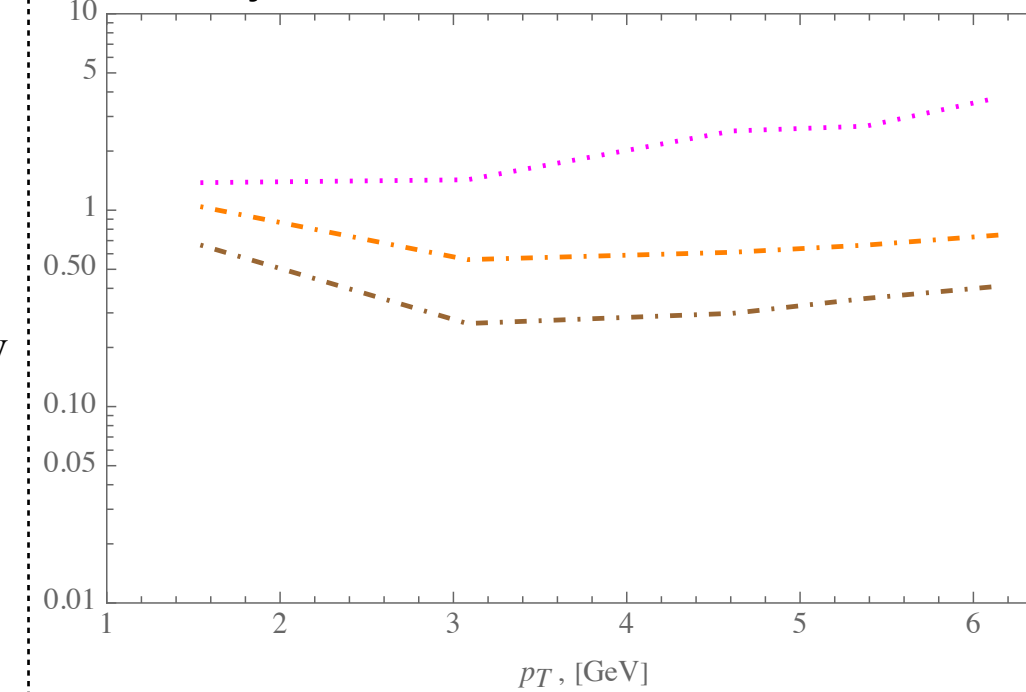
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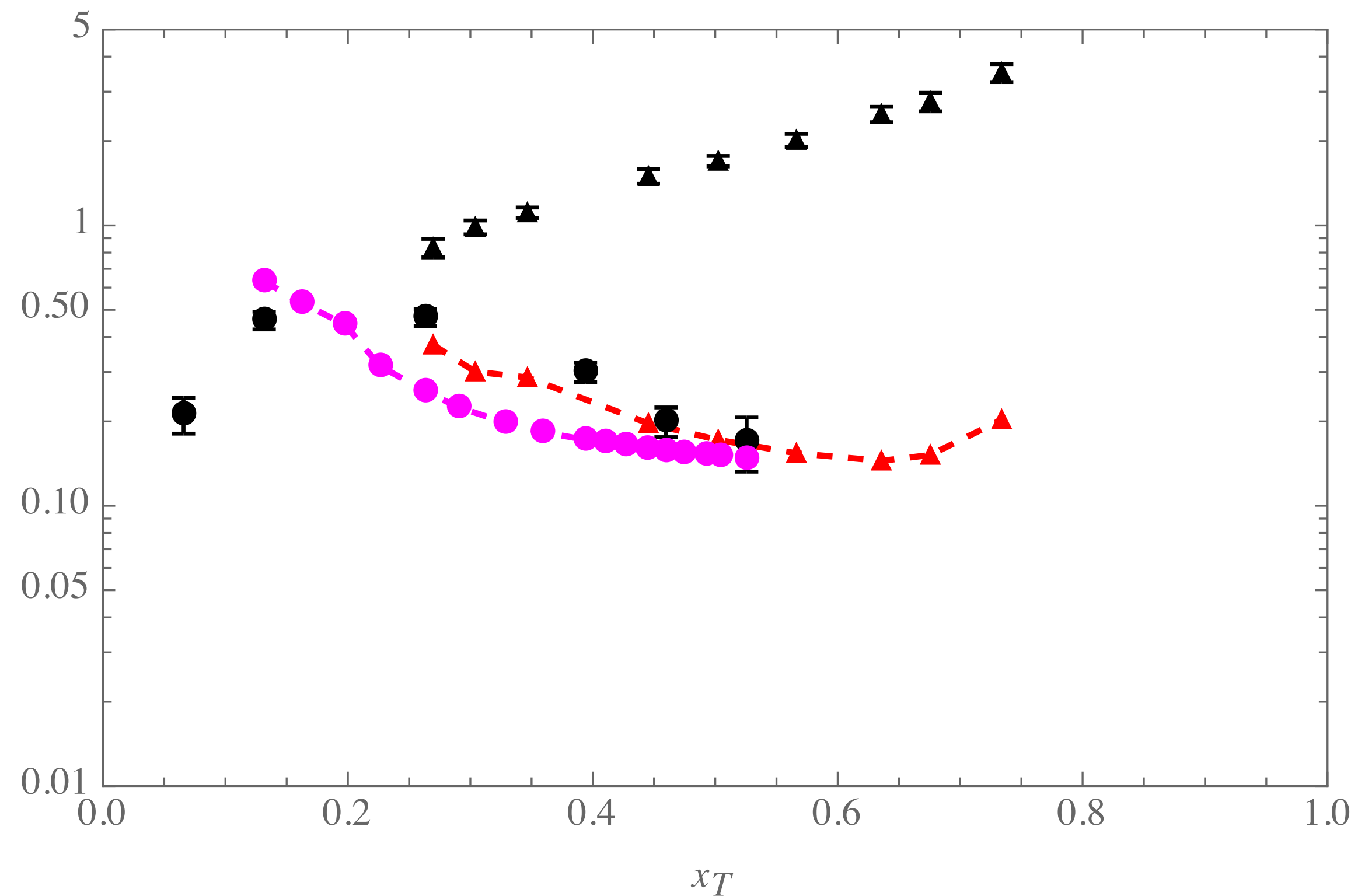
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p/π^+ ratio without Diquark



p/π^+ Ratio



p/π^+ Ratio with $\theta_{\text{cms}} = 90^\circ$ in pp -collisions and also comparison with data

IHEP, Protvino (\blacktriangle) для $\sqrt{s} = 11.5$ GeV
FODS, V.V. Abramov et al. (1985)

FNAL, Batavia (\bullet) для $\sqrt{s} = 23.4$ GeV
D.Antreasyan et al. (1979)

Calculation results:

Red line — $\sqrt{s} = 11.5$ GeV,

Magenta — $\sqrt{s} = 23.4$ GeV,

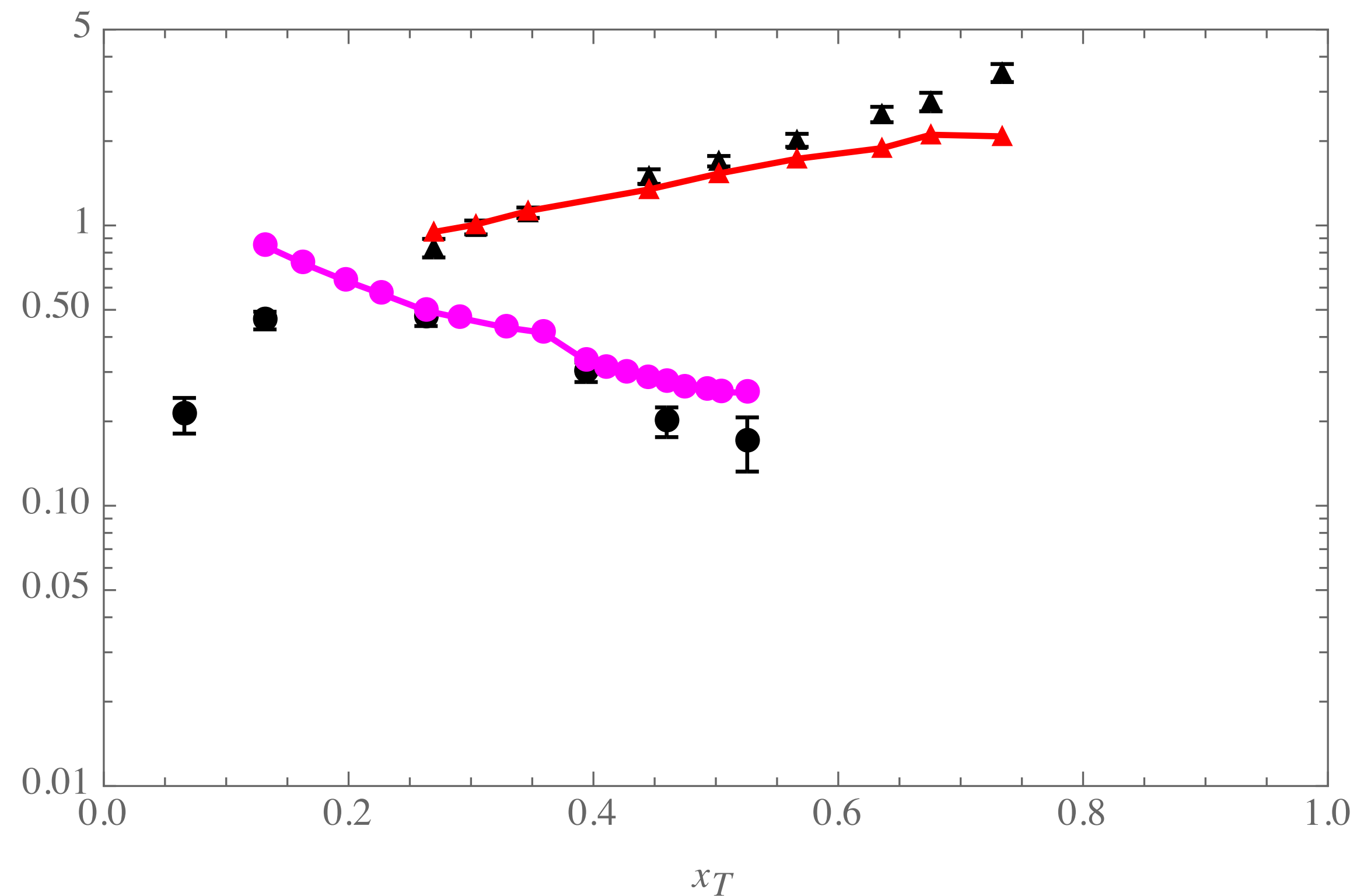
$$x_T = 2p_T/\sqrt{s}$$



p/π^+ ratio with Diquark



p/π^+ Ratio



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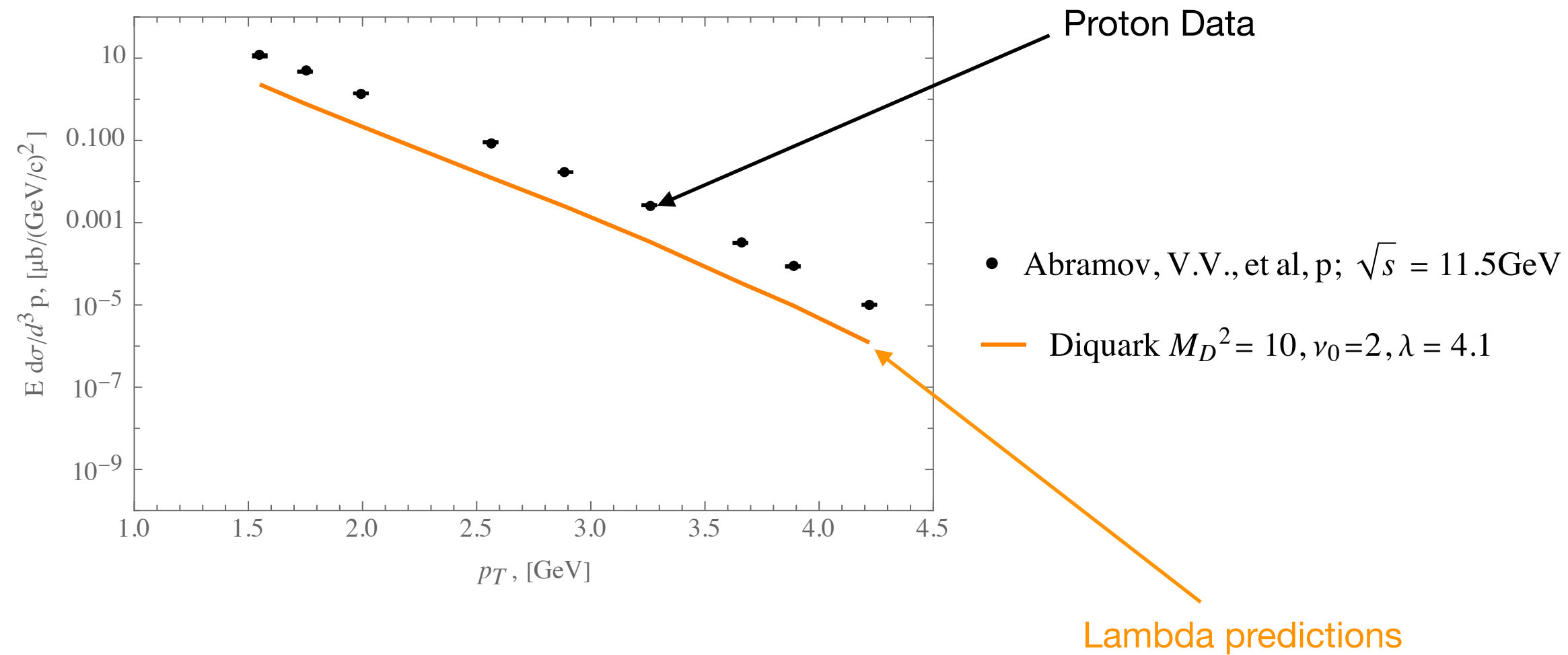
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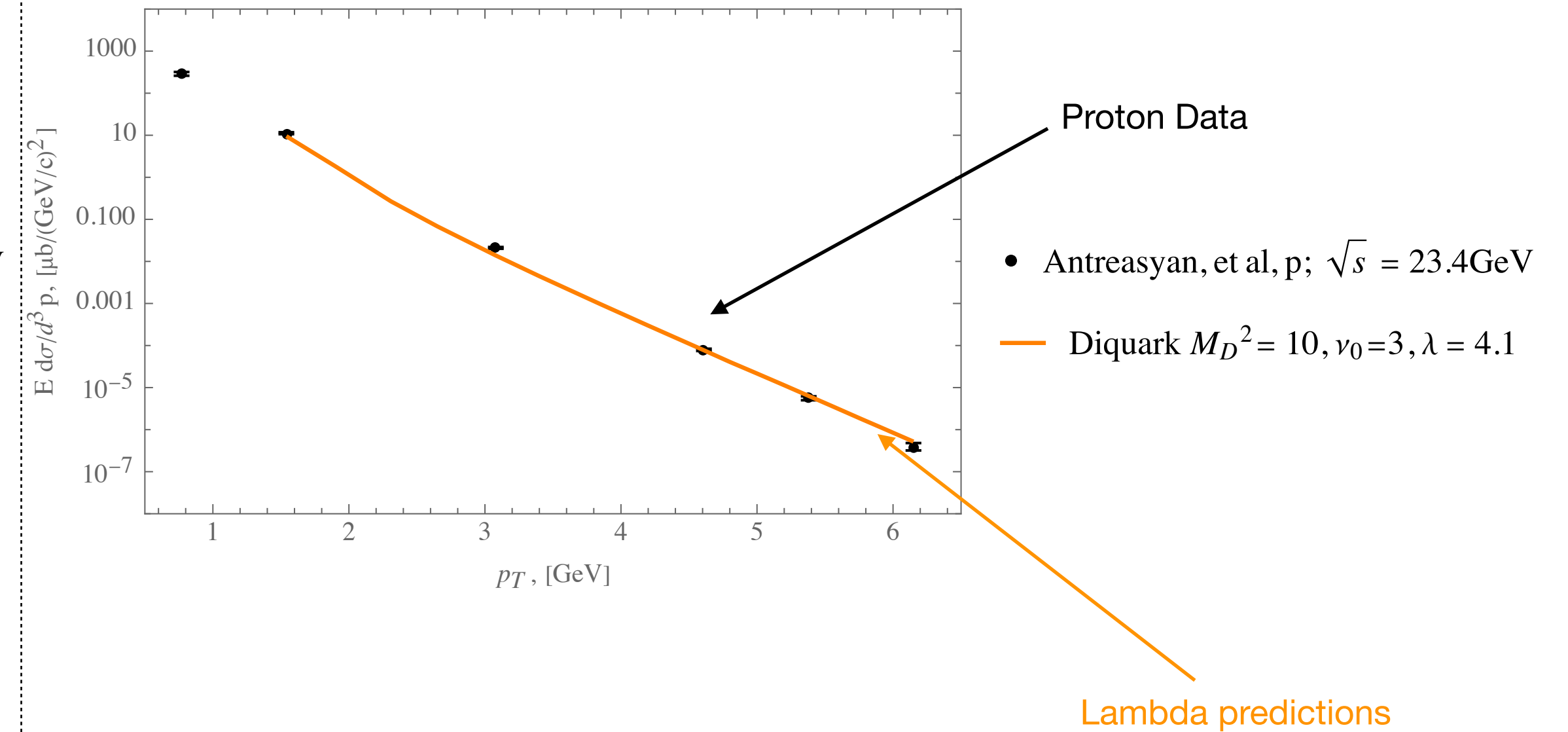
Large- p_T $\Lambda(uds)$ production

$\sqrt{s} = 11.5$ GeV



IHEP, Protvino, $\sqrt{s} = 11.5$ GeV
FODS, V.V. Abramov et al. (1985)

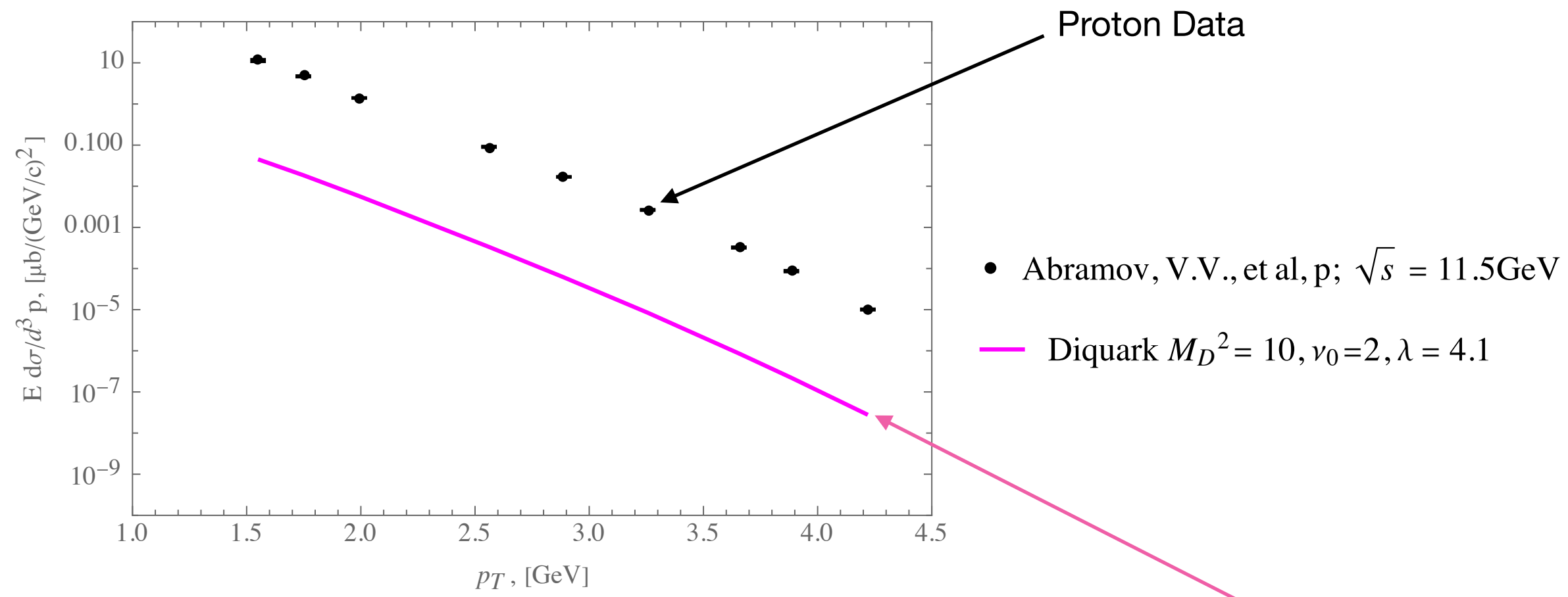
$\sqrt{s} = 23.4$ GeV



FNAL, Batavia, $\sqrt{s} = 23.4$ GeV
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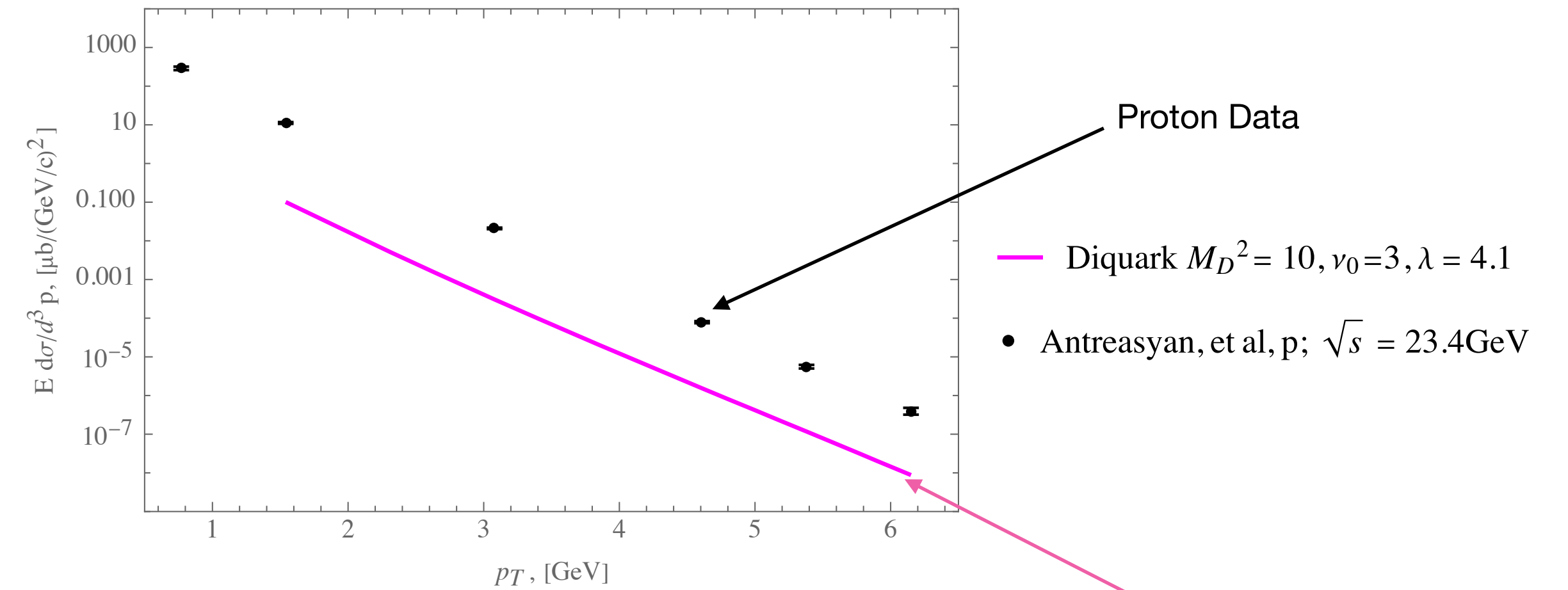
Exotic state production. Tetraquark $(qq\bar{q}\bar{q})$ $a_0(980)$: $\{(ud)\bar{u}\bar{d}\}$



$$\sqrt{s} = 11.5 \text{ GeV}$$

Tetraquark Predictions

IHEP, Protvino, $\sqrt{s} = 11.5 \text{ GeV}$
FODS, V.V. Abramov et al. (1985)



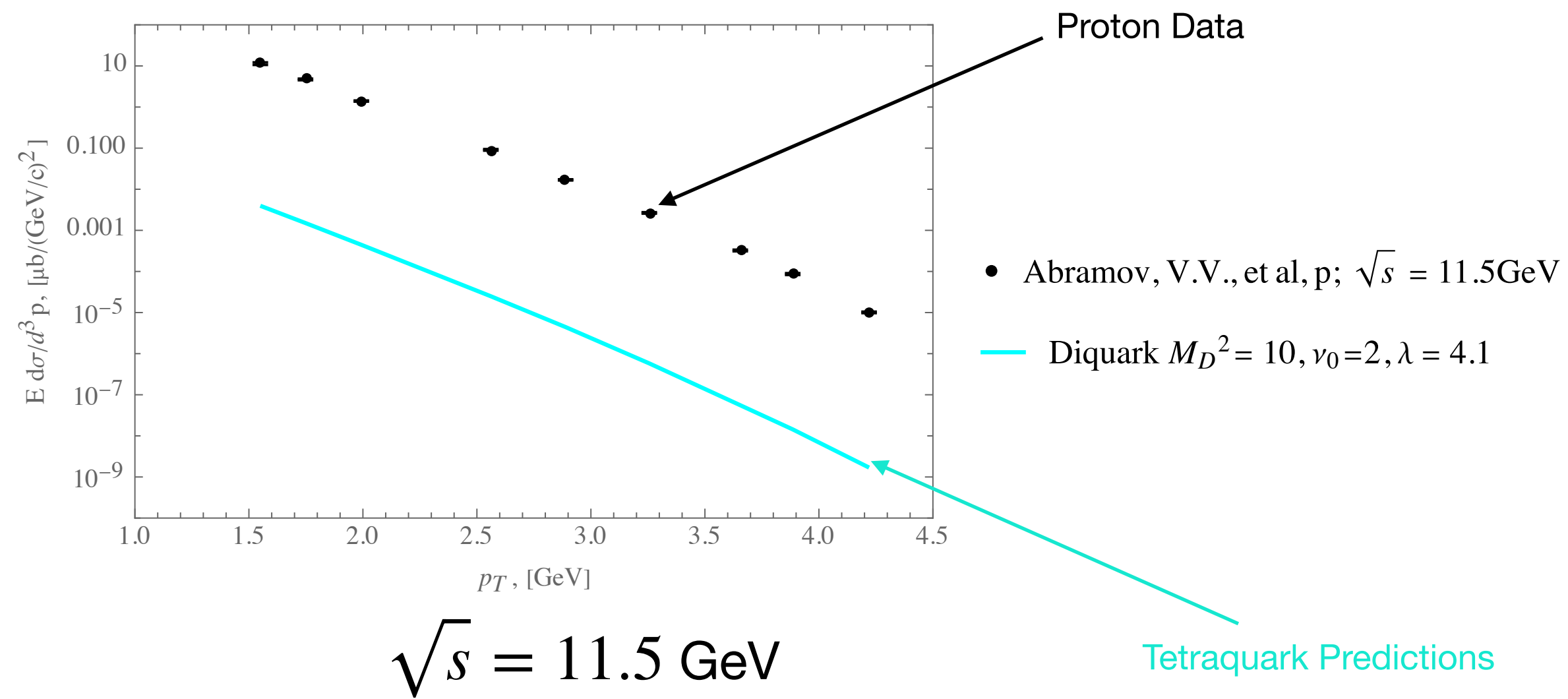
$$\sqrt{s} = 23.4 \text{ GeV}$$

Tetraquark Predictions

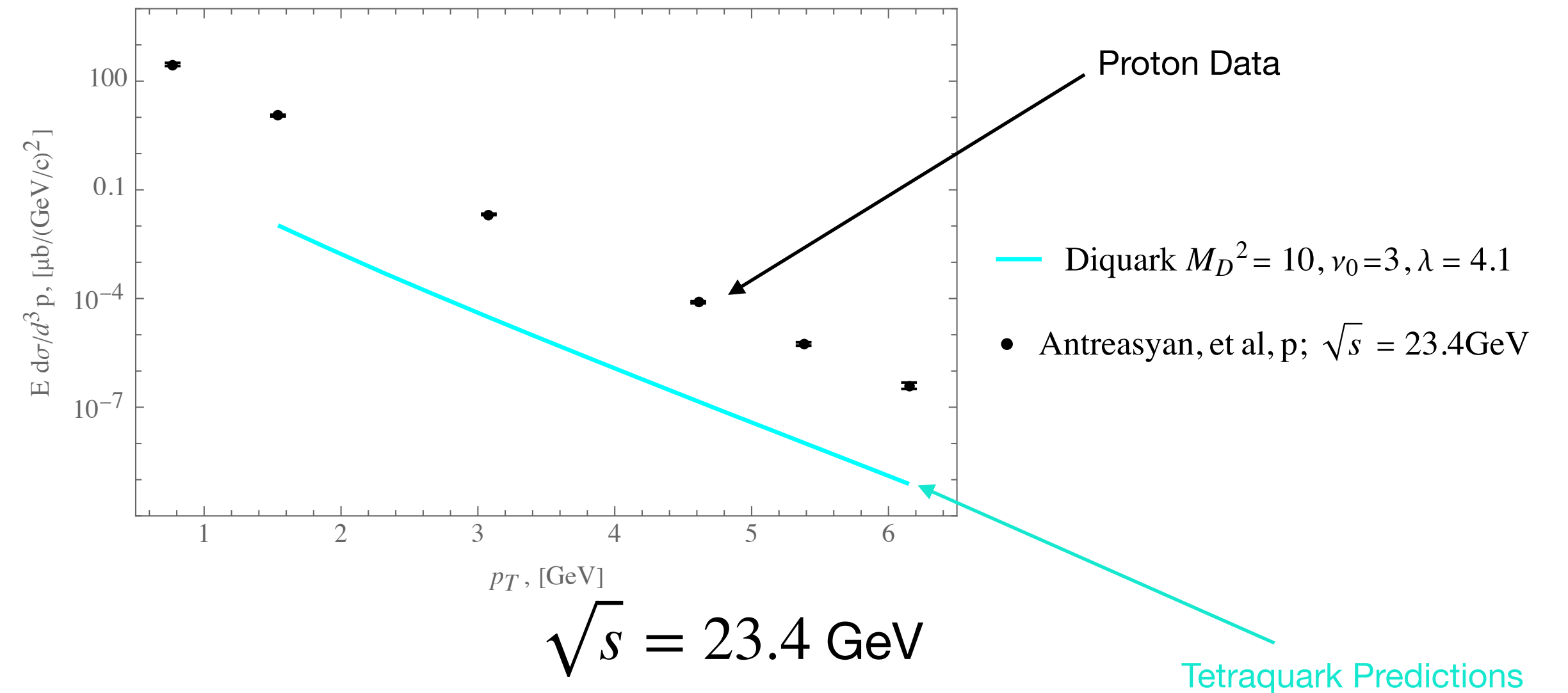
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Exotic state production. Tetraquark $(qq\bar{q}\bar{q})$ $X: \{(ud)\bar{s}\bar{s}\}$



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✓ Done:

- Implementation of scalar (ud) Diquark in hard hadronic processes:
 - Diquark structure function
 - Evolution of diquark structure function

➡ In Progress:

- Multiparton interactions with Diquarks
- Implementation of vector (uu) Diquark in hard hadronic processes
- Diquark parameters tuning for ULYSSES



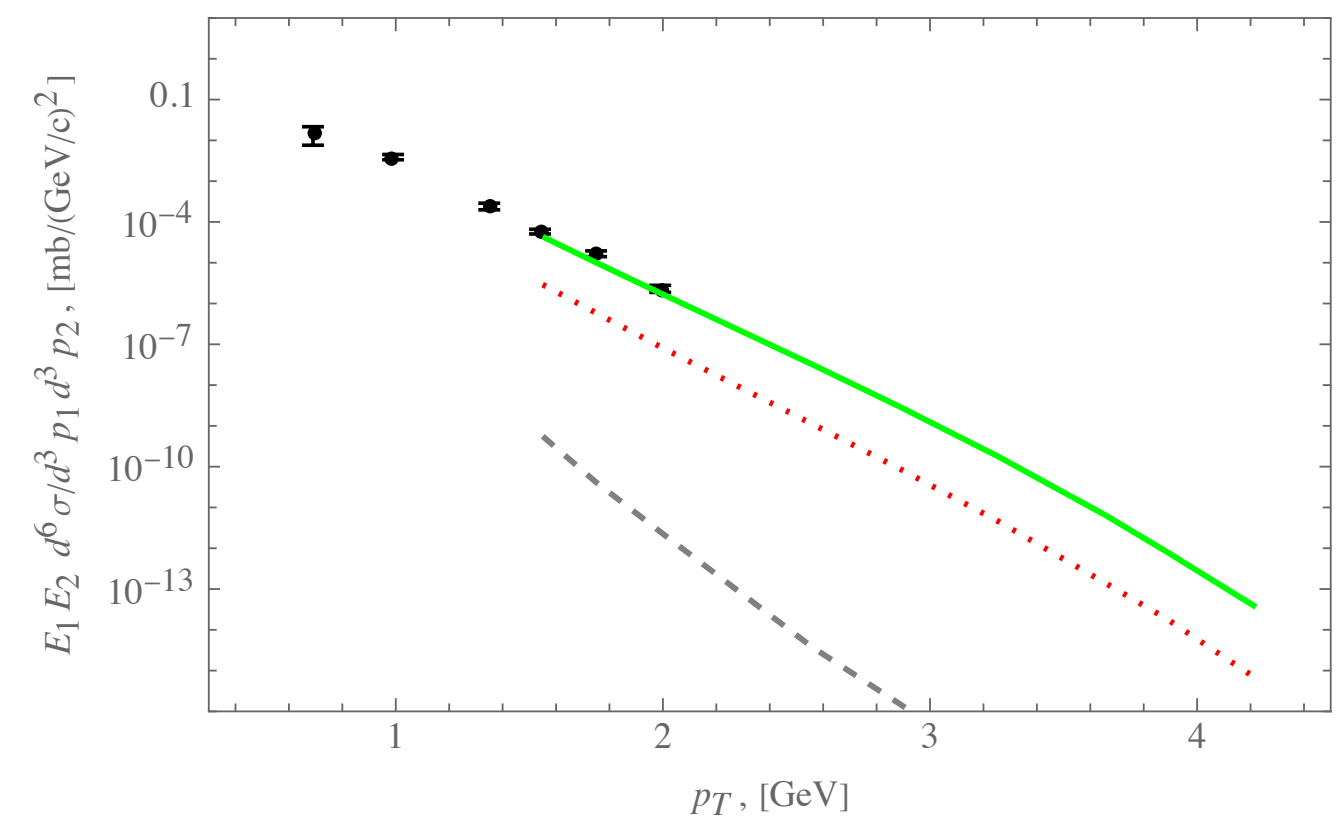
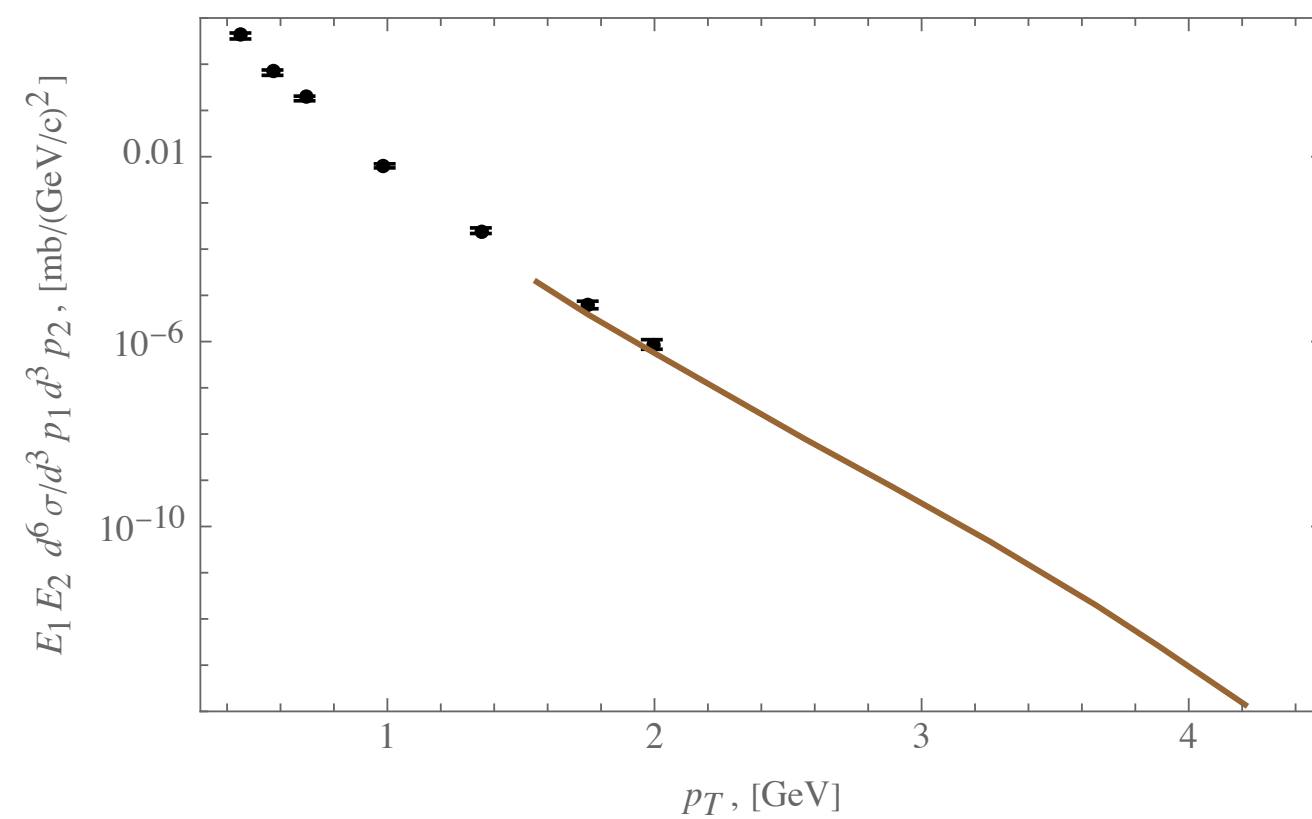
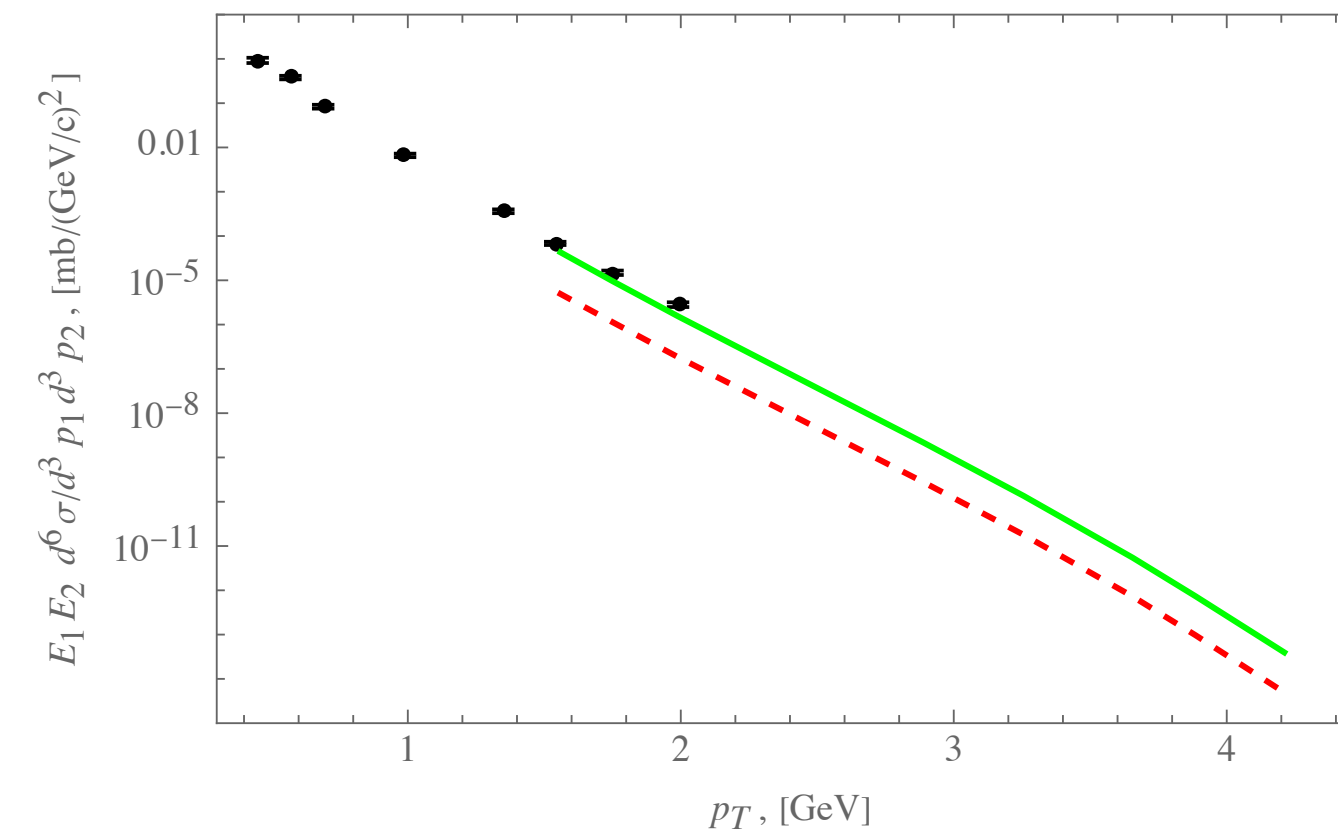
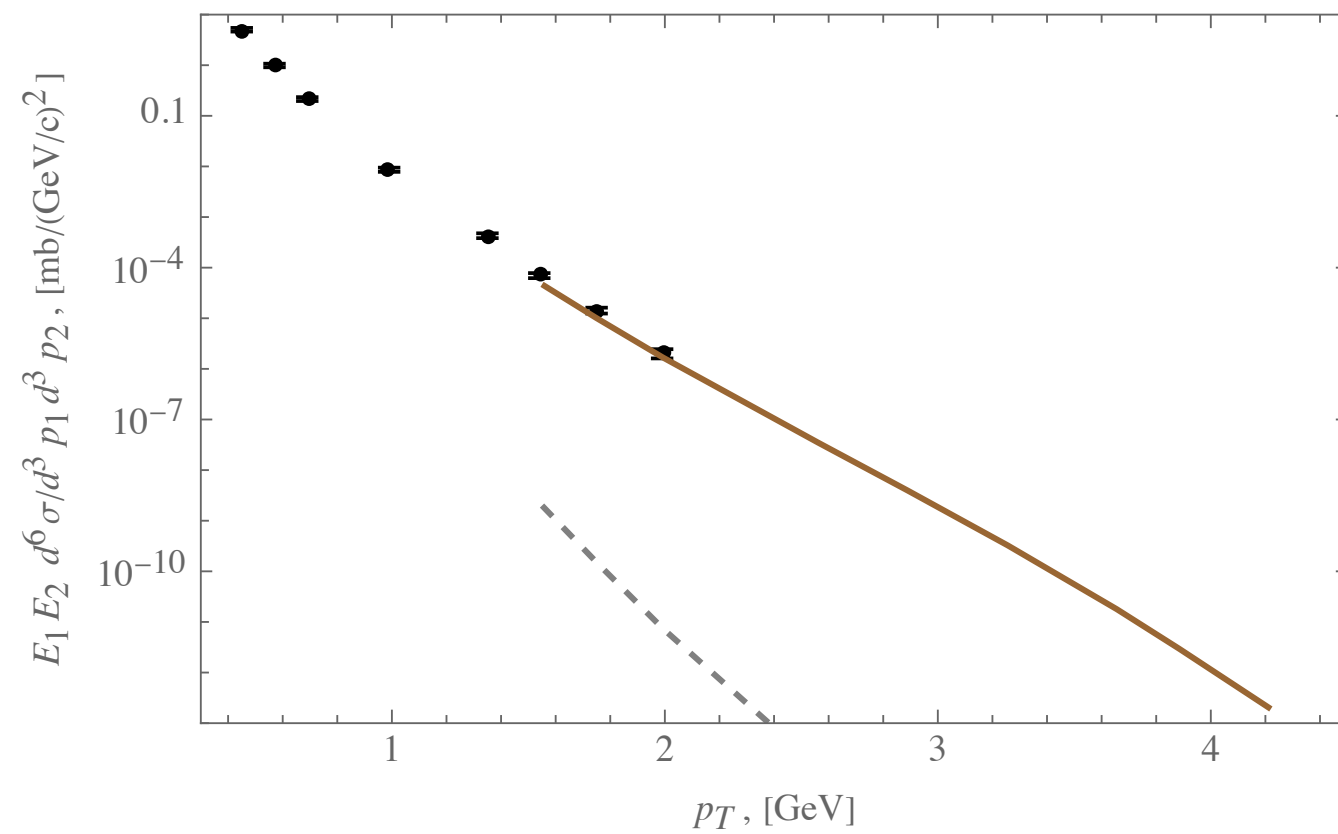
- ▶ Two-quark correlations (Diquarks) can describe the strong scaling violation in large- p_T proton production in hard nucleon collisions at **SPD** energies.
- ▶ The **SPD** at **NICA** collider provides a unique opportunity to improve understanding of Diquark role for large- p_T baryon production in pp -collisions.
- ▶ On the basis of Diquark approach, estimations of the tetraquarks (exotic multiquark hadron states) production at the **SPD** energies have been made. [To appear in Lett. Phys. Elem. Part. At. Nucl. \(Jan. 2025\)](#)
- ▶ These results will be used to tune the MC generator **ULYSSES** which is developing in NRC «Kurchatov Institute» - PNPI, Gatchina.



Hadron symmetric pairs production

$$p_{T_1} = p_{T_2}, \Delta\phi = (\phi_2 - \phi_1) = \pi; \theta_1 = \pi/2 \text{ and } \theta_2 = -\pi/2$$

Red line — in standard approach (without diquarks), Green — with diquarks

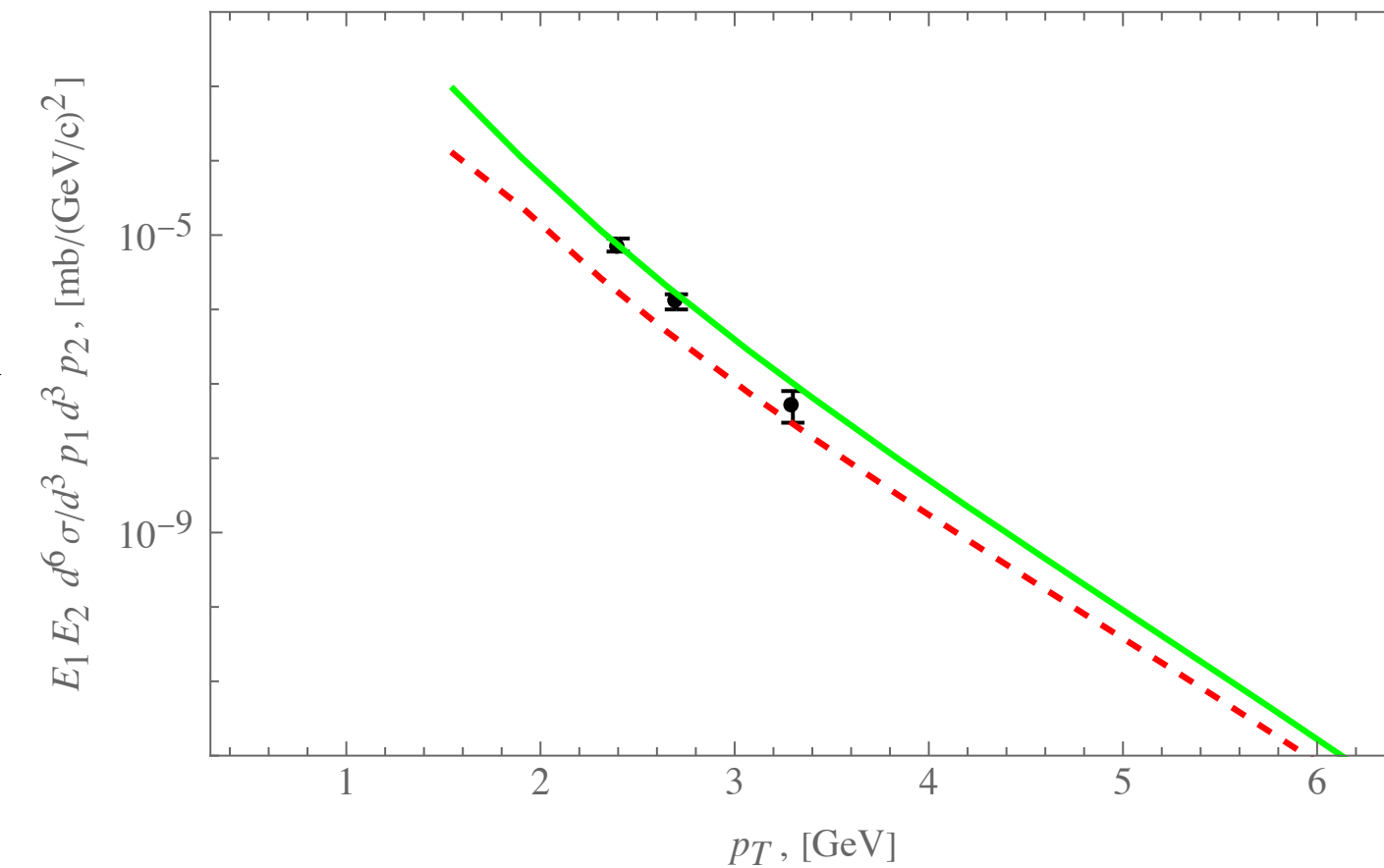
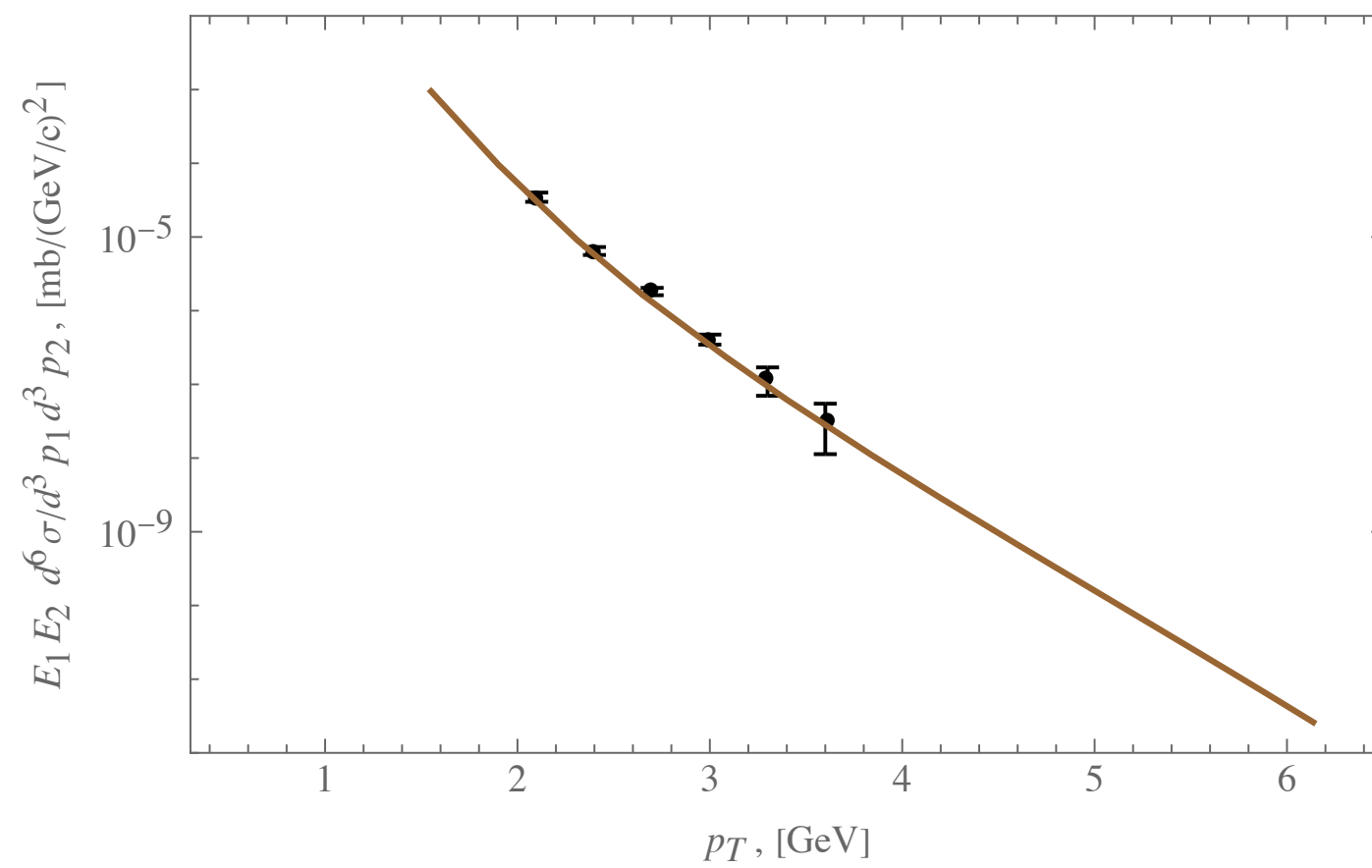




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$$\sqrt{s} = 23.4 \text{ GeV}$$