

Light hadron spectra obtained with MPDRoot

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The task

- Obtain spectra of π^\pm , K^\pm , and p with MPDRoot.
 - Fit spectra, obtain physical parameters.
 - Integrate spectra and obtain yields.
-
- See into PID by STAR as an alternative method.

Contents

- MpHadronSpectra wagon
- Processing of spectra
- pidAM vs pidSTAR
- Conclusions

MpdHadronSpectra wagon

Initial developer: Alexander Mudrokh

`mpdroot/physics/MpdHadronSpectra/`

- `MpdHadronSpectraParams.h (*.cxx)`: input file readers
- `MpdHadronSpectra.h (*.cxx)`: main source files
- `MpdHadronSpectraLinkDef.h`
- `CMakeLists.txt`

How to run the MpdHadronSpectra wagon:

- In `mpdroot/physics/CMakeLists.txt` add line
`add_subdirectory(MpdHadronSpectra)`
- In `mpdroot/physics/pairKK/macros/RunAnalyses.C` add lines
`MpdHadronSpectra pSpec("pHS", "pHS");
man.AddTask(&pSpec);`
- `$ root -b -q -l RunAnalyses.C`

MpdHadronSpectra.cxx (principally)

```
#include "MpdTrack.h"
#include "MpdMCTrack.h"
#include "MpdVertex.h"

ClassImp(MpdHadronSpectra);

void ProcessEvent(MpdAnalysisEvent &event){...}

void FillMcSpectra(MpdAnalysisEvent &event){...}
void FillMcTOFSpectra(MpdAnalysisEvent &event){...}
void FillRcSpectra(MpdAnalysisEvent &event){...}

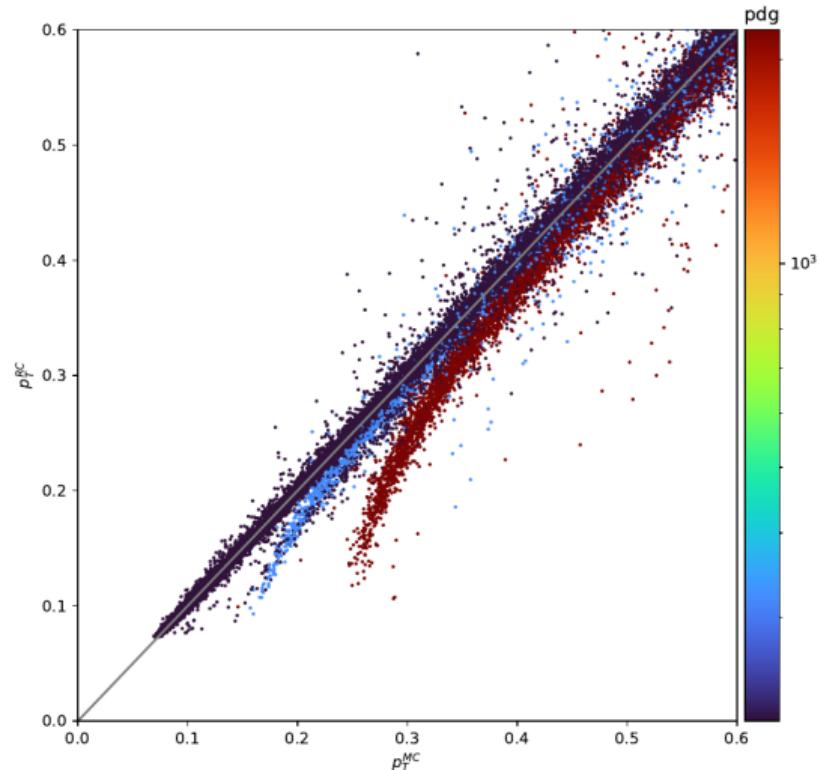
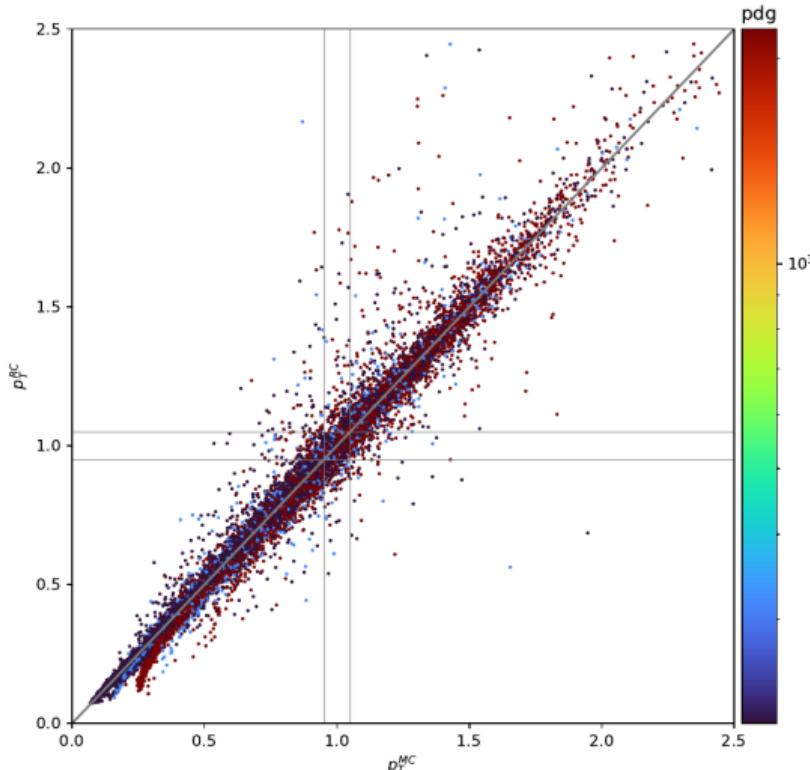
void FillTPCEfficiency(MpdAnalysisEvent &event){...}
void FillTOFEfficiency(MpdAnalysisEvent &event){...}
void FillTOFMCefficiency(MpdAnalysisEvent &event){...}
void FillPIDEfficiency(MpdAnalysisEvent &event){...}
void FillDCAcontribution(MpdAnalysisEvent &event){...}
void FillCoordEfficiency(MpdAnalysisEvent &event){...}
void FillSplitting(MpdAnalysisEvent &event){...}

bool selectEvent(MpdAnalysisEvent &event){...}

double Eloss_Pi(double *x, double *par){...}
double Eloss_Kplus(double *x, double *par){...}
double Eloss_Kminus(double *x, double *par){...}
double Eloss_Proton(double *x, double *par){...}
double Eloss_AntiProton(double *x, double *par){...}
```

$p_t^{(RC)}$ vs $p_t^{(MC)}$

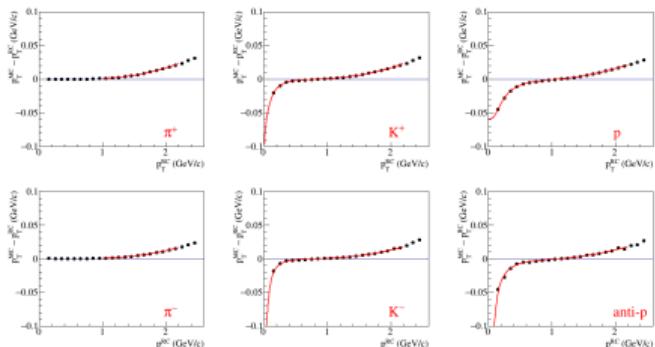
$|y| < 0.1$, centrality 0-10% (4000 events)



MpdHadronSpectra wagon

A. Mudrokh:

evSpecs wagon: Energy loss corrections



EnLoss functions are included within MpdHadronSpectra.h (*.cxx) – hardcoded.
In void **MpdHadronSpectra::UserInit()** function:

```
fEloss_Piplus = new TF1("fEloss_Piplus", this, &MpdHadronSpectra::Eloss_Pi,
    PtMin, PtMax, 3, "MpdHadronSpectra", "Eloss_Pi");
fEloss_Piplus->SetParameters(0.0117, -0.0235021, 0.0130318); // already fitted in external analysis
```

P_T corrections are using within each RcTrack loop

PWG-II meeting

November 16, 2023

7

$$p_T^{\text{Rc}} = p_T^{\text{Rc}} + \text{Eloss}(p_T^{\text{Rc}}); \quad E = \sqrt{m^2 + p_T^2 + (p_z^{\text{Rc}})^2}; \quad y = \frac{1}{2} \ln \frac{E + p_z^{\text{Rc}}}{E - p_z^{\text{Rc}}}$$

MpdHadronSpectra.cxx (principally)

```
#include "MpdTrack.h"
#include "MpdMCTrack.h"
#include "MpdVertex.h"

ClassImp(MpdHadronSpectra);

void ProcessEvent(MpdAnalysisEvent &event){...}

void FillMcSpectra(MpdAnalysisEvent &event){...}
void FillMcTOFSpectra(MpdAnalysisEvent &event){...}
void FillRcSpectra(MpdAnalysisEvent &event){...}

void FillTPCefficiency(MpdAnalysisEvent &event){...}
void FillTOFefficiency(MpdAnalysisEvent &event){...}
void FillTOFMCefficiency(MpdAnalysisEvent &event){...}
void FillPIDefficiency(MpdAnalysisEvent &event){...}
void FillDCAcontribution(MpdAnalysisEvent &event){...}
void FillCoordEfficiency(MpdAnalysisEvent &event){...}
void FillSplitting(MpdAnalysisEvent &event){...}

bool selectEvent(MpdAnalysisEvent &event){...}

double Eloss_Pi(double *x, double *par){...}
double Eloss_Kplus(double *x, double *par){...}
double Eloss_Kminus(double *x, double *par){...}
double Eloss_Proton(double *x, double *par){...}
double Eloss_AntiProton(double *x, double *par){...}
```

MpdHadronSpectra wagon

pHS.txt

```
-----Parameters used for analysis-----
# Abs[pdg] for considered particles:
mAbsPDGs      211 321 2212
# Event selection:
mZvtxCut     100 // cut on vertex z coordinate
# Centrality binning
mCentMin       0 10 20 30 40
mCentMax       10 20 30 40 80
# Track cuts:
mNofHitsCut   20 // minimal number of hits for a track
mDCAMax        3.0 // maximal |DCA|
#
mUseELC       true
# Pt for hists
mPtMin         0.05 // minimal pt for a track
mPtMax         4.05 // maximal pt for a track
mPtWidth       0.1 // GeV
# Rapidity for hists
mRapMin        -2.5
mRapMax         2.5
mRapWidth       0.1
# PID cuts:
mSigE          3.0 // non-zero distance
//                      from the average dE/dx (in sigmas)
// 
mSigB          3.0 // non-zero distance
//                      from the average beta (in sigmas)
```

<EffCont>:

TPCeff, PIDeff
PIDcont

pHS.root

```
hMcd2Ndyydpt_<particle>_k
hMcd2Nptydydpt_<particle>_k

hMcTOFd2Ndyydpt_<particle>_k
hMcTOFd2Nptydydpt_<particle>_k

hRcd2Ndyydpt_<particle>_k
hRcd2Nptydydpt_<particle>_k

hEv_k

h<FracPart><EffCont>_<particle>_k
```

CoordEff	SecondariesEff	TOFMatchEff	TOFMatchMCEff
CoordCont	SecondariesCont	TOFMatchCont	

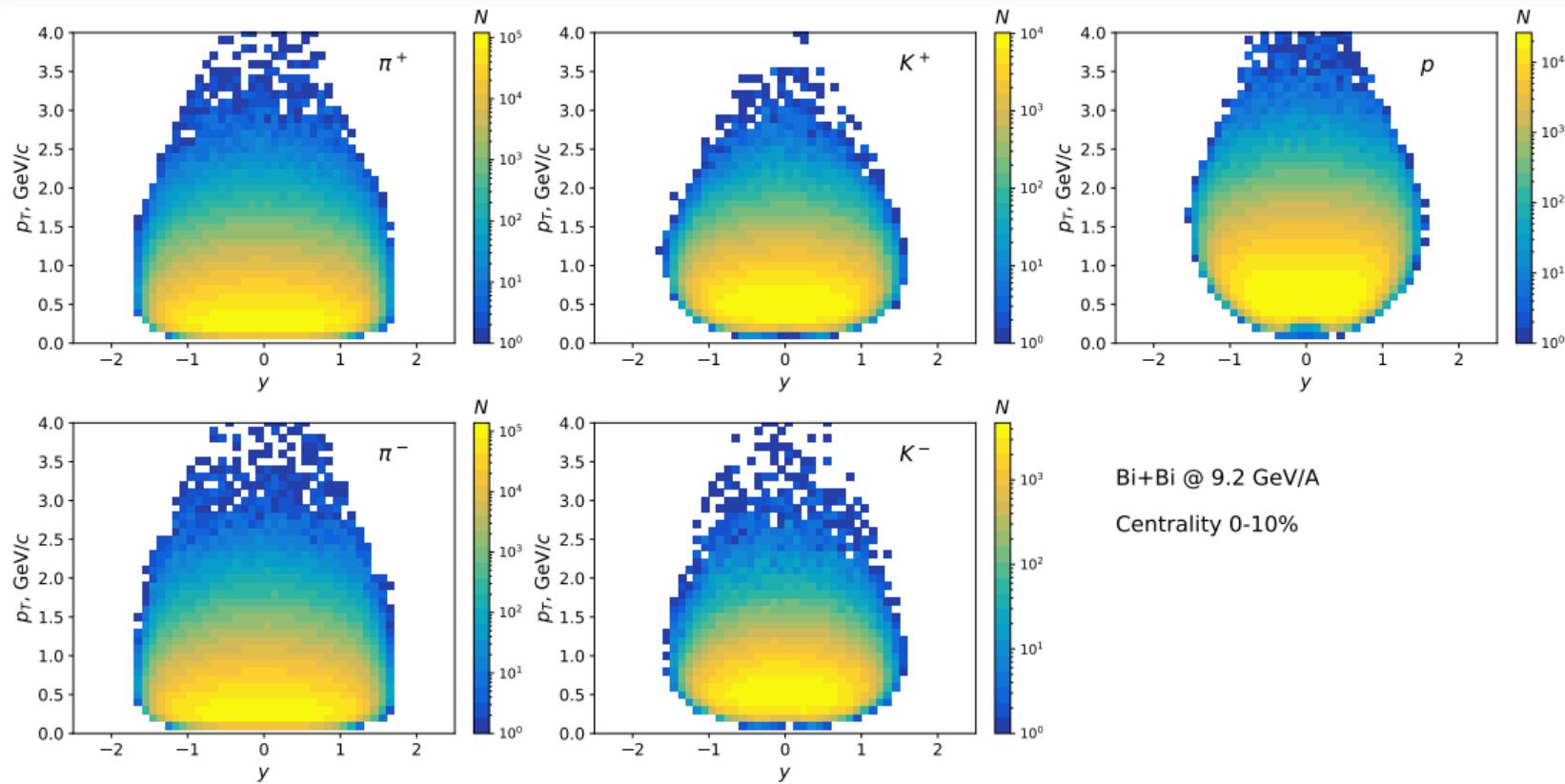
<particle>: Piplus, Piminus, Kplus, Kminus, Proton, AntiProton

<FracPart>: Num, Denom

k – number of centrality bin

Example:
hNumPIDeff_Kplus_4

Phase Spaces



Efficiencies & Contaminations

Total efficiency:

$$W = \frac{\prod_i \text{Eff}_i}{\prod_j (1 - \text{Cont}_j)}$$

$$\text{TPCeff} = \text{TPCeff} = \frac{N_{\text{RC}}[\text{TOFMC, PRIMMC, PIDMC, CELLMC}]}{N_{\text{MC}}[\text{TOFMC, PRIMMC, PIDMC, CELLMC}]}$$

$$\text{TOFeff} = \frac{N_{\text{RC}}[\text{TOFRC\&TOFMC, PRIMMC, PIDMC, CELLMC}]}{N_{\text{RC}}[\text{TOFMC, PRIMMC, PIDMC, CELLMC}]}$$

$$\text{TOFcont} = \frac{N_{\text{RC}}[\text{TOFRC\&(!TOFMC), PRIMMC, PIDMC, CELLMC}]}{N_{\text{RC}}[\text{TOFRC, PRIMMC, PIDMC, CELLMC}]}$$

$$\text{SecEff} = \frac{N_{\text{RC}}[\text{TOFRC, PRIMRC\&PRIMMC, PIDMC, CELLMC}]}{N_{\text{RC}}[\text{TOFRC, PRIMMC, PIDMC, CELLMC}]}$$

$$\text{SecCont} = \frac{N_{\text{RC}}[\text{TOFRC, PRIMRC\&(!PRIMMC), PIDMC, CELLMC}]}{N_{\text{RC}}[\text{TOFRC, PRIMRC, PIDMC, CELLMC}]}$$

$$\text{PIDeff} = \frac{N_{\text{RC}}[\text{TOFRC, PRIMRC, PIDRC = PIDMC, CELLMC}]}{N_{\text{RC}}[\text{TOFRC, PRIMRC, PIDMC, CELLMC}]}$$

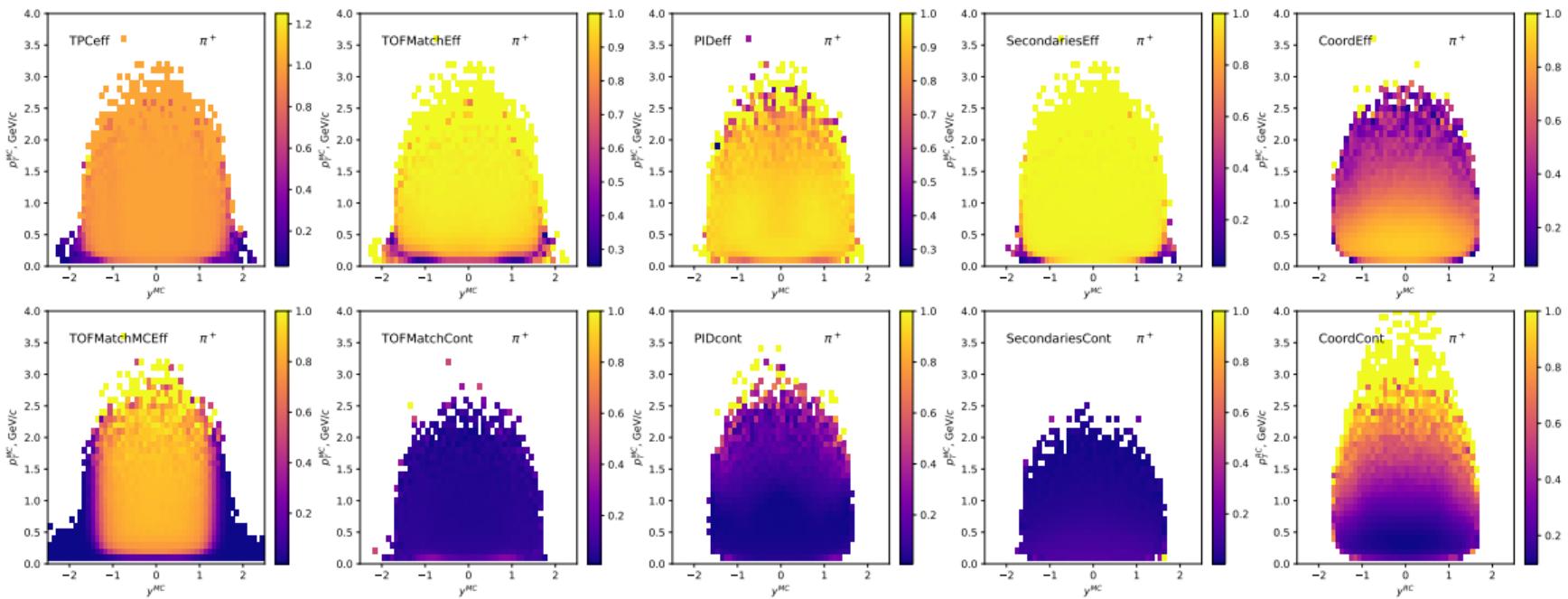
$$\text{PIDcont} = \frac{N_{\text{RC}}[\text{TOFRC, PRIMRC, PIDRC \neq PIDMC, CELLMC}]}{N_{\text{RC}}[\text{TOFRC, PRIMRC, PIDRC, CELLMC}]}$$

$$\text{CELLeff} = \frac{N_{\text{RC}}[\text{TOFRC, PRIMRC, PIDRC, CELLRC=CELLMC}]}{N_{\text{RC}}[\text{TOFRC, PRIMRC, PIDRC, CELLMC}]}$$

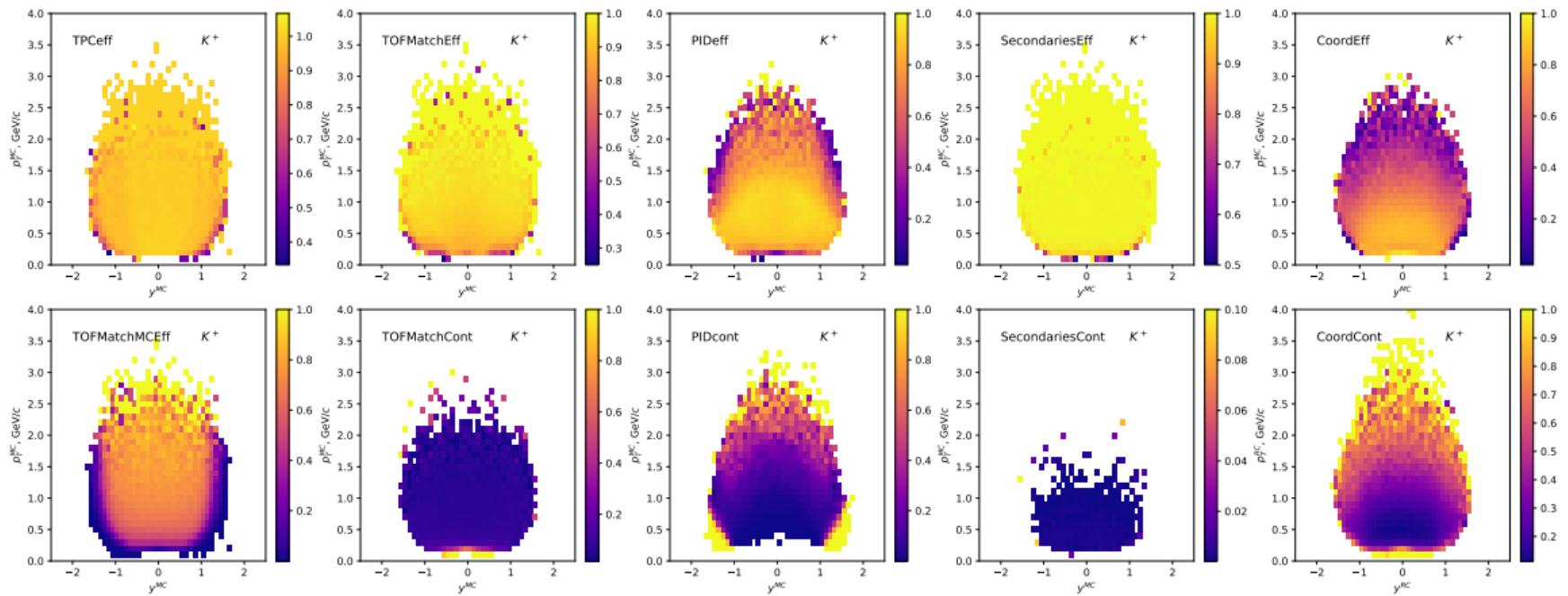
$$\text{CELLcont} = \frac{N_{\text{RC}}[\text{TOFRC, PRIMRC, PIDRC, CELLRC\neqCELLMC}]}{N_{\text{RC}}[\text{TOFRC, PRIMRC, PIDRC, CELLRC}]}$$

$$\text{TOFMCeff} = \frac{N_{\text{MC}}[\text{TOFMC, PRIMMC, PIDMC, CELLMC}]}{N_{\text{MC}}[\text{PRIMMC, PIDMC, CELLMC}]}$$

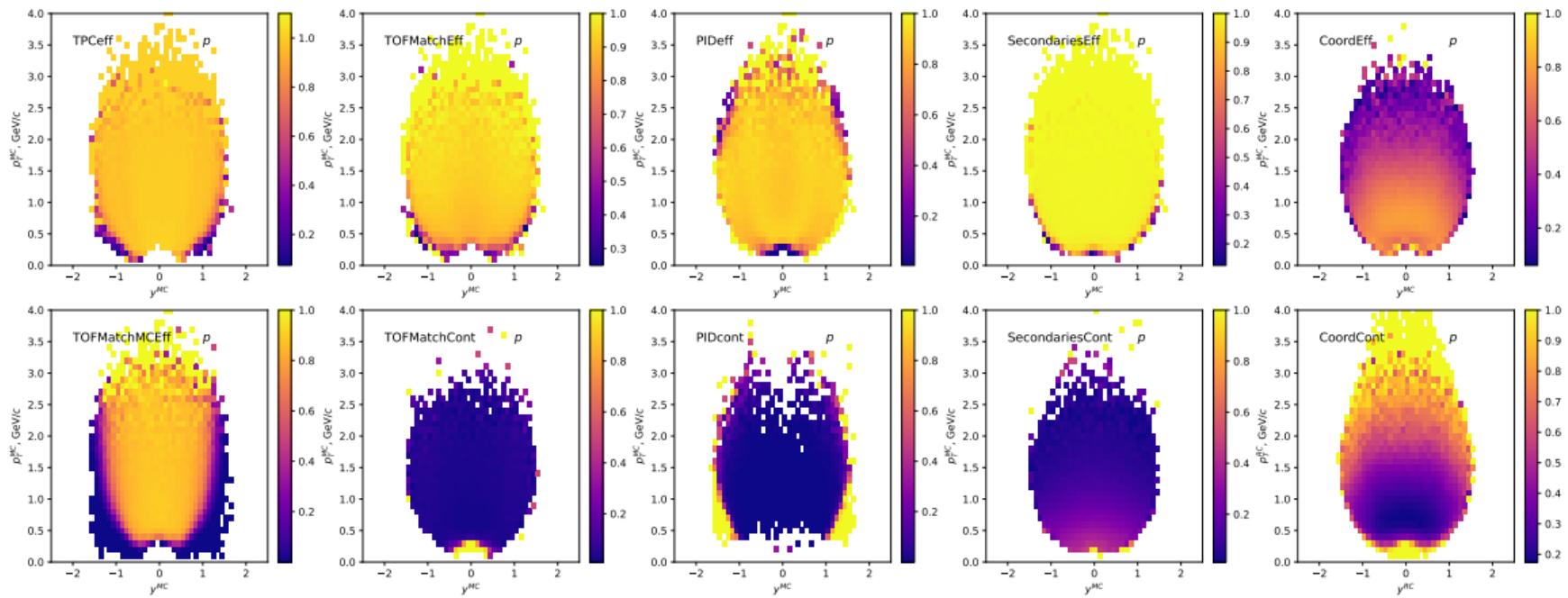
Efficiencies & Contaminations: π^+



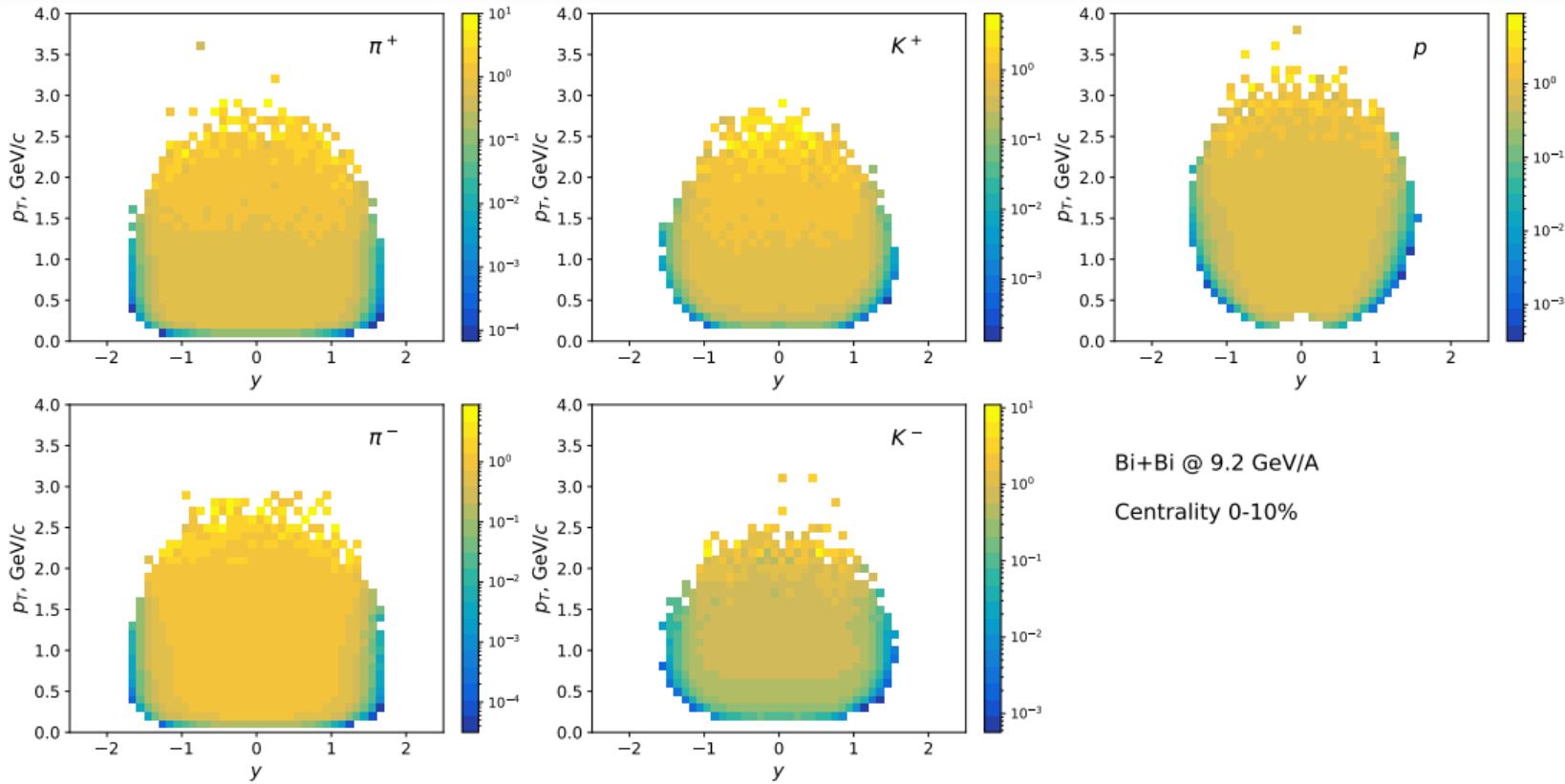
Efficiencies & Contaminations: K^+



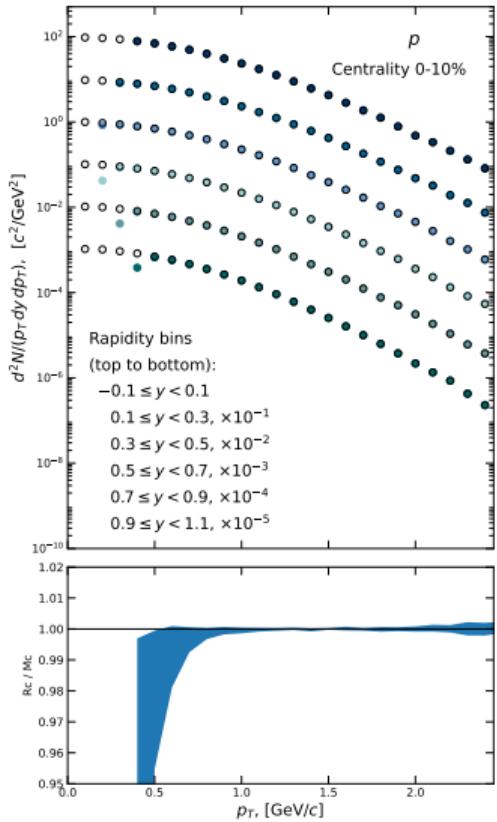
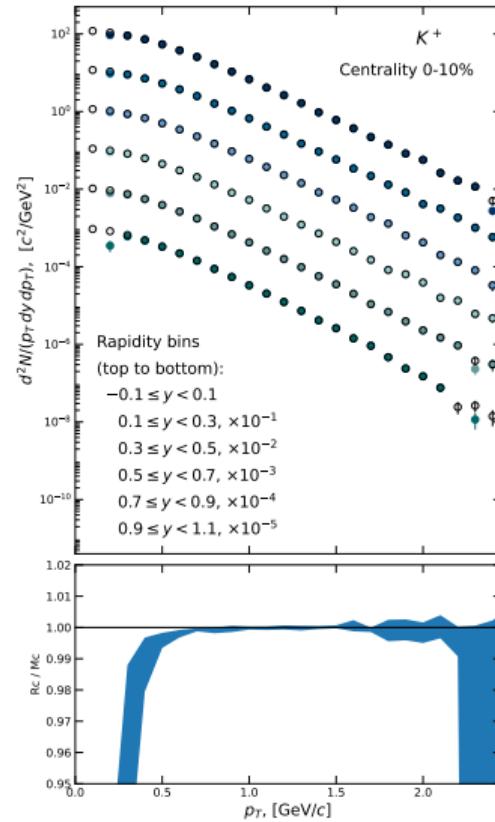
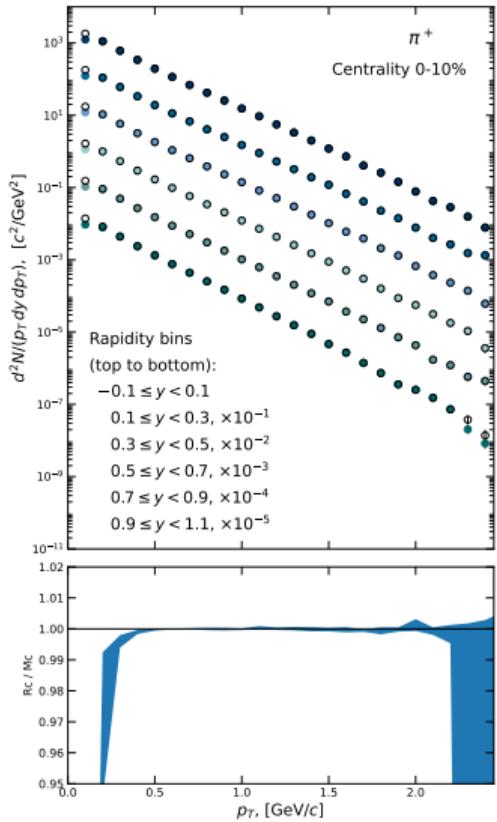
Efficiencies & Contaminations: Proton



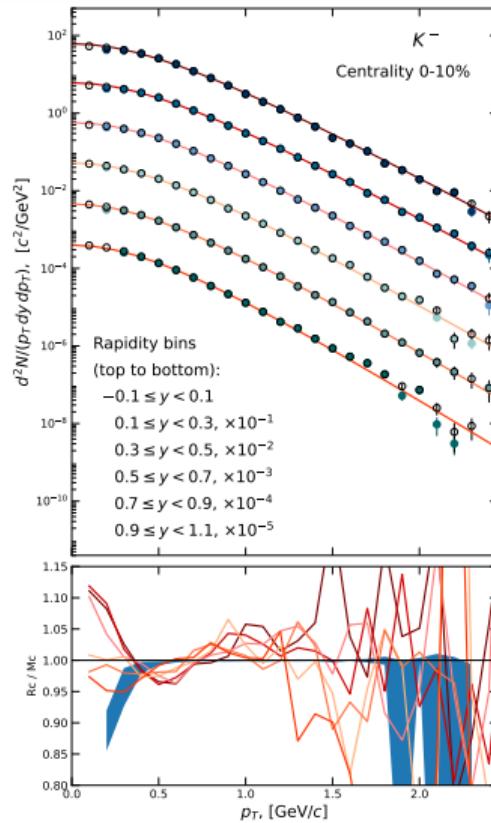
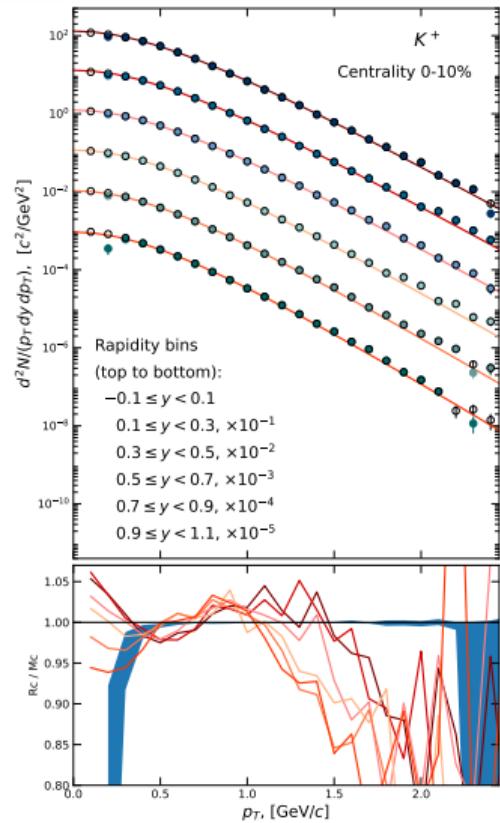
Total Efficiency



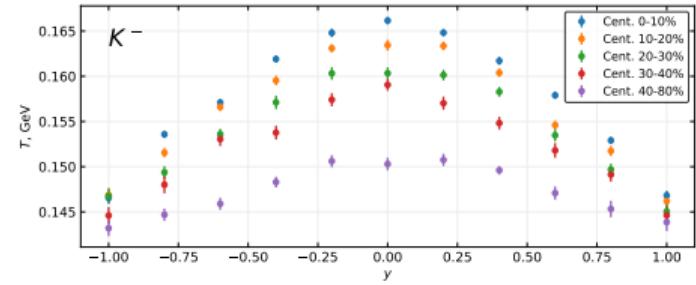
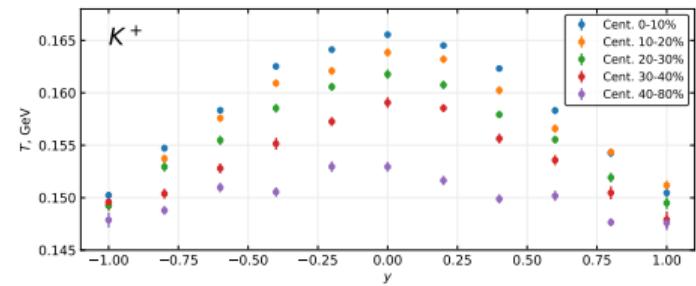
Spectra



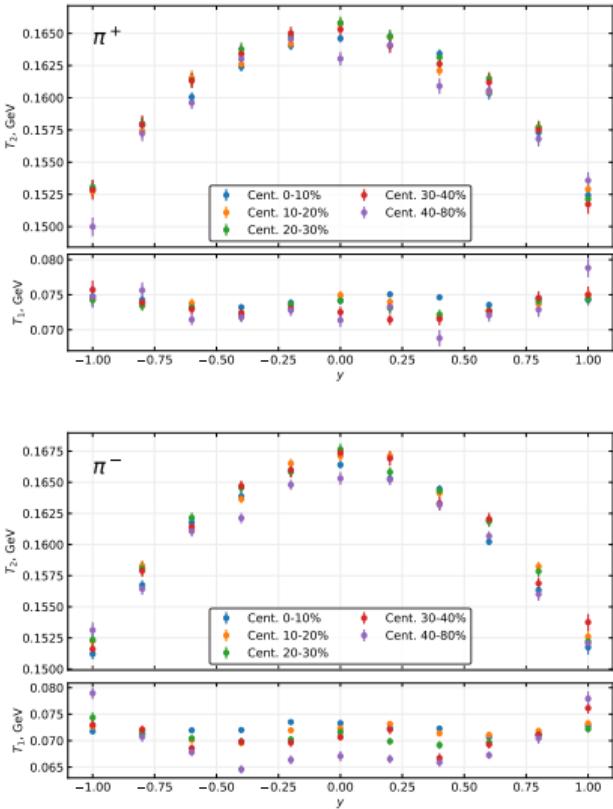
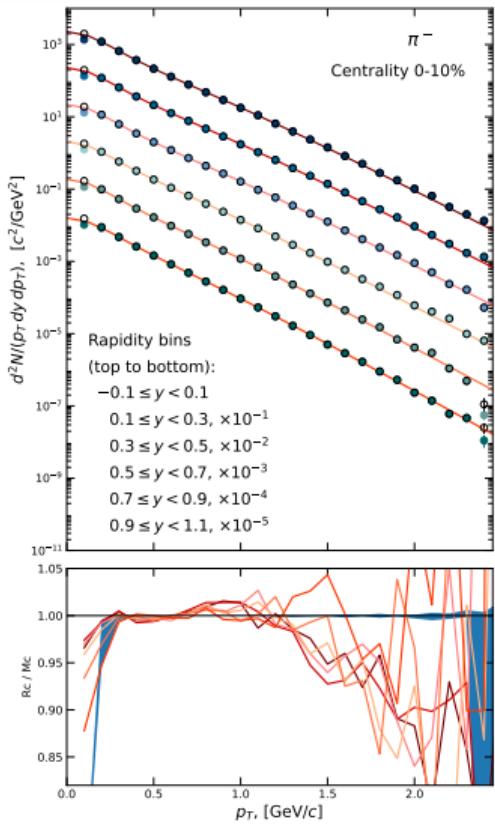
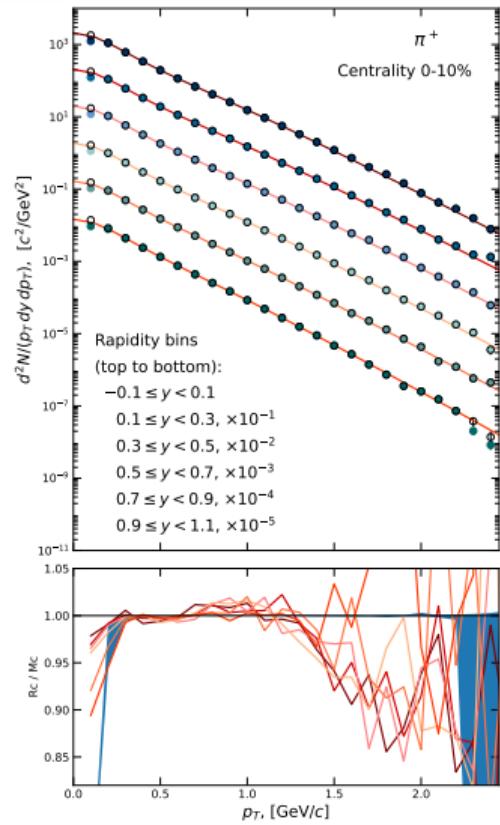
Spectra Fitting: Thermal Exponential



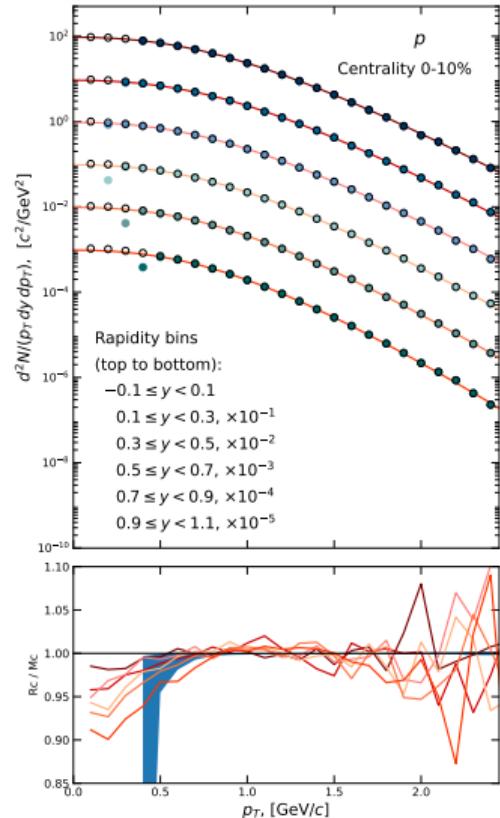
$$f(p_T) = \frac{dN/dy}{T[(m + T)^2 + T^2]} \cdot m_T \cdot e^{-(m_T - m)/T}$$



Spectra Fitting: Sum of Two Thermal Exponentials



Spectra Fitting: Blast Wave



$$\frac{d^2N}{p_T dp_T dy} = C(y) \cdot m_T \int_0^1 \chi d\chi \exp \left[-\frac{m_T \operatorname{ch} \rho \operatorname{ch}(y - \eta)}{T} \right] I_0 \left(\frac{p_T \operatorname{sh} \rho}{T} \right)$$

Boost angles: $\rho = \operatorname{arth} \beta_r, \quad \eta = \operatorname{arth} \beta_z$

Parametrization of transverse velocity:

$$\beta_r(r) = \beta_{\max} \left(\frac{r}{R} \right)^n = \beta_{\max} \cdot \chi^n; \quad n = 1 \Rightarrow \text{linear BW model}$$

$r \in [0; R]$; R is the radius of freeze-out surface.

$C(y) \Leftrightarrow$ shape of freeze-out surface and chemical potential.

I_0 – modified Bessel function.

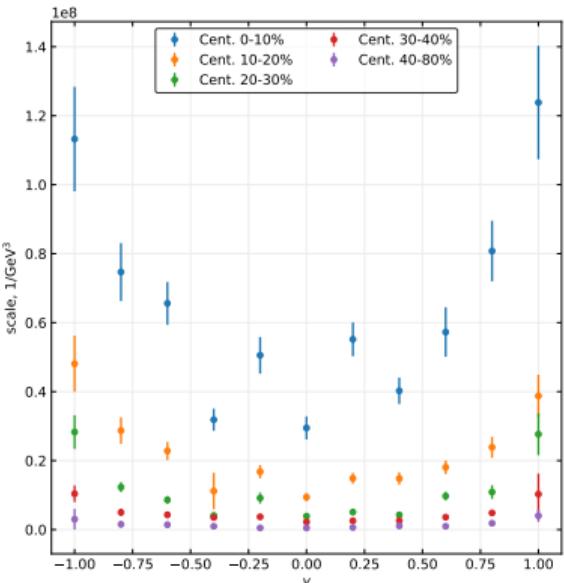
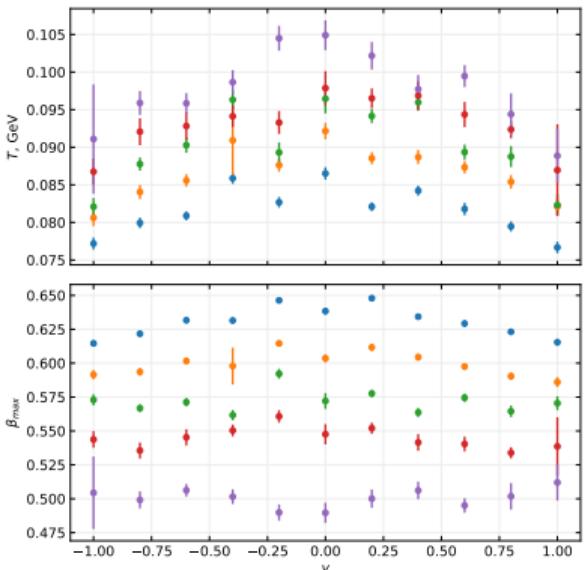
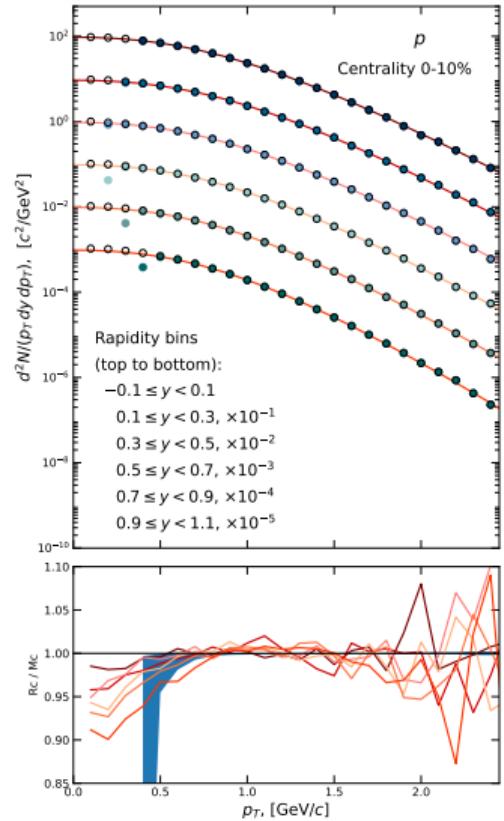
For our spectra $\operatorname{ch}(y - \eta) = 1$ is kept fixed.

Fit parameters: $C(y), \quad T, \quad \beta_{\max}$.

Based on

- [1] E. Schnedermann, J. Sollfrank and U. W. Heinz, Phys. Rev. C **48**, 2462-2475 (1993) [arXiv:nucl-th/9307020 [nucl-th]].

Spectra Fitting: Blast Wave



Spectra Fitting: Estimation of Errors

The Jackknife method:

- data are divided into K portions;
- error for estimated parameter \hat{A} :

$$\delta\hat{A} = \sqrt{\frac{K-1}{K} \sum_{k=1}^K \left(\hat{A}_{(k)} - \hat{A} \right)^2},$$

$\hat{A}_{(k)}$ – estimate of A without k -th portion.

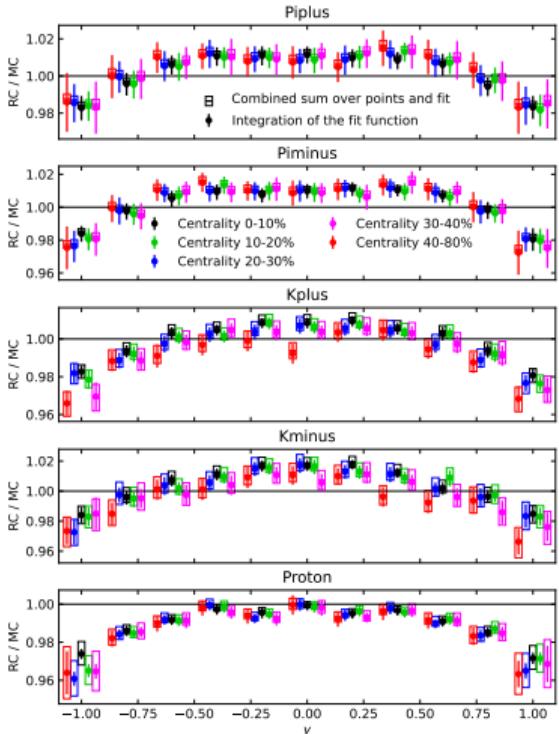
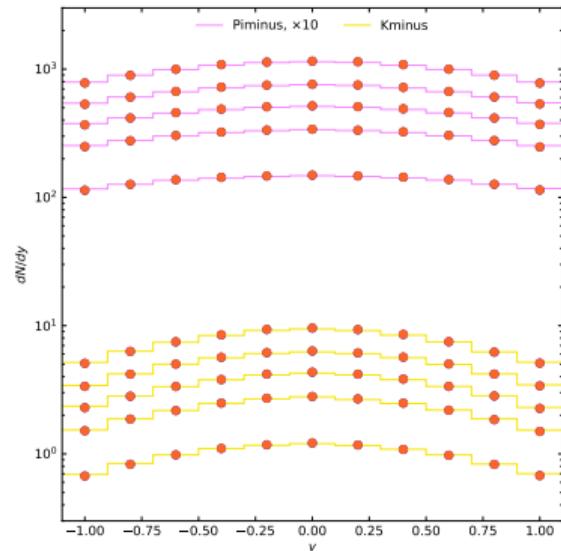
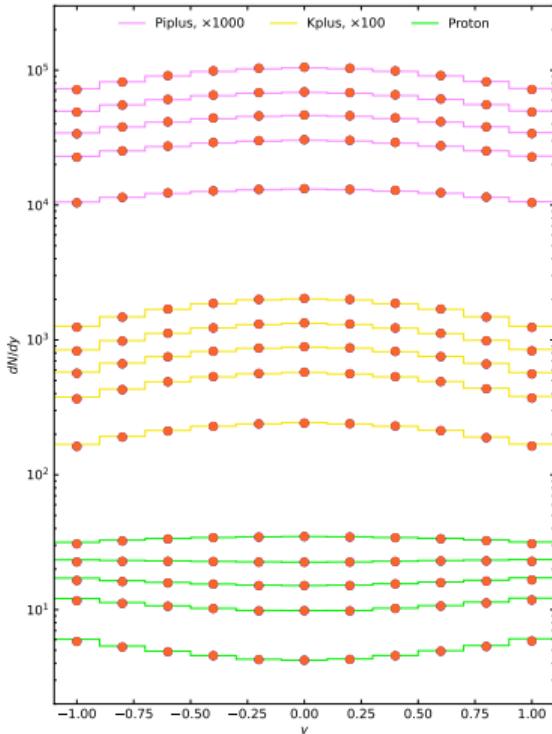
- The method is not sensitive to the distribution of data.
- For uncorrelated data the result does not depend on K .
- For normally distributed uncorrelated data $\delta\hat{A} \rightarrow$ standard deviation.
- The method requires large enough statistics.

[2] B. Efron, SIAM Review, 21(4), 460–480 (1979)

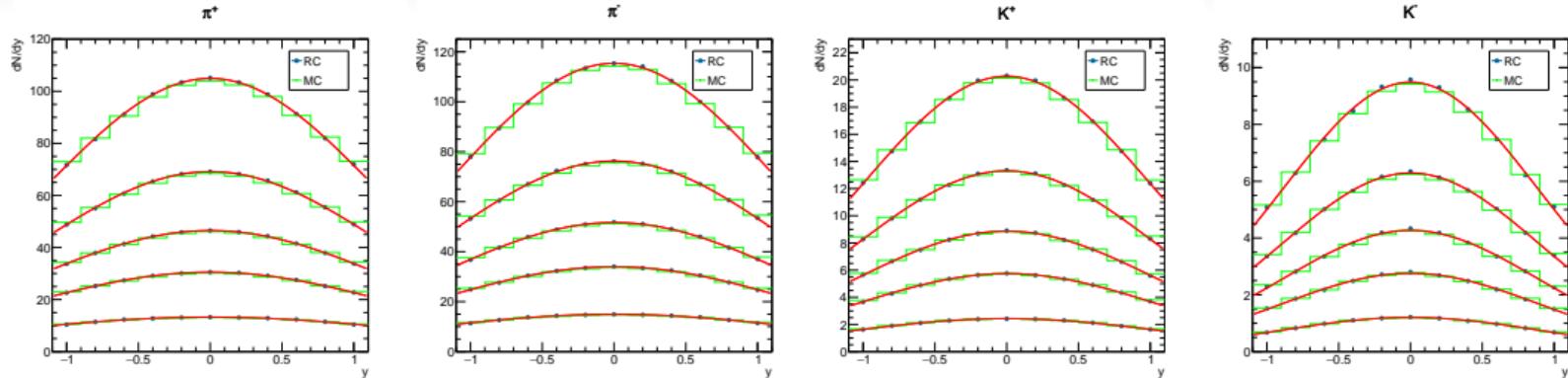
[3] B. Efron, “The Jackknife, the Bootstrap and Other Resampling Plans”, SIAM (1982)

[4] M. Fukugita, M. Okawa and A. Ukawa, Nucl. Phys. B 337, 181-232 (1990)

dN/dy



Yields



Cent.	N	\tilde{N}	\tilde{N}_{MC}	N	\tilde{N}	\tilde{N}_{MC}	N	\tilde{N}	\tilde{N}_{MC}	N	\tilde{N}	\tilde{N}_{MC}
0-10%	300(2)	199.6	199.3	325(1)	218.5	218.1	51.1(1)	37.1	37.1	21.04(5)	16.5	16.5
10-20%	208(2)	133.3	132.9	226(1)	146.3	146.1	34.2(1)	24.5	24.6	14.06(4)	11.0	11.0
20-30%	146(1)	90.5	90.3	158(1)	100.0	99.7	23.3(1)	16.4	16.5	9.42(3)	7.43	7.42
30-40%	99(1)	59.9	59.7	107(1)	66.2	66.1	15.3(1)	10.7	10.7	6.22(3)	4.84	4.85
40-80%	49(1)	26.7	26.1	52(1)	29.7	29.6	6.86(3)	4.61	4.65	2.80(1)	2.14	2.15

$$f(y) = \frac{N}{\sqrt{2\pi\sigma^2}} \exp\left[-\frac{y^2}{2\sigma^2}\right] \quad \Rightarrow \quad N$$

$$\tilde{N} = \int_{-1.1}^{1.1} f(y) dy$$

pidAM vs pidSTAR: General Remarks

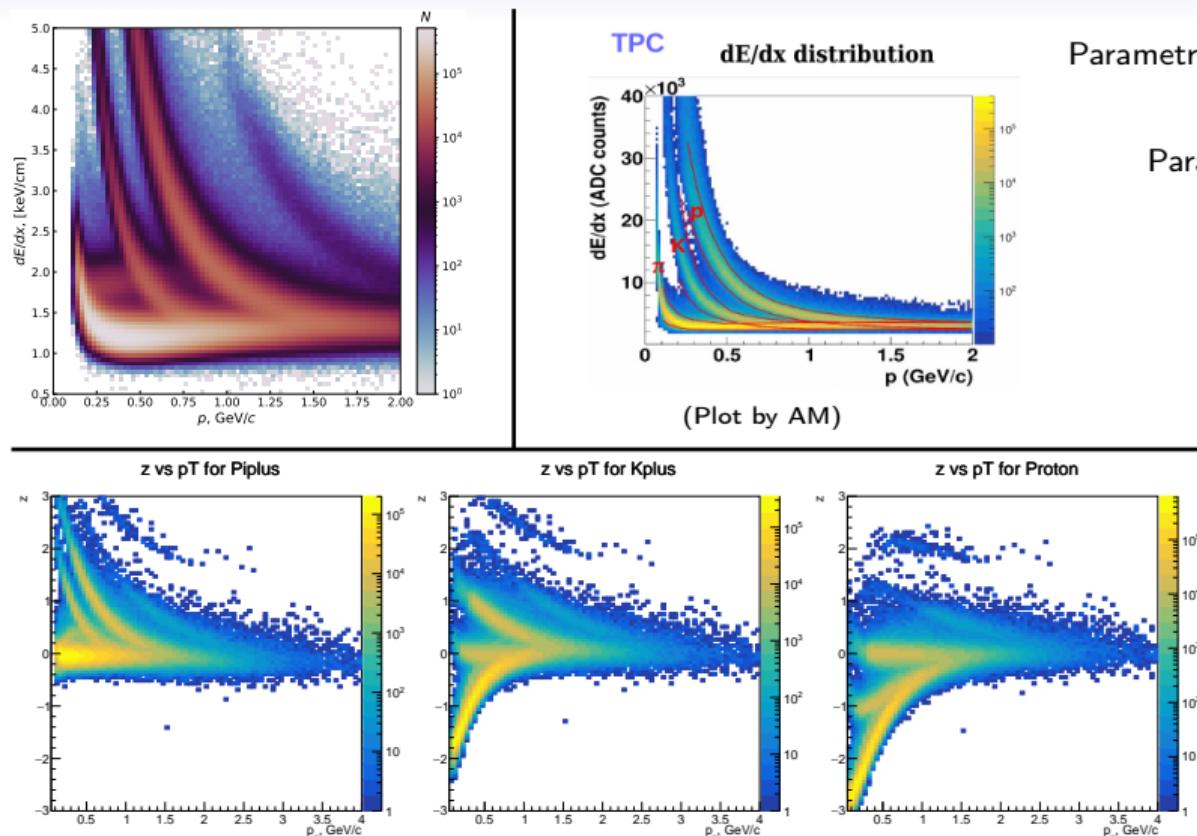
PID is based on 2 devices: TPC and ToF

pidAM (AM = A. Mudrokh) [MpdPid class]	pidSTAR
<ul style="list-style-type: none">based on $p = \vec{p}$.both TPC and ToF information is used for all p.PID is applied to each track. <p style="text-align: center;">↓</p> <p>For each track we know 'who' is it</p> <ul style="list-style-type: none">Requires less memory/disk space.	<ul style="list-style-type: none">based on p_T.TPC at low p_T, ToF at high p_T.PID is applied to the final set of tracks. <p style="text-align: center;">↓</p> <p>We know, how many particles of a given sort are in the sample.</p> <ul style="list-style-type: none">May be implemented in model-independent way.

pidSTAR implementation is based on

- [5] L. Adamczyk *et al.* [STAR], Phys. Rev. C 96, no.4, 044904 (2017) [[arXiv:1701.07065 \[nucl-ex\]](#)].
- [6] B. I. Abelev *et al.* [STAR], Phys. Rev. C 79, 034909 (2009) [[arXiv:0808.2041 \[nucl-ex\]](#)].
- [7] J. Adam *et al.* [STAR], Phys. Rev. C 101, no.2, 024905 (2020) [[arXiv:1908.03585 \[nucl-ex\]](#)].
- [8] M. S. Abdallah *et al.* [STAR], Phys. Rev. C 107, no.2, 024901 (2023) [[arXiv:2208.00653 \[nucl-ex\]](#)].
- [9] [STAR], [[arXiv:2311.11020 \[nucl-ex\]](#)].

pidAM vs pidSTAR: dE/dx



Parametrization of the Bethe-Bloch (BB) formula



Parametrization of deviations from BB



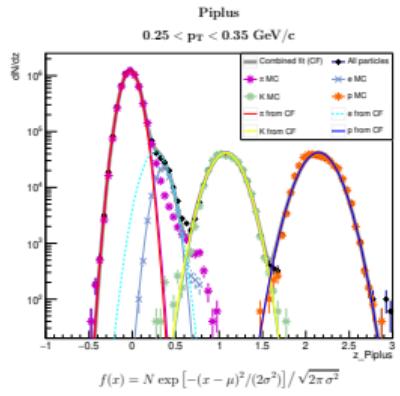
$N\sigma$ method / Bayes method

$$z_i = \ln \left(\frac{\langle dE/dx \rangle}{\langle dE/dx \rangle_{i}^{BB}} \right)$$

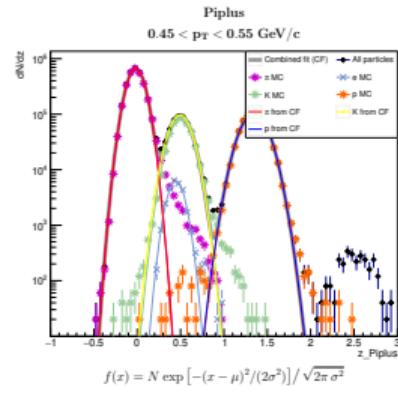
i – type of particle

For a given particle at given p_T , z_i has Gauss distr. with $\langle z_i \rangle \sim 0$.

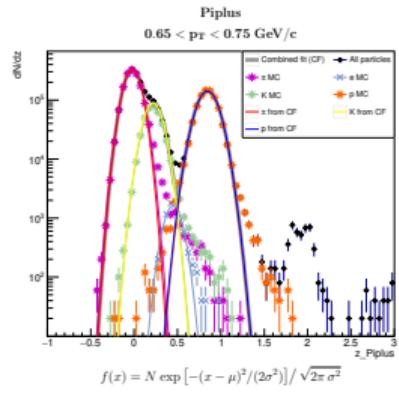
pidAM vs pidSTAR: dE/dx Results



Notes:
 Repeated fit with fixed $\sigma_e = (\sigma_\pi + \sigma_K)/2$.

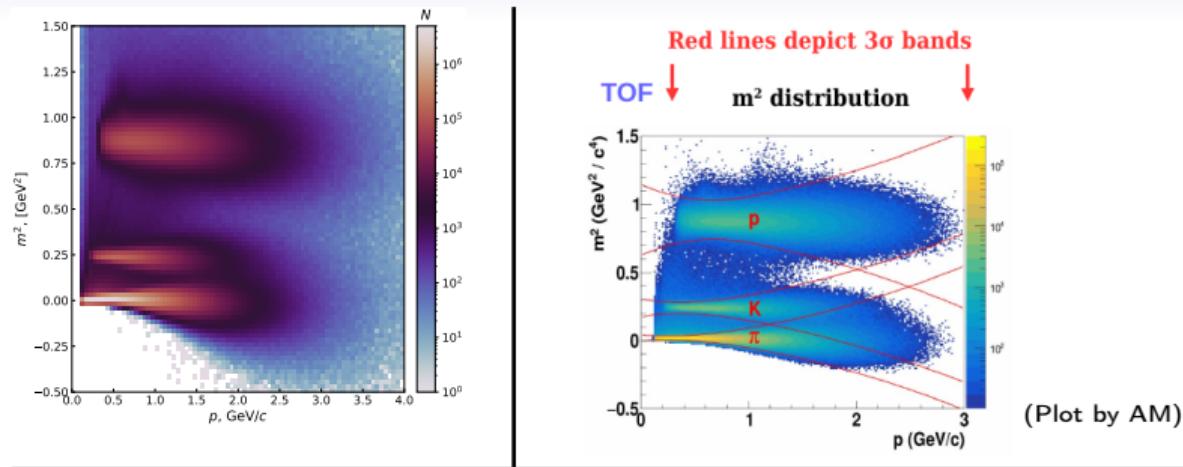


Notes:
 Kaon result contains also Electrons!
 Repeated fit with fixed $\sigma_K = (\sigma_e + \sigma_p)/2$.



Notes:
 Electrons are excluded from fit (too few of them).
 Repeated fit with fixed $\sigma_K = (\sigma_e + \sigma_p)/2$.

pidAM vs pidSTAR: m^2



Parametrization of deviations



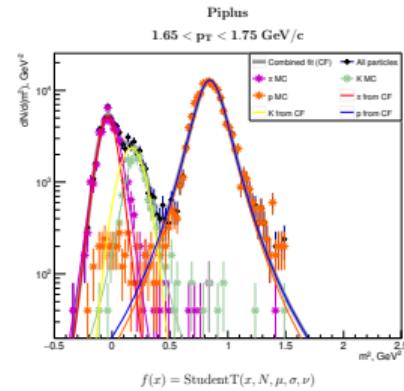
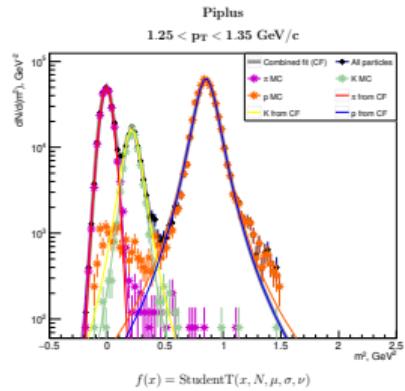
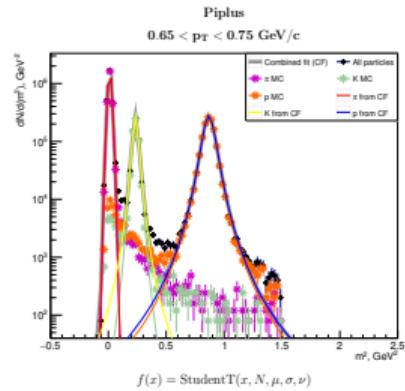
$N\sigma$ method / Bayes method

Fit p_T sections with sum of StudentT PDFs.

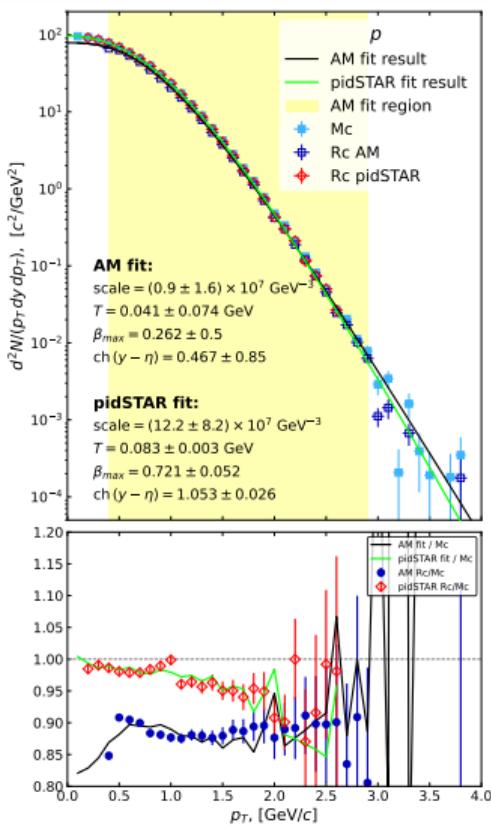
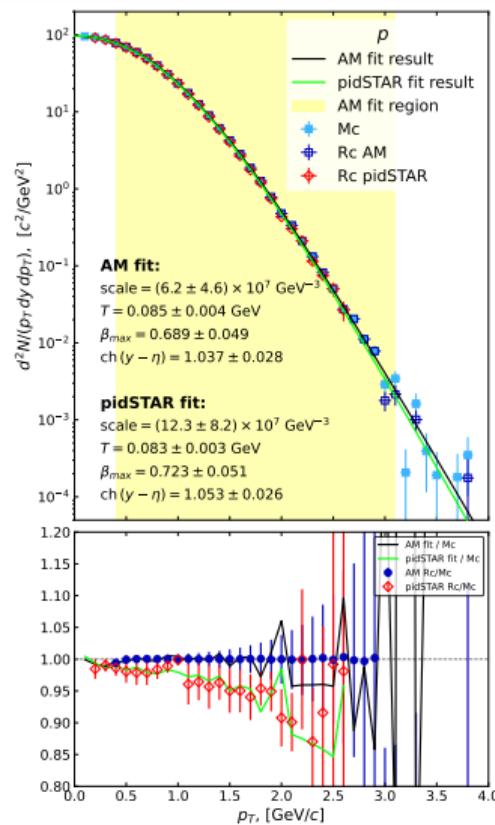
$$f(x) = N \cdot \frac{\left(\frac{\nu}{\nu + (x - \mu)^2 / \sigma^2} \right)^{(1+\nu)/2}}{\sqrt{\nu} \sigma B \left(\frac{\nu}{2}, \frac{1}{2} \right)}$$

$$B(a, b) = \frac{\Gamma(a) \Gamma(b)}{\Gamma(a+b)} = \int_0^1 t^{a-1} (1-t)^{b-1} dt \quad - \text{beta-function}$$

pidAM vs pidSTAR: m^2 Results



pidAM vs pidSTAR: Comparison of Results



Right plot: w/o PID corections

Conclusions

- MpHadronSpectra wagon is updated.
- Efficiency corrected invariant spectra for π^\pm , K^\pm , p are obtained.
- Yields for π^\pm and K^\pm are obtained.

- Trial implementation of STAR PID method is done. The results are compared with ones of pidAM method.