

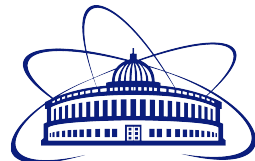
# First results and perspectives of the anisotropic flow measurements at the BM@N experiment

Mikhail Mamaev, Arkady Taranenko, Peter Parfenov, Valerii Troshin,  
Alexandr Demanov, Irina Zhavoronkova  
JINR, MEPhI

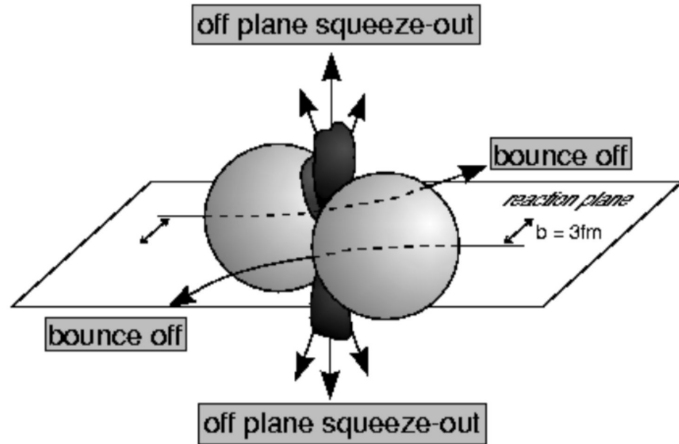
The work has been supported by the Ministry of Science and Higher Education of the Russian Federation, Project "Fundamental and applied research at the NICA megascience experimental complex" № FSWU-2024-0024



Workshop on physics performance studies at NICA (NICA-2024)  
27/11/2024



# Anisotropic flow & spectators



The azimuthal angle distribution is decomposed in a Fourier series relative to reaction plane angle:

$$\rho(\varphi - \Psi_{RP}) = \frac{1}{2\pi} \left( 1 + 2 \sum_{n=1}^{\infty} v_n \cos n(\varphi - \Psi_{RP}) \right)$$

Anisotropic flow:

$$v_n = \langle \cos [n(\varphi - \Psi_{RP})] \rangle$$

Anisotropic flow is sensitive to:

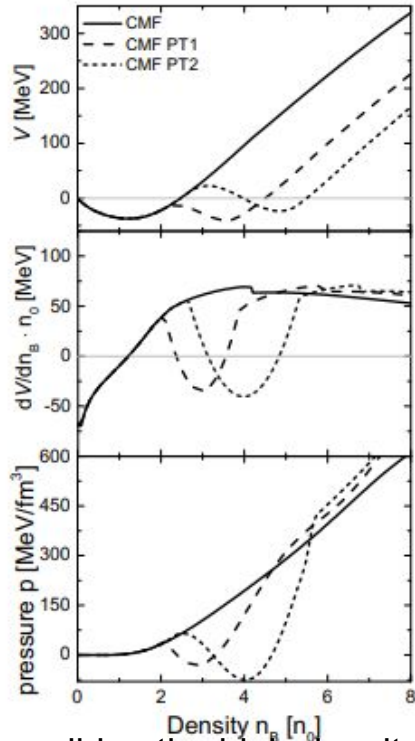
- Time of the interaction between overlap region and spectators
- Compressibility of the created matter

# $v_n$ as a function of collision energy

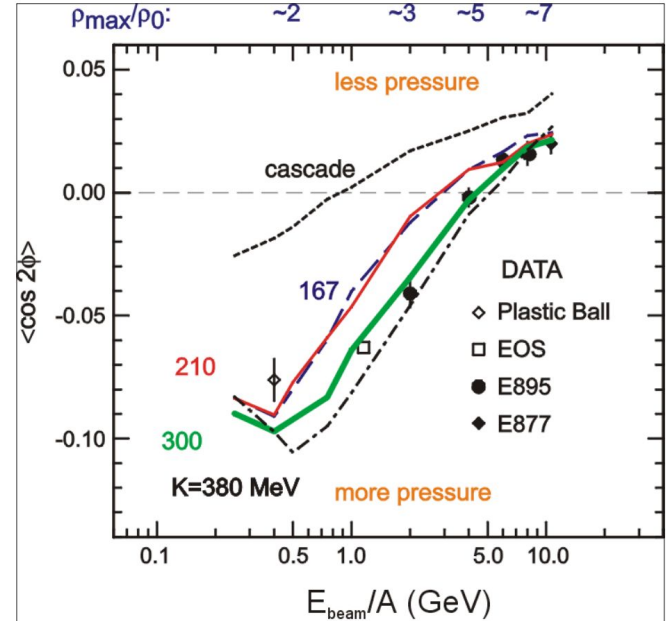
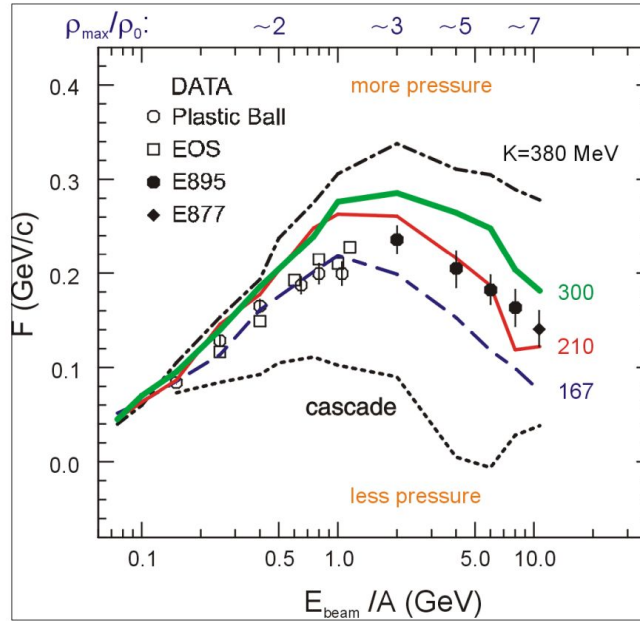
P. DANIELEWICZ, R. LACEY, W. LYNCH  
[10.1126/science.1078070](https://doi.org/10.1126/science.1078070)

$v_1$  suggests softer EOS

$v_2$  suggests harder EOS



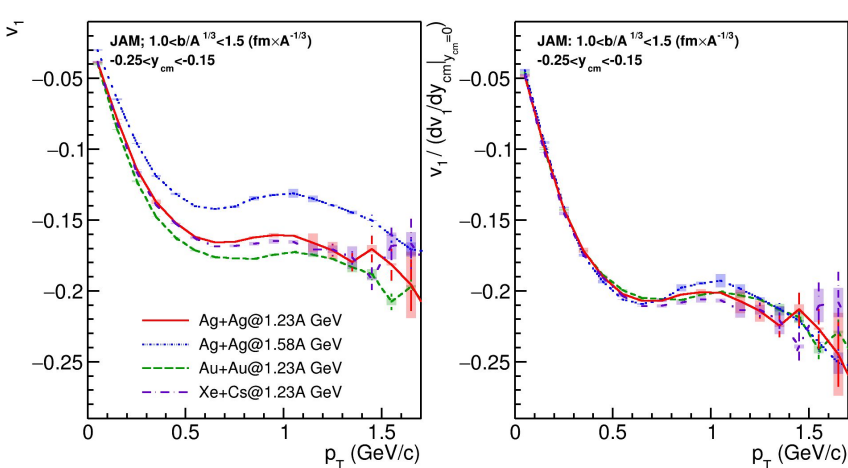
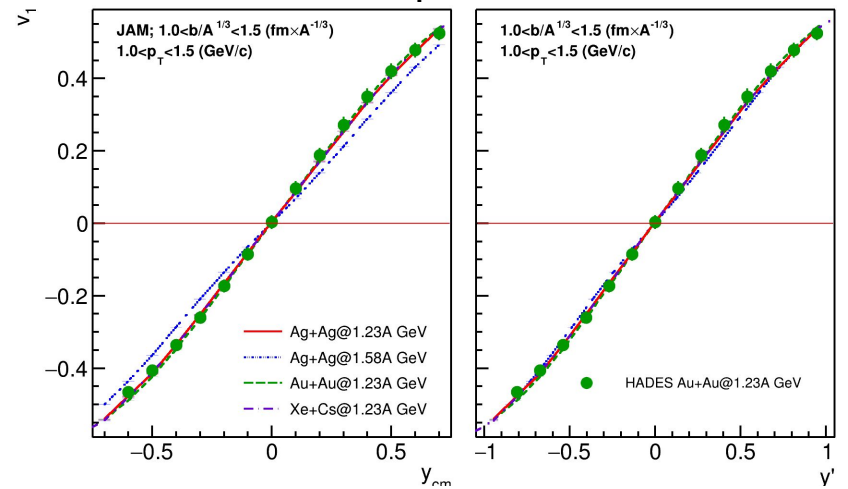
EPJ Web of Conferences 276, 01021 (2023)



Describing the high-density matter using the mean field  
 Flow measurements constrain the mean field

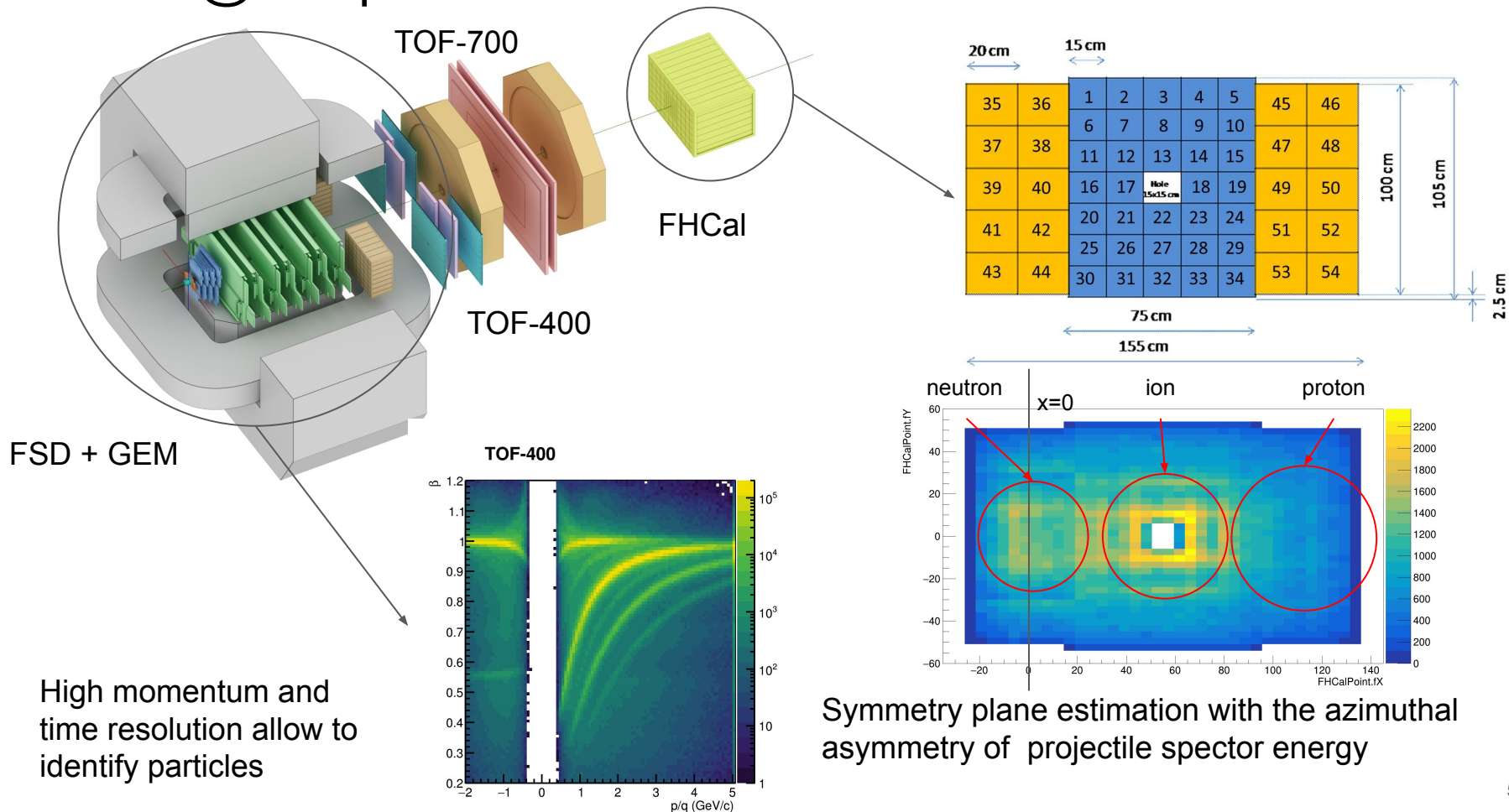
Discrepancy is probably due to non-flow correlations

# HADES: $dv_1/dy$ scaling with collision energy and system size



- Scaling with collision energy is observed in model and experimental data
- Scaling with system size is observed in model and experimental data
- We can compare the results with HIC-data from other experiments (e.g. STAR-FXT Au+Au)

# The BM@N experiment in Xe+CsI at 3.8A GeV run



# Flow vectors

From momentum of each measured particle define a  $u_n$ -vector in transverse plane:

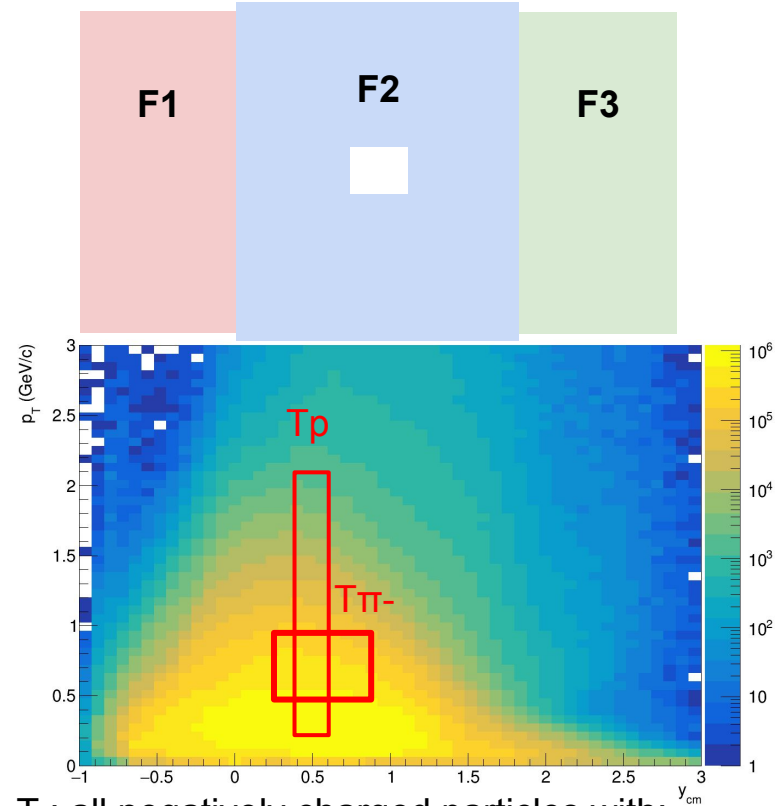
$$u_n = e^{in\phi}$$

where  $\phi$  is the azimuthal angle

Sum over a group of  $u_n$ -vectors in one event forms  $Q_n$ -vector:

$$Q_n = \frac{\sum_{k=1}^N w_n^k u_n^k}{\sum_{k=1}^N w_n^k} = |Q_n| e^{in\Psi_n^{EP}}$$

$\Psi_n^{EP}$  is the event plane angle



T-: all negatively charged particles with:

- $1.5 < \eta < 4$
- $p_T > 0.2 \text{ GeV/c}$

T+: all positively charged particles with:

- $2.0 < \eta < 3$
- $p_T > 0.2 \text{ GeV/c}$

# Flow methods for $v_n$ calculation

Tested in HADES: M Mamaev et al 2020 PPNuclei 53, 277–281  
 M Mamaev et al 2020 J. Phys.: Conf. Ser. 1690 012122

Scalar product (SP) method:

$$v_1 = \frac{\langle u_1 Q_1^{F1} \rangle}{R_1^{F1}} \quad v_2 = \frac{\langle u_2 Q_1^{F1} Q_1^{F3} \rangle}{R_1^{F1} R_1^{F3}}$$

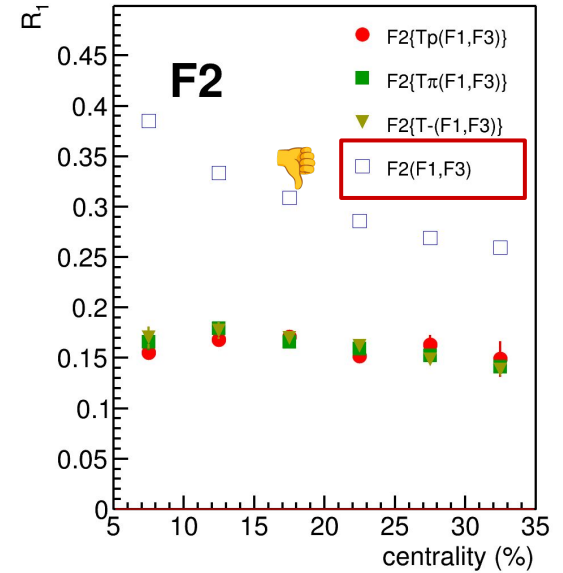
Where  $R_1$  is the resolution correction factor

$$R_1^{F1} = \langle \cos(\Psi_1^{F1} - \Psi_1^{RP}) \rangle$$

Symbol “F2(F1,F3)” means  $R_1$  calculated via  
 (3S resolution):

$$R_1^{F2(F1,F3)} = \frac{\sqrt{\langle Q_1^{F2} Q_1^{F1} \rangle \langle Q_1^{F2} Q_1^{F3} \rangle}}{\sqrt{\langle Q_1^{F1} Q_1^{F3} \rangle}}$$

Method helps to eliminate non-flow  
 Using 2-subevents doesn't



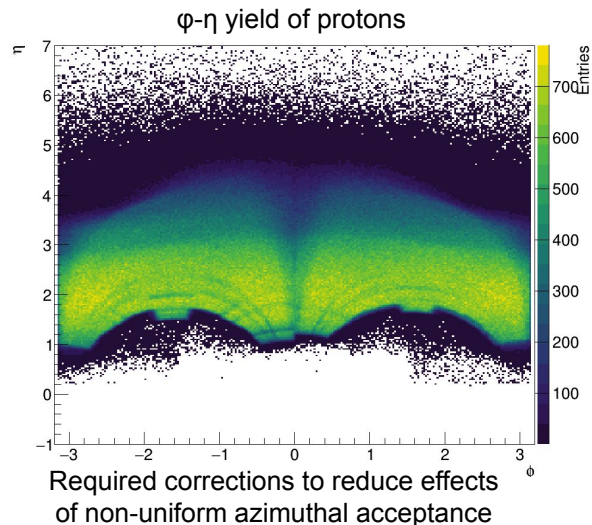
Symbol “F2{Tp}(F1,F3)” means  $R_1$   
 calculated via (4S resolution):

$$R_1^{F2\{Tp\}(F1,F3)} = \langle Q_1^{F2} Q_1^{Tp} \rangle \frac{\sqrt{\langle Q_1^{F1} Q_1^{F3} \rangle}}{\sqrt{\langle Q_1^{Tp} Q_1^{F1} \rangle \langle Q_1^{Tp} Q_1^{F3} \rangle}}$$

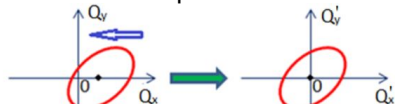
# Performance Analysis



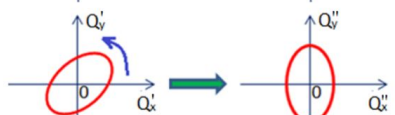
# Azimuthal asymmetry of the BM@N acceptance



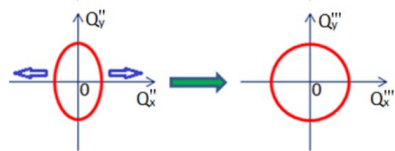
1. Recentering



2. Twist

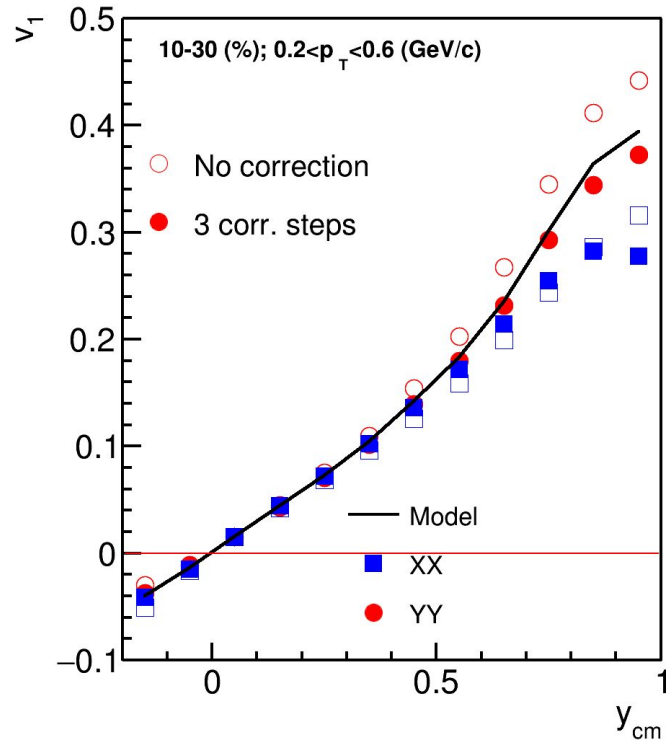


3. Rescaling



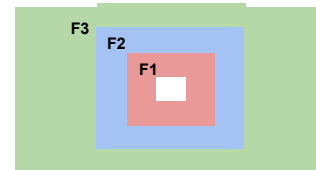
Corrections are based on method in:

I. Selyuzhenkov and S. Voloshin PRC77, 034904 (2008)

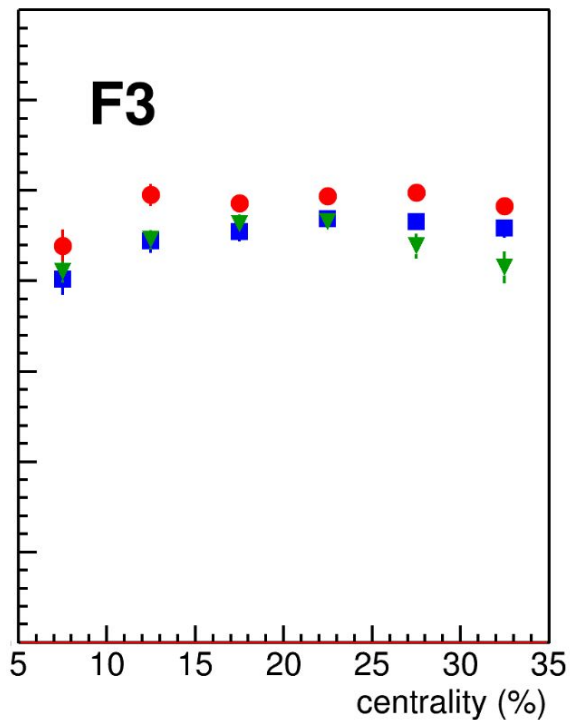
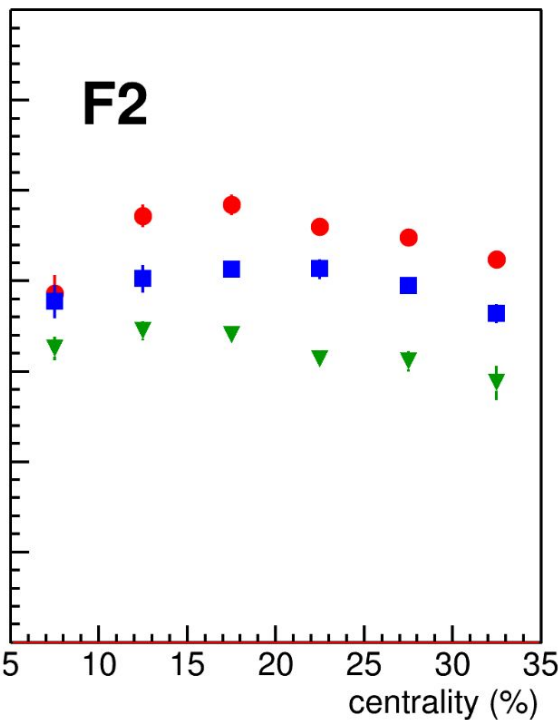
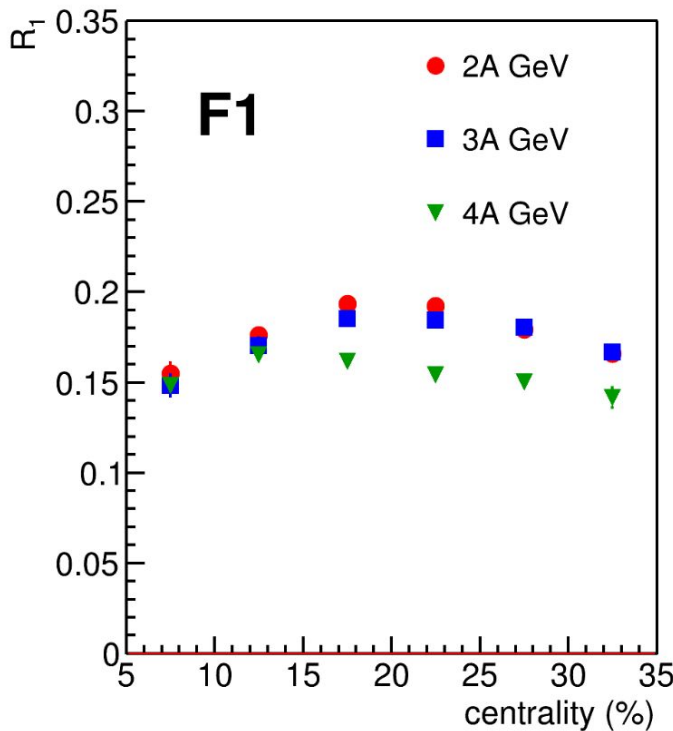


- Better agreement after rescaling for YY
- XX component has too large bias (due to magnetic field)

# Performance study: R1

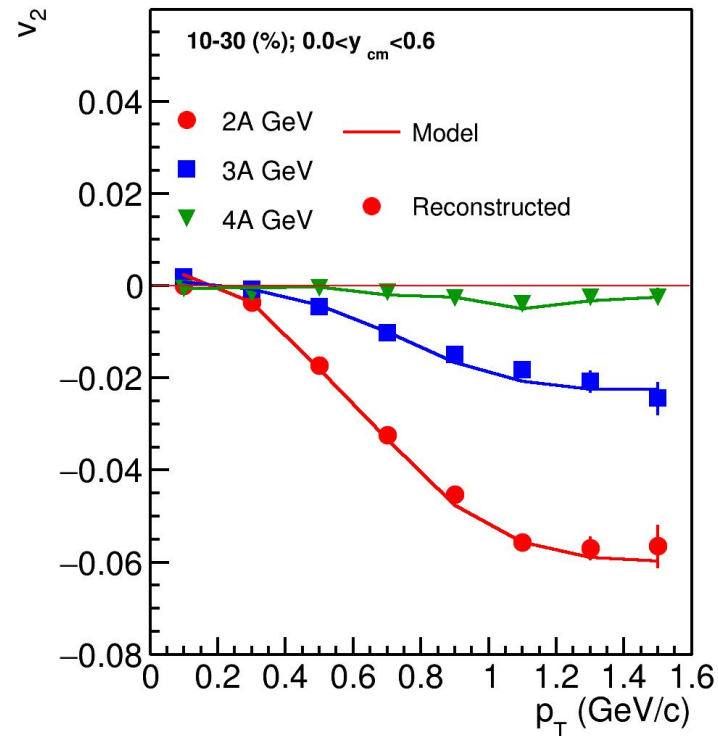
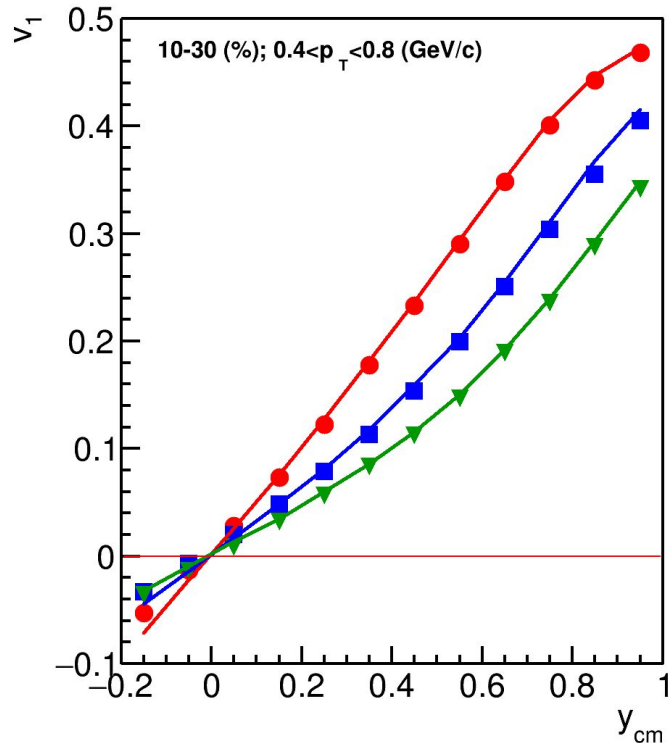


DCMQGSM-SMM



Resolution is lower for higher energies due to lower  $v_1$

# Performance study: $v_1$ and $v_2$ in Xe+Cs (JAM)

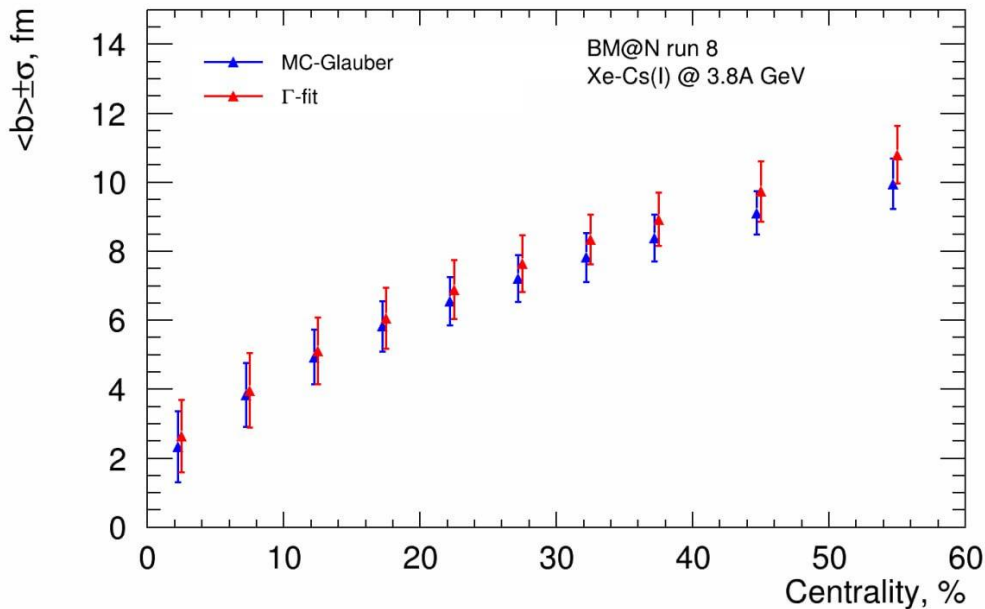


- Good agreement between reconstructed and pure model data for all three energies

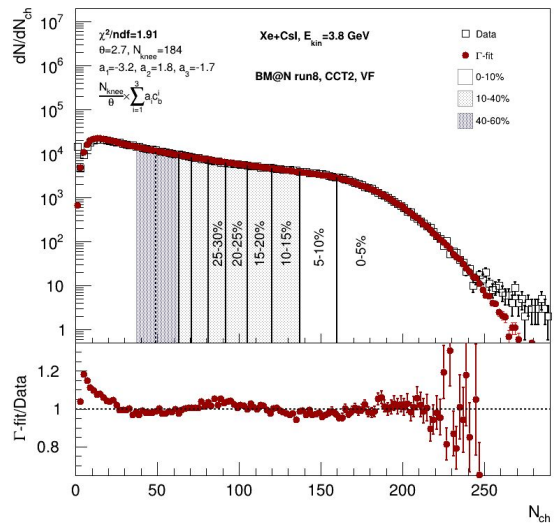
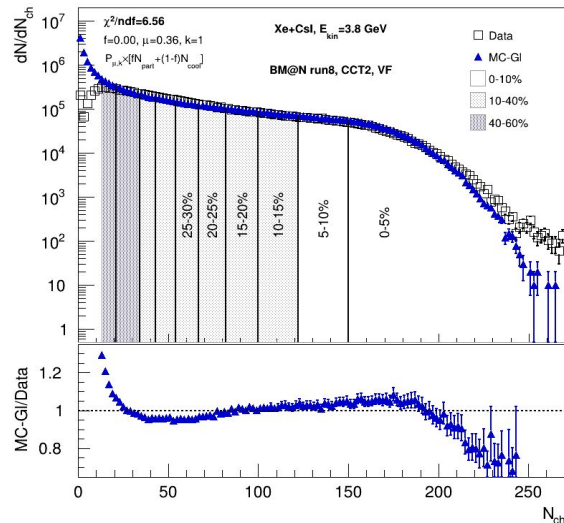
# Data Analysis

# Centrality determination methods

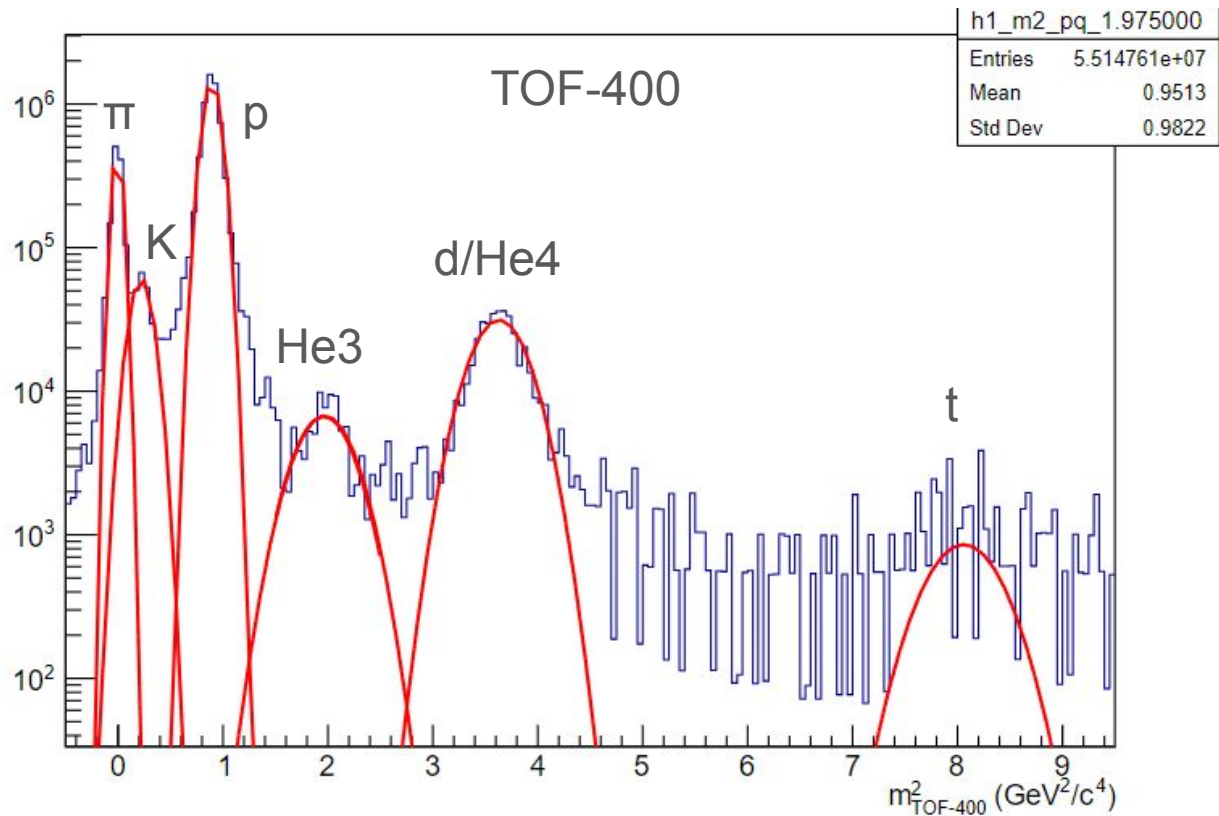
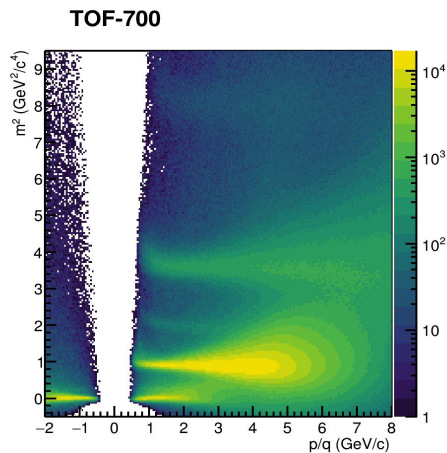
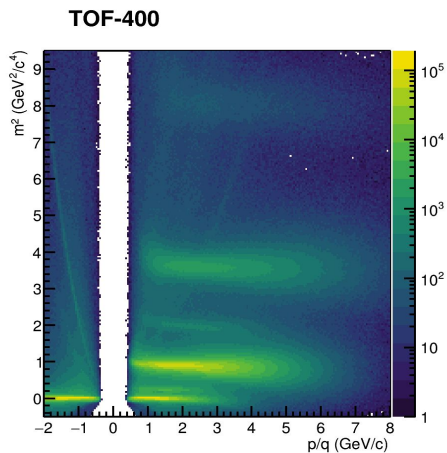
Physics of Atomic Nuclei, 2024, Vol. 87, No. 1, pp. 389–394

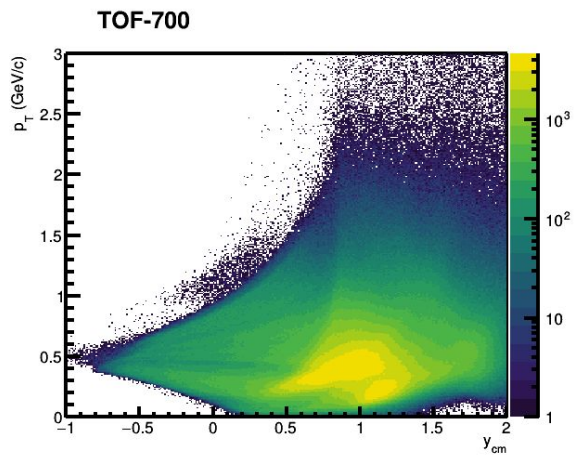
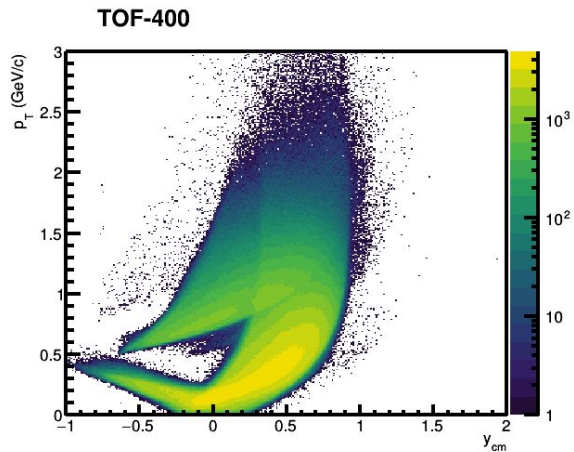


Two methods for centrality determination: MC-Glauber and  $\Gamma$ -fit method are in a good agreement

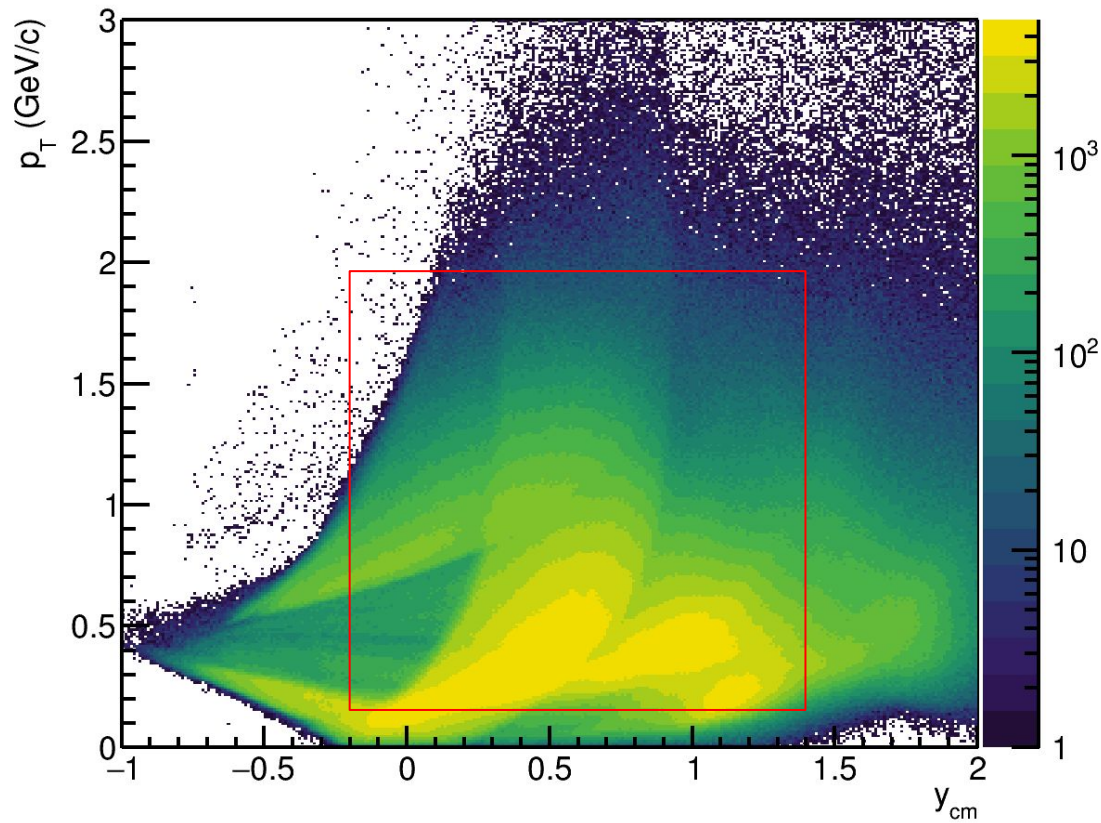


# Particle identification



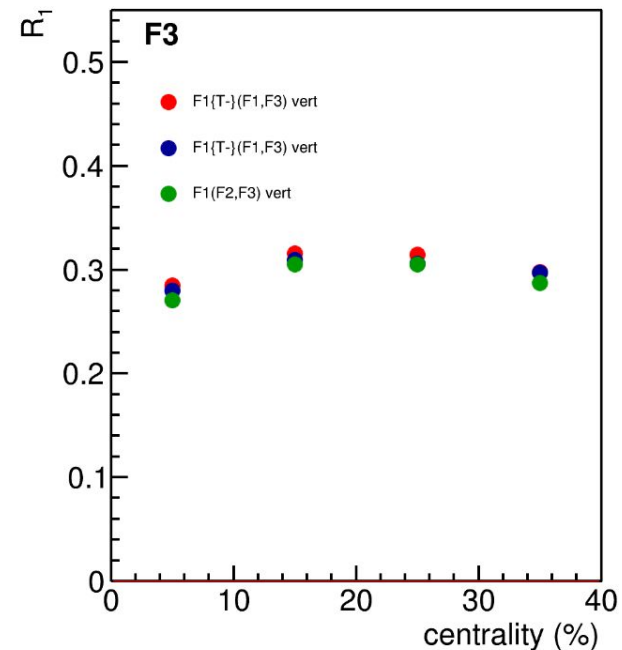
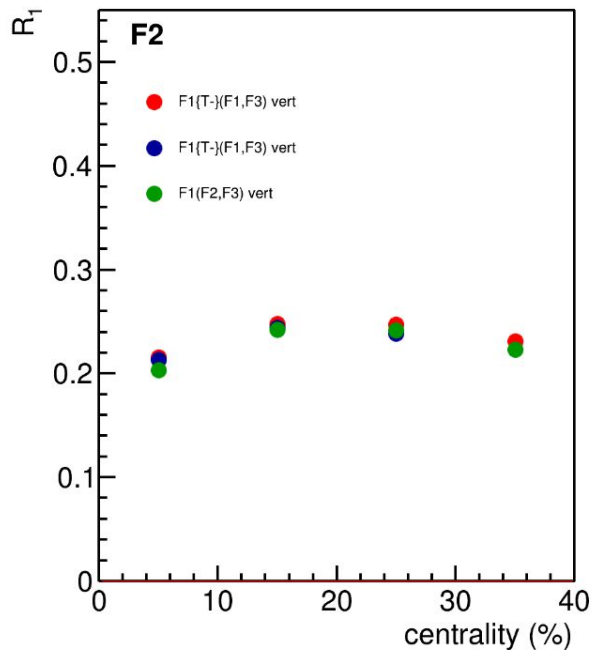
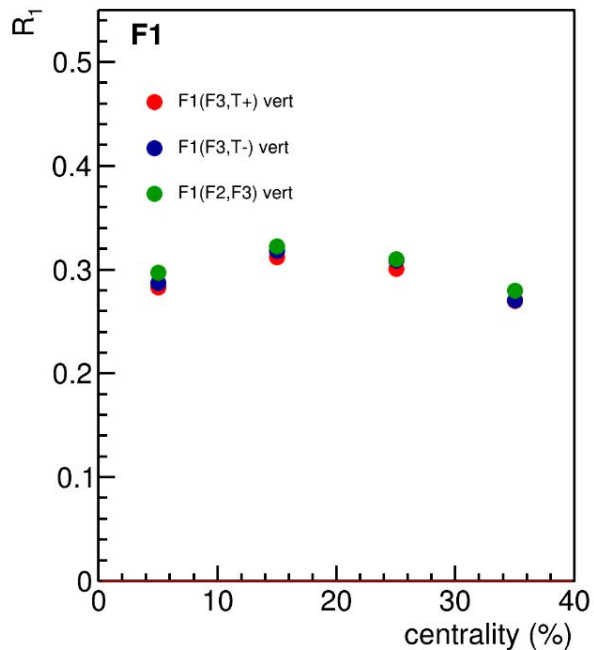
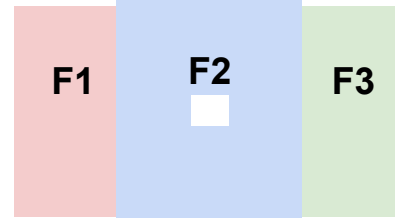


# Combined Proton $p_T$ - $y$ acceptance



Data is corrected for  $p_T$ - $y$  acceptance

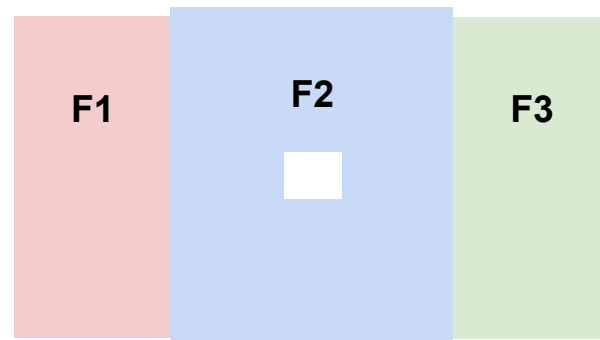
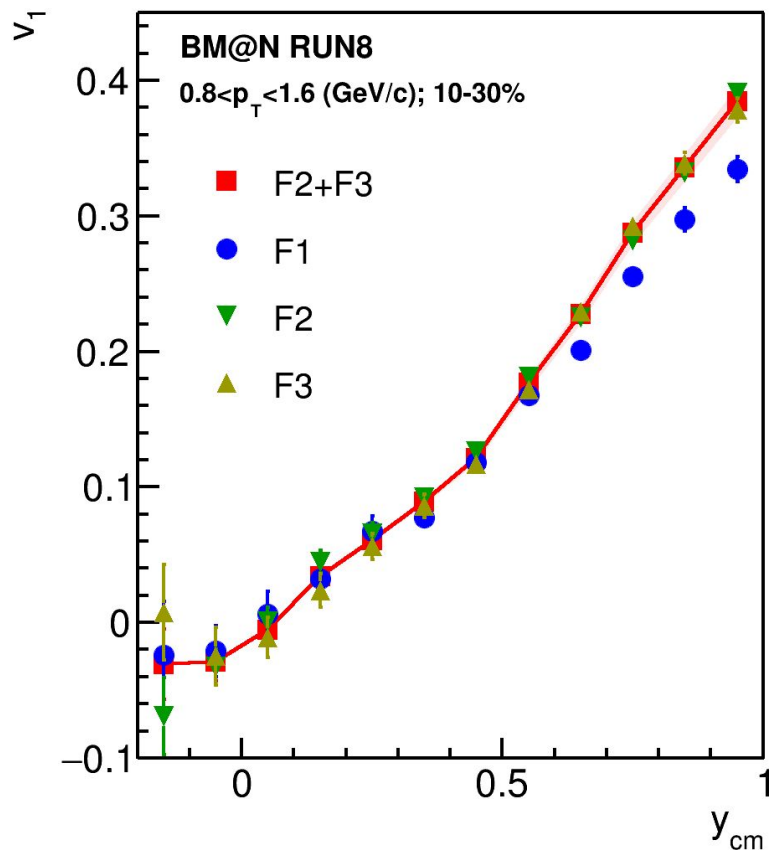
# DATA: $R_1$ in Xe+Cs(I) collisions



All the estimations for symmetry plane resolutions are in a good agreement

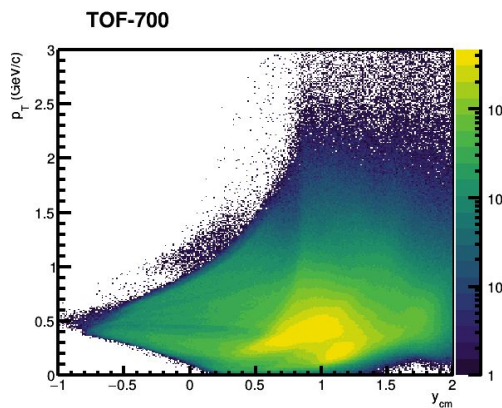
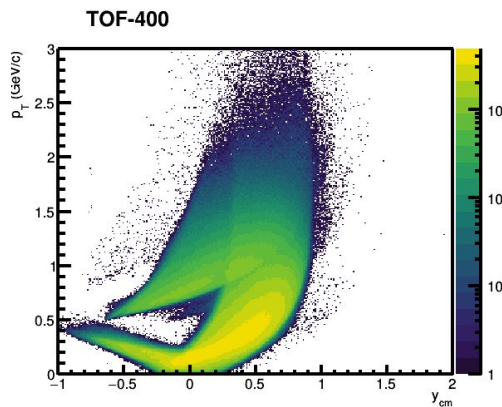
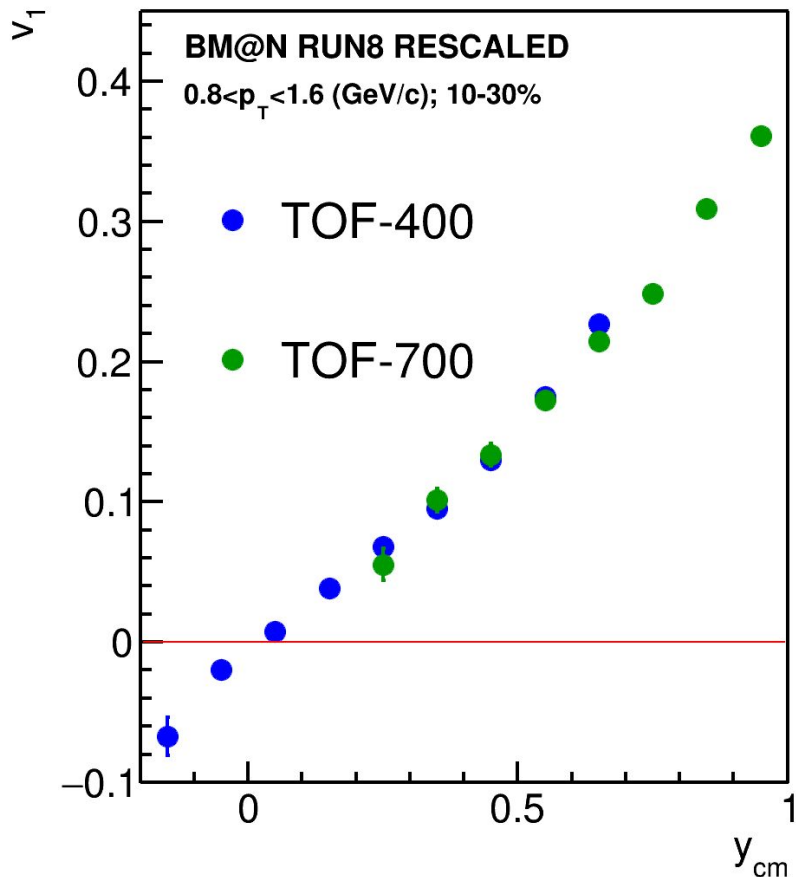


# Systematics due to symmetry plane estimation (non-flow)



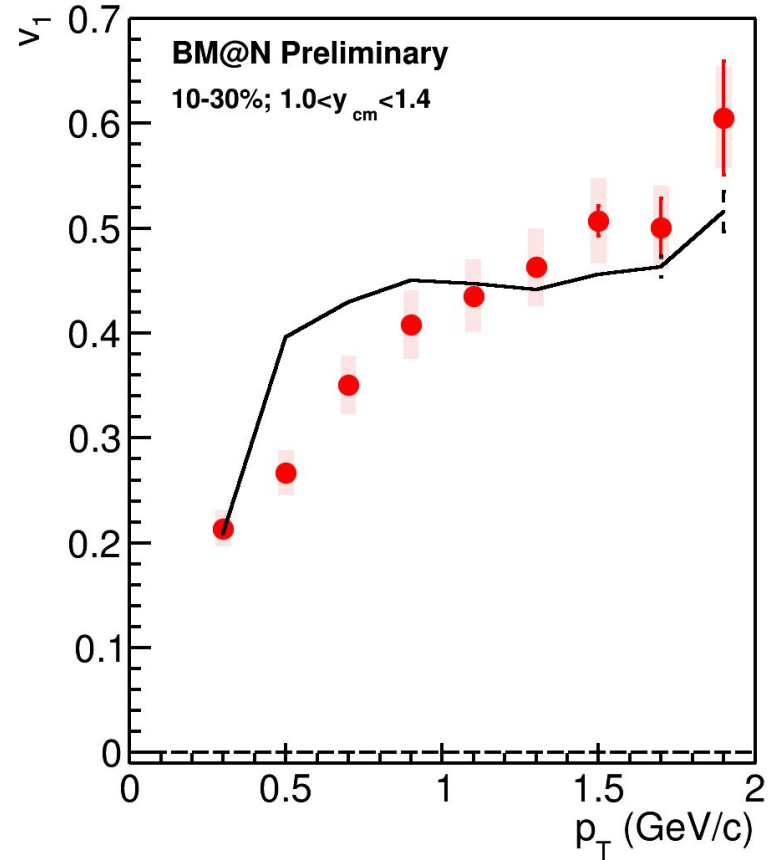
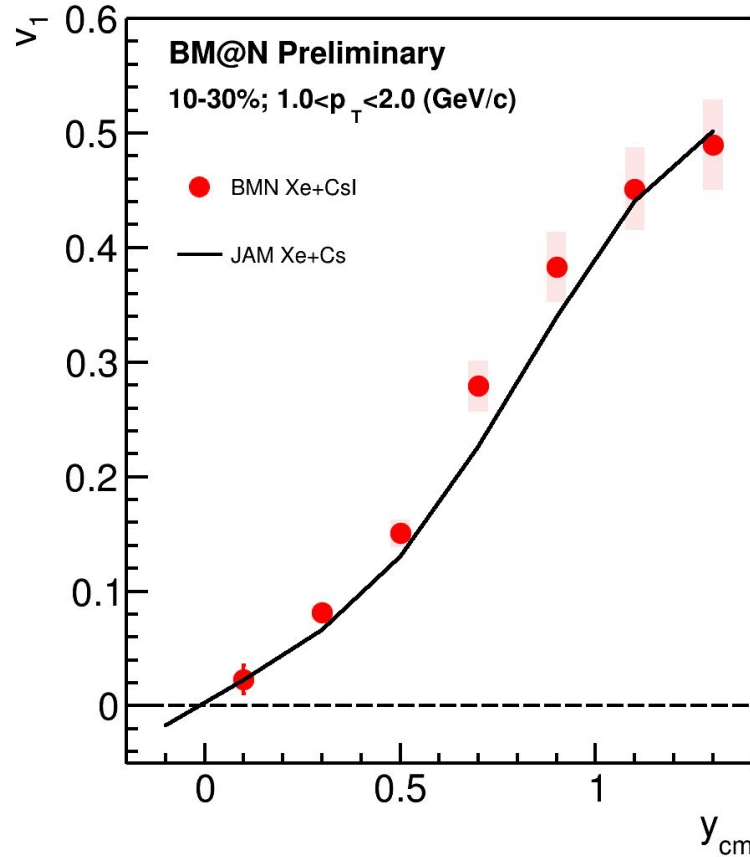
The systematics is below 3%

# Comparison of the TOF performances



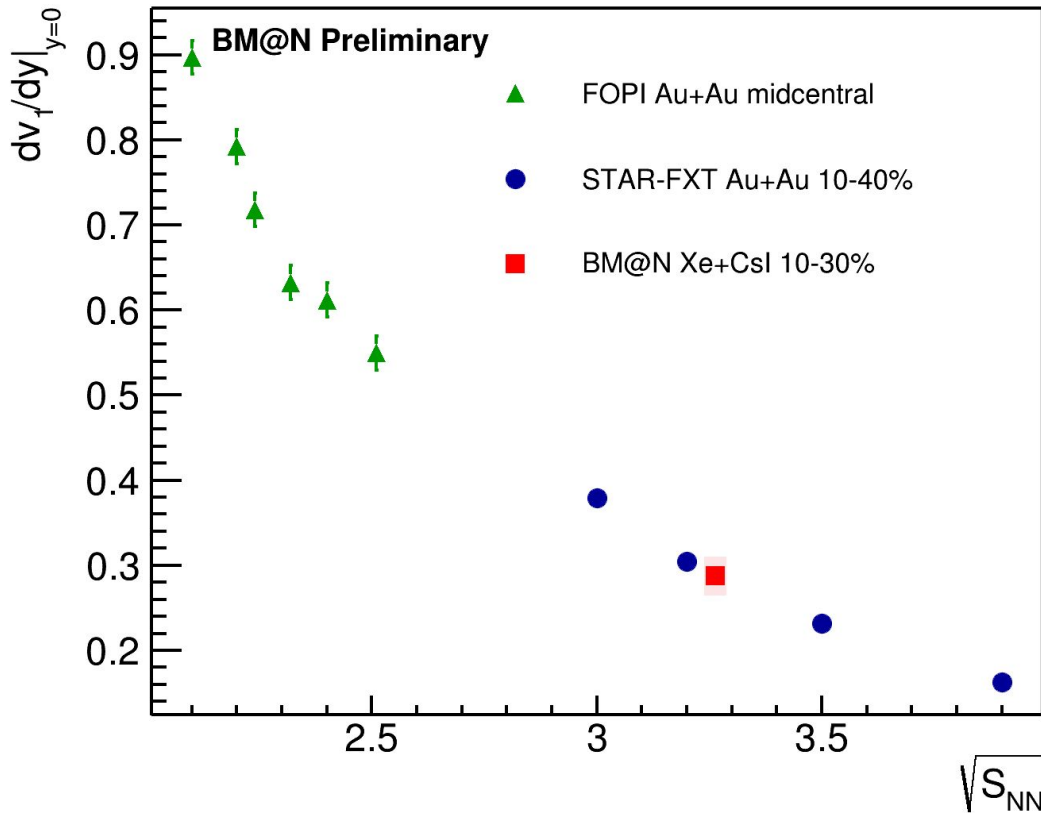
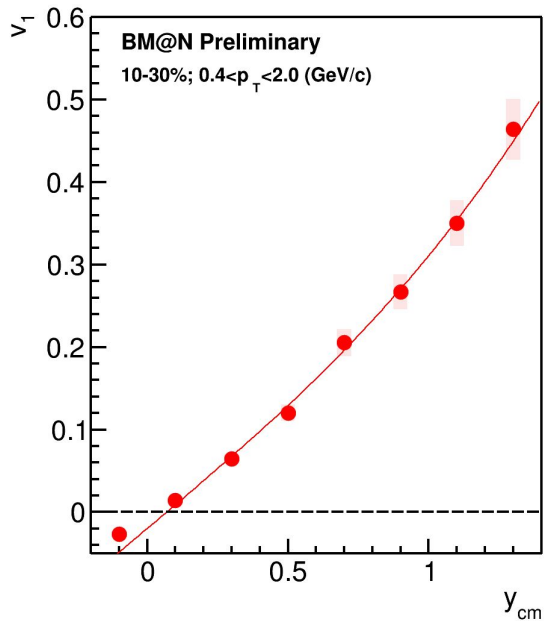
The results from TOF-400 and TOF-700 are in a good agreement

# $v_1$ as a function of $p_T$ and $y$



JAM model describes  $v_1(y)$  well

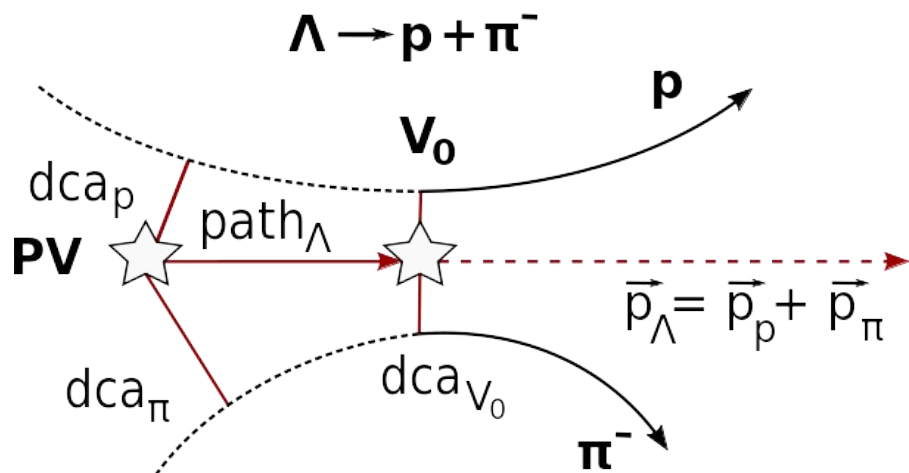
# $dv_1/dy|_{y=0}$ vs collision energy



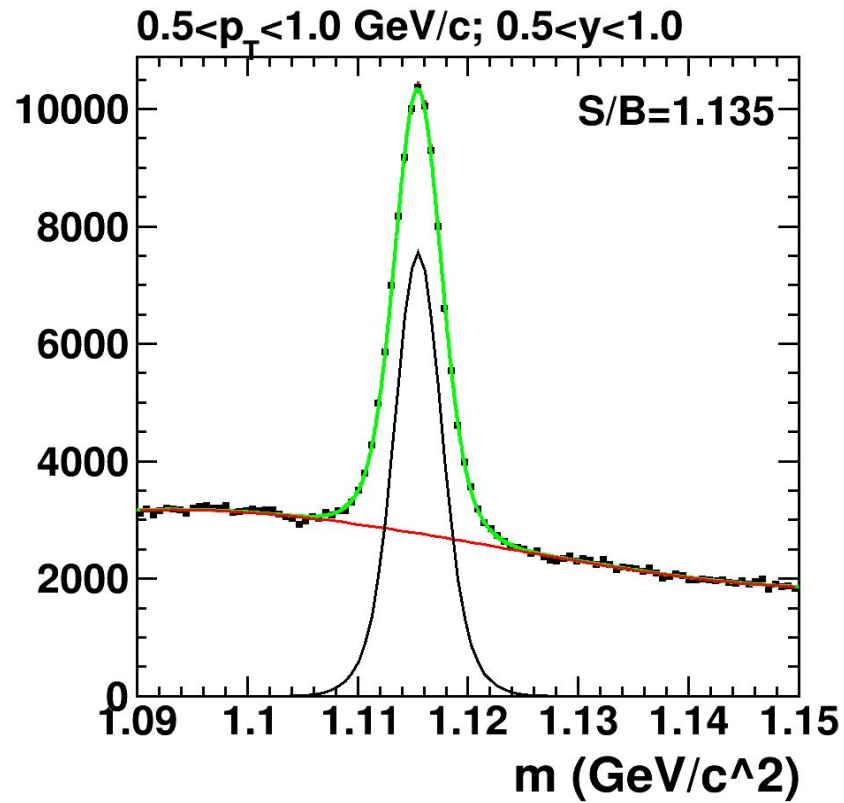
$dv_1/dy$  is in a good agreement with the world data

# $\Lambda$ -hyperon reconstruction

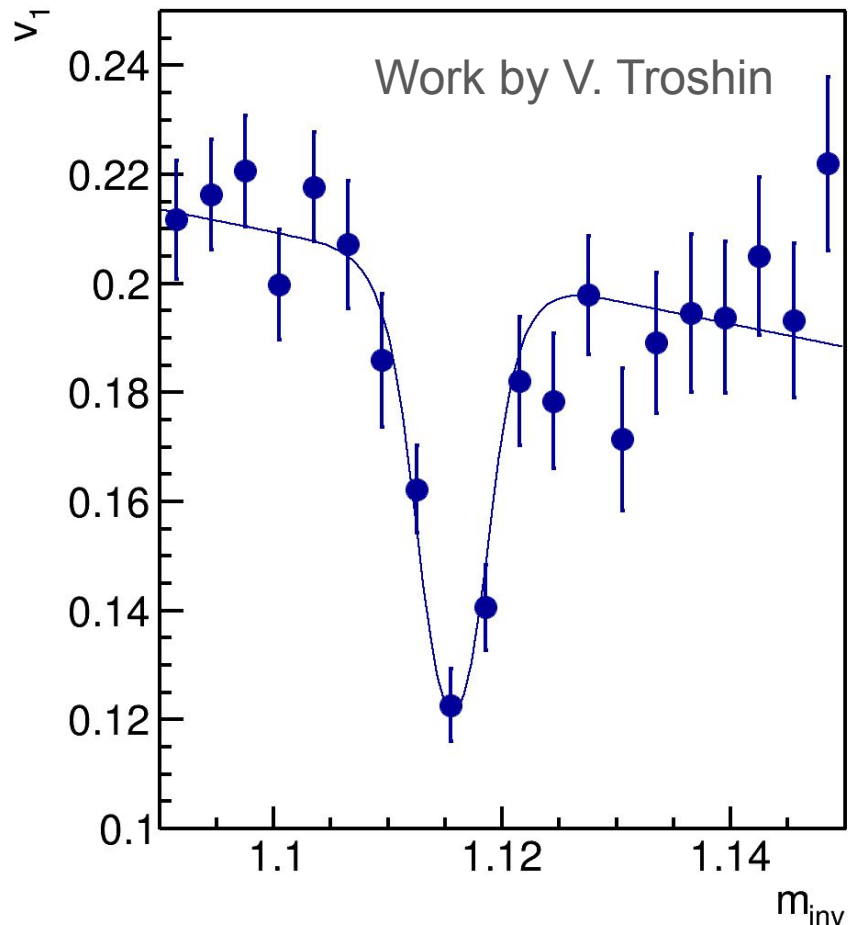
Work by V. Troshin



$\Lambda$ -hyperon reconstruction is carried out using the KFParticle package tested in STAR, ALICE, NA61/SHINE and CBM



# $v_1$ of $\Lambda$ -hyperons with invariant mass fit method



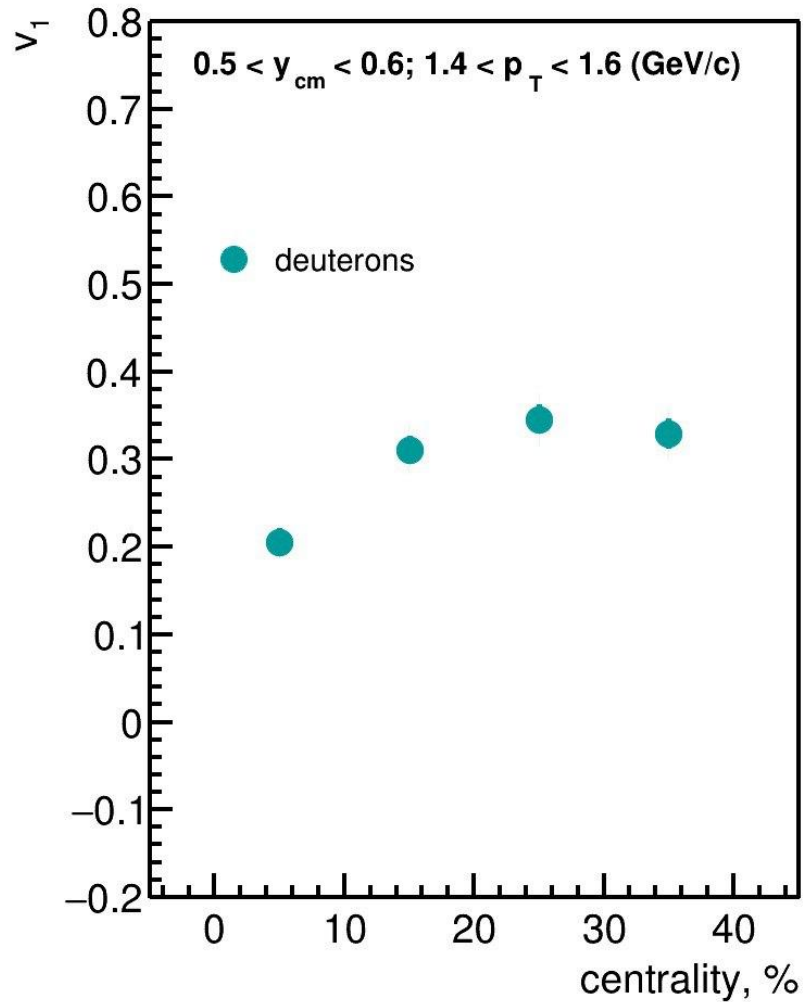
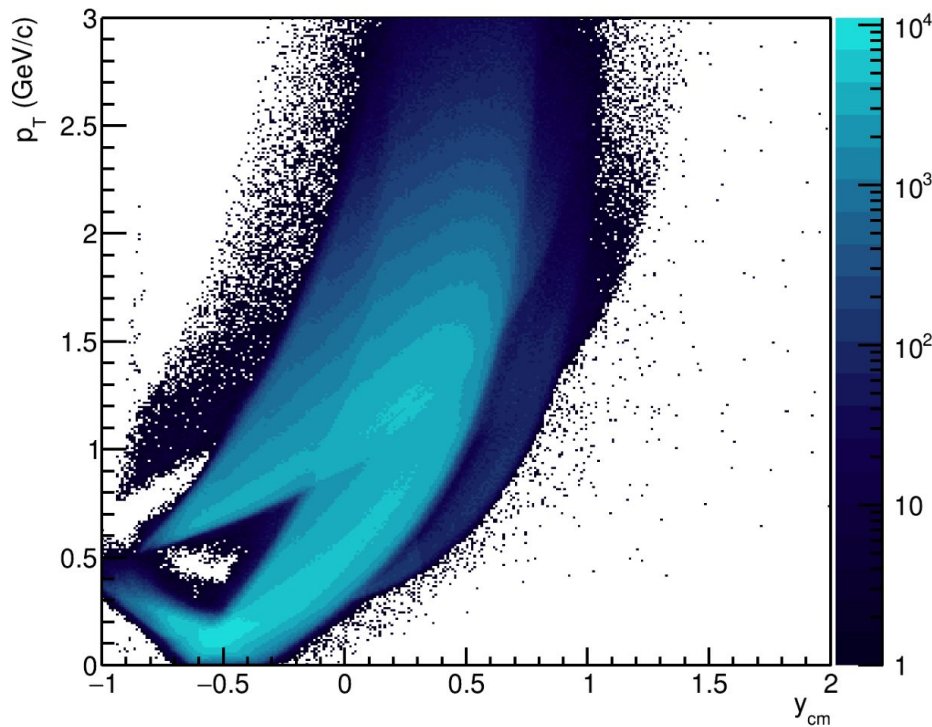
Directed flow for  $\Lambda$ -candidates is measured as a function of  $m_{inv}$ . Then  $v_1(m_{inv})$  is fitted with a function:

$$v_1^{S+B} = v_1^S \frac{N^S}{N^S + N^B} + v_1^B \frac{N^B}{N^S + N^B}$$

# Directed flow of deuterons

Work by I. Zhavoronkova

Combined



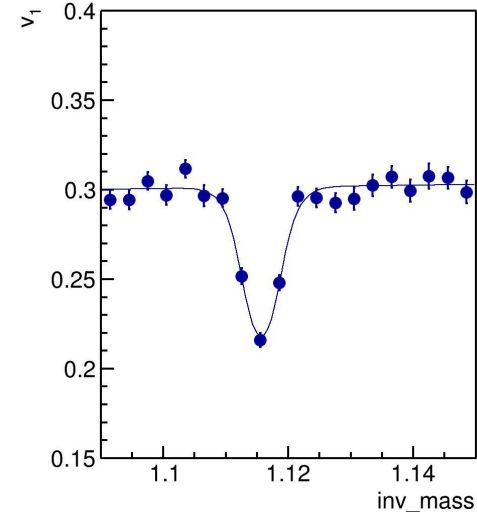
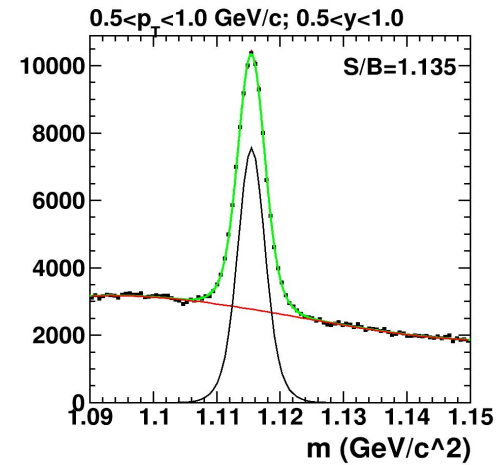
# Summary

- Directed flow of protons is measured multidifferentially as a function of  $p_T$ ,  $y$  and centrality
- The JAM model describes the  $v_1(y)$  reasonably well in high transverse momentum region
- The directed flow slope at midrapidity  $dv_1/dy|_{y=0}$  was extracted
- The results for directed flow slope  $dv_1/dy$  of protons are in a good agreement with the world data

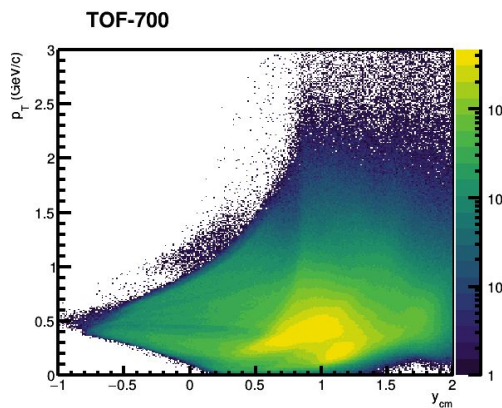
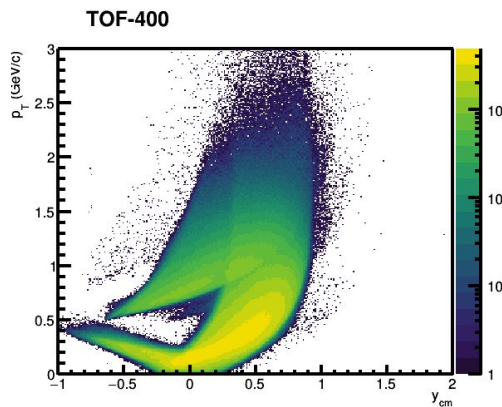
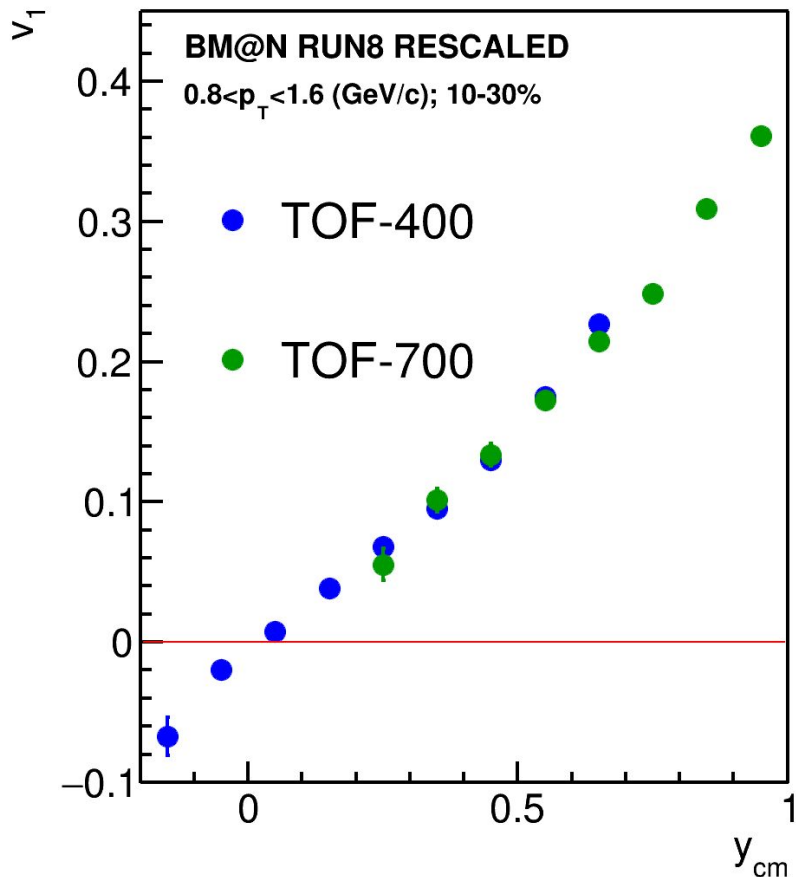


# Outlook

- 2025-2026 we expect the Beam-Energy scan program (2A, 3A, 4A GeV)
- The results for higher-harmonics flow is in the process of analysis
- The analysis for  $\Lambda v_1$  is undergoing
- Started the analysis for d flow

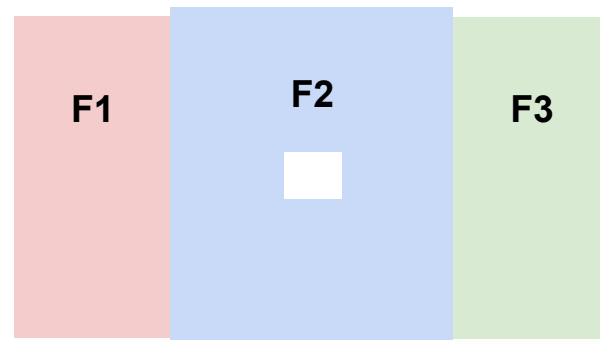
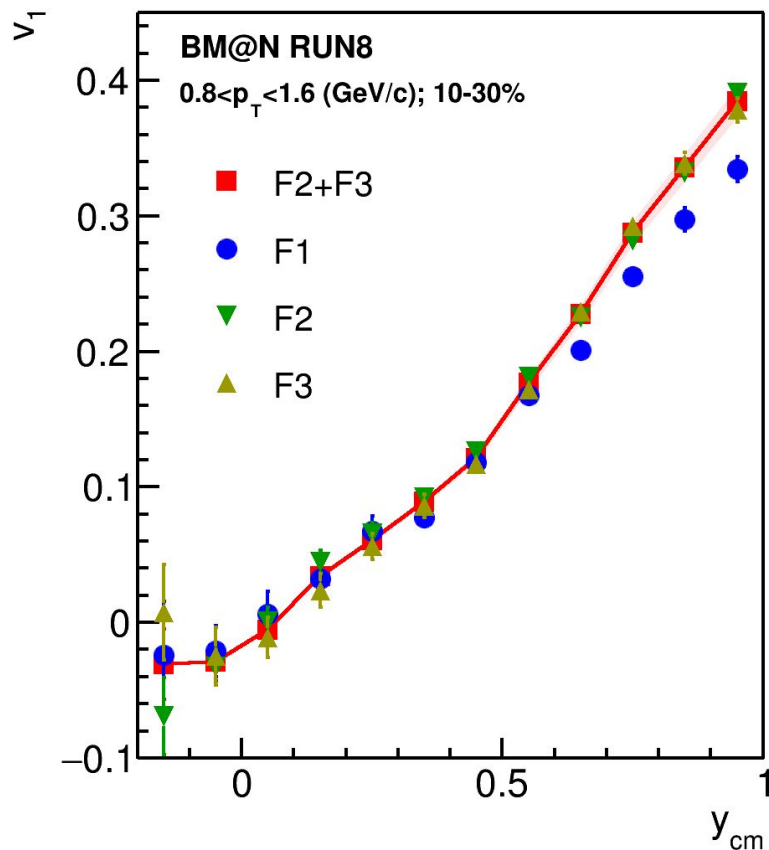


# Comparison of the TOF performances



The results from TOF-400 and TOF-700 are in a good agreement

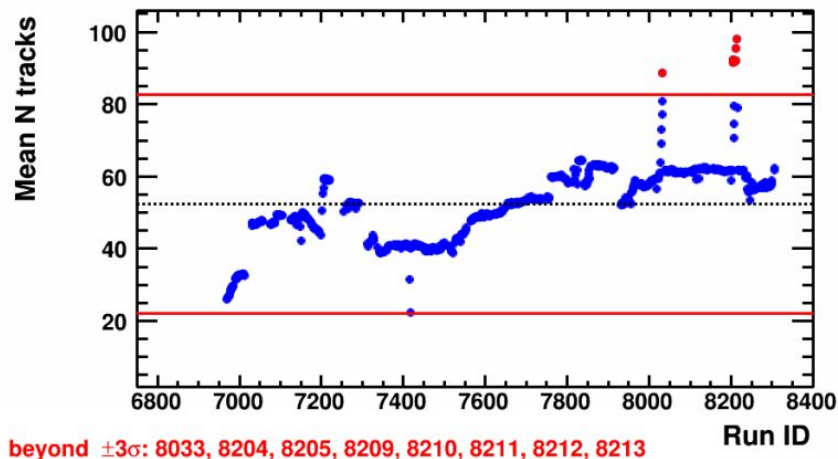
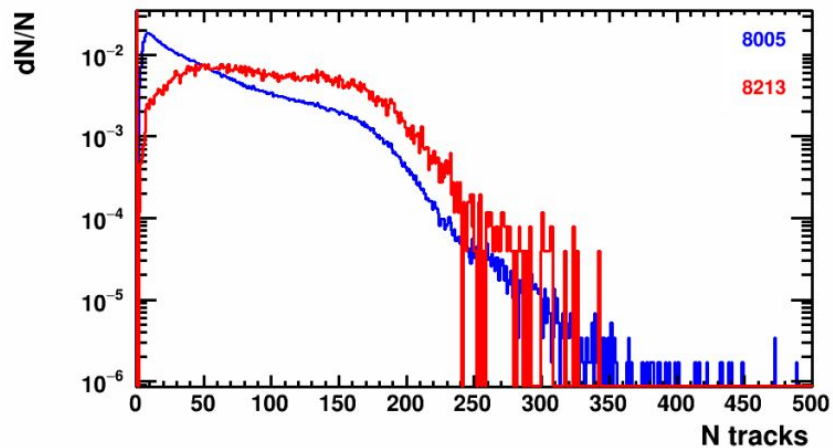
# Systematics due to symmetry plane estimation (non-flow)



The systematics is below 3%

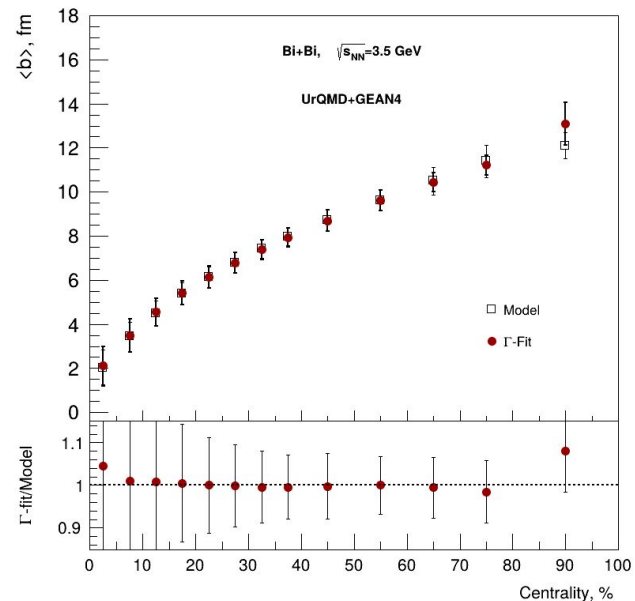
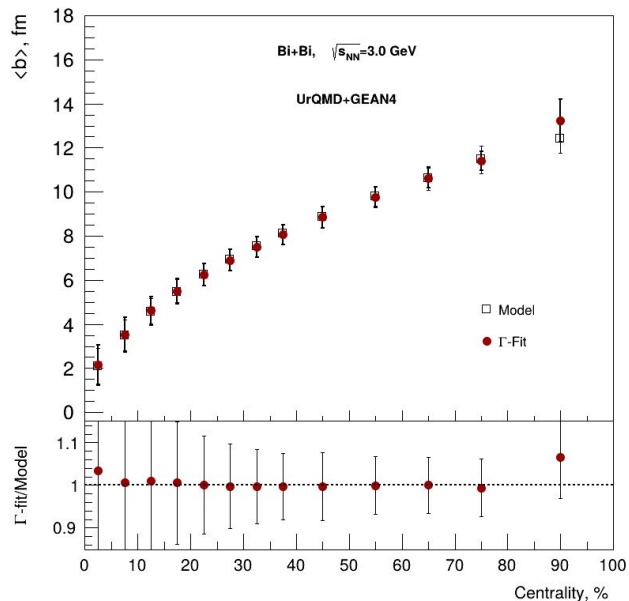
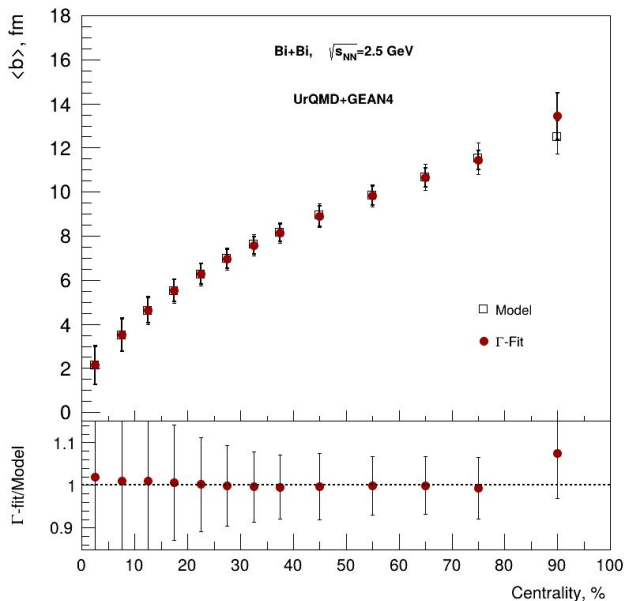
# Backup

# Quality assurance for the recent data



The preliminary list of bad runs based on QA study [18M events] RunId: 6968, 6970, 6972, 6973, 6975, 6976, 6977, 6978, 6979, 6980, 6981, 6982, 6983, 6984, 7313, 7326, 7415, 7417, 7435, 7517, 7520, 7537, 7538, 7542, 7543, 7545, 7546, 7547, 7573, 7575, 7657, 7659, 7679, 7681, 7843, 7847, 7848, 7850, 7851, 7852, 7853, 7855, 7856, 7857, 7858, 7859, 7865, 7868, 7869, 7907, 7932, 7933, 7935, 7937, 7954, 7955, 8018, 8031, 8032, 8033, 8115, 8121, 8167, 8201, 8204, 8205, 8208, 8209, 8210, 8211, 8212, 8213, 8215, 8289.

# Centrality determination: $\langle b \rangle$ vs Centrality



Cuts on tracks:

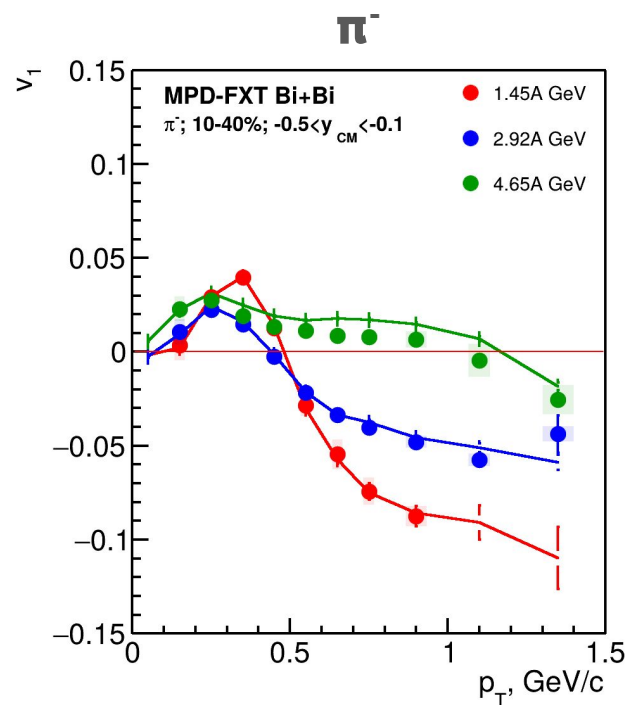
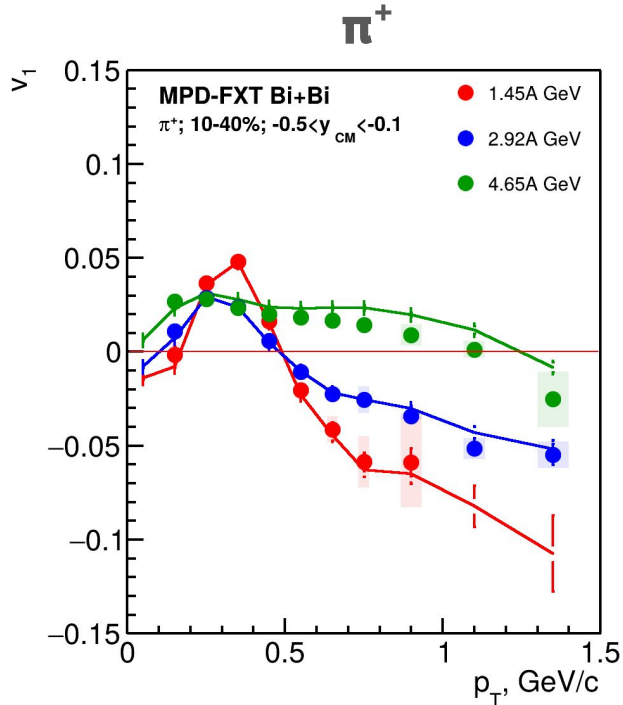
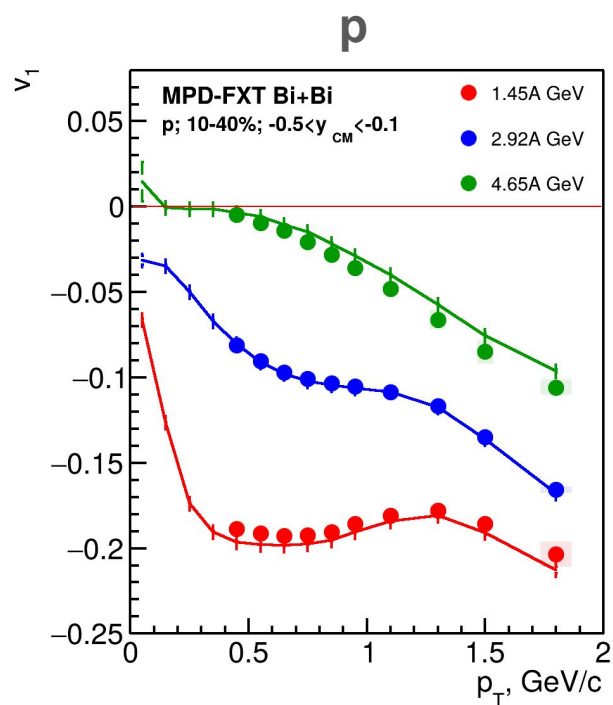
- $N_{\text{hits}} > 16$
- $0 < \eta < 2$

Good agreement between fit and data

Multiplicity-based centrality determination using inverse Bayes was used

# Results: $v_1(p_T)$

Systematics: xx, yy, F1, F2, F3

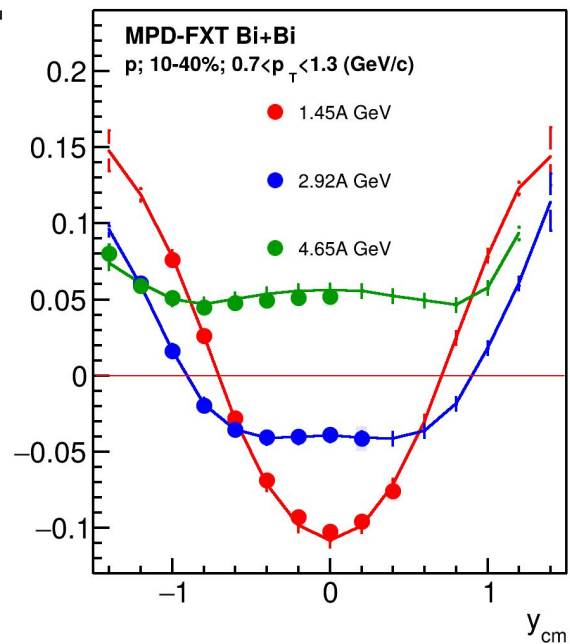


Good agreement with MC data

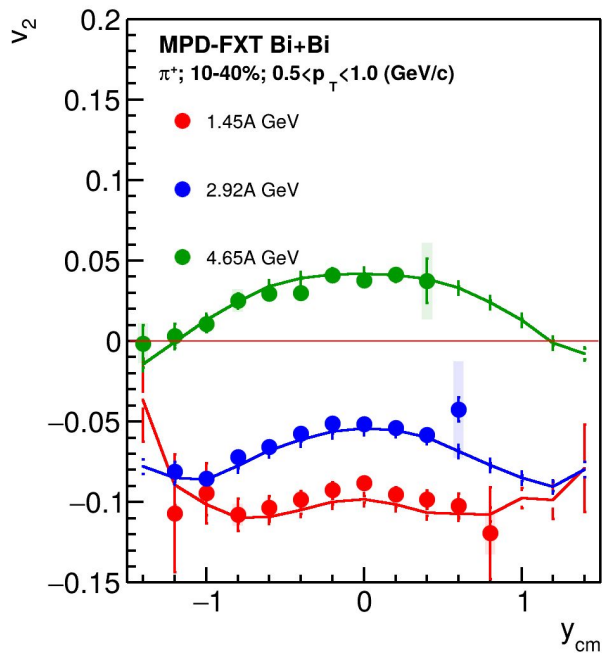
# Results: $v_2(y)$

Systematics: xxx, xyy

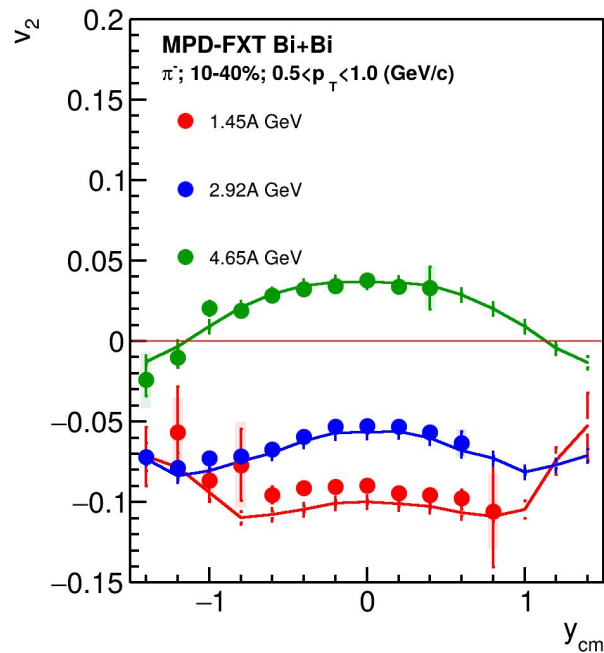
**p**



**$\pi^+$**



**$\pi^-$**



Good agreement with MC data



# The Bayesian inversion method ( $\Gamma$ -fit)

Relation between multiplicity  $N_{ch}$  and impact parameter  $b$  is defined by the fluctuation kernel:

$$P(N_{ch}|c_b) = \frac{1}{\Gamma(k(c_b))\theta^k} N_{ch}^{k(c_b)-1} e^{-N_{ch}/\theta} \quad \frac{\sigma^2}{\langle N_{ch} \rangle} = \theta \approx const, k = \frac{\langle N_{ch} \rangle}{\theta}$$

$$c_b = \int_0^b P(b') db' - \text{centrality based on impact parameter}$$

Mean multiplicity as a function of  $c_b$  can be defined as follows:

$$\langle N_{ch} \rangle = N_{knee} \exp\left(\sum_{j=1}^3 a_j c_b^j\right) \quad N_{knee}, \theta, a_j - 5 \text{ parameters}$$

Fit function for  $N_{ch}$  distribution:

$b$ -distribution for a given  $N_{ch}$  range:

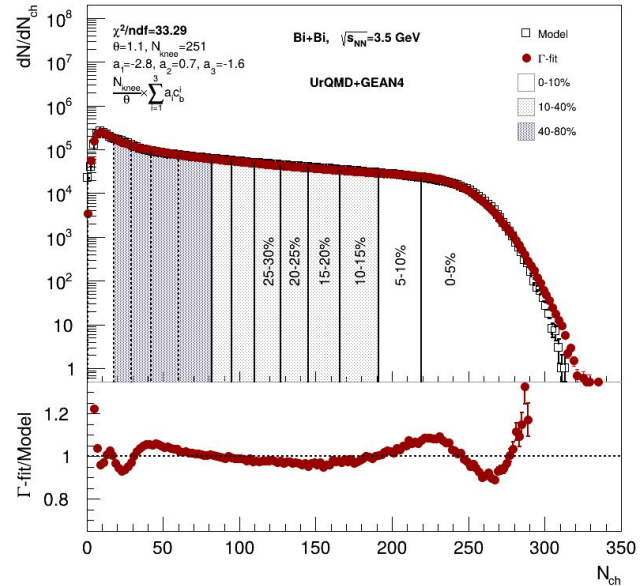
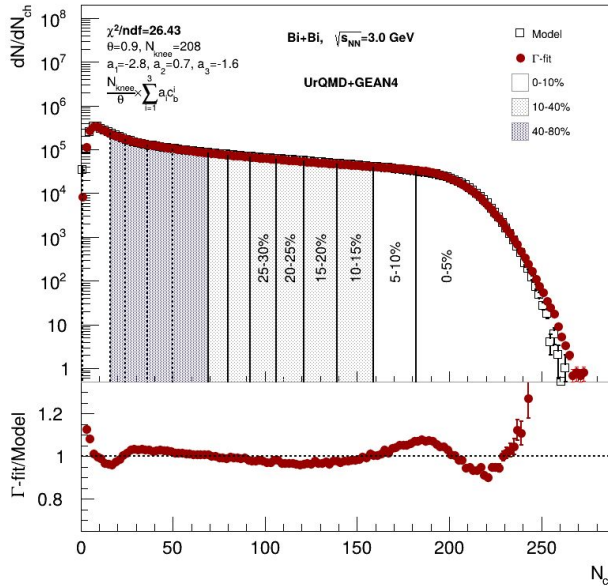
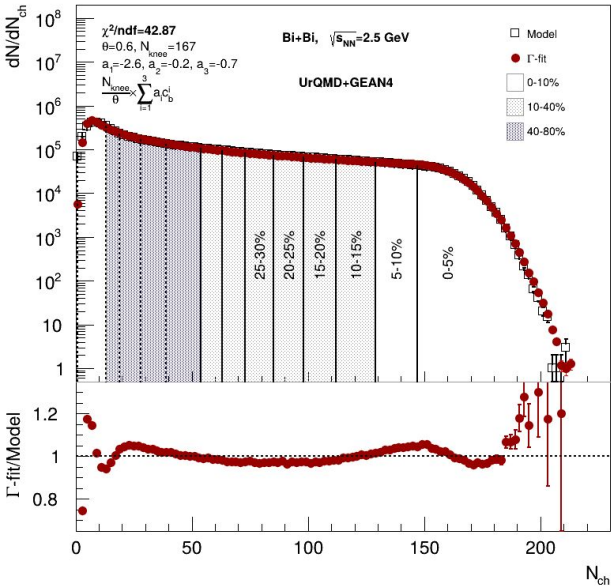
$$P(N_{ch}) = \int_0^1 P(N_{ch}|c_b) dc_b \quad P(b|n_1 < N_{ch} < n_2) = P(b) \frac{\int_{n_1}^{n_2} P(N_{ch}|b) dN_{ch}}{\int_{n_1}^{n_2} P(N_{ch}) dN_{ch}}$$

**2 main steps of the method:**

Fit experimental (model) distribution with  $P(N)$

Construct  $P(b|E)$  using Bayes' theorem:  
 $P(b|N) = P(b)P(N|b)/P(N)$

# Centrality determination: multiplicity fit



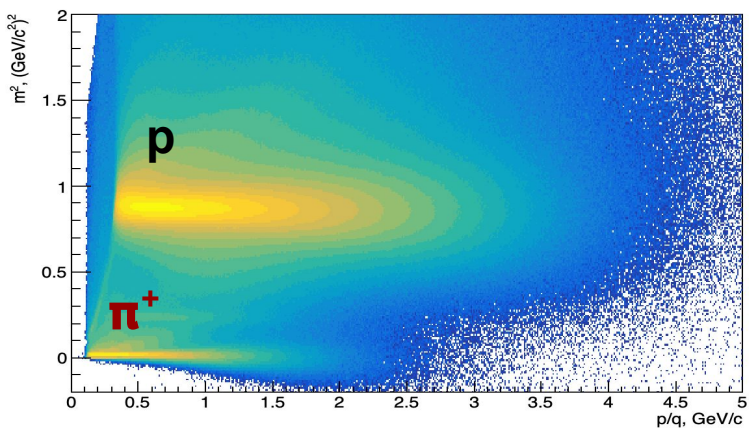
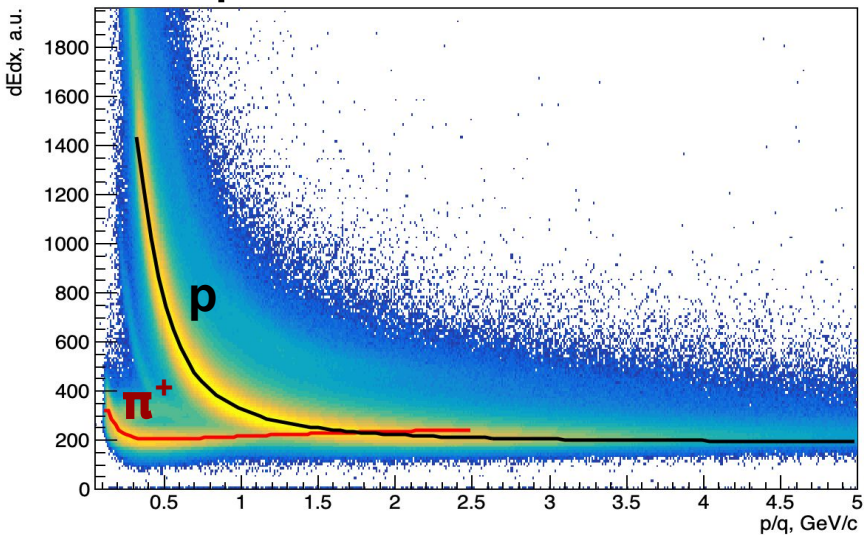
Cuts on tracks:

- $N_{hits} > 16$
- $0 < \eta < 2$

Good agreement between fit and data

Multiplicity-based centrality determination ( $\Gamma$ -fit) was used

# PID procedure



Fit  $dE/dx$  distributions with Bethe-Bloch parametrization:

$$f(\beta\gamma) = \frac{p_1}{\beta^{p_4}} \left( p_2 - \beta^{p_4} - \ln \left( p_3 + \frac{1}{(\beta\gamma)^{p_5}} \right) \right)$$

$$\beta^2 = \frac{p^2}{m^2 + p^2}, \beta\gamma = \frac{p}{m} \quad p_i - \text{fit parameters}$$

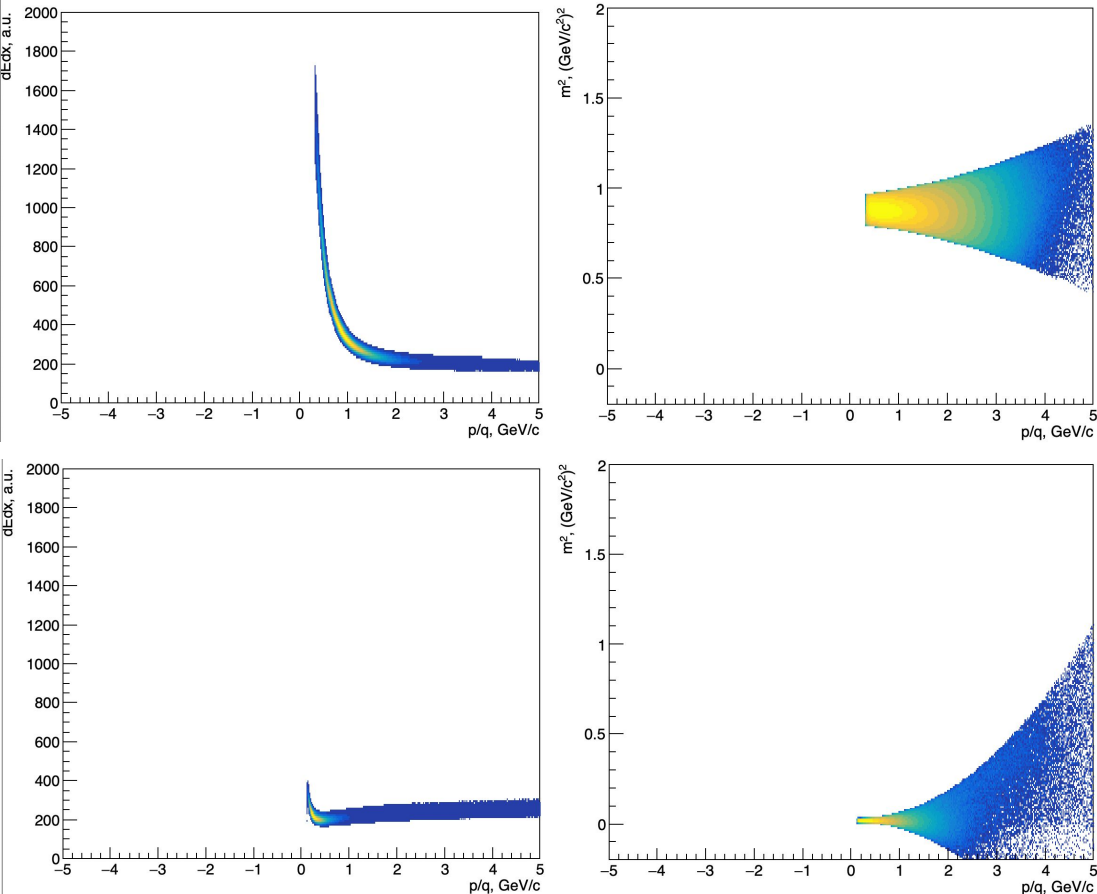
Fit  $(dE/dx - f(\beta\gamma))/f(\beta\gamma)$  with gaus in the slices of  $p/q$  and get  $\sigma_p(dE/dx)$

Fit  $m^2$  with gaus in the slices of  $p/q$  and get  $\sigma_p(m^2)$

**$(dE/dx, m) \rightarrow (x, y)$  coordinates for PID:**

$$x_p = \frac{(dE/dx)^{meas} - (dE/dx)_p^{fit}}{(dE/dx)_p^{fit} \sigma_p^{dE/dx}}, \quad y_p = \frac{m^2 - m_p^2}{\sigma_p^{m^2}}$$

# PID procedure: Results



$$x_p = \frac{(dE/dx)^{meas} - (dE/dx)_p^{fit}}{(dE/dx)_p^{fit} \sigma_p^{dE/dx}}$$

$$y_p = \frac{m^2 - m_p^2}{\sigma_p^{m^2}}$$

Protons:

$$\sqrt{x_p^2 + y_p^2} < 2, \sqrt{x_\pi^2 + y_\pi^2} > 3$$

Pions ( $\pi^+$ ):

$$\sqrt{x_\pi^2 + y_\pi^2} < 2, \sqrt{x_p^2 + y_p^2} > 3$$

Pions ( $\pi^-$ ):

charge < 0

# (y-pt) distribution, efficiency and $\delta p_T$ (protons)

$$\text{eff} = \frac{\frac{dN}{dydp_T}(\text{reco})}{\frac{dN}{dydp_T}(\text{sim})}$$

$$\Delta p_T = \frac{|p_T^{\text{reco}} - p_T^{\text{mc}}|}{p_T^{\text{mc}}}$$

**Bi+Bi  $\sqrt{s_{NN}}=2.5$  GeV**

Cuts for reco tracks:

- Nhits>27
- DCA< 1 cm
- PID (TPC+TOF)
- Primary (DCA<1 cm)

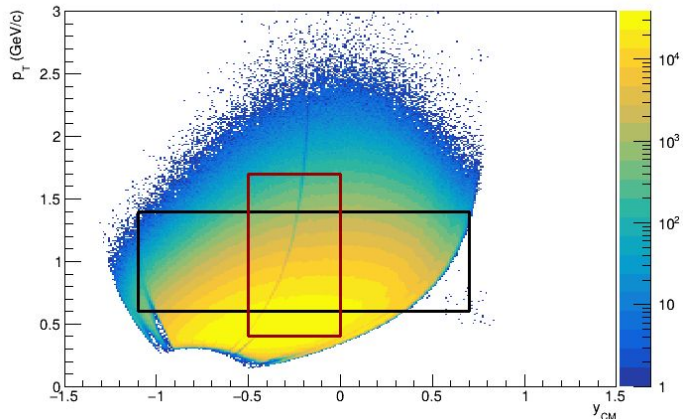
Cuts for sim particles:

- PID (pdg code)
- Primary (motherId)

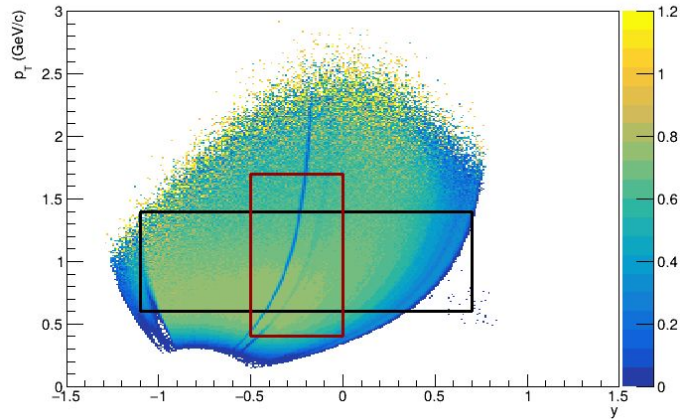
**Black box:** acceptance window for  $v_n(y)$

**Red box:** acceptance window for  $v_n(p_T)$

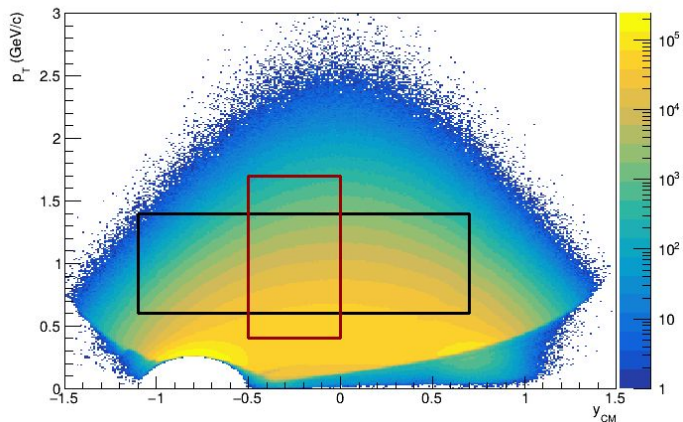
Reconstructed protons Ycm-pT



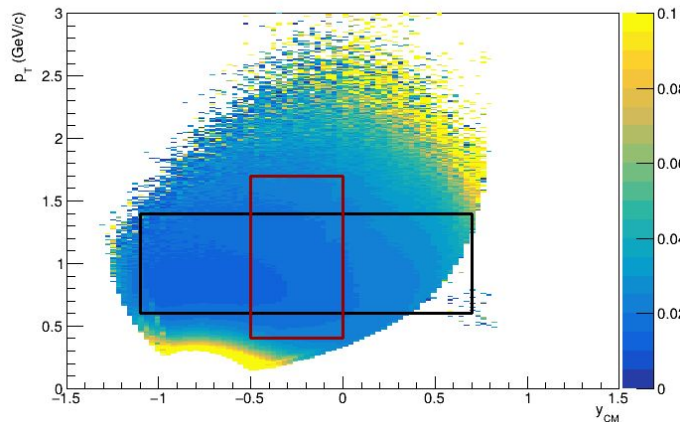
Efficiency (Y-pT) of primary protons



Simulated protons Ycm-pT



Pt-resolution for reconstructed protons in Ycm-pT plane



# Flow vectors

From momentum of each measured particle define a  $u_n$ -vector in transverse plane:

$$u_n = e^{in\phi}$$

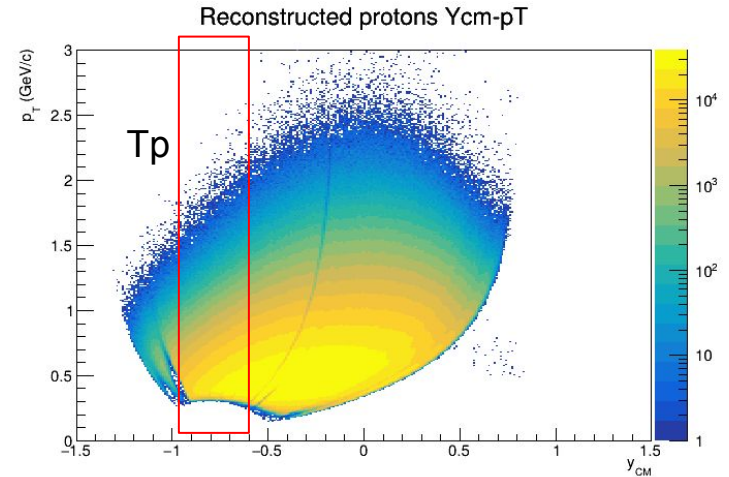
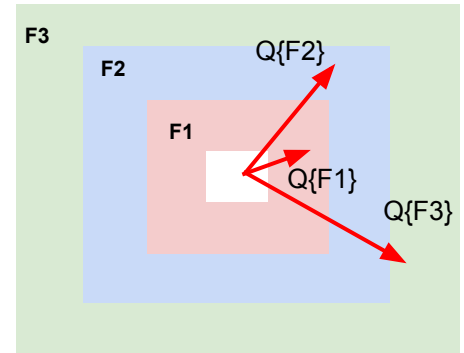
where  $\phi$  is the azimuthal angle

Sum over a group of  $u_n$ -vectors in one event forms  $Q_n$ -vector:

$$Q_n = \frac{\sum_{k=1}^N w_n^k u_n^k}{\sum_{k=1}^N w_n^k} = |Q_n| e^{in\Psi_n^{EP}}$$

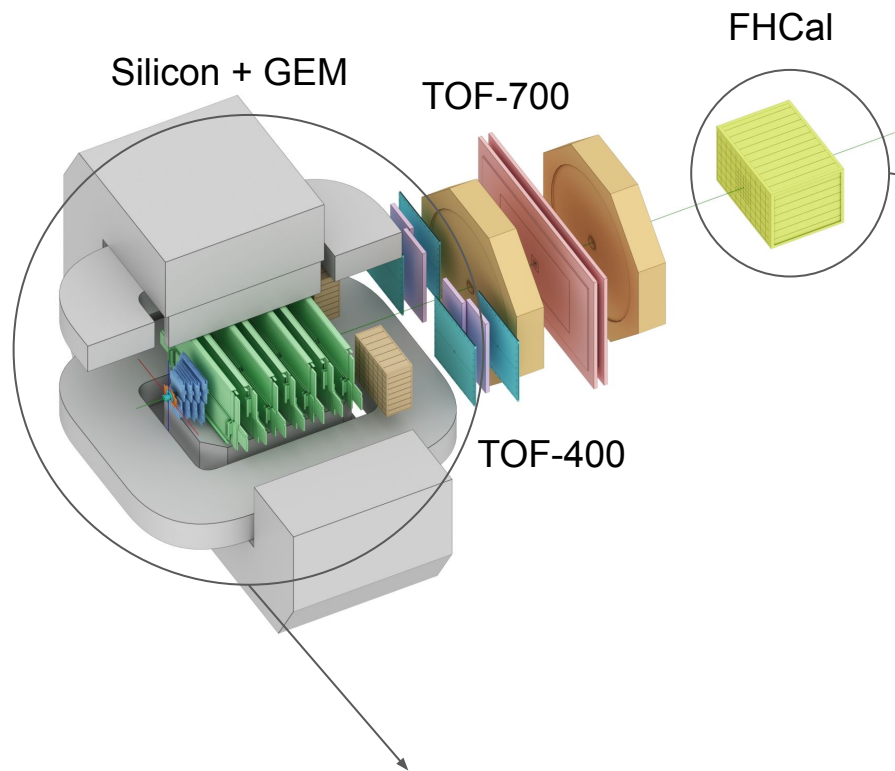
$\Psi_n^{EP}$  is the event plane angle

Modules of FHCAL divided into 3 groups

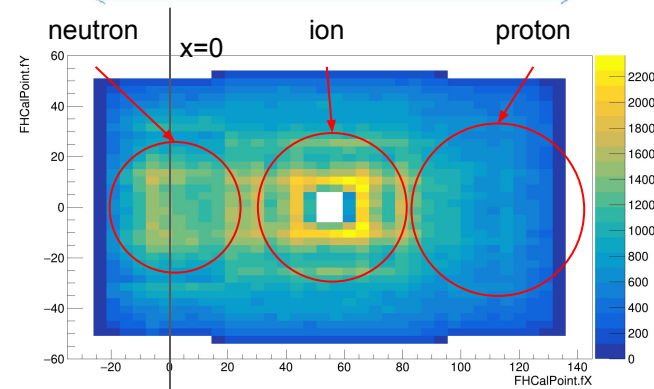
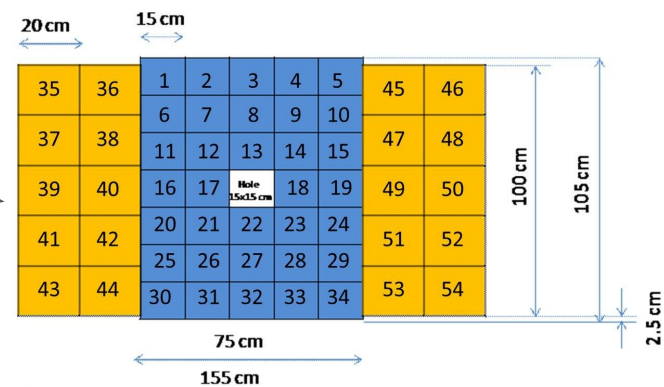


**Additional subevents from tracks not pointing at FHCAL:**  
**Tp:** p;  $-1.0 < y < -0.6$ ;

# The BM@N experiment (GEANT4 simulation for RUN8)

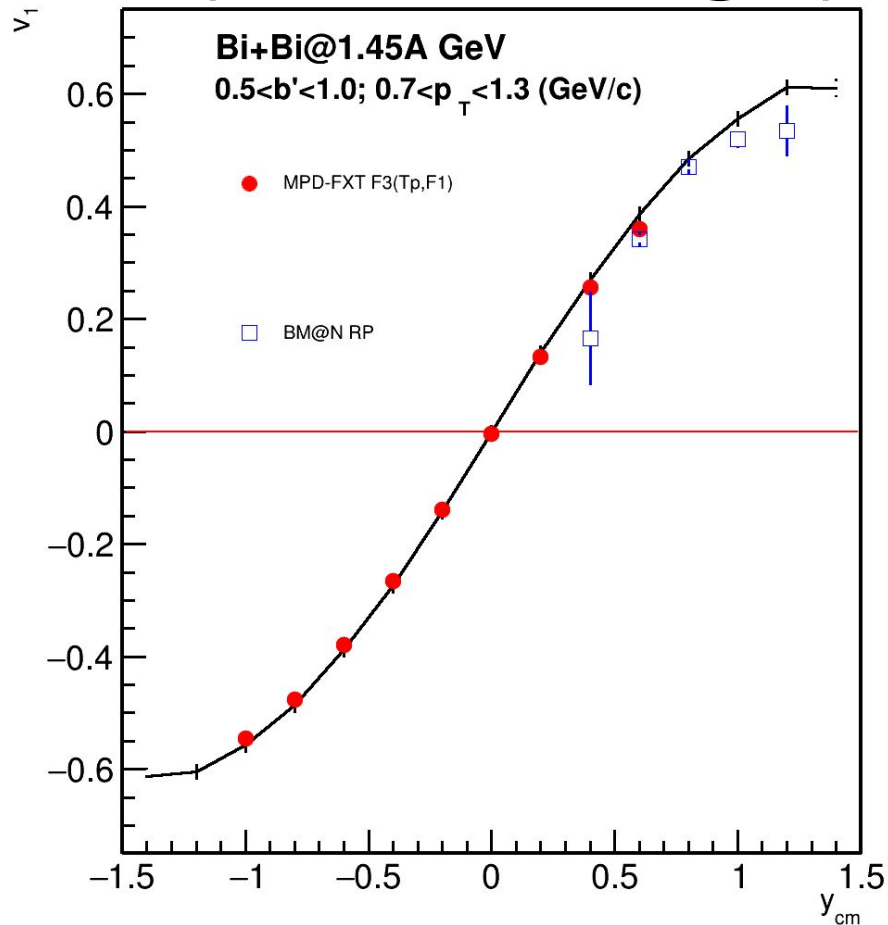


Square-like tracking system within the magnetic field deflecting particles along X-axis



Charge splitting on the surface of the FHCaI is observed due to magnetic field

# Comparison with BM@N performance



BM@N TOF system (TOF-400 and TOF-700) has poor midrapidity coverage at  $\sqrt{s_{NN}} = 2.5$  GeV

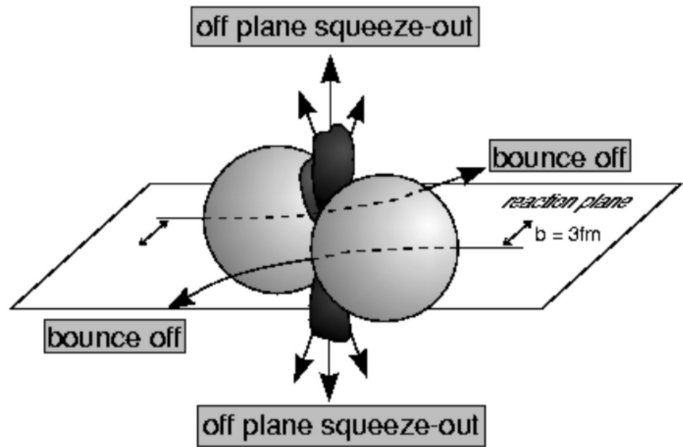
- One needs to check higher energies ( $\sqrt{s_{NN}} = 3, 3.5$  GeV)
- More statistics are required due to the effects of magnetic field in BM@N:
  - Only “yy” component of  $\langle uQ \rangle$  and  $\langle QQ \rangle$  correlation can be used

Despite the challenges, both MPD-FXT and BM@N can be used in  $v_n$  measurements:

- To widen rapidity coverage
- To perform a cross-check in the future



# Anisotropic flow & spectators



The azimuthal angle distribution is decomposed in a Fourier series relative to reaction plane angle:

$$\rho(\varphi - \Psi_{RP}) = \frac{1}{2\pi} \left( 1 + 2 \sum_{n=1}^{\infty} v_n \cos n(\varphi - \Psi_{RP}) \right)$$

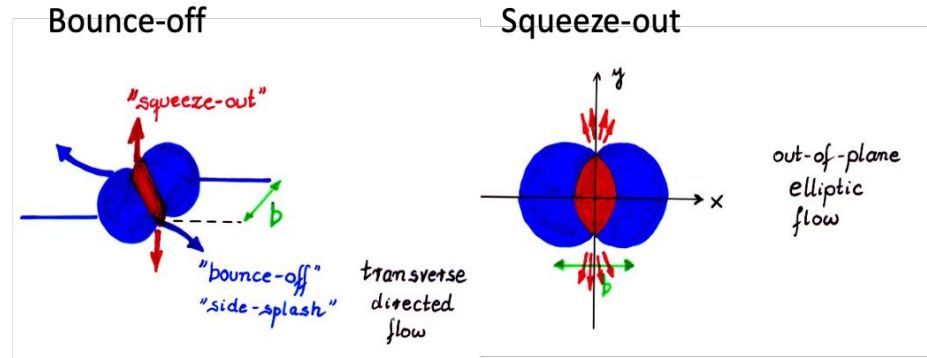
Anisotropic flow:

$$v_n = \langle \cos [n(\varphi - \Psi_{RP})] \rangle$$

$v_1$  - directed flow,  $v_2$  - elliptic flow

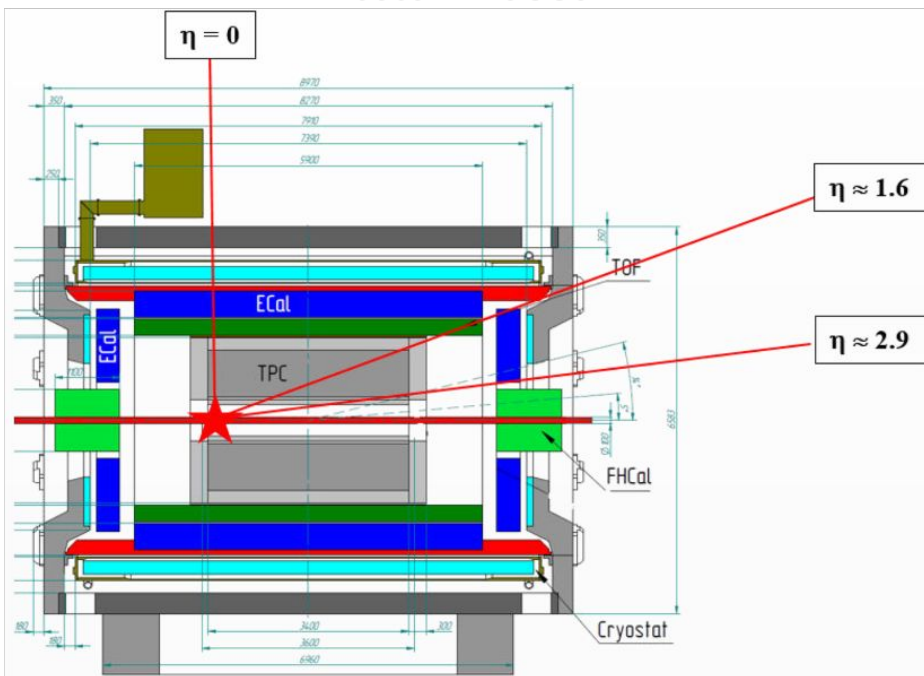
**Anisotropic flow is sensitive to:**

- **Compressibility of the created matter**  
 $(t_{exp} = R/c_s, c_s = c\sqrt{dp/d\varepsilon})$
- **Time of the interaction between overlap region and spectators**  
 $(t_{pass} = 2R/\gamma_{CM}\beta_{CM})$



# MPD in Fixed-Target Mode (FXT)

## MPD-FXT



- Model used: UrQMD mean-field
  - Bi+Bi,  $E_{\text{kin}} = 1.45$  AGeV ( $\sqrt{s_{\text{NN}}} = 2.5$  GeV)
  - Bi+Bi,  $E_{\text{kin}} = 2.92$  AGeV ( $\sqrt{s_{\text{NN}}} = 3.0$  GeV)
  - Bi+Bi,  $E_{\text{kin}} = 4.65$  AGeV ( $\sqrt{s_{\text{NN}}} = 3.5$  GeV)
- Point-like target at  $z = -115$  cm
- GEANT4 transport
- Multiplicity-based centrality determination
- PID using information from TPC and TOF
- Primary track selection:  $\text{DCA} < 1$  cm
- Track selection:
  - $N_{\text{hits}} > 27$  (protons),  $N_{\text{hits}} > 22$  (pions)

# Flow vectors

From momentum of each measured particle define a  $u_n$ -vector in transverse plane:

$$u_n = e^{in\phi}$$

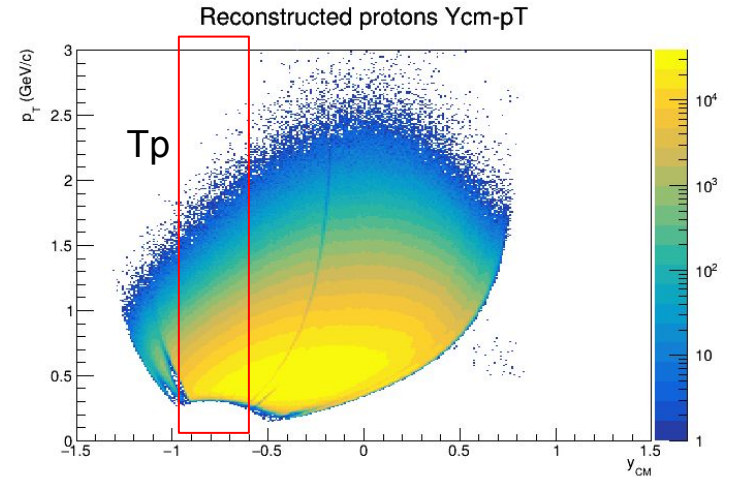
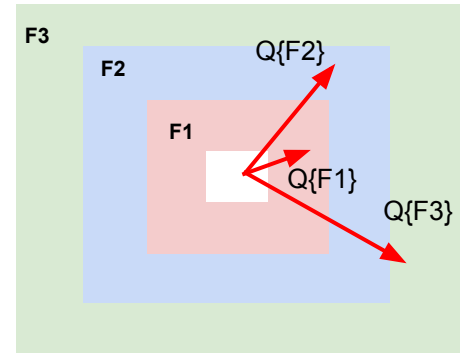
where  $\phi$  is the azimuthal angle

Sum over a group of  $u_n$ -vectors in one event forms  $Q_n$ -vector:

$$Q_n = \frac{\sum_{k=1}^N w_n^k u_n^k}{\sum_{k=1}^N w_n^k} = |Q_n| e^{in\Psi_n^{EP}}$$

$\Psi_n^{EP}$  is the event plane angle

Modules of FHCAL divided into 3 groups

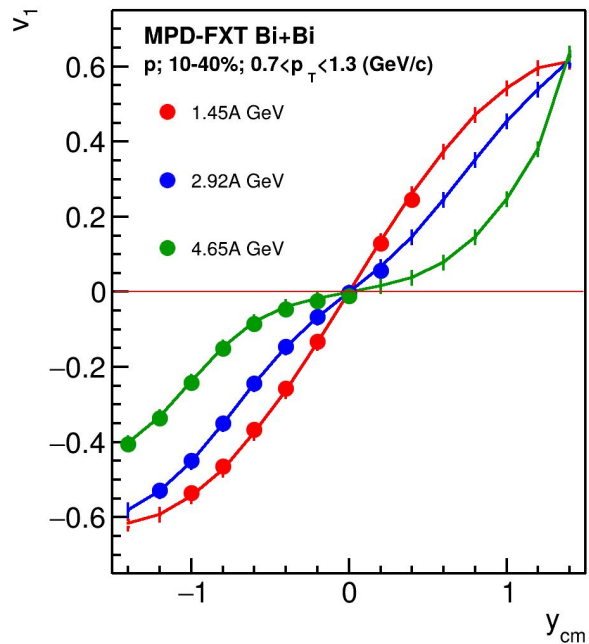


**Additional subevents from tracks not pointing at FHCAL:**  
**Tp: p;  $-1.0 < y < -0.6$ ;**

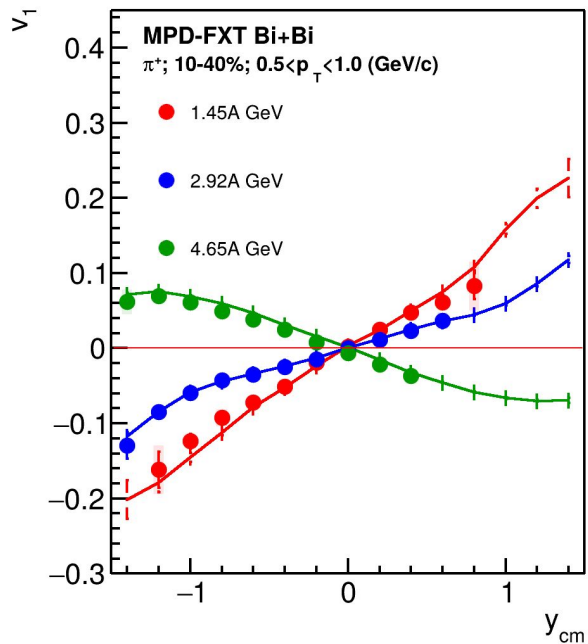
# Results: $v_1(y)$

Systematics: xx, yy, F1, F2, F3

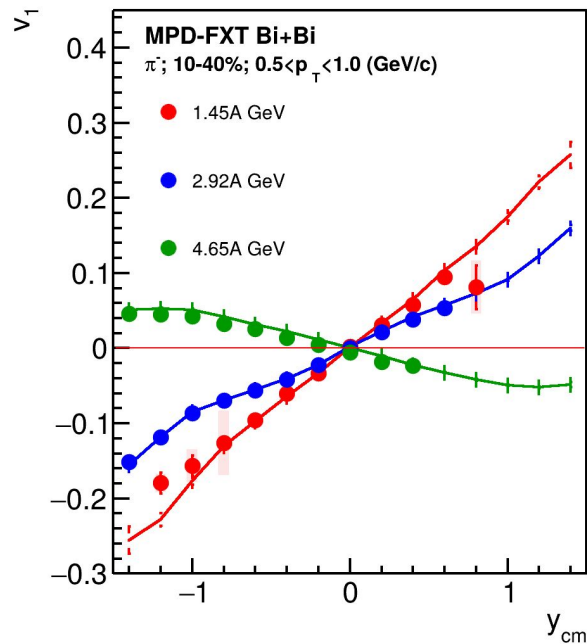
**p**



**$\pi^+$**



**$\pi^-$**

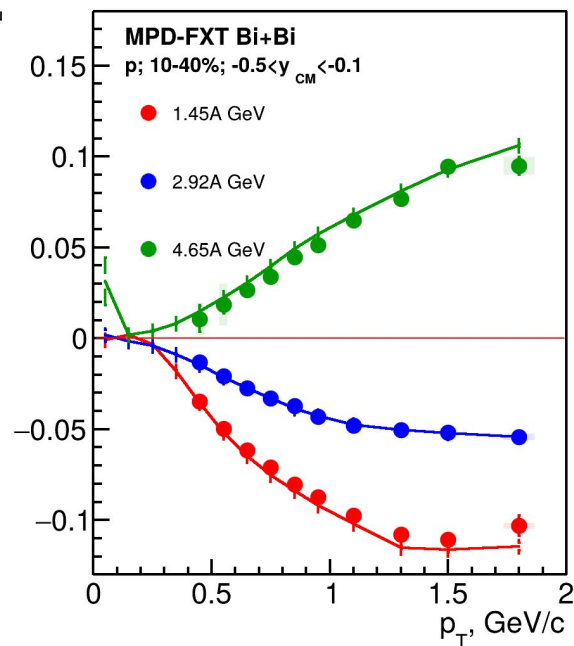


Good agreement with MC data

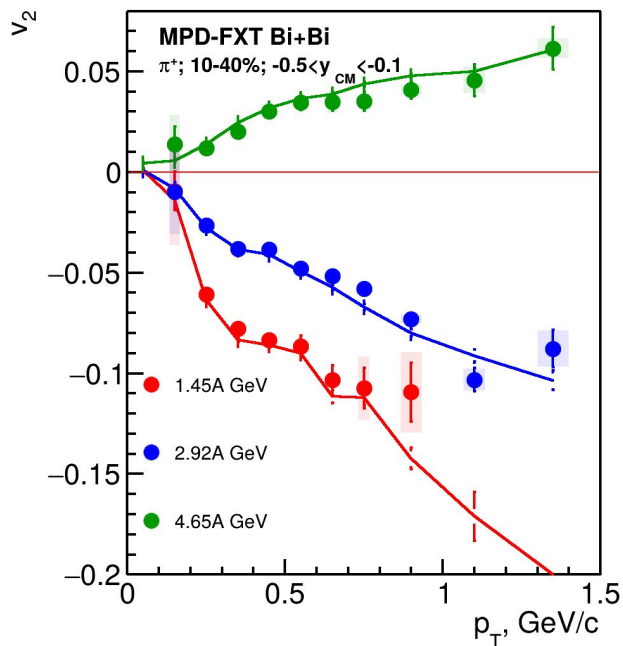
# Results: $v_2(p_T)$

Systematics: xxx, xyy

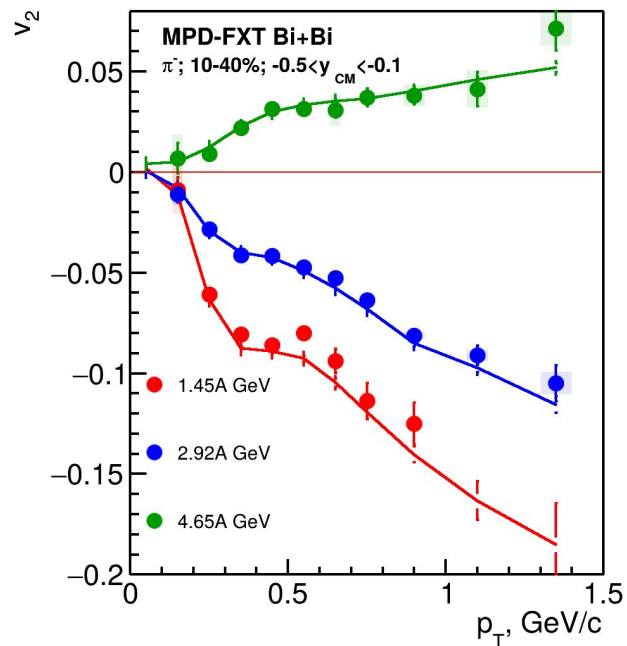
**p**



**$\pi^+$**

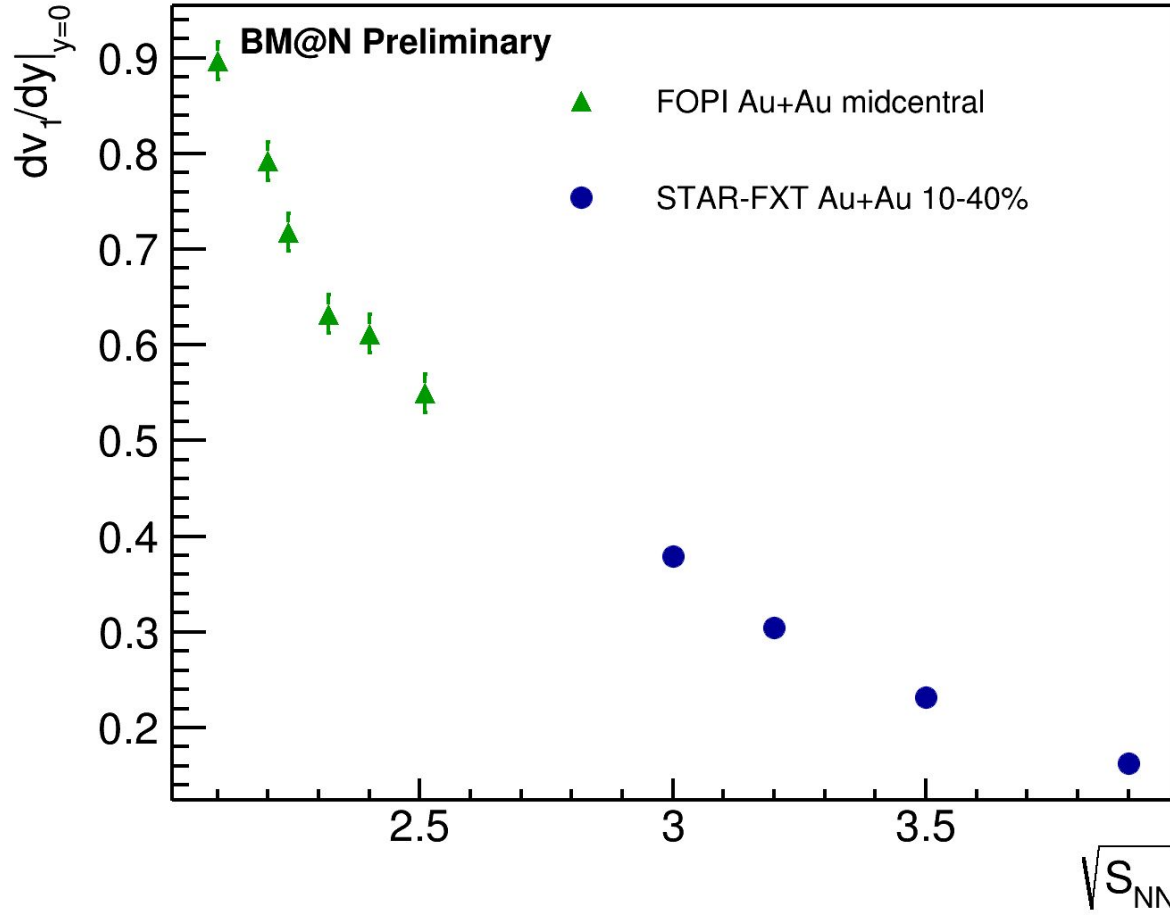


**$\pi^-$**

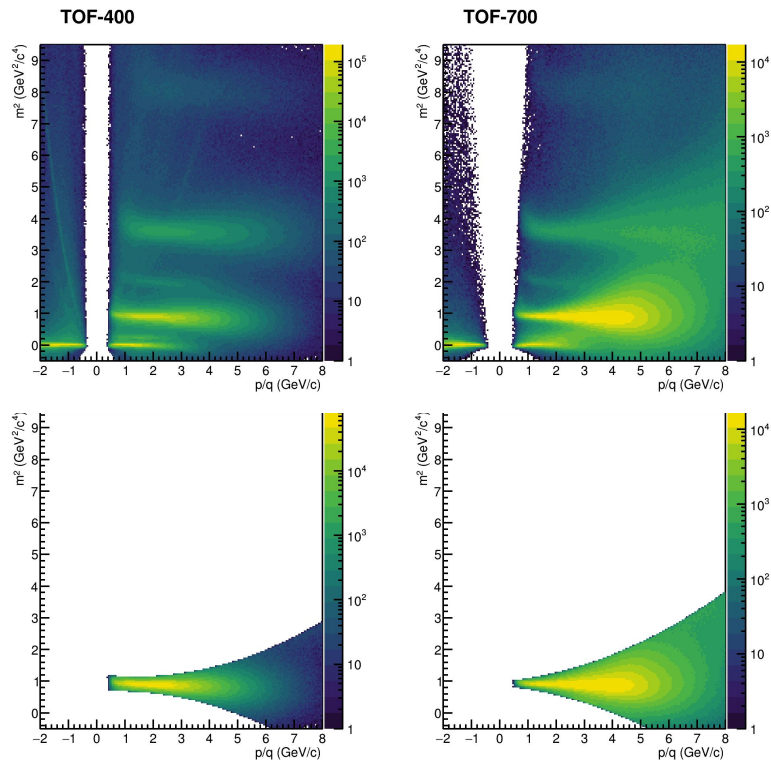
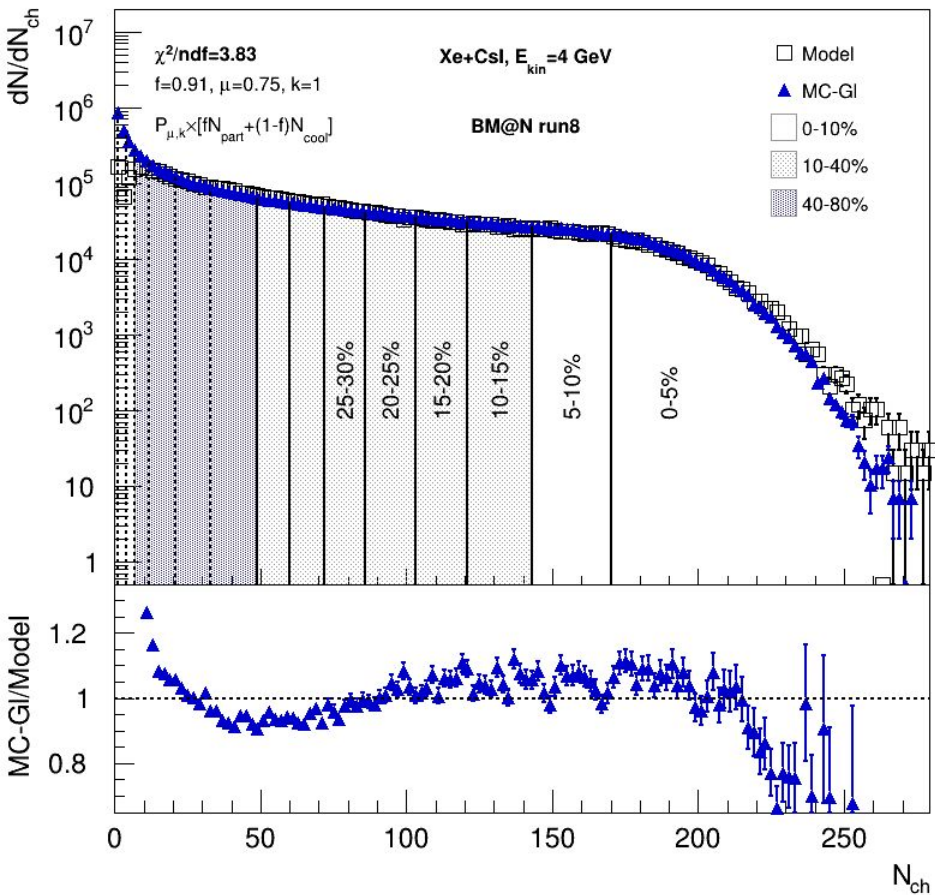


Good agreement with MC data

# $dv_1/dy|_{y=0}$ vs collision energy



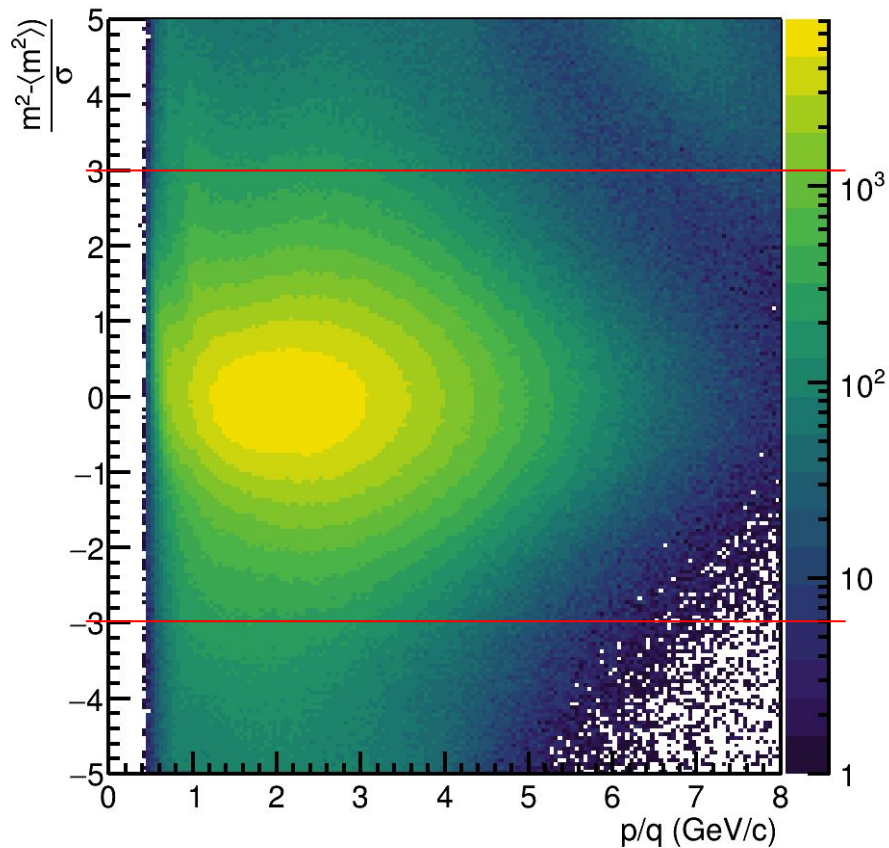
# Centrality and particle selection



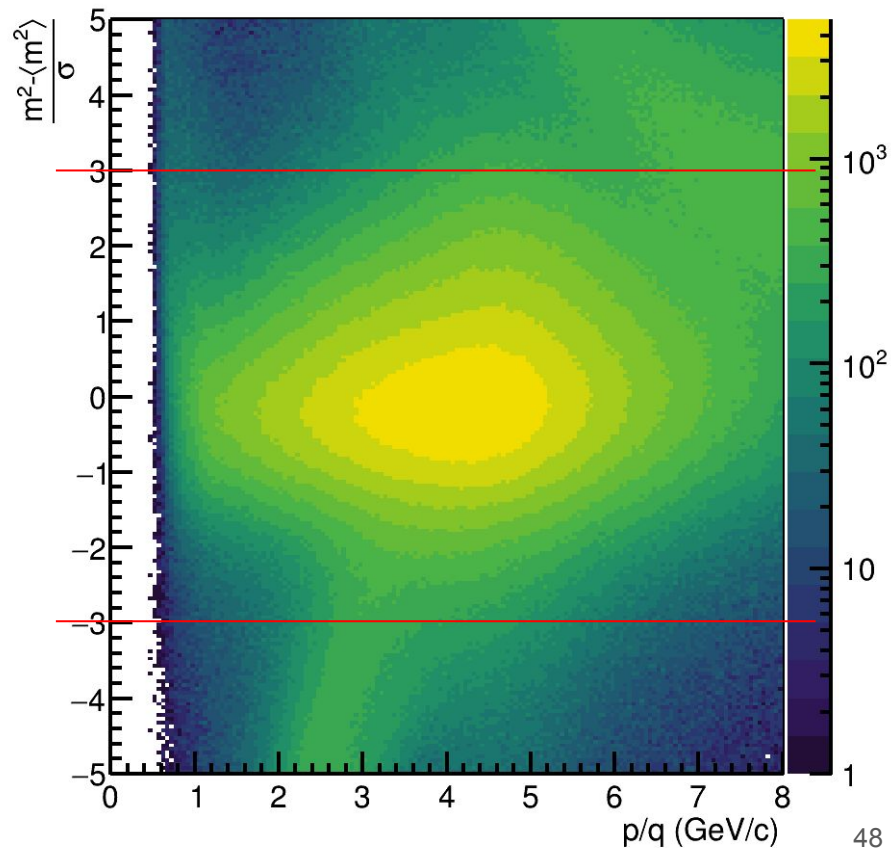
- Half of the recent VF production was analysed
- Event selection criteria (~100M events selected)
  - CCT2 trigger
  - Pile-up cut
  - Number tracks for vertex > 1
- Track selection criteria :  $\chi^2 < 5$ ;  $M_p^2 - 3\sigma < m^2 < M_p^2 + 3\sigma$ ;  $N_{hits} > 57$

# Proton N-sigma distributions

## TOF-400

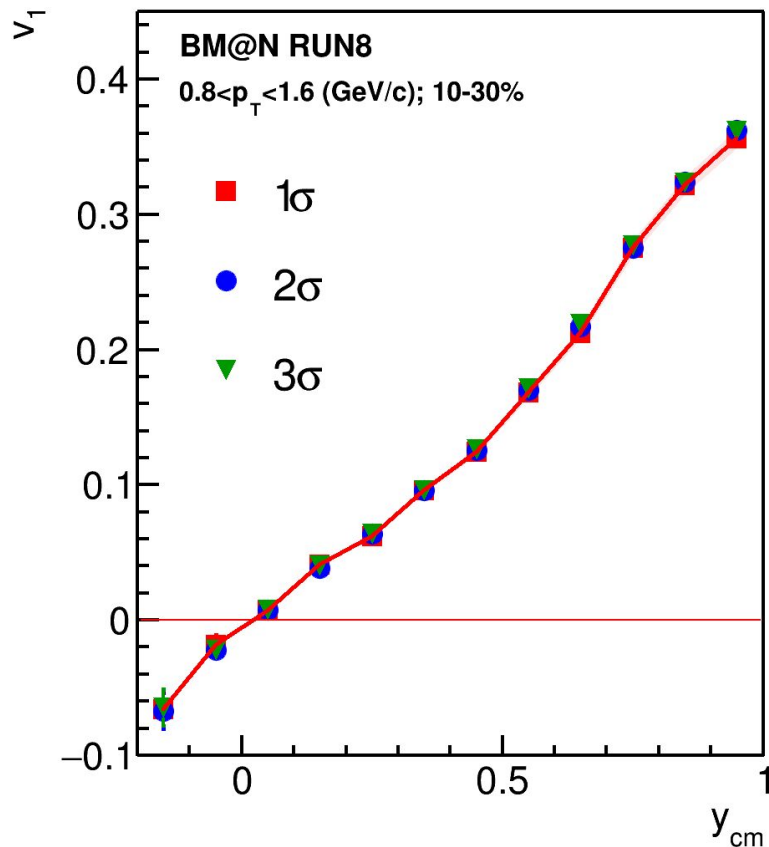


## TOF-700





# Systematics due to identification and tracking



The systematics is below 2%

