



# The equivalence principle and acceleration effect

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# Outline



- Introduction: two optical effects which seems related
- > Discovering of Accelerating matter effect
- Acceleration effect and The Equivalence principle
- Acceleration effect and differential Doppler effect
- Acceleration effect and quantum mechanics
- Neutron scattering on an accelerating nucleon and open questions in neutron optics
- Plans and intentions
- Conclusion

#### Prehistory. Theoretical prediction of two new effects



Kazuo Tanaka

Reflection and transmission of electromagnetic waves by a linearly accelerated dielectric slab. Phys.Rev. A **25**, 385, 1982



 $\omega_{p} \cong \omega_{0} + \frac{aL}{c^{2}}\omega_{0} \left[ (2p-1)n - 1 \right]$ 

 $\Delta \omega \cong \frac{\mathbf{wL}}{c^2} \omega_0(\mathbf{n-1})$ 



Fig. 1. The source, S, emits a neutron which propagates through the slab of material to the receiver, R. The slab, S, and R all accelerate rigidly with constant acceleration g in the direction shown. Points A and B are fixed in the inertial frame discussed in the text.



He founded a contradiction with the equivalence principle when calculated the problem but the effect of energy changes was predicted

> The result was confirmed by alternative approaches by V.G.Nosov and A.I.Frank In 1998

#### Effect was discovered in 2007-2008 by the JINR – ILL Group

F.W. Kowalsky

Interaction f neutrons with accelerating matter: test of the

equivalence principle. Phys. Lett. A 25, 335, 1992

To our knowledge, the Tanaka effect has not yet been observed.

#### 23-24 December 2025

A. Frank. 60-th meeting of the Programme Advisory Committee for Nuclear Physics

(**p** = 1)

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#### **Precise UCN spectrometry**





# The periodic variation of the neutron energy, caused by the sample acceleration, leads to the periodical oscillation of the count rate

#### First observation of the effect of acceleration in neutron optics







 $\mathbf{f}(\mathbf{t}) = \mathbf{1} + \mathbf{B}\sin(\mathbf{\Omega}\mathbf{t} - \mathbf{\phi})$ 

Frequency f = 40, 60 Hz Oscillation period 0.025, 0.017 sec Time of flight 0.11 sec



 $w_{max} = A\Omega^2 \approx 60 m / s^2$ 

 $\Delta \mathbf{E} \cong -\mathbf{K}\mathbf{m}\mathbf{A}\mathbf{\Omega}^{2}\mathbf{L}\left(\frac{1}{n}-1\right)\mathbf{sin}\,\mathbf{\Omega}\mathbf{t}$ 

$$K = 0.94 \pm 0.06$$

A.I. Frank, P.Geltenbort, G.V.Kulin, et al, Phys. At. Nuclei, 71 (2008) 1656.

# **Observation of the weak time focusing due to AME**





# Accelerating sample and the equivalence principle





# $\Delta E = mgH$ Detector W=Q

- 1. In both cases the energy, measured by the detector, must be the same due to the equivalence principle
- 2. Inserting the refracting slab does not change the energy due to the energy conservation law (see left fig.)
- Delay time due to refraction is  $\Delta \tau$

$$\Delta v = w \Delta \tau$$

#### During this delay time the detector will continue to accelerate

# Accelerating sample and the equivalence principle





 $\Delta \mathbf{v} = \mathbf{w} \Delta \tau \qquad \qquad \left| \Delta \mathbf{E} \right| = \mathbf{m} \mathbf{v} \cdot \Delta \mathbf{v}$ 

If the time delay  $\Delta \tau$  is the only effect associated with the sample, then introduction of (accelerating) sample would result in change in the detected energy which is contrary to the equivalence principle

Consequently, for the validity of the equivalence principle it is necessary that time delay time  $\Delta \tau$  due to refraction must be accompanied by the change of energy

We concluded that AME is a very general optical phenomenon, since the concept of the refractive index can be introduced for any particles.

A.I. Frank, P.Geltenbort, G.V.Kulin, et al, Phys. At. Nuclei, <u>71</u> (2008) 1656.



# Is AME is really just an optical effect?



$$\Delta \mathbf{v} = \mathbf{w} \Delta \tau \qquad \Delta \mathbf{E} = -\mathbf{m} \mathbf{v} \cdot \Delta \mathbf{v}$$

Previously we came to the conclusion that in order to fulfill the equivalence principle, the time delay  $\Delta \tau$  arising due to the difference in wave vectors in the vacuum and the sample must be accompanied by a change in energy

#### But why did we associate the time delay $\Delta \tau$ only with optical phenomena ?

# Is AME really just an optical effect?





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Previously we came to the conclusion that in order to fulfill the equivalence principle, the time delay  $\Delta \tau$  arising due to the difference in wave vectors in the vacuum and the sample must be accompanied by a change in energy

#### But why did we associate the time delay $\Delta \tau$ only with optical phenomena ?

Any interaction is necessarily associated with a time delay

**General relation** 

$$\Delta \omega = k w \Delta \tau$$



# **Acceleration Effect**

# Any object which is scattering a wave or transmitting narrow-band signal shifts the frequency if it is moving with acceleration.

The acceleration effect (AE) is apparently as general as the Doppler effect. However, the frequency shift of the wave is determined not by the speed of the scatterer but by its acceleration

A.I. Frank.. Physics-Uspeckhi, 63, 500-502 (2020)

### Acceleration effect in classical physics – Differential Doppler Effect



## Acceleration Effect in neutron and light optics (Acceleration matter effect)



$$\Delta \omega = k w \Delta \tau$$

**Neutrons** 

$$k = \frac{mv}{\hbar}$$
  $\Delta \tau = \frac{d}{v} \left( \frac{l-n}{n} \right)$   $\Delta E = \hbar \Delta \omega$ 

 $\Delta \mathbf{E} \cong \mathbf{mwd} \left( \frac{1}{\mathbf{n}} - 1 \right)$ 

KNF formula

Light, neutrino and ultra-relativistic particles

$$k = \frac{\omega}{c}$$
  $\Delta \tau = \frac{nd}{c} - \frac{d}{c} = \frac{d}{c}(n-1)$ 

$$\Delta \omega \cong \frac{\omega w d}{c^2} (n-1)$$

Tanaka formula

# Refraction of a wave at the border of the moving matter

$$e^{i(k_0x-\omega_0t)} \bigvee e^{i(k_ix-\omega_it)} n$$

$$\mathbf{k}_{i} = \mathbf{n}\mathbf{k}_{0} \left(1 + \frac{1 - \mathbf{n}}{\mathbf{n}} \frac{\mathbf{V}}{\mathbf{V}_{0}}\right)$$

Massive particle (neutron)

A.I.Frank and V.A.Naumov. Phys. of Atom. Nuc., 76,1423 (2013)

$$\mathbf{k}_{0} = \frac{\mathbf{m}\mathbf{v}_{0}}{\hbar} \qquad \left(\frac{\mathbf{V}}{\mathbf{v}_{0}} << 1\right)$$
$$\mathbf{n} \equiv \mathbf{n}(\mathbf{k}_{0}') = \mathbf{n}\left(\mathbf{k}_{0} - \mathbf{k}_{v}\right)$$

$$\boldsymbol{\omega}_{\mathbf{i}} = \boldsymbol{\omega}_0 + (\mathbf{n} - 1) \mathbf{k}_0 \mathbf{V}$$

Doppler shift at refraction Light

C. Yeh. J. Appl. Phys. 36, 3513 (1965)

$$\mathbf{k}_{0} = \frac{\boldsymbol{\omega}_{0}}{\mathbf{c}} \qquad \left(\frac{\mathbf{v}}{\mathbf{c}} <<1\right)$$
$$\mathbf{v}_{ph} = \frac{\mathbf{c}}{\mathbf{n}} + \mathbf{v} \left(1 - \frac{1}{\mathbf{n}^{2}}\right) \quad \text{Fresnel drag}$$

# Transmission of a wave through the moving sample (constant velocity)





When the wave enters the sample from free space, its frequency changes. When the wave exit the medium into free space, the frequency of the wave also changes but this change has the opposite sign. When moving at a constant speed, these two frequency shifts compensate for each other.

# Transmission of a wave through the moving sample (accelerated motion)





For the accelerated motion, two frequency shifts do not compensate each other because the velocity of the medium is not constant.

**Calculations based on the concept of differential Doppler shift leads to the formula:** 



Assumptions:

1) Quasi – classical approach is correct

2) The model of effective potential is also valid in the case of accelerating matter

Kowalski-Nosov-Frank



# **Differential Doppler effect and Accelerating Matter Effect** *at refraction of light*

$$\Delta \omega \cong \frac{\omega w d}{c^2} (n-1) \qquad \stackrel{??}{\longleftarrow} \quad \Delta \omega = \frac{\omega w dn}{c^2} (n-1)$$

#### Tanaka result and Acceleration effect

#### **Differential Doppler effect**

The discrepancy probably occurred because the fact of the (accelerating) movement of the medium was not taken into account

#### Transmission of neutrons through an accelerating crystal near the Bragg conditions. Is it also differential Doppler effect?





Fig. 1. Scheme of experimental setup: (*n*) collimated neutron beam,  $(K_{1-3})$  quartz single crystals of temperature  $T_{1-3}$ , (PG) pyrolytic-graphite crystals, (*D*) neutron detector, and (*S*) detector shield.

V.V. Voronin et al., JETP letters, 100, 497 (2014) Yu. P. Braginetz et al., Phys.At. Nucl. 80, 32 (2017) Change of the neutron energy at its transmission through the accelerating crystal in the condition of the Bragg diffraction was detected

The observed effect can be explained in the framework of differential Doppler shift at the boundary of a moving matter. But calculations are more complicated than in the case of refraction.

$$k = F(k_0)$$
$$k'_0(t) = k_0 - mwt$$
$$v = \frac{\hbar k}{m^*} = \frac{\hbar}{2m} \left(\frac{dF}{d(k_0'^2)}\right)^{-1}$$



#### The authors of the work have a different point of view regarding the nature of the effect.

# Can the Acceleration effect always be interpreted as the Differential Doppler effect?



It seems that the acceleration effect always may be interpreted as a differential Doppler effect, when the absorption of a wave and its emission are separated by a time interval during which the velocity of the object changes. Although sometimes the calculations are not entirely trivial

But that is not true in quantum mechanics, where the process of interaction of a particle with an accelerating object (potential structure) can hardly be separated by absorption and radiation phases?



# The important question is whether the concept of a universal Acceleration Effect in quantum mechanics is correct.

And if this is true, what should be taken as a measure of time delay?  $\Delta \omega = kw\Delta \tau$ 

Assumption: The time delay is determined by Group delay time (GDT) of Bohm-Wigner



Bohm D., *Quantum Theory*, Prentice-Hall, New York, 1951. Wigner E.P., Phys. Rev., **98**, 145 (1955).

#### Numerical calculations based on the method of the evolution operator splitting





M. A. Zakharov, G. V. Kulin, and A. I. Frank. Eur. Phys. J. D 75, 47 (2021).

The Acceleration Effect when a neutron passes through a potential structure moving with acceleration. Under the barrier passage. The interference effects are significant.



M. A. Zakharov, G. V. Kulin, and A. I. Frank. Eur. Phys. J. D 75, 47 (2021).

A. Frank. 60-th meeting of the Programme Advisory

Committee for Nuclear Physics



#### Neutron reflection from a potential barrier moving with acceleration





#### Tunneling of a neutron through a resonant potential structure moving with acceleration.





M. A. Zakharov, G. V. Kulin, and A. I. Frank. Eur. Phys. J. D 75, 47 (2021).



# Acceleration effect that complements the Doppler effect, but does not depend on speed, but on acceleration, should take place in quantum mechanics

# What follows from that for neutron optics ?

#### Group delay time at neutrons scattering by atomic nucleus





 $\Delta v = w \Delta \tau$ 

# Unsolved problems of the theory

- 1. The relationship we accepted between the change in velocity and GDT during scattering on an atomic nucleus is unlikely to be true for such shorts period of time. Should there be an Accelerating Effect in this case as well?
- **2.** If there is an acceleration effect when scattering on an accelerating nucleus, then what is the effect of multiple scattering in the case of a medium?
- 3. The assumption of an inelastic and probably non-isotropic scattering pattern by an individual nucleus contradict the basic principles underlying the existing theory of neutron wave dispersion

 $\Delta v = w \Delta \tau(?)$ 



Apparently, neutron optics of accelerating media does not currently exist as a field of science, and the question of creating an appropriate theory turns out to be very relevant.

This is one of our tasks for the near future.

#### We are looking for the new experimental approaches





Neutron transmission above potential barrier

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### Neutron diffraction by SAW for the test of the dispersion law in accelerating matter





Fig. 2 The layout of sample with IDTs and the structure of the SAW formation, here  $\Lambda$  is a SAW wavelength

Acceleration of the surface and near-surface layer is up to  $10^9$  m/ $s^2$ 





G. V. Kulin, A. I.Frank, N.V.Rebrova et al. Eur. Phys. J. B , 97 (2024) 194

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#### Acceleration effect in the case of birefringent and nonstationary spin precession





 $\Delta E \approx 10^{-16} eV$ 

## G.Badurek, H.Rauch, and D.Tuppinger, Phys.Rev.A, 34 (1986), 2600



In a fixed observation point and in neglecting by t dependence of  $\Delta \chi$  spin rotation frequency  $\Omega$  is

$$\varphi(t) = \Omega t \qquad \qquad \Omega = \frac{mwL}{\hbar} \left( \frac{n_{+} - n_{-}}{n_{+}n_{-}} \right)$$

A I Frank, P Geltenbort, M Jentschel, et al. Journ.of Phys.: Conf. Series 340 (2012) 012042. A.I.Frank, V.A.Naumov.. Phys. At.Nuc., 76 (2013), 1423

#### Birefringence of the neutron waves (two samples)



#### 1. Region with magnetic field or magnetic sample

$$n_{\pm} = \sqrt{1 \mp \frac{\mu B}{E}} \qquad \Delta n \approx \frac{\mu B}{E} \quad \left(\mu B \ll E\right) \qquad \Omega = \frac{\mu B}{\hbar} \frac{mwd}{2E} = \omega_{L} \frac{mwd}{2E} \qquad \omega_{L} = \frac{2\mu B}{\hbar}$$

#### 2. Polarized neutrons and polarized matter (nuclear pseudo magnetism)

V.G.Baryshevskii, M.I.Podgoretsky. JETP 47 (1964) 1050. A.Abragam, et al., Phys.Rev.Lett, 31 (1973) 776.

$$\mathbf{n}_{\pm} = \left(1 \mp \frac{\mathbf{U}_{\pm}}{\mathbf{E}}\right)^{1/2} \qquad \mathbf{U}_{\pm} = \frac{2\pi\hbar^2}{\mathbf{m}}\rho\mathbf{b}_{\pm} \qquad b_{\pm} \to J = I \pm 1/2$$

$$\Omega = p_{nuc} \frac{mwd}{\hbar} \frac{\overline{U}}{n^2 2E} \frac{\Delta b}{b}$$

For UCN, w=10g and d=1mm

$$\Omega = p_{nuc} \frac{\Delta b}{b} \times 10^6$$

# Possibility of the experimental observation (birefringence in the magnetic field)



UCN B=1 Gauss  $n_{\pm} = 1 \pm 2.8 \times 10^{-5}$ d =1cm a = 50cm/s<sup>2</sup>, T = 0.5s S = 10cm  $V_{max} = 24.5$  cm/s



 $\Delta \mathbf{E} = \pm \hbar \Omega / 2 \approx \pm 1.5 \times 10^{-15} eV$ 

#### A.I.Frank. Journal of Physics: Conf. Ser. 711 (2016) 012016.

# **Conclusion**



Any object that scatters a wave or receives and then emits a signal shifts frequency of the wave if it is moving with acceleration

This conclusion is also true for quantum objects

We can talk about the Acceleration Effect as a general effect that complements the Doppler effect but differs from it in that the frequency shift is determined not by the speed of the object but by its acceleration.

It can be assumed that the acceleration effect should also take place in the case of neutron scattering on atomic nuclei of accelerating matter. This assumption raises a number of new questions for the theory

Some approaches to the possible future experiments are discussed

# Many thanks to my colleagues



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