Centrality determination by forward detectors

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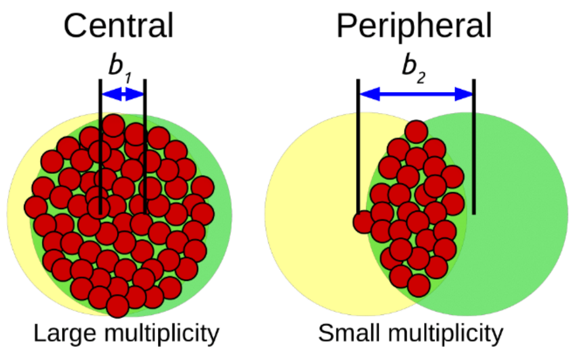
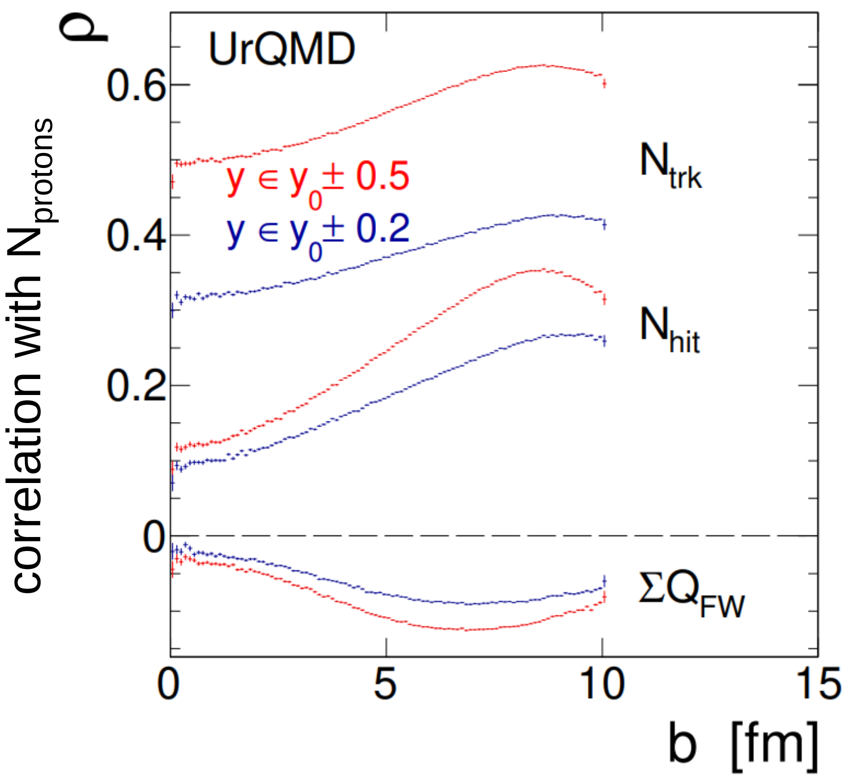
04-05 March 2025

Centrality

- Evolution of matter produced in heavy-ion collisions depend on its initial geometry
- Centrality procedure maps initial geometry parameters with measurable quantities (multiplicity or energy of the spectators)
- **This allows comparison of the future BMAN results with the data from other experiments (STAR BES, NA49/NA61 scans) and theoretical models**

$$c(b) = \frac{\int_0^b \frac{d\sigma}{db'} db'}{\int_0^\infty \frac{d\sigma}{db'} db'} = \frac{1}{\sigma_{A-A}} \int_0^b \frac{d\sigma}{db'} db'$$



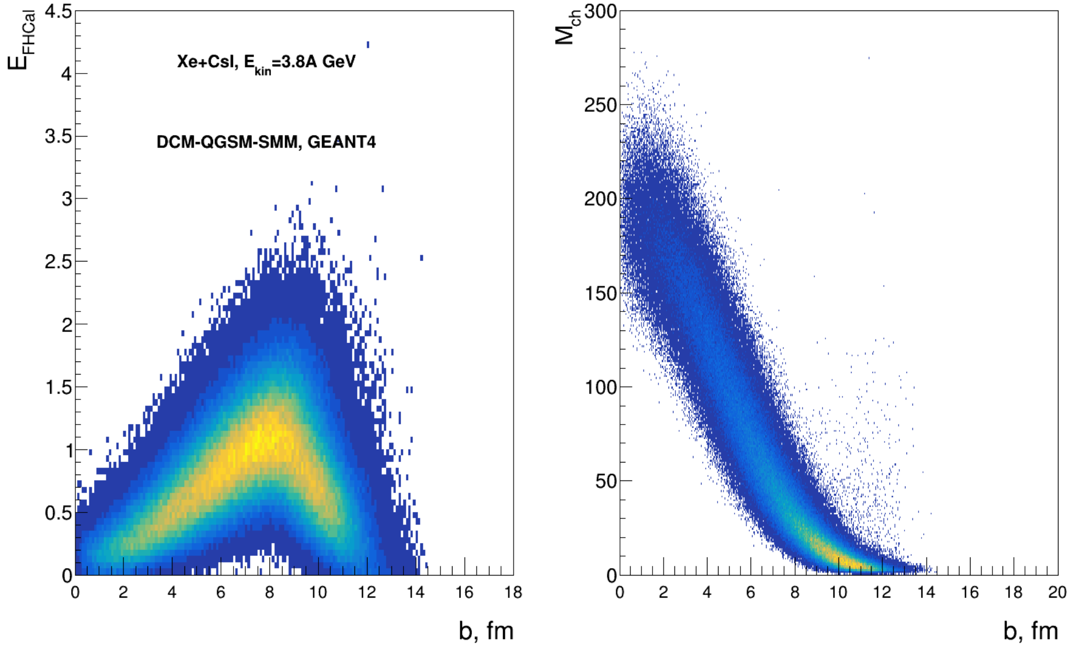


HADES; Phys.Rev.C 102 (2020) 2, 024914

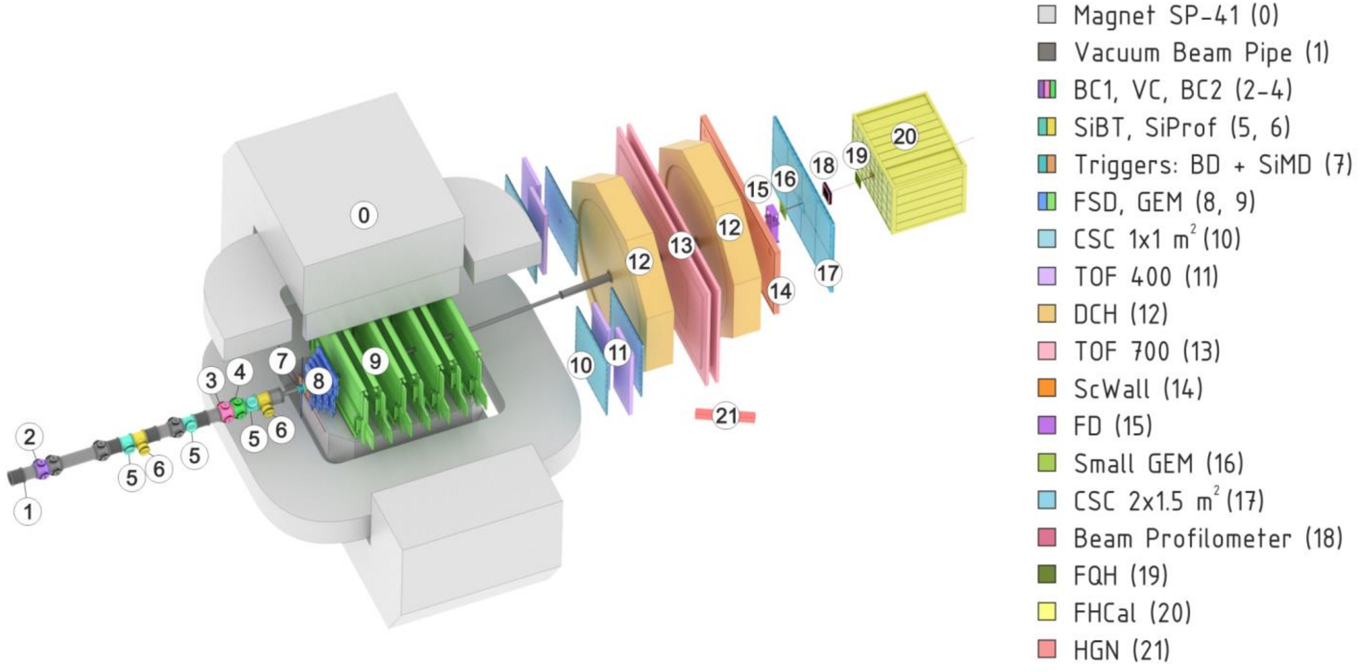
- A number of produced protons is stronger correlated with the number of produced particles (track & RPC+TOF hits) than with the total charge of spectator fragments (FW)
- to suppress self-correlation biases, it is necessary to use spectators fragments for centrality estimation

Centrality determination in BM@N

DCM-QGSM-SMM → GEANT4 → Reconstruction → Centrality determination



Dependence of energy in FHCal and track multiplicity
on the impact parameter



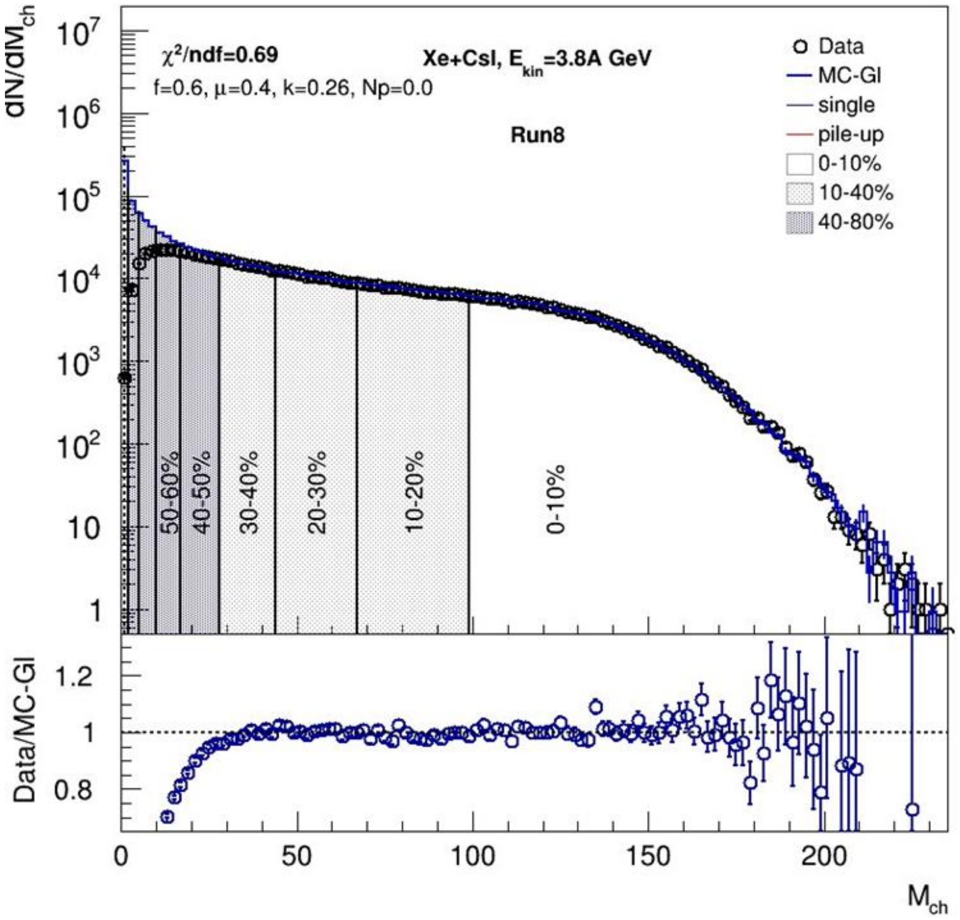
BM@N setup overview

MC-Glauber based centrality framework

MC Glauber data → Evaluate N_a: $N_a = fN_{part}+(1-f)N_{coll}$ → Call $NBD(\mu,k) \times N_a$ → Build multiplicity fitting function

Input multiplicity distribution

Build multiplicity fitting function + Input multiplicity distribution → Evaluate χ^2 → Minimize χ^2 to find α, μ, k



NBD – negative binomial distribution

Parameters of the fit:

- **f** – the fraction of multiplicity from the soft component
- **μ** – mean multiplicity value
- **k** – width of the multiplicity distribution, can be connected to the fluctuations

Implemantation for MPD: https://github.com/FlowNICA/CentralityFramework

P. Parfenov, et al., Particles. 2021; 4(2):275-287

The Bayesian inversion method (Γ-fit): DCM-QSM-SMM based

- The fluctuation kernel Gamma distr.:

$$P(M \mid c_b) = \frac{1}{\Gamma(k(c_b))\theta^2} M^{k(c_b)-1} e^{-M/\theta}$$

$$c_b = \int_0^b P(b')db'$$ – centrality based on impact parameter

$$\theta = \frac{D(M)}{\langle M \rangle}, \quad k = \frac{\langle M \rangle}{\theta}$$

$\langle M \rangle, D(M)$ – average and variance of Multiplicty

$$P(M) = \int_0^1 P(M \mid c_b) dc_b$$

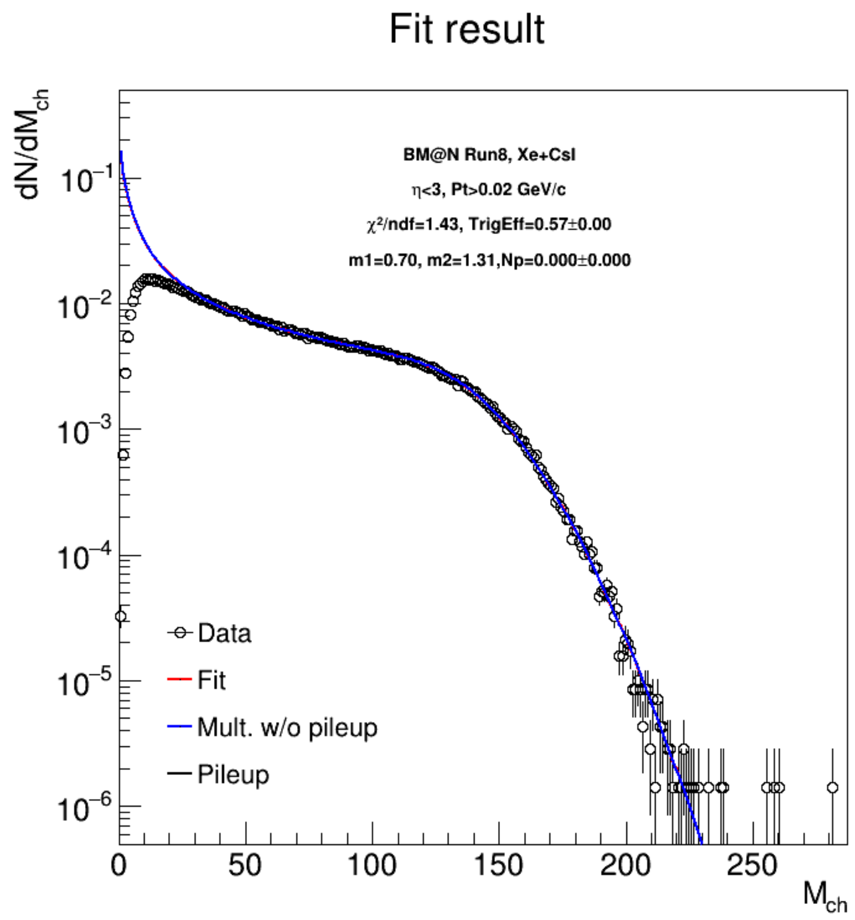
$$\langle M \rangle = m_1 \cdot \langle M' \rangle$$

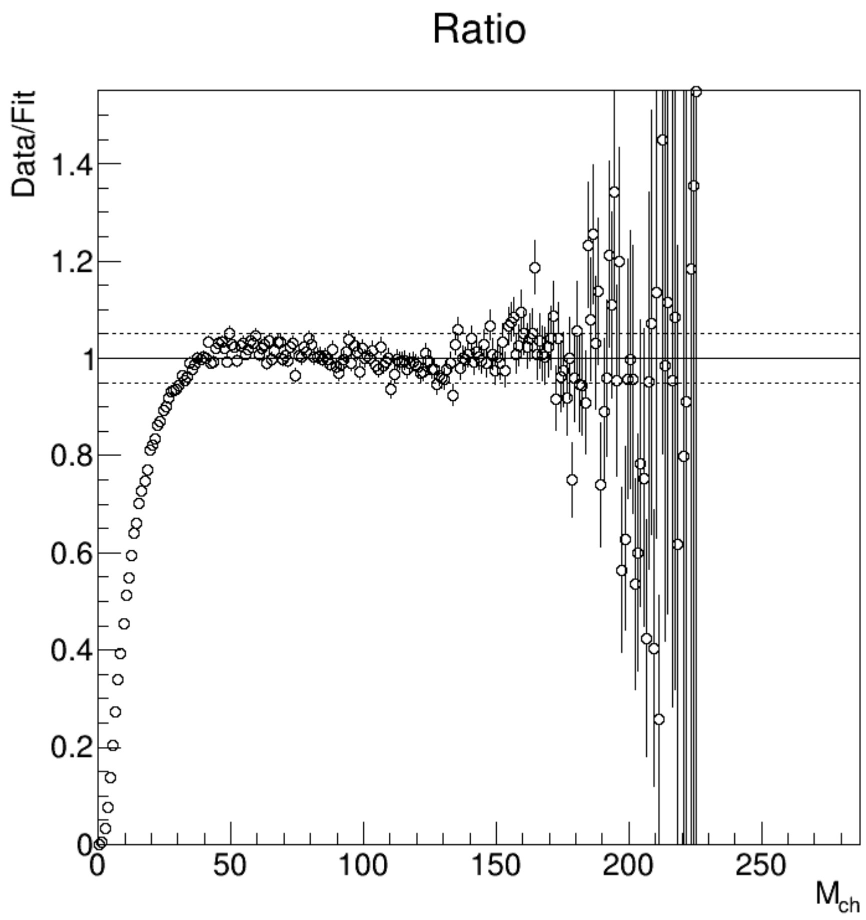
$$D(M) = m_1^2 \cdot D(M') + m_1 \cdot m_2 \langle M' \rangle$$

$\langle M'(c_b) \rangle$, $D(M'(c_b))$ – average value and var. of energy/mult. from the rec. model data

- can be approximated by polynomials and exponential polynomial

Fit results





Vertex Cuts: CCT2, N_{vtxTr}>1,|$V_{x,y}$ –(0.3,0.14)|<1 cm, |V_z -0.07|< 0.2 cm

Good agreement with data

Track selection: Nhit>4, η<3, Pt>0.05 GeV/c

The Bayesian inversion method (Γ-fit): 2D fit

- The fluctuation kernel for energy and multiplicity at fixed impact parameter can be describe by 2D Gamma distr.:

$$P(E,M\,|\,c_b)=G_{2D}(E,M,\langle E\rangle,\langle M\rangle,D(E),D(M),R)$$

$$c_b=\int_0^b P(b')db'$$ – centrality based on impact parameter

$\langle E\rangle, D(E)$ – average value and variance of energy

$\langle M\rangle, D(M)$ – average value and variance of mult.

$R(E,M)$ – Pirson correlation coefficient

$$R(E,M)=\frac{\varepsilon_1^2 m_1^2}{\varepsilon_2 m_2}R(E',M')$$

$\varepsilon_1,\varepsilon_2,m_1,m_2$ - fit parameters

$\langle E'(c_b)\rangle$, $D(E'(c_b))$ – average value and var. of energy/mult. from the rec. model data

$$\langle E\rangle=\varepsilon_1\langle E'(c_b)\rangle,\quad D(E)=\varepsilon_2 D(E'(c_b))$$
$$\langle M\rangle=m_1\langle M'(c_b)\rangle,\quad D(M)=m_2 D(M'(c_b))$$

$\langle E'(c_b)\rangle,\quad D(E'(c_b))$ - can be approximated by polynomials

$$\langle E'(c_b)\rangle=\sum_{j=1}^{8}a_j c_b^j,\quad D(E'(c_b))=\sum_{j=1}^{6}b_j c_b^j$$

$$\langle M'(c_b)\rangle=\sum_{j=1}^{8}a_j c_b^j,\quad D(M'(c_b))=\sum_{j=1}^{6}b_j c_b^j$$

The fluctuation of energy and multiplicity at fixed impact parameter

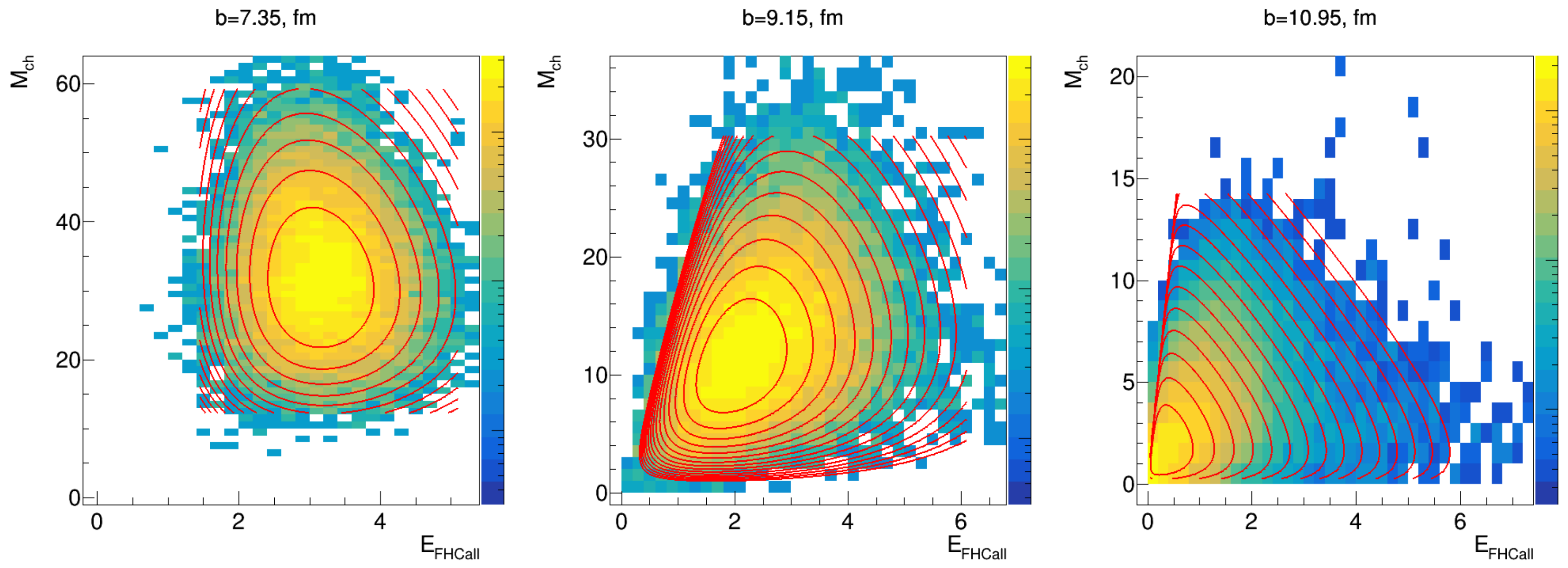
It is possible to find such a rotation angle of the system that $\mathrm{cov}(x,y)=0$

$$\langle x\rangle = \cos(\alpha)\langle E\rangle + \sin(\alpha)\langle M\rangle$$

$$\langle y\rangle = -\sin(\alpha)\langle E\rangle + \cos(\alpha)\langle M\rangle$$

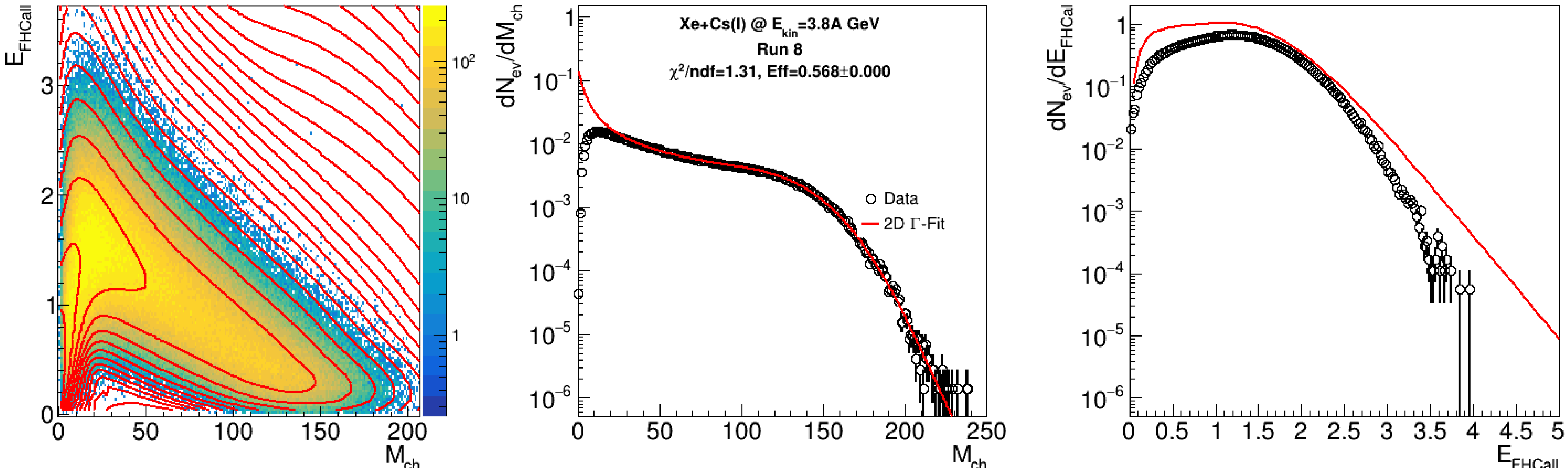
$$\alpha = \arctan\left(\frac{2\sqrt{D(E)D(M)}R(E,M)}{D(E)-D(M)}\right)$$

$$G_{2D}(E_{FH}, M_{ch}, \langle E\rangle, \langle M\rangle, D(E), D(M), R) = G(x,\theta_x,k_x)\cdot G(y,\theta_y,k_y)$$



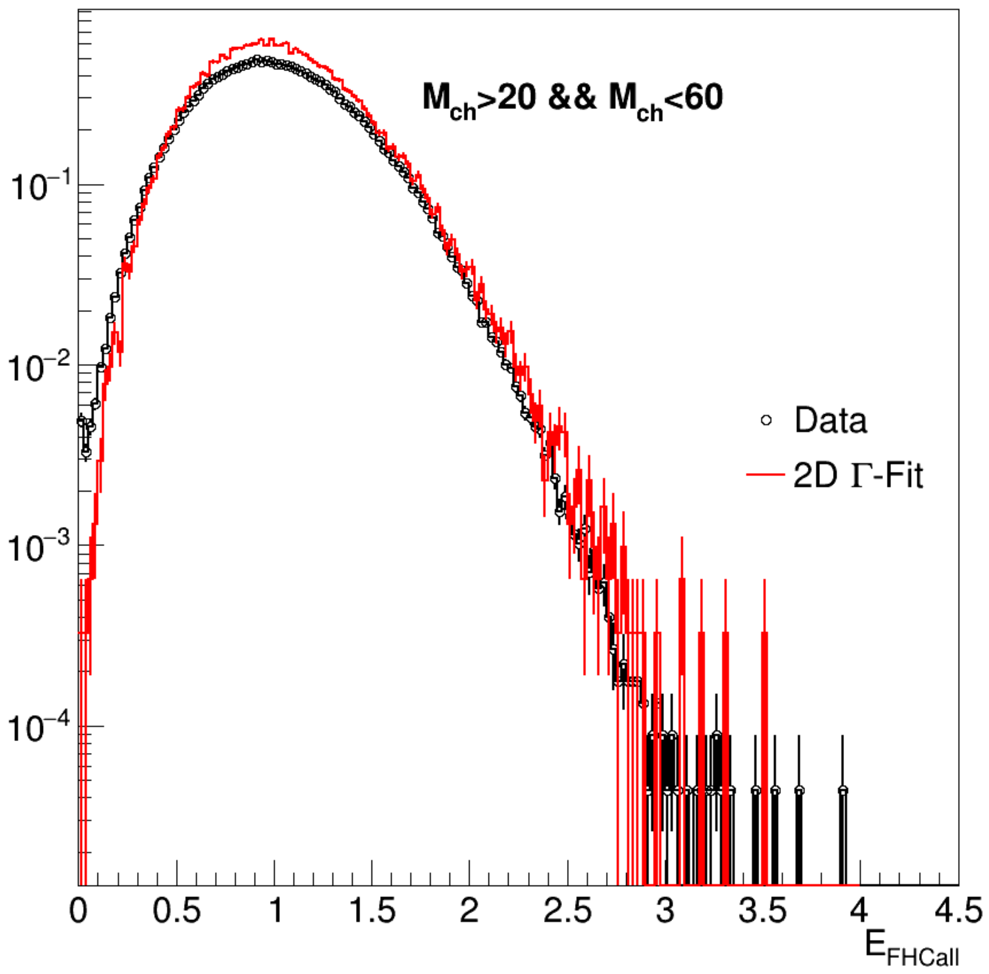
The distribution of energy and multiplicity at a fixed impact parameter is well described by the gamma distribution

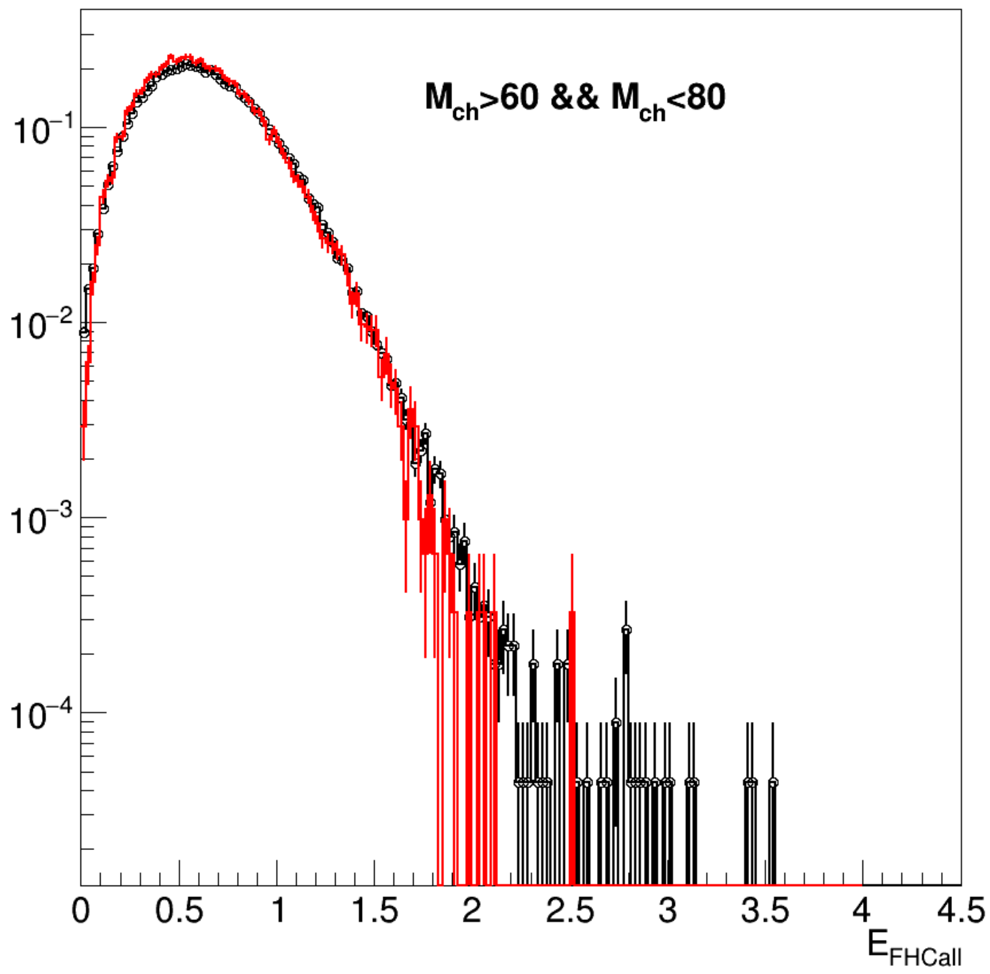
2D fit results



The fit function qualitatively reproduces the multiplicity-energy correlation from FHCal

Energy distributions from FHCal for different multiplicity cuts

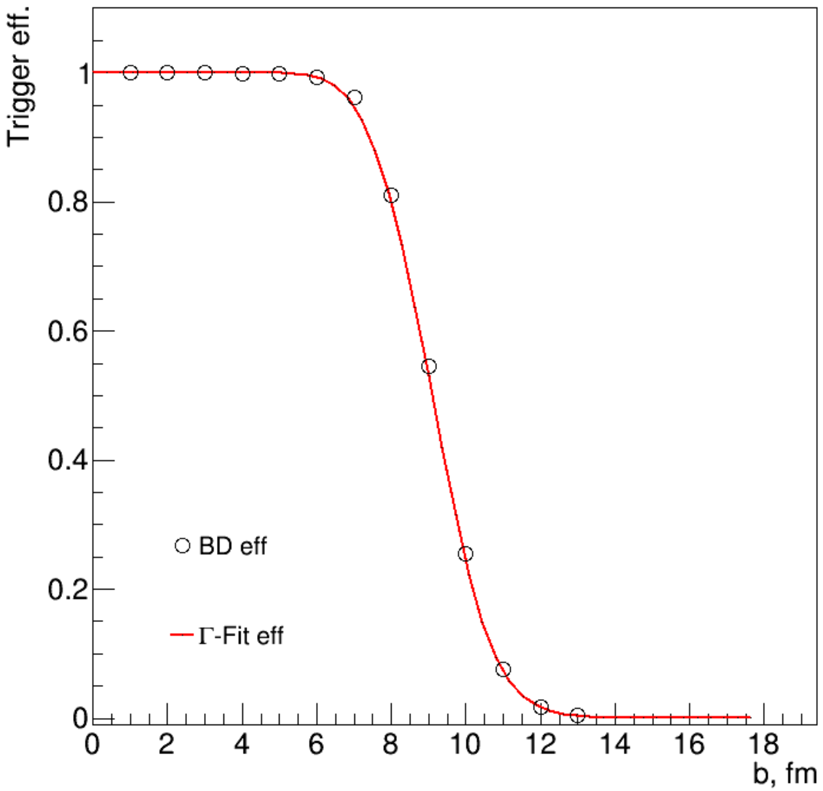


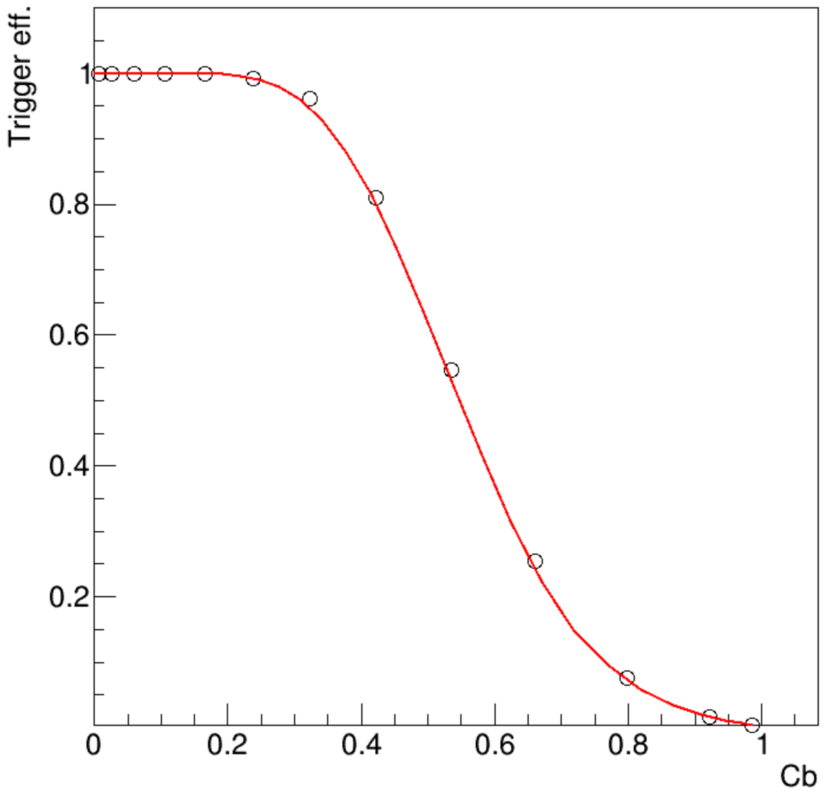


Good agreement between fit and data for the area below the anchorpoint

The total efficiency of event registration

$$P_{eff}(b) = \int_0^{M_{max}} P_{eff}(\mathrm{M}) P(\mathrm{M} \,|\, \mathrm{b}) dM$$

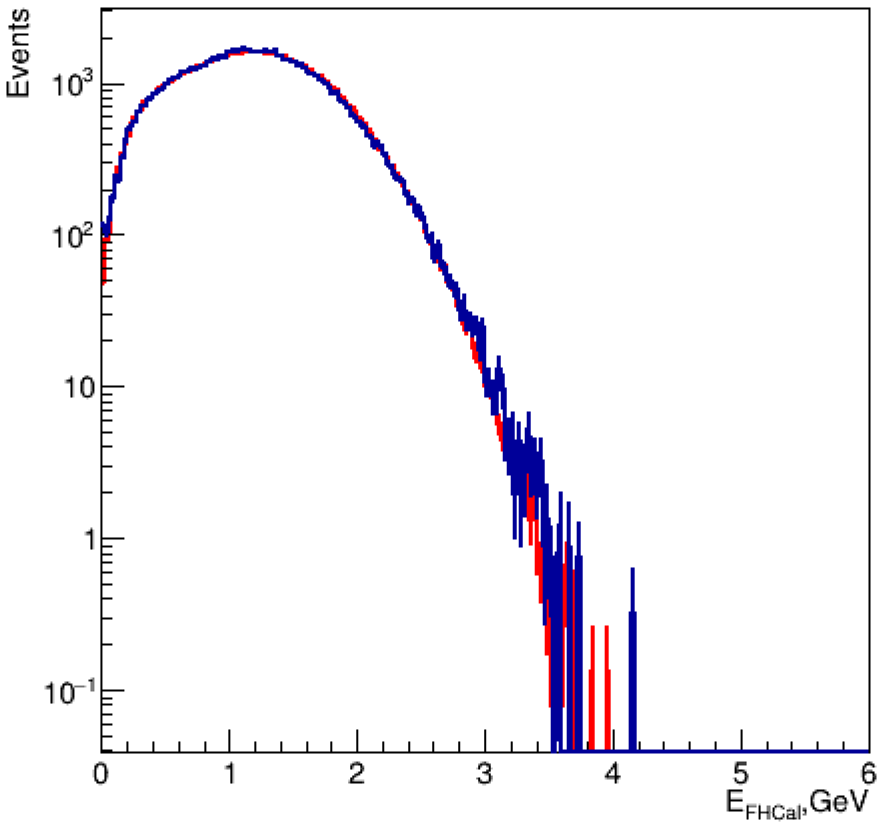


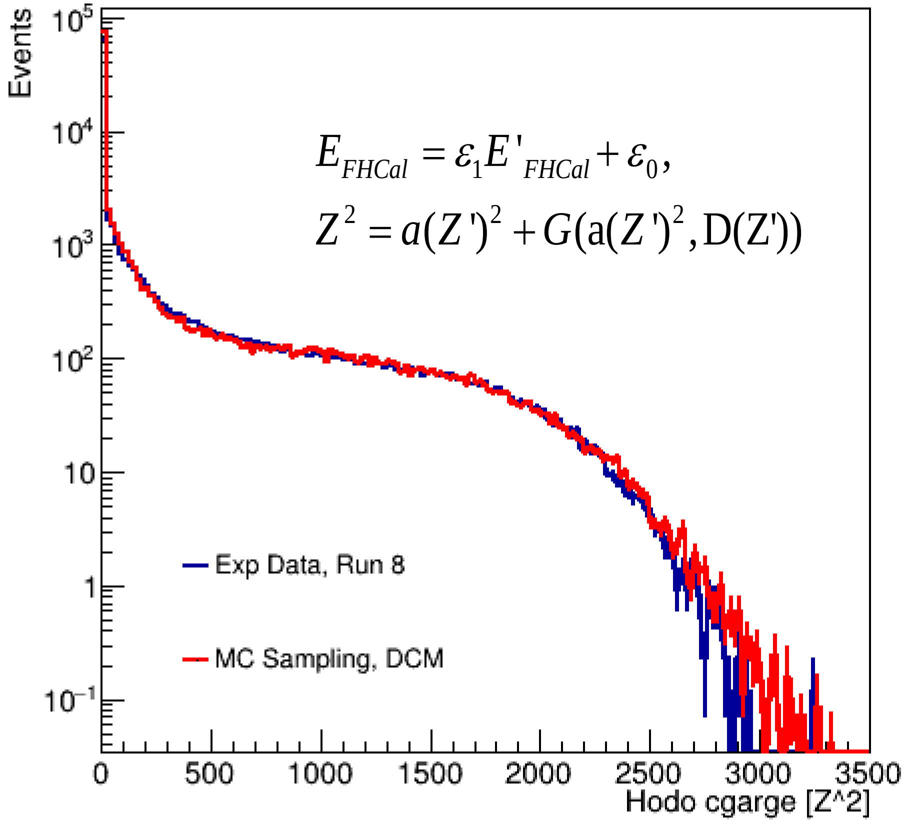


The trigger efficiency obtained from the Bayesian approach is consistent with the results, obtained on the basis of simulations

https://indico.jinr.ru/event/4762/contributions/28478/attachments/20298/35273/lashmanov_report_BM@N-meeting_Oct-2024.pdf

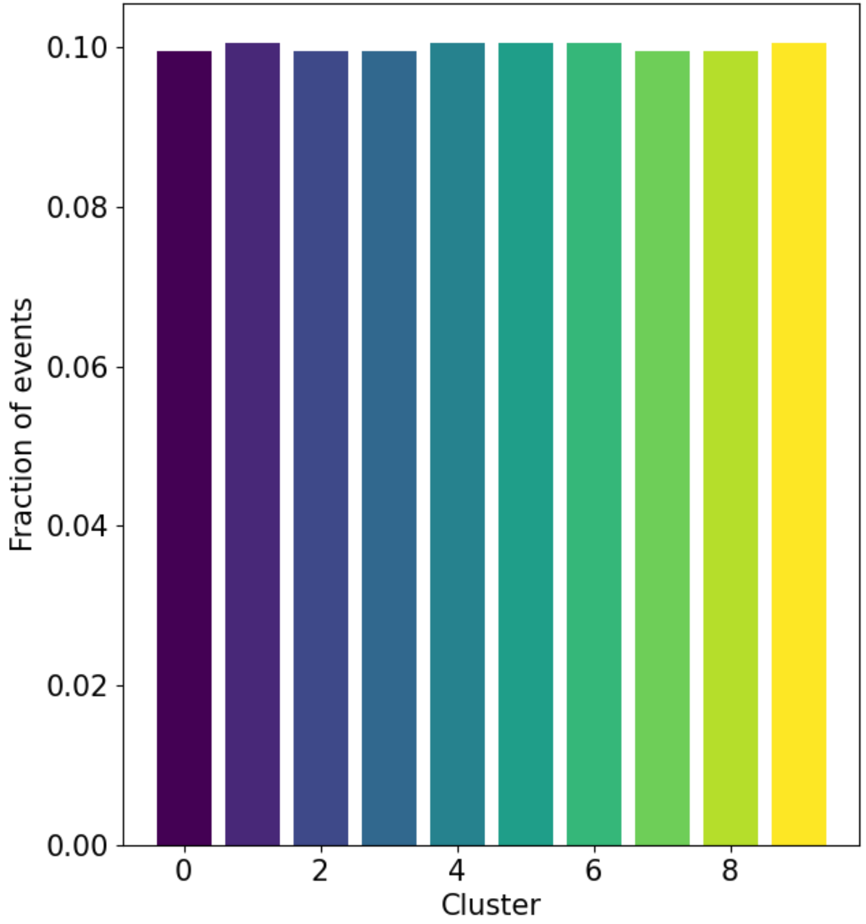
The results of the fit signals from the calorimeter and hodoscope

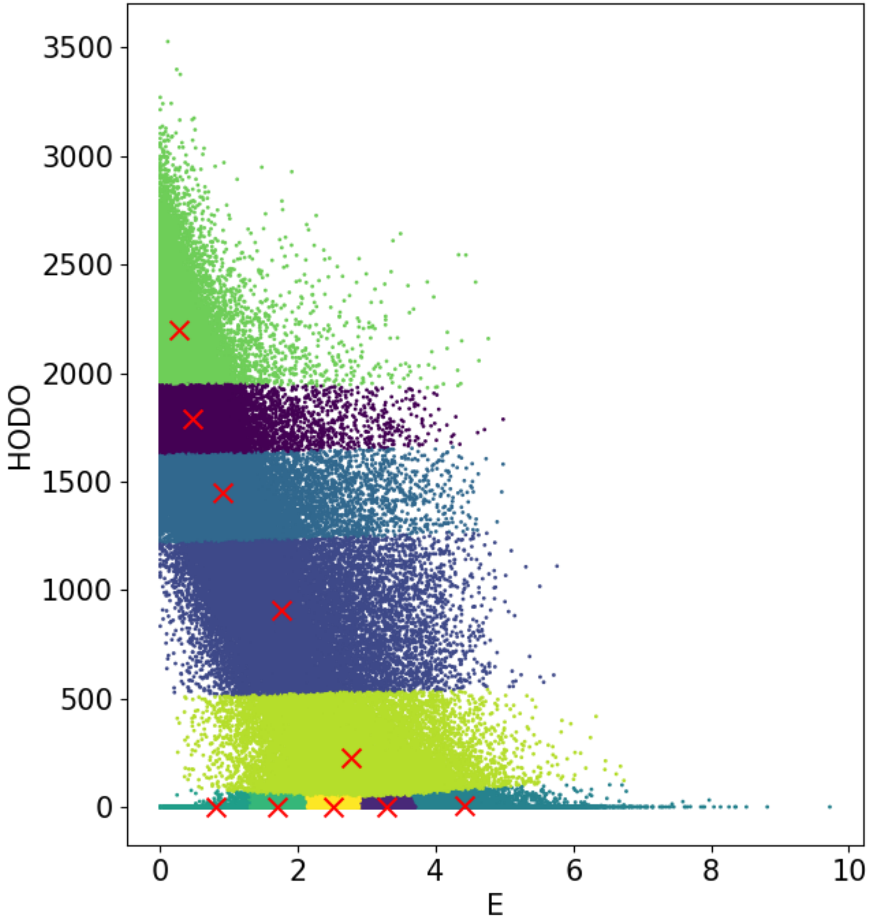




Good agreement of fit results for the calorimeter
The fit procedure for the hodoscope is in the process of developing

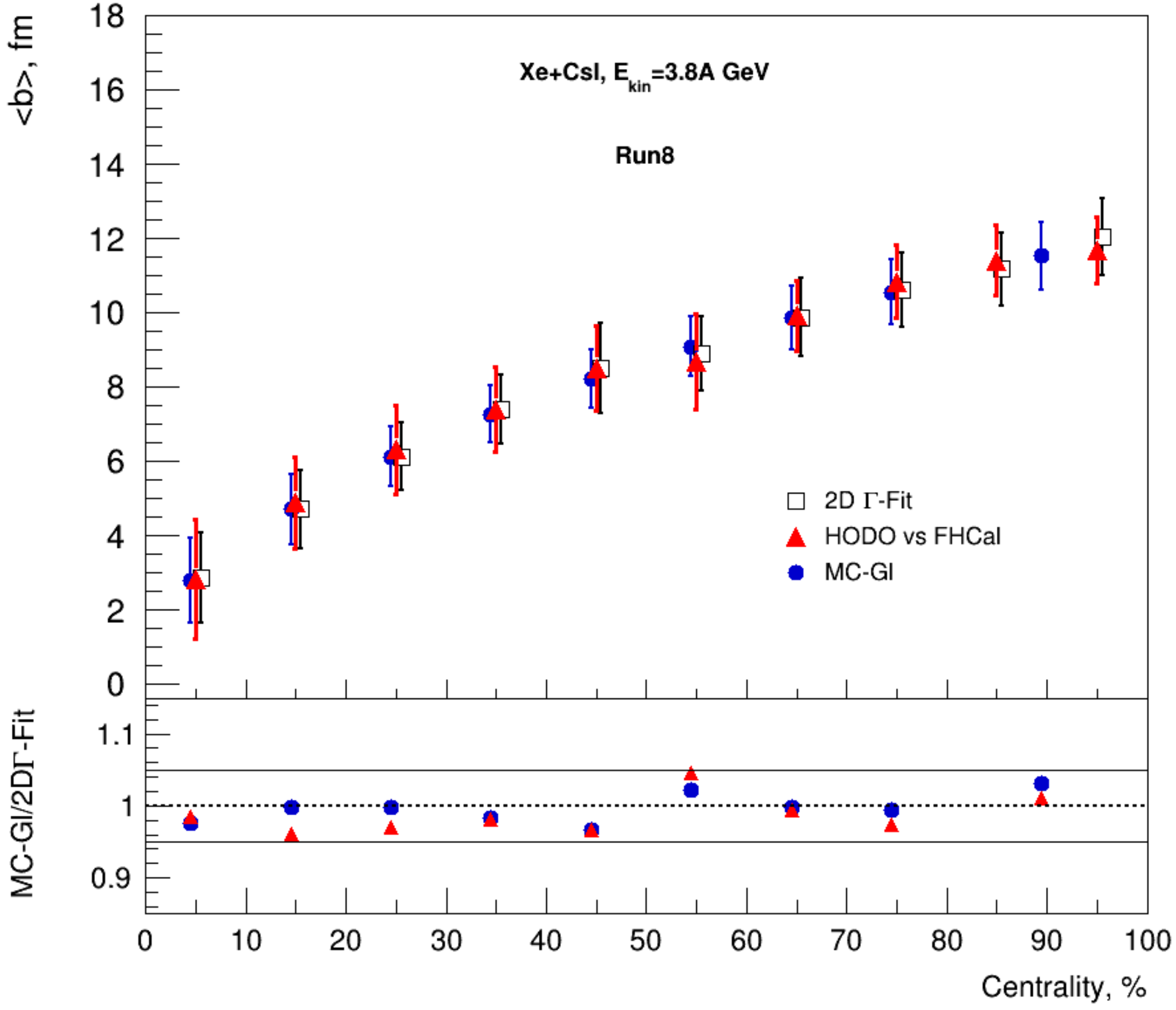
Centrality determination using an forward calorimeter and hodoscope

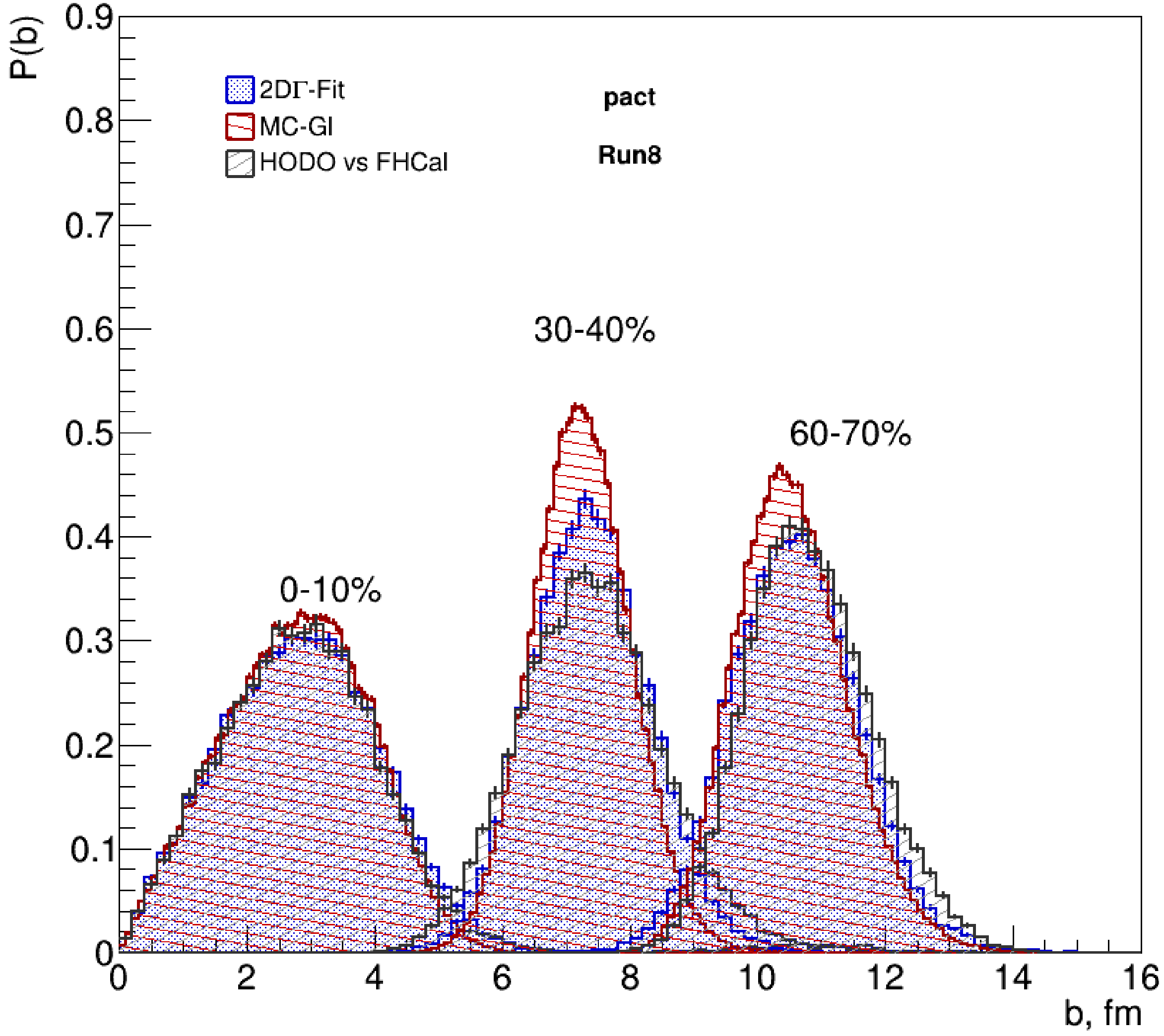




The K-means method allows to divide a two-dimensional distribution into centrality classes.
In order to correctly apply the class boundaries, it is necessary to match the simulation results with the experiment

Comparison with MC-Glauber fit





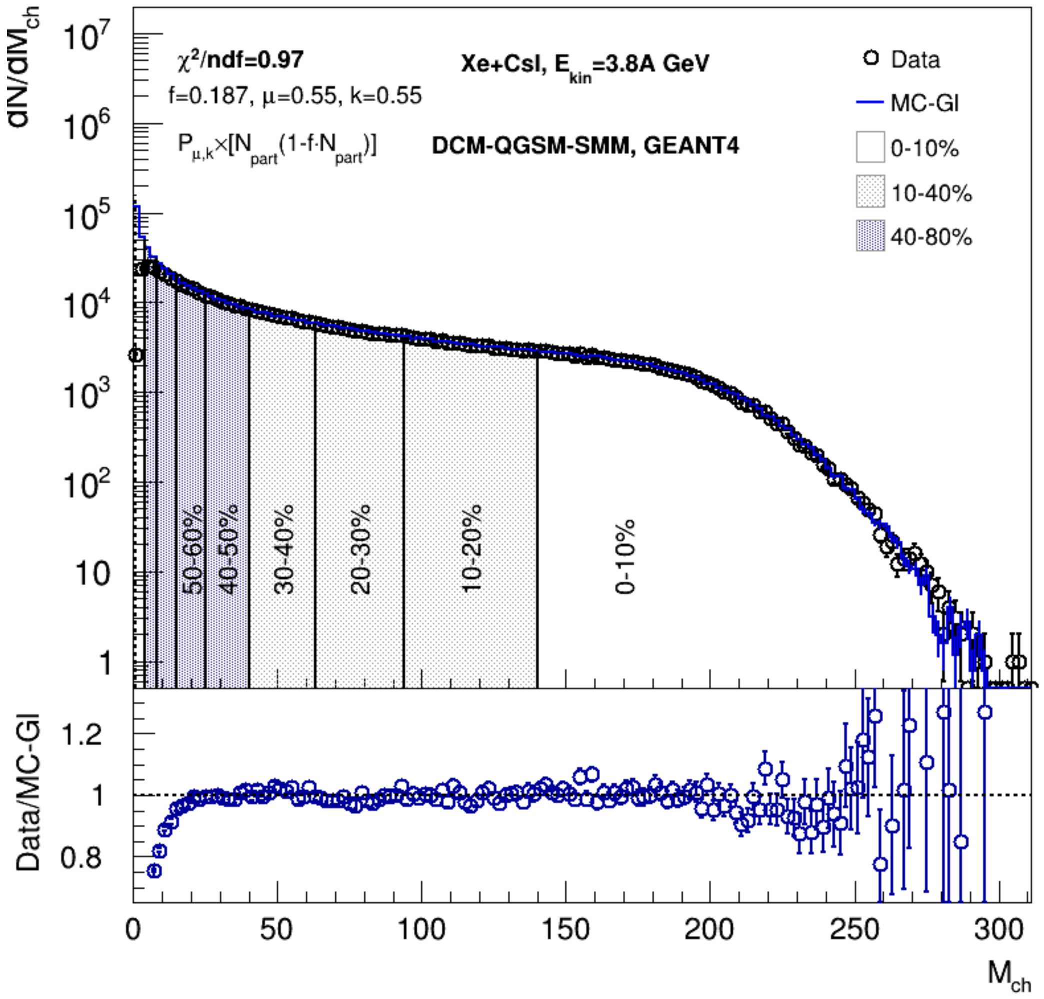
There is agreement within 5%.

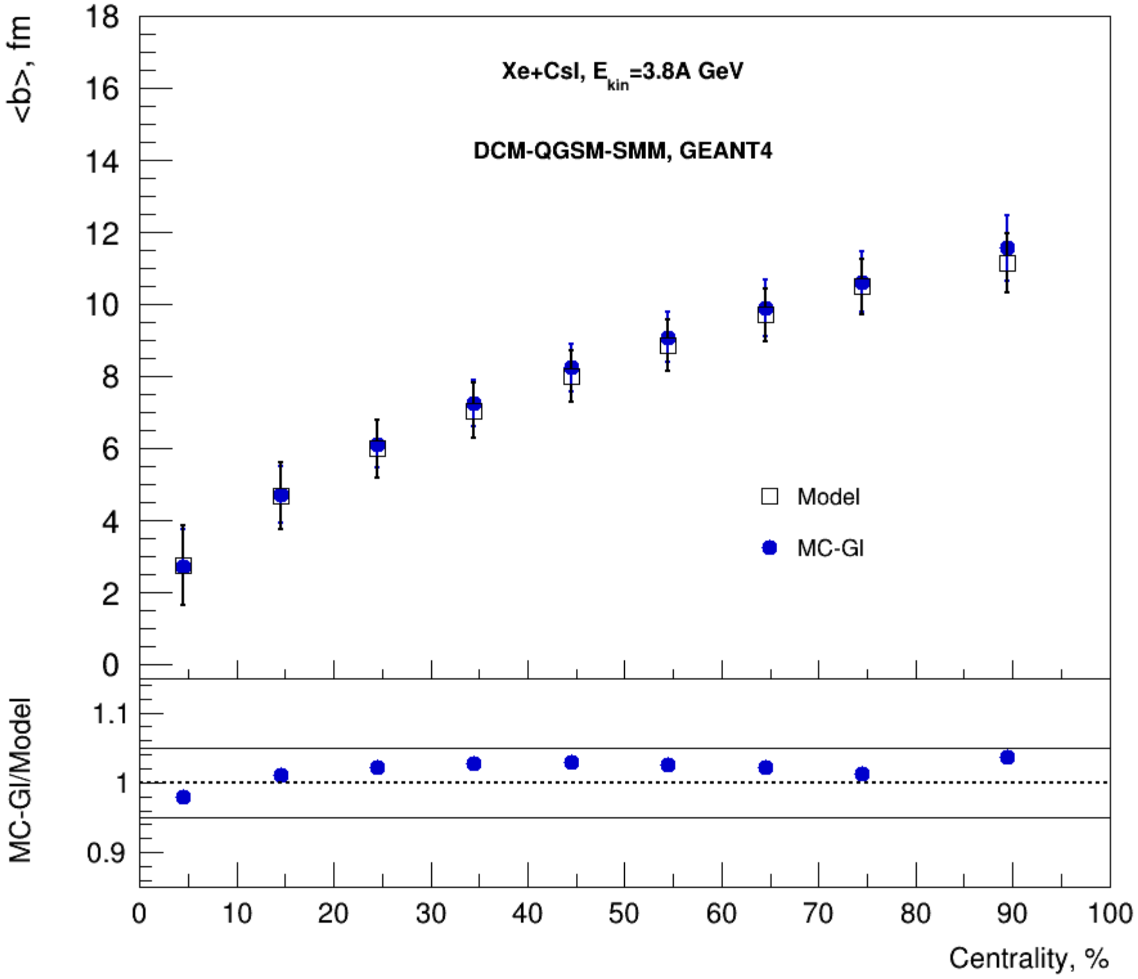
Summary

- The Bayesian inversion method reproduce charged particle multiplicity for fixed-target experiment at BM@N
- A new approach for centrality determination with energy of spectators and multiplicity of charged particles was proposed and tested on the data from BM@N experiment
- The procedure for centrality determination based on the signal from the hodoscope and the energy from the FHCal was developed
- The proposed methods for centrality determination are in good agreement with the classical approach based on the Glauber model

Конфуз матрицы

Centrality determination for reconstructed data

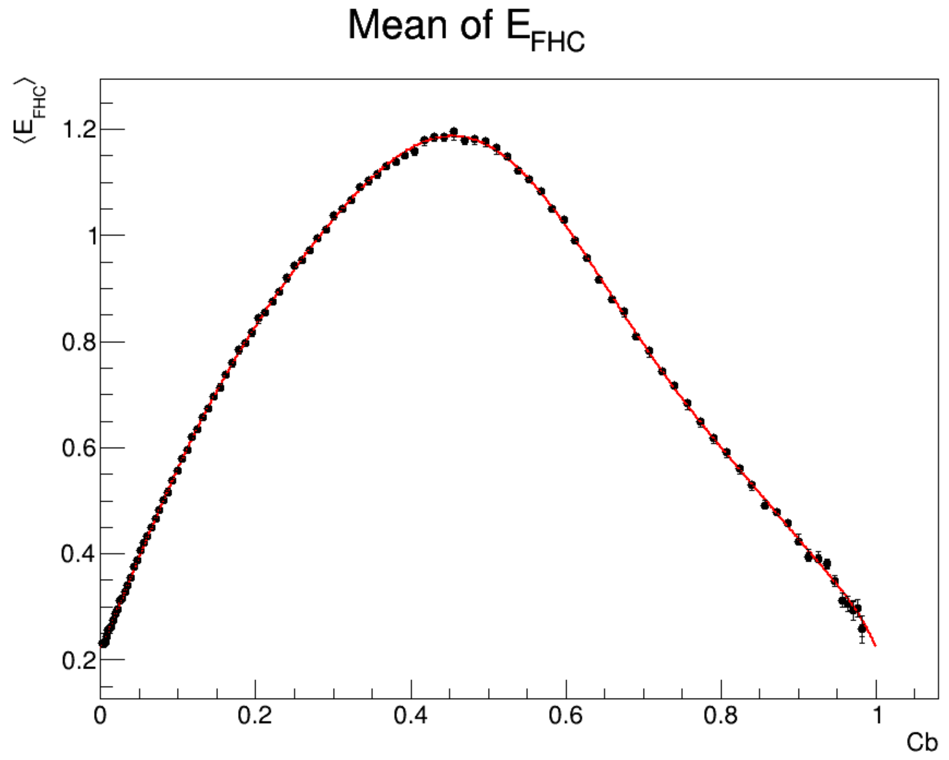


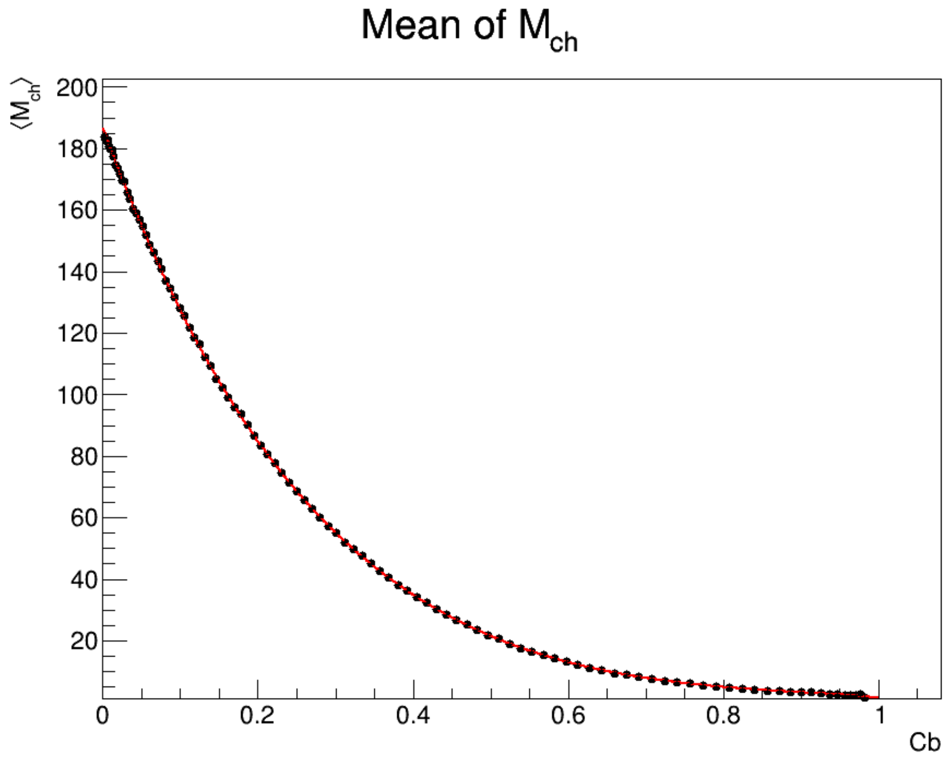


Good agreement with data

Thank you for your attention!

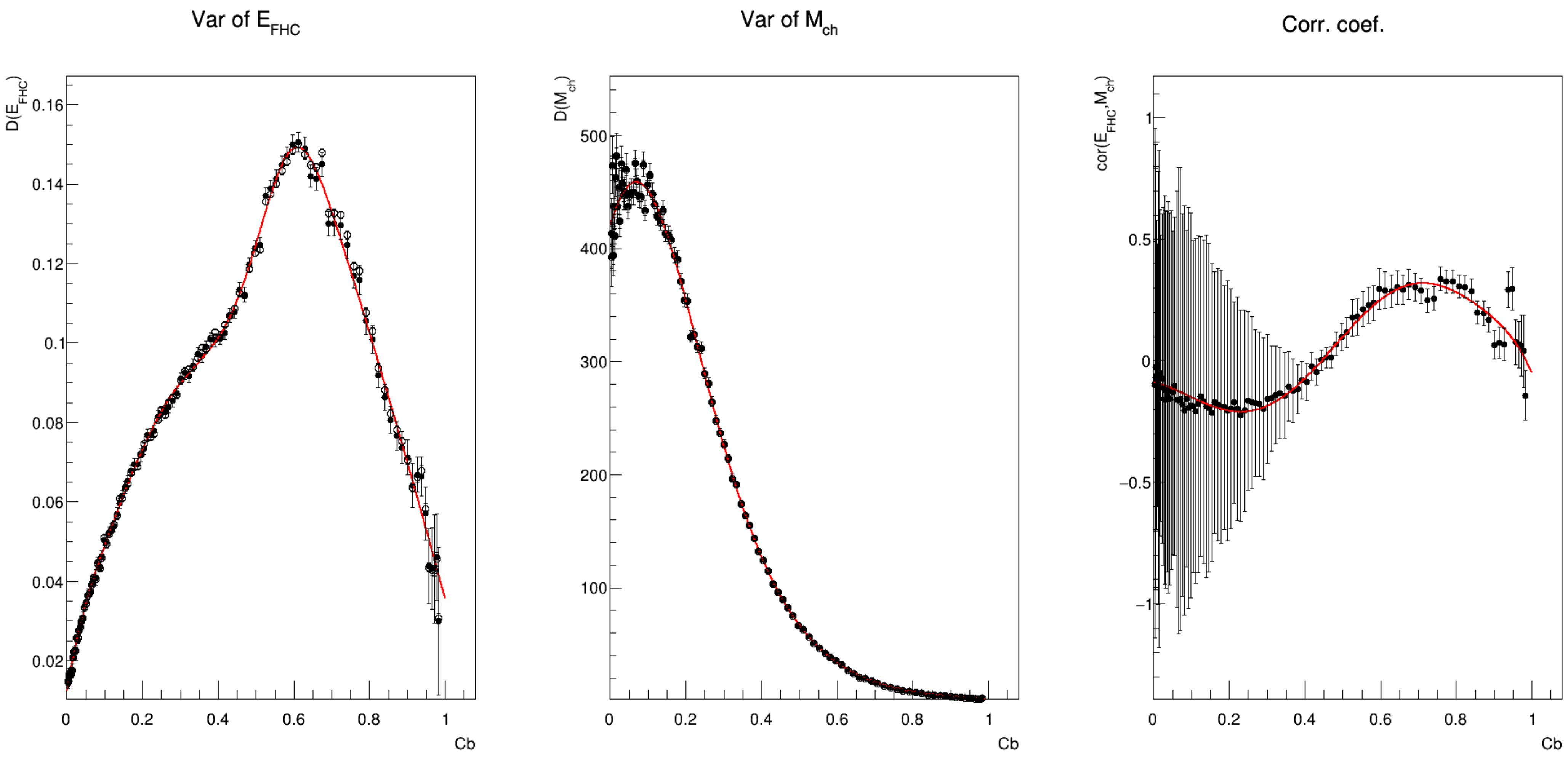
Dependence of the average value of multiplicity and energy on centrality





Good fit quality

Dependence of the variance of multiplicity and energy on centrality



Good fit quality

Corrections for efficiency and pileup

- **Correction for efficiency of normalized multiplicity distribution P(M)**

$$P(M) = \frac{dN}{dM} / N^{ev}_{ideal} = \frac{N^{ev}_{raw}}{N^{ev}_{ideal}} \cdot \frac{1}{N^{ev}_{raw}} \frac{dN_r}{dM} = \frac{1}{K} \cdot Norm.Histogr$$

$$Eff = \frac{N^{ev}_{raw}}{N^{ev}_{ideal}} = \frac{1}{K}$$ integral efficiency

- **Fit function for multiplicity distribution P(M)**

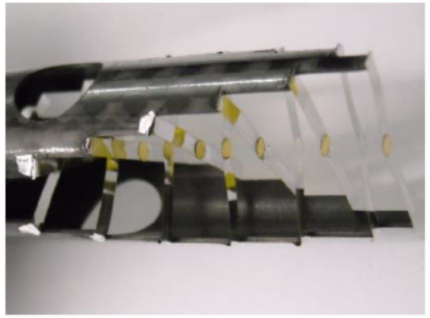
$$F(M) = K \cdot P_{total}(M), \;\; P_{total}(M) = N_p \cdot P_{pu}(M) + (1 - N_p) \cdot P(M)$$

μ, f, k, K, N_p- fit parameters, $F(M) -$ fit function, corrected for efficiency and pileup

Event cleaning in HADES

Segmented gold target:

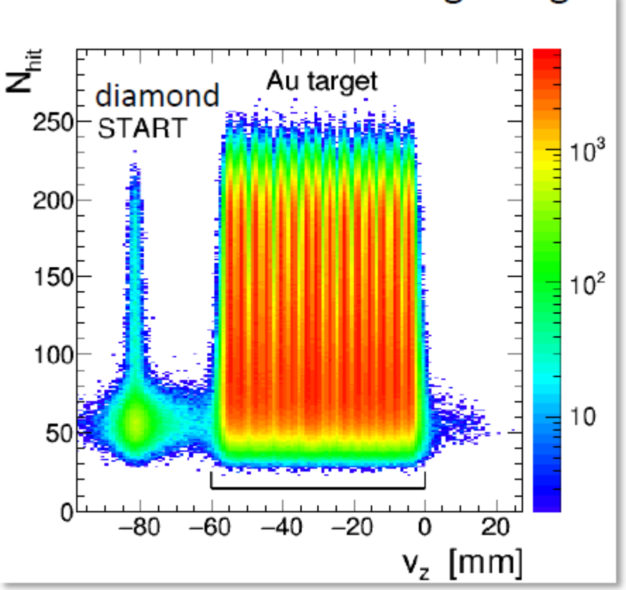
- ^{197}Au material
- 15 discs of Ø = 2.2 mm mounted on kapton strips
- Δz = 3.6 mm
- 2.0% interaction prob.

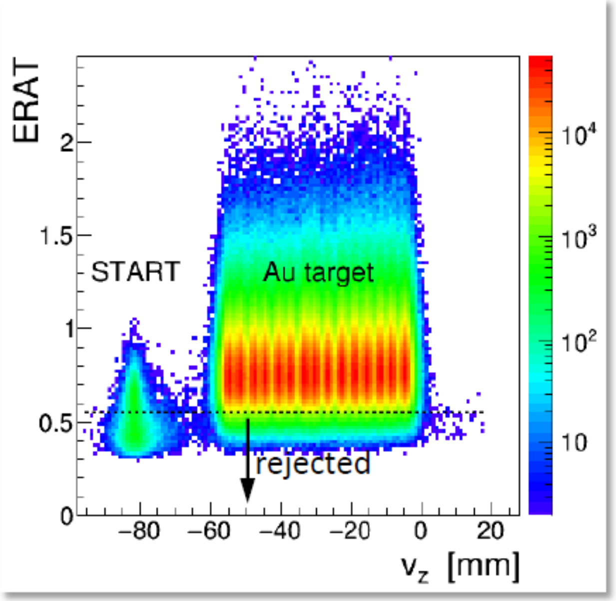


Kindler et al.,
NIM A 655 (2011) 95

Remove Au+C bkgd on the kapton with a cut on $ERAT = \sum E_t / \sum E_l$

Event vertex cut on target region

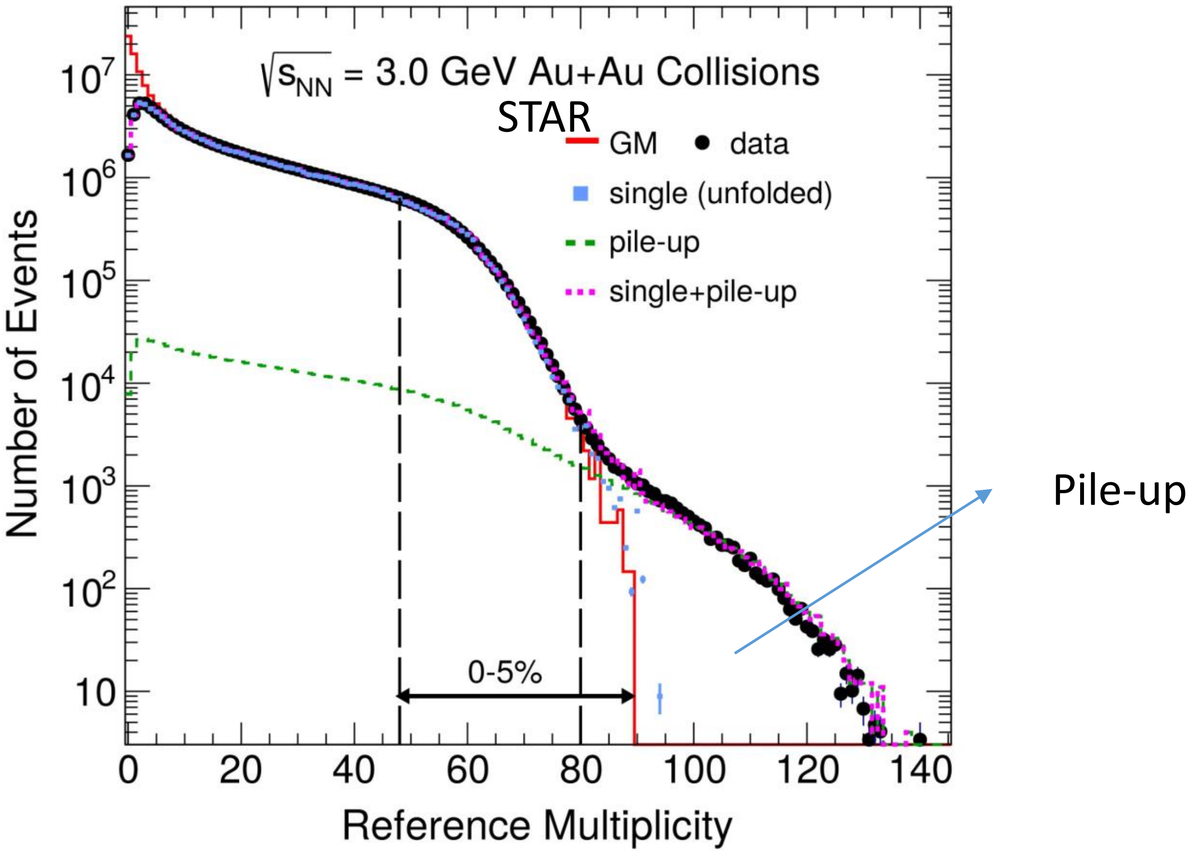




beam direction

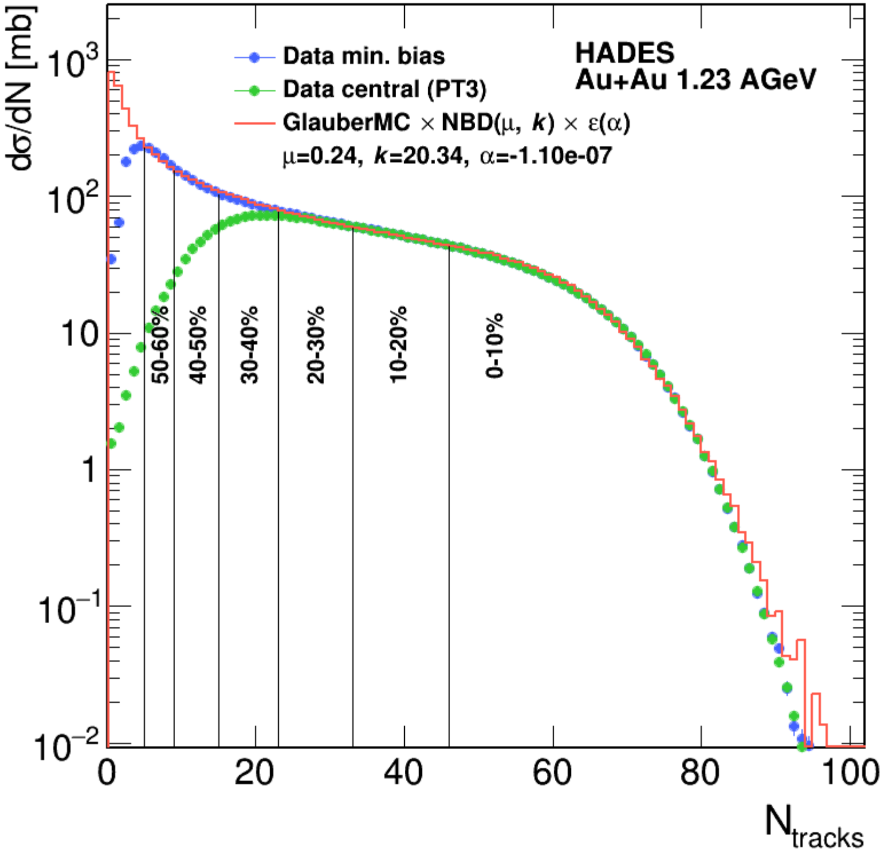
http://indico.oris.mephi.ru/event/221/session/1/contribution/1/material/slides/0.pdf

Centrality determination in the FIX-target experiments



Reference multiplicity distributions (black markers) in the kinematic acceptance within −0.5 < y < 0 and 0.4 < pT < 2.0 GeV/c ,
GM (red histogram), and single and pile-up contributions from unfolding.

https://arxiv.org/abs/2112.00240



The cross section as a function of Ntracks for minimum bias (blue symbols) and central (PT3 trigger, green symbols) data in comparison with a fit using the Glauber MC model (red histogram).

https://arxiv.org/abs/1712.07993

Reconstruction of *b*

- Normalized multiplicity distribution $P(N_{ch})$

$$P(N_{ch}) = \int_0^1 P(N_{ch}|c_b)dc_b$$

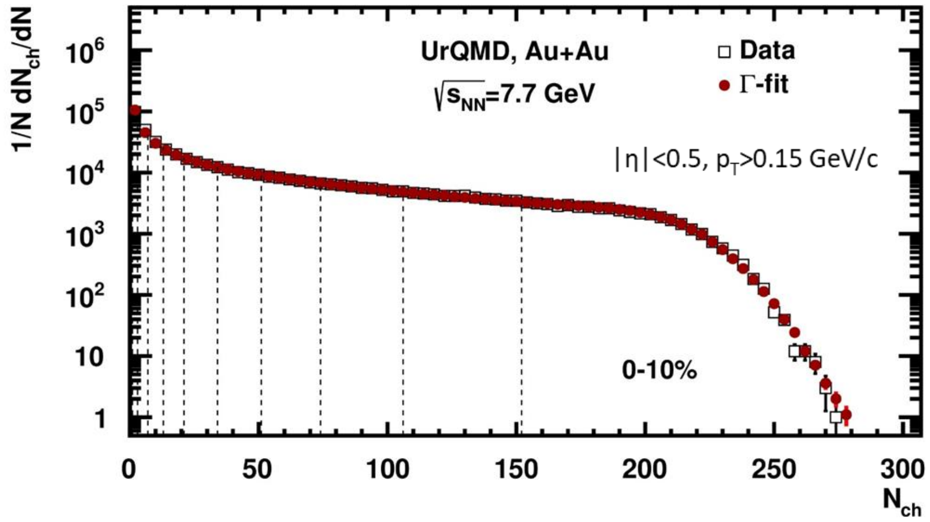
- Find probability of *b* for fixed range of N_{ch} using Bayes' theorem:

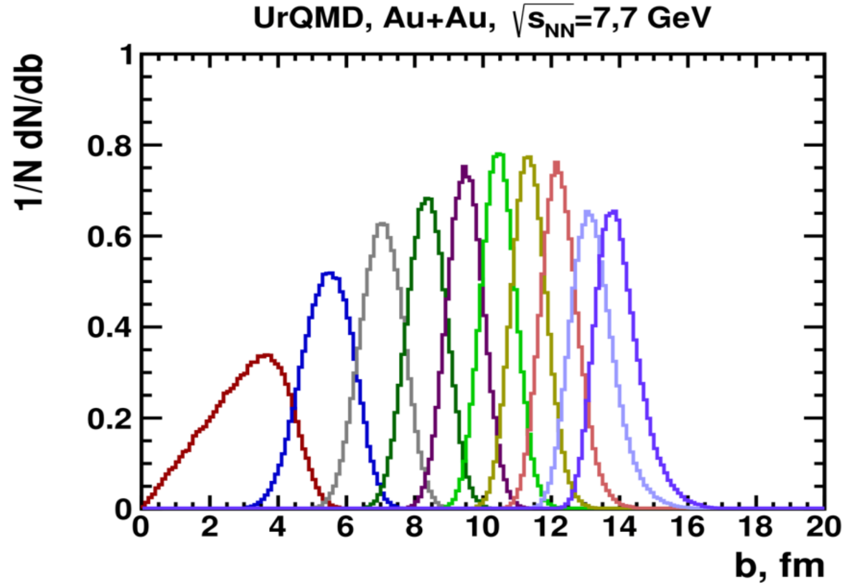
$$P(b|n_1 < N_{ch} < n_2) = P(b)\frac{\int_{n_1}^{n_2} P\,(N_{ch}|b)dN_{ch}}{\int_{n_1}^{n_2} P\,(N_{ch})dN_{ch}}$$

- **The Bayesian inversion method consists of 2 steps:**

–Fit normalized multiplicity distribution with $P(N_{ch})$

–Construct $P(b|N_{ch})$ using Bayes' theorem with parameters from the fit





R. Rogly, G. Giacalone and J. Y. Ollitrault, Phys.Rev. C98 (2018) no.2, 024902

Implementation in MPD: https://github.com/Dim23/GammaFit