



# Hypernuclear properties and hyperonic interactions

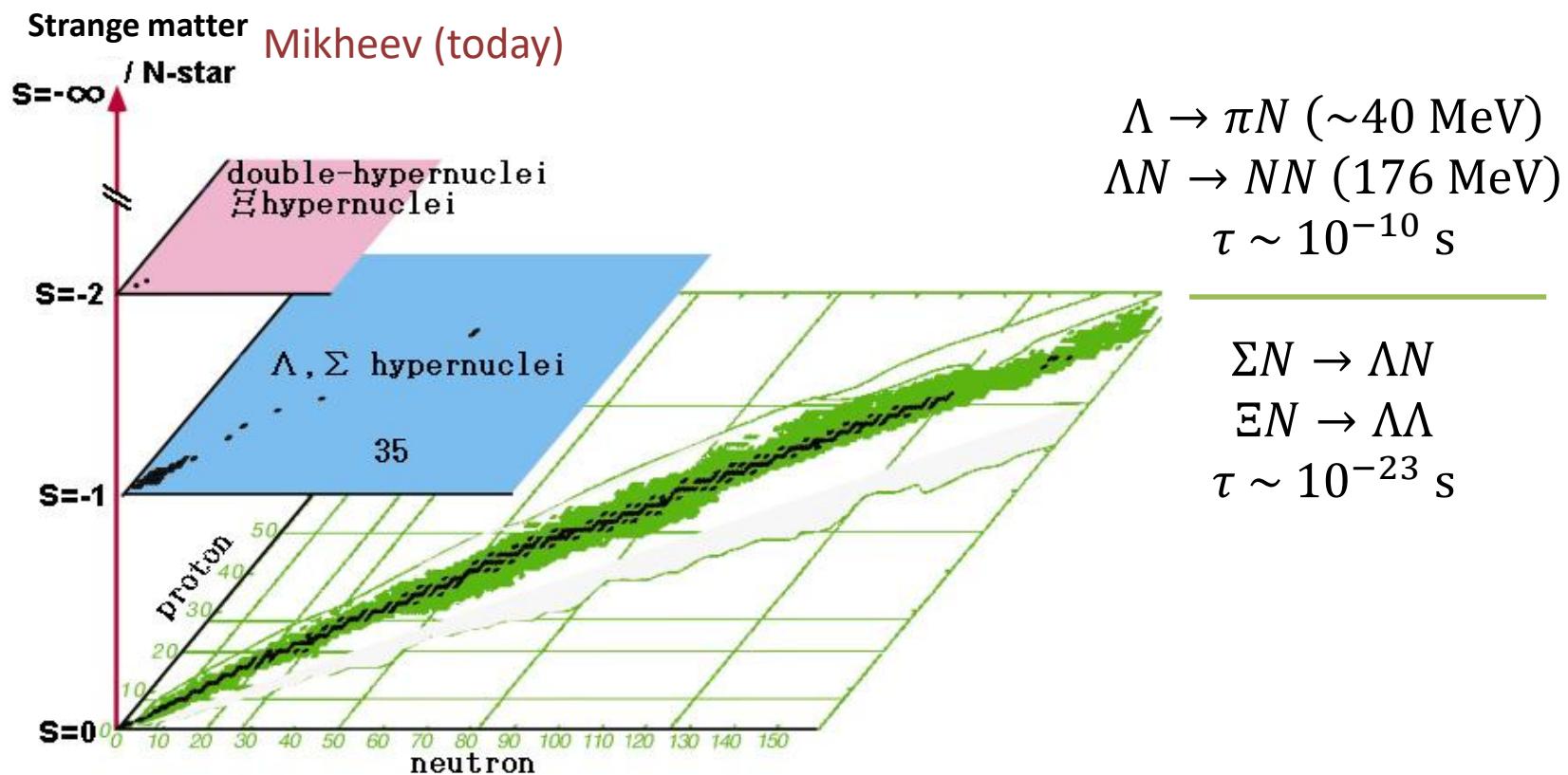
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# Hypernuclear systems

- Experiment vs theory – state of art
- Some hot points:
  - Drip lines
  - Hypertriton
  - Double-strange systems



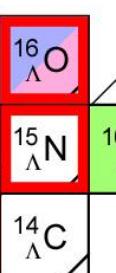
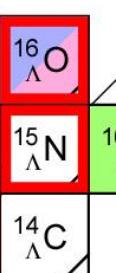
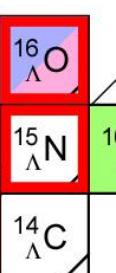
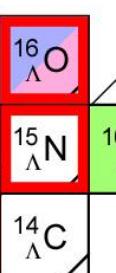
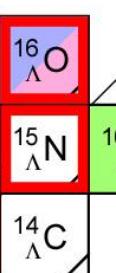
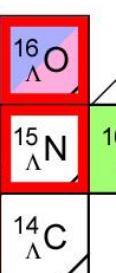
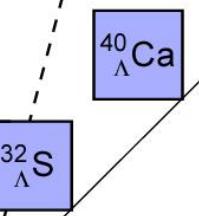
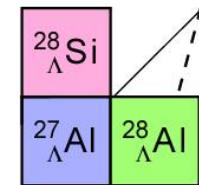
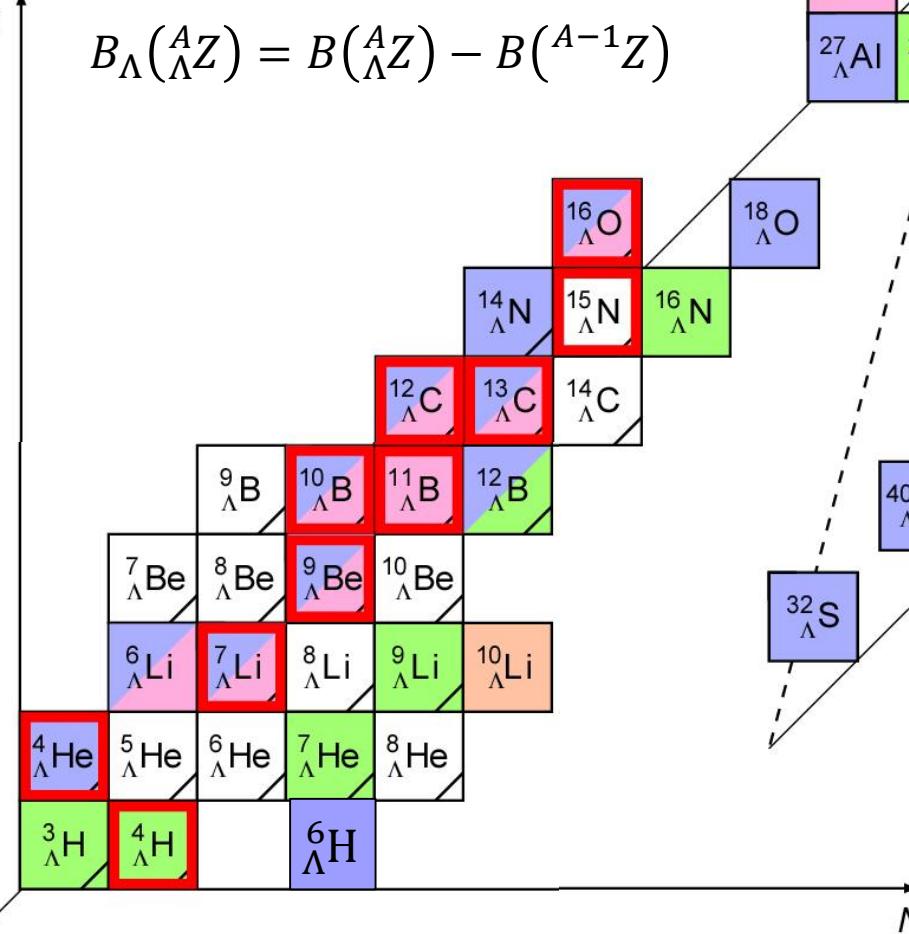
# $\Lambda$ -hypernuclei

<= Few-body / Cluster models

Mean-field models =>

$\Lambda$  separation energies

$$B_\Lambda(^A_Z\Lambda) = B(^A_Z\Lambda) - B(^{A-1}_Z\Lambda)$$

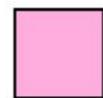


Spectroscopic studies by

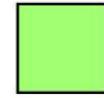
( $K^-, \pi^-$ )  
( $K_{\text{stop}}, \pi^-$ )  
( $K_{\text{stop}}, \pi^+$ )



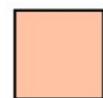
$\gamma$ -ray data



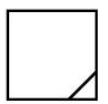
$(\pi^+, K^+)$



$(e, e' K^+)$

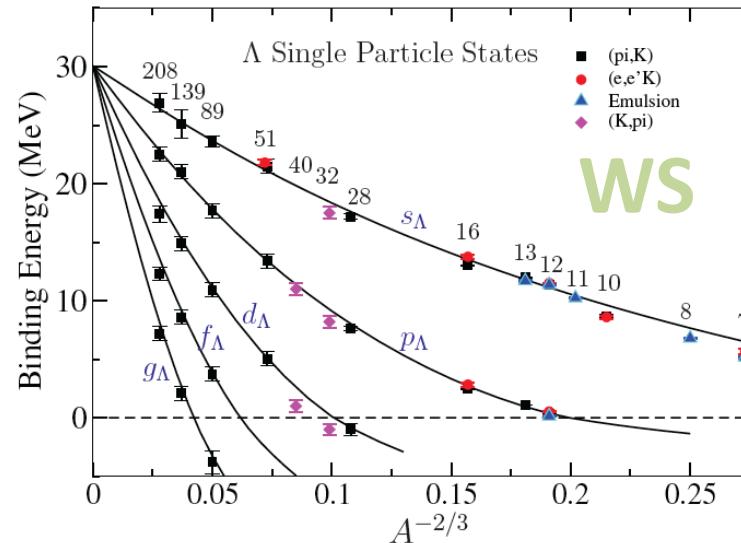
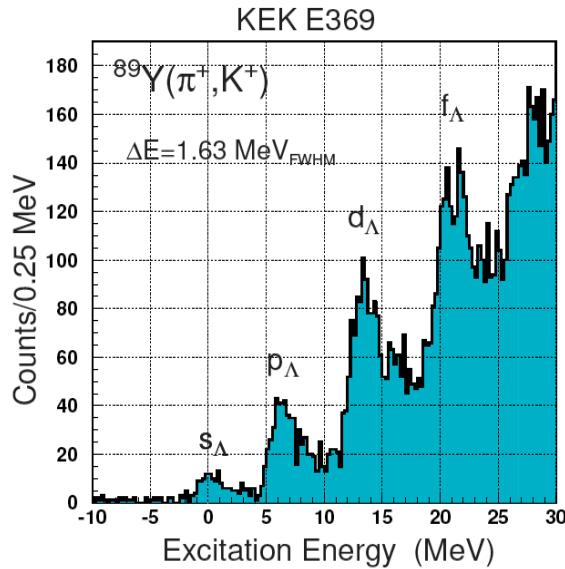


$(\pi^-, K^+)$

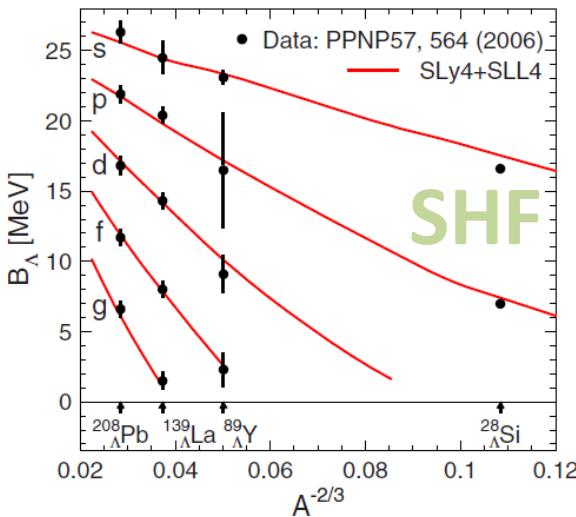


emulsion  
data

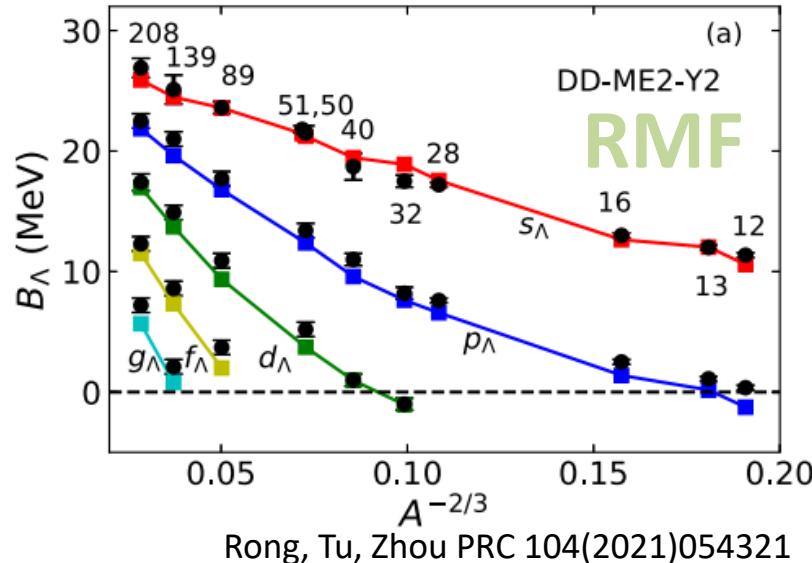
# $\Lambda$ -hypernuclei



Gal, Hungerford, Millener RMP 88(2016)035004



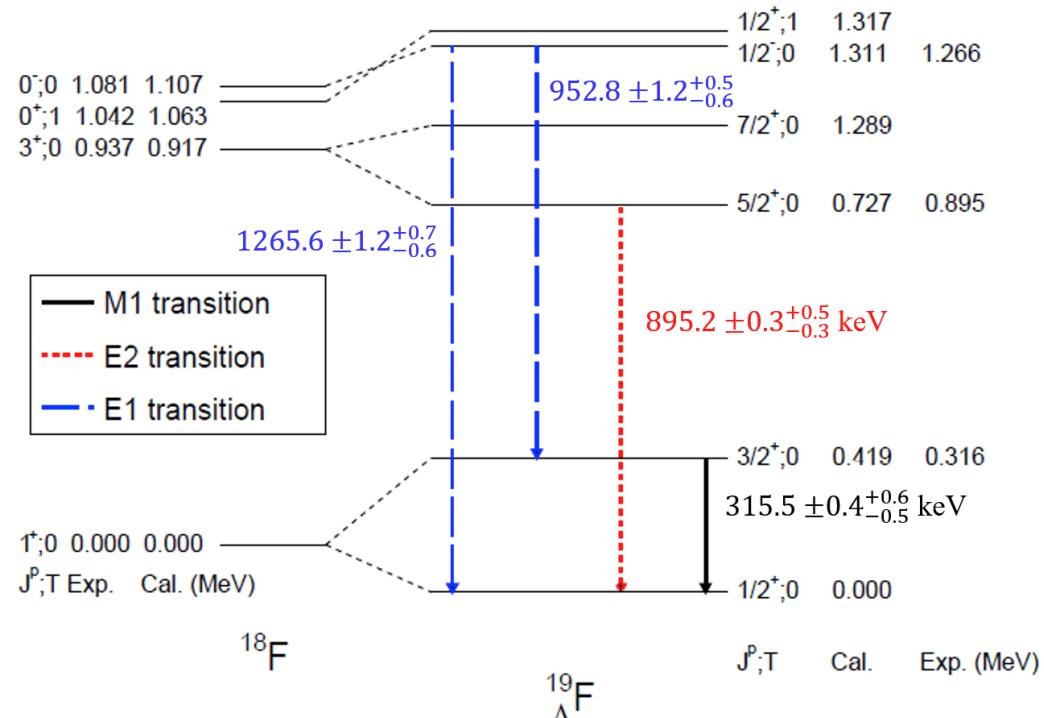
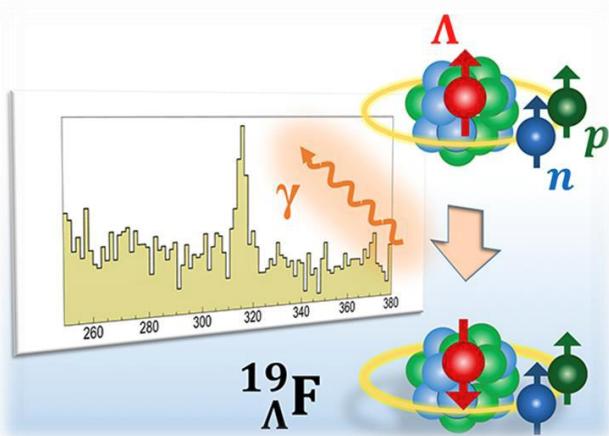
Schulze, Hiyama PRC 90(2014)047301



# $\Lambda$ -hypernuclei

$\Lambda$  spin-orbit splitting (keV): 150 in  $^{13}_{\Lambda}\text{C}$  & related 43 in  $^9_{\Lambda}\text{Be}$

Precise structure  $p$ - hypernuclei  $^7_{\Lambda}\text{Li}$ ,  $^9_{\Lambda}\text{Be}$ ,  $^{10,11}_{\Lambda}\text{B}$ ,  $^{12,13}_{\Lambda}\text{C}$ ,  $^{15}_{\Lambda}\text{N}$ ,  $^{16}_{\Lambda}\text{O}$



$$U_{\Lambda N} = U_0 + U_S(\mathbf{s}_N \mathbf{s}_\Lambda) + W_{LS}(\mathbf{l}_N \mathbf{s}_\Lambda) + W'_{LS}(\mathbf{l}_\Lambda \mathbf{s}_N) + TS_{12}$$

$$B_\Lambda(A \rightarrow \infty) = U_0 \approx -28 \text{ MeV}$$

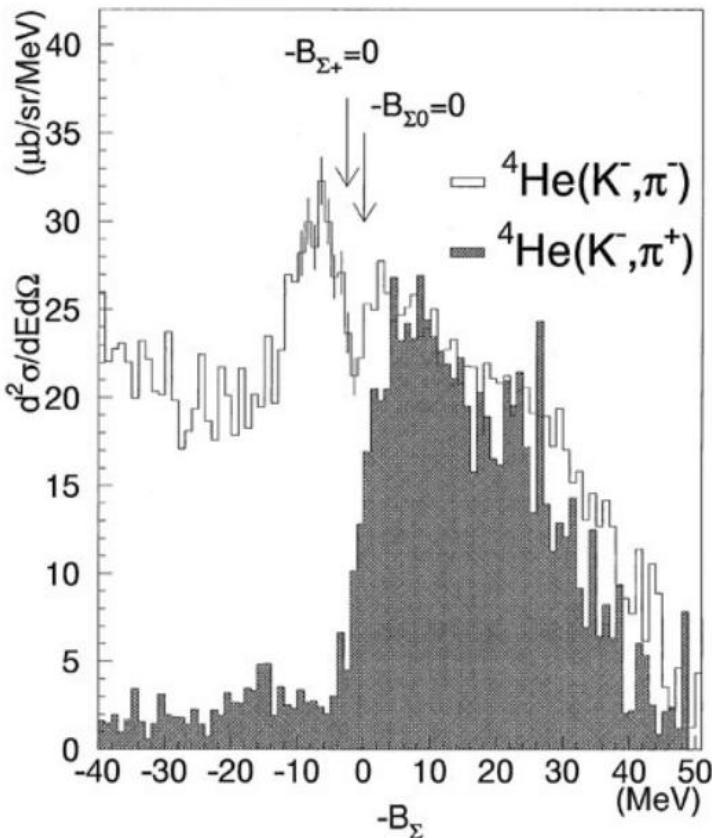
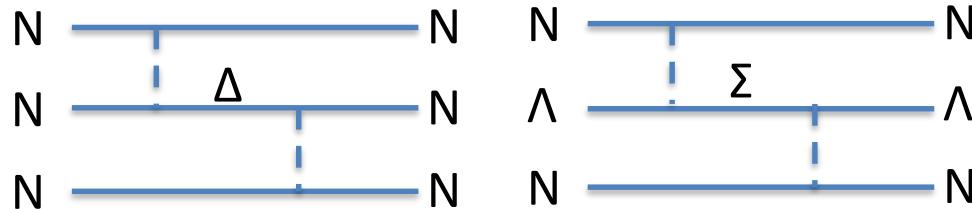
$$U_S, W_{LS}, W'_{LS}, T - \text{small}$$

# $\Sigma$ -hypernuclei

$$\Sigma^\pm \rightarrow N\pi (\sim 113 \text{ MeV})$$

$$\Sigma^0 \rightarrow \Lambda\gamma (74 \text{ MeV})$$

$$\Sigma N \rightarrow \Lambda N (\sim 75 \text{ MeV})$$



$$B_{\Sigma+}({}^4\text{He}) = 4.4 \pm 0.3 \pm 1 \text{ MeV}$$

$$\Gamma = 7.0 \pm 0.7^{+1.2}_{-0.0} \text{ MeV}$$

$$U_\Sigma(r) = (U_0 + U_L(\tau_{core}\tau_\Sigma)/A) \frac{\rho(r)}{\rho_0}$$

$$U_0 = +30 \pm 20 \text{ MeV}$$

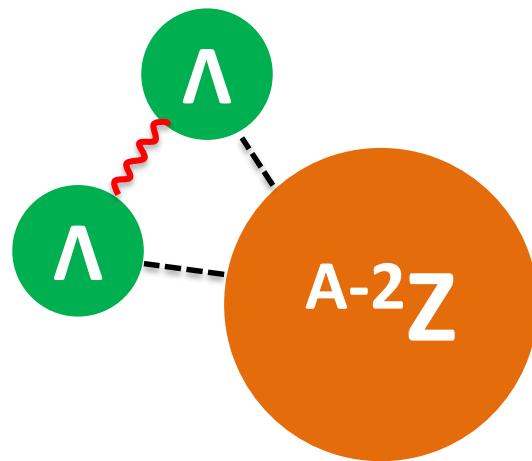
$$U_L \approx 80 \text{ MeV}$$

Excitation energy spectra of  ${}^4\text{He}(K^-, \pi^-)$  at 600 MeV/c  $K^-$  momentum (BNL AGS) [Nagae et al PhysRevLett 80 (1998)1605]

T. Nagae, in HandBook in Nuclear Physics. Springer 2023

# Double-strangeness hypernuclei

a unique source of information on baryon interactions  
in the S=-2 sector



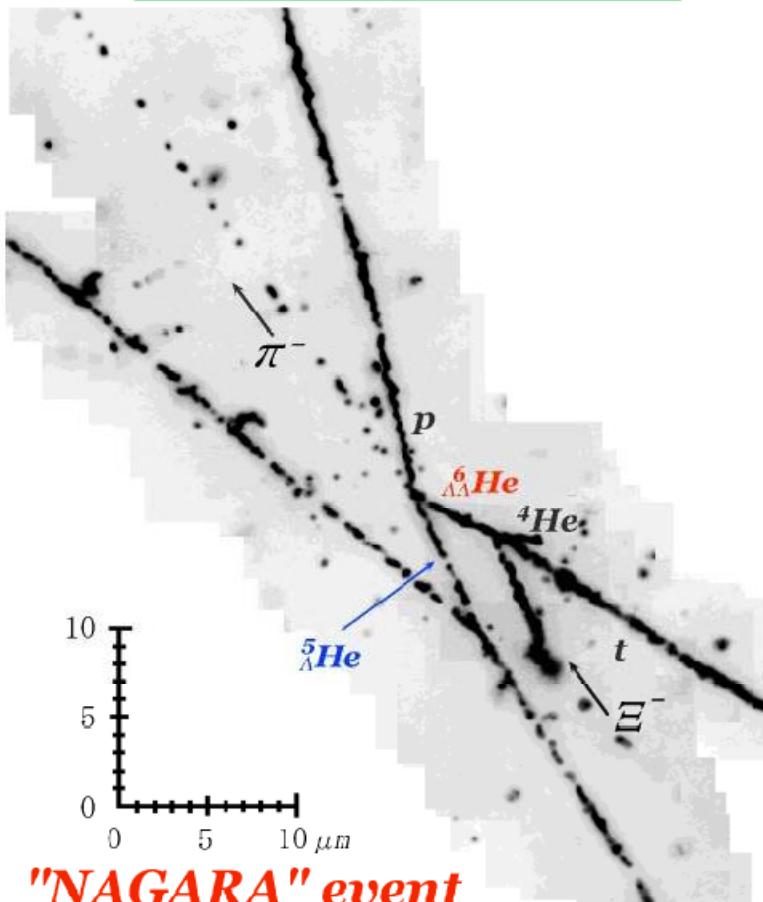
$$B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^AZ) = B({}_{\Lambda\Lambda}^AZ) - B({}^{A-2}Z)$$

$$\Delta B_{\Lambda\Lambda} = B_{\Lambda\Lambda} - 2B_\Lambda$$

# Double-strangeness hypernuclei

$^{6}_{\Lambda\Lambda}\text{He}$  double-hypernucleus

*Unique interpretation!!*



- C(K<sup>-</sup>, K<sup>+</sup>) reaction to produce Ξ<sup>-</sup> then stop it in emulsion  
(H. Takahashi et al., PRL87(2001)212502)

- Binding energy of  ${}^{6}_{\Lambda\Lambda}\text{He}$  is obtained to be

$$B_{\Lambda\Lambda} = 7.3 \pm 0.3 \text{ MeV}$$

(from  $\alpha+2\Lambda$ )

- In order to extract  $\Lambda\Lambda$  interaction, we take

$$\Delta B_{\Lambda\Lambda} = B_{\Lambda\Lambda} - 2B_{\Lambda}({}^5_{\Lambda}\text{He})$$
$$= 1.0 \pm 0.3 \text{ MeV}$$

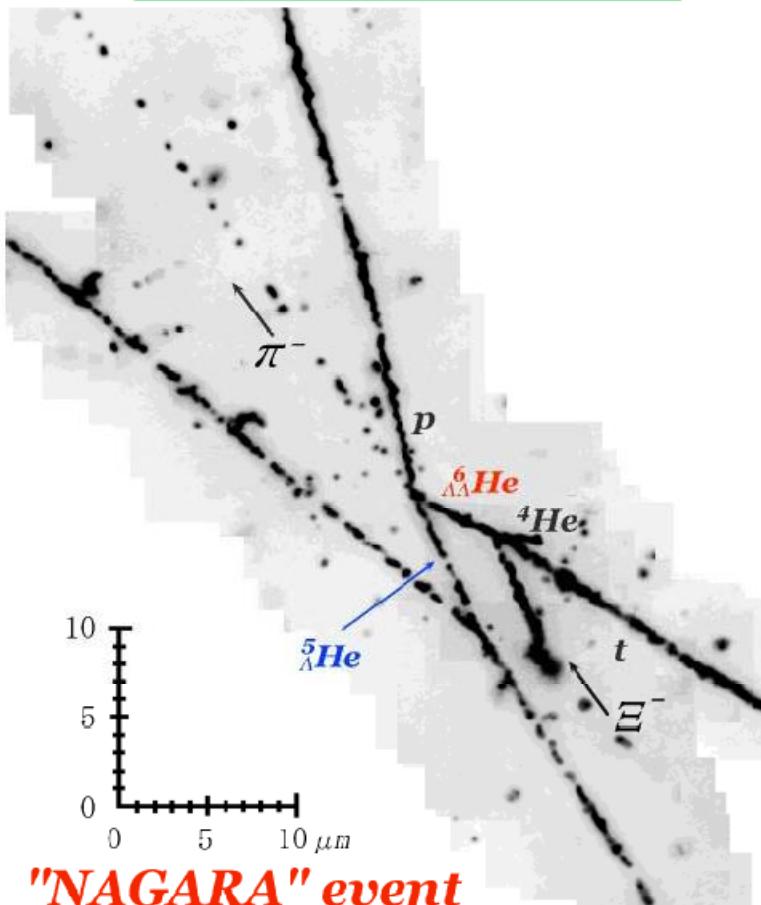
→ weakly attractive

Phys Rev Lett 87 (2001) 212502

# Double-strangeness hypernuclei

$^{6}_{\Lambda\Lambda}\text{He}$  double-hypernucleus

*Unique interpretation!!*



- C(K<sup>-</sup>, K<sup>+</sup>) reaction to produce Ξ<sup>-</sup> then stop it in emulsion  
(H. Takahashi et al., PRL87(2001)212502)

- Hyperon binding energy of  ${}^{6}_{\Lambda\Lambda}\text{He}$  is obtained to be

$$B_{\Lambda\Lambda} = 6.91 \pm 0.16 \text{ MeV}$$

(from  $\alpha+2\Lambda$ )

- In order to extract  $\Lambda\Lambda$  interaction, we take

$$\Delta B_{\Lambda\Lambda} = B_{\Lambda\Lambda} - 2B_\Lambda({}^5_{\Lambda}\text{He})$$
$$= 0.67 \pm 0.17 \text{ MeV}$$

→ weakly attractive

Ahn et al Phys Rev C 88 (2013) 014003

# Double-strangeness hypernuclei

K. Nakazawa, in HandBook in Nuclear Physics. Springer 2023

Ev. name	Nuclide	Target	$B_{\Lambda\Lambda}$ (MeV)	$\Delta B_{\Lambda\Lambda}$ (MeV)	Comments
Nagara	$^6_{\Lambda\Lambda}\text{He}$	$^{12}\text{C}$	$6.91 \pm 0.16$	$0.67 \pm 0.17$	Uniquely identified
Danysz et al.	$^{10}_{\Lambda\Lambda}\text{Be}$	$^{12}\text{C}$	$14.7 \pm 0.4$	$1.3 \pm 0.4$	$^{10}_{\Lambda\Lambda}\text{Be} \rightarrow ^9_{\Lambda}\text{Be}^*$ ( $Ex. = 3.0 \text{ MeV}$ )
E176	$^{13}_{\Lambda\Lambda}\text{B}$	$^{14}\text{N}$	$23.3 \pm 0.7$	$0.6 \pm 0.8$	$^{13}_{\Lambda\Lambda}\text{B} \rightarrow ^{13}_{\Lambda}\text{C}^*$ ( $Ex. = 4.9 \text{ MeV}$ )
Demachi-Yanagi	$^{10}_{\Lambda\Lambda}\text{Be}^*$	$^{12}\text{C}$	$11.90 \pm 0.13$	$-1.52 \pm 0.15$	Most probable (topology) $Ex. \approx 2.8 \text{ MeV}$ for $^{10}_{\Lambda\Lambda}\text{Be}^*$
Mikage	$^6_{\Lambda\Lambda}\text{He}$	$^{12}\text{C}$	$10.01 \pm 1.71$	$3.77 \pm 1.71$	Most probable (mesonic decay)
	$^{11}_{\Lambda\Lambda}\text{Be}$	$^{12}\text{C}$	$22.15 \pm 2.94$	$3.95 \pm 3.00$	
	$^{11}_{\Lambda\Lambda}\text{Be}$	$^{14}\text{N}$	$23.05 \pm 2.59$	$4.85 \pm 2.63$	
Hida	$^{11}_{\Lambda\Lambda}\text{Be}$	$^{12}\text{C}$	$20.83 \pm 1.27$	$2.61 \pm 1.34$	
	$^{12}_{\Lambda\Lambda}\text{Be}$	$^{14}\text{N}$	$20.48 \pm 1.21$	$(2.00 \pm 1.21)$	Assumed 10.24 MeV for $B_{\Lambda}(^{11}_{\Lambda}\text{Be})$
Mino	$^{10}_{\Lambda\Lambda}\text{Be}$	$^{16}\text{O}$	$15.05 \pm 0.11$	$1.63 \pm 0.14$	
	$^{11}_{\Lambda\Lambda}\text{Be}$	$^{16}\text{O}$	$19.07 \pm 0.11$	$1.87 \pm 0.37$	Most probable ( $\chi^2$ minimum)
	$^{12}_{\Lambda\Lambda}\text{Be}$	$^{16}\text{O}$	$13.68 \pm 0.11$	$-2.7 \pm 1.0$	
D001	$^8_{\Lambda\Lambda}\text{Li}$	$^{12}\text{C}$	$17.50 \pm 1.46$	$6.34 \pm 1.46$	
	$^{10}_{\Lambda\Lambda}\text{Be}$	$^{14}\text{N}$	$15.05 \pm 2.78$	$1.63 \pm 2.78$	Likely by $B_{\Lambda\Lambda}$

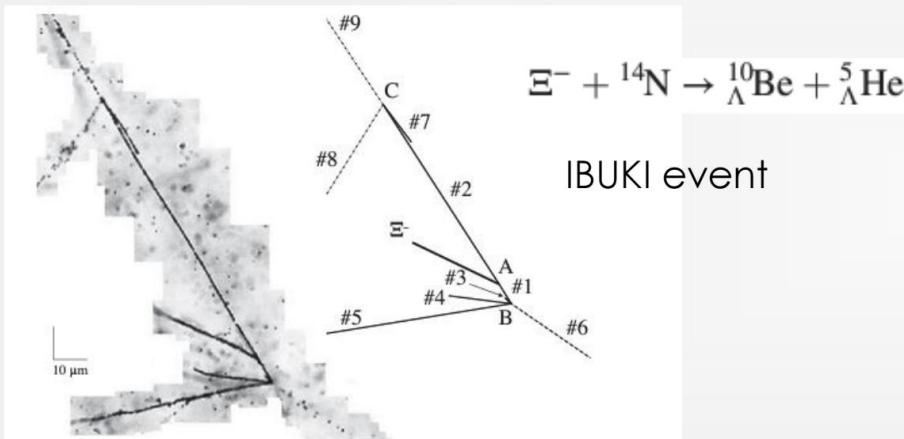
# Double-strangeness hypernuclei

## $\Xi^-$ -Nuclear Bound States

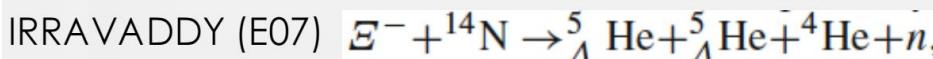
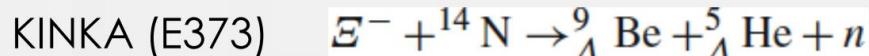
KEK E373 and J-PARC E07 experiments

Coulomb-Assisted  $\Xi^-$ - $^{14}\text{N}$   $1\text{p}_{\Xi^-}$  nuclear bound state

Hayakawa (J-PARC E07), PRL (2021)

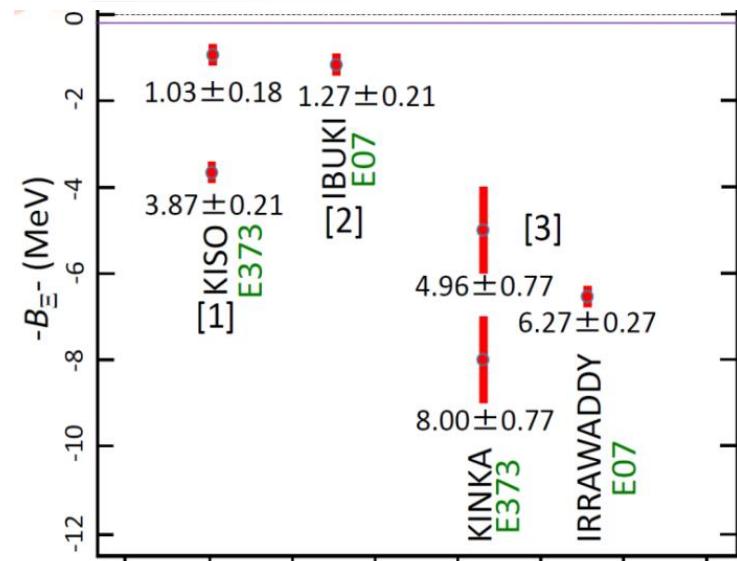


Yoshimoto, PTEP (2021)



$\rightarrow 1s_{\Xi^-}$  nuclear state

## $\Xi$ hypernucleus ( ${}^{15}\text{C}$ [ $\Xi^-$ - $^{14}\text{N}$ ])



[1] K. Nakazawa, et. al., Prog. Theor. Exp. Phys. **2015**, 033D02 (2015).  
E. Hiyama and K. Nakazawa, Ann. Rev. Nucl. Part. Sci. **68**, 131 (2018).

[2] S. Hayakawa, et. al., Phy. Rev. Lett., **126**, 062501 (2021).

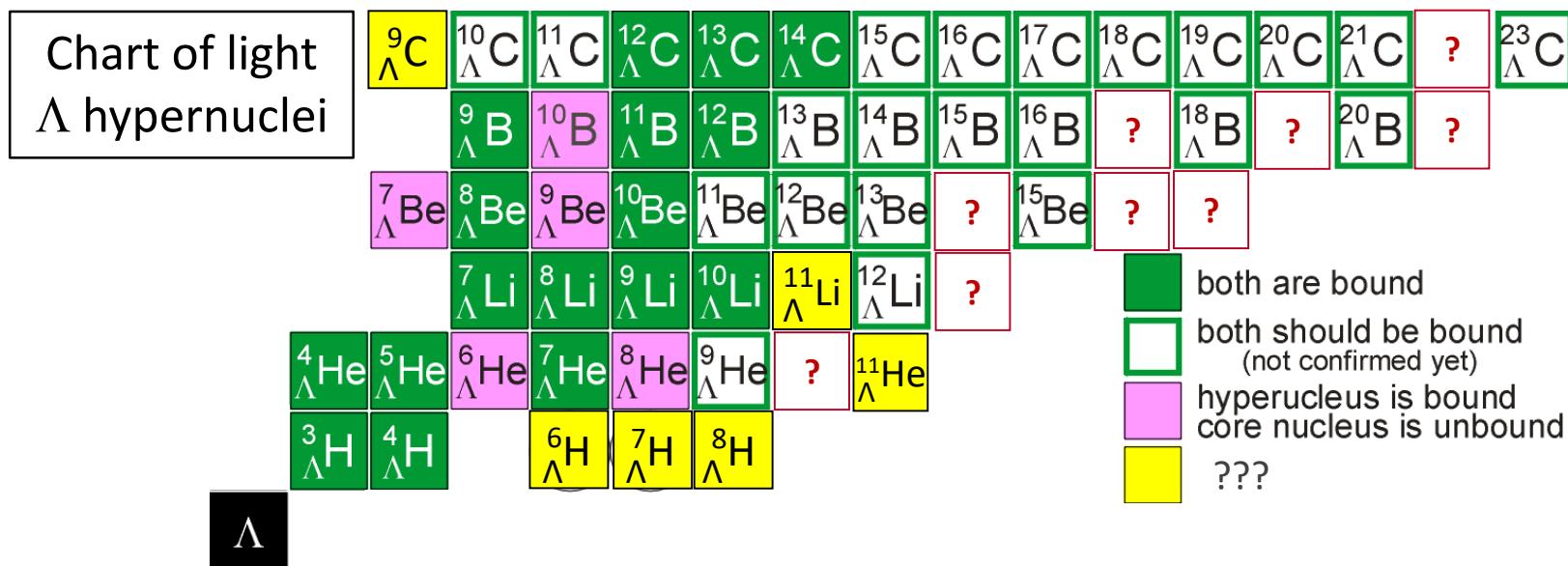
[3] M. Yoshimoto, et. al., Prog. Theor. Exp. Phys. **2021**, 073D02 (2021).

$U_{0\Xi} \sim 14 \text{ MeV}$

# $\Lambda$ hypernuclei near drip-lines

- Chart of  $\Lambda$  hypernuclei
  - Particle-stable core nuclei guarantee stable  $\Lambda$  hypernuclei
    - Still there are many unobserved  $\Lambda$  hypernuclei
  - $\Lambda$ -hyperon may reinforce the nuclear binding
    - Glue-like role of  $\Lambda$ -hyperon: also particle-unstable nuclei may form core of stable  $\Lambda$  hypernuclei

L. Majling, Nucl. Phys. A585 (1995) 211c



# Neutron-rich hypernuclei

## Study by using DCX reaction: ${}^{10}_{\Lambda}Li$

- **KEK E521:** P.K. Saha et al. PRL 94 (2005) 052501

- Study of the  ${}^{10}B(\pi^-, K^+)$  reaction
  - Successfully produced  ${}^{10}_{\Lambda}Li$
  - Almost background free
- Promising production method
- Tiny production cross section

$$\frac{d\sigma}{d\Omega}(\text{DCX}, {}^{10}_{\Lambda}Li) \approx 10 \text{ nb/sr}$$

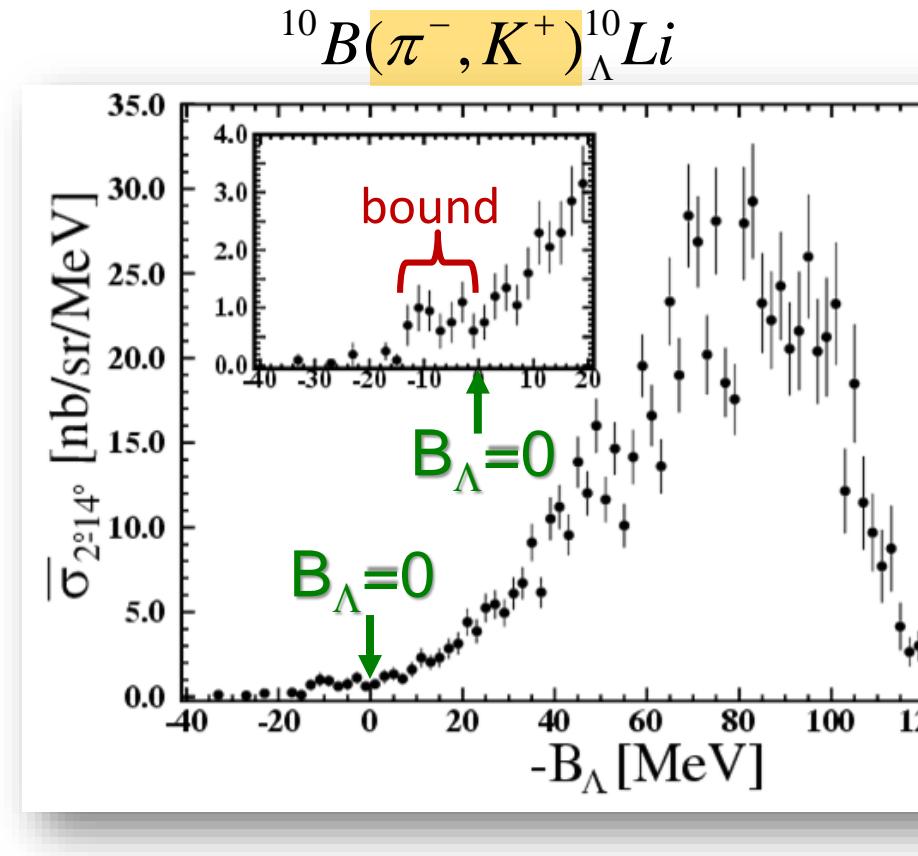
### Reaction mechanisms

$$\text{DCX: } \begin{cases} \pi^- p \rightarrow K^0 \Lambda & \begin{cases} \pi^- p \rightarrow \pi^0 \Lambda \\ \pi^0 p \rightarrow K^+ n \end{cases} \\ K^0 p \rightarrow K^+ n & \end{cases}$$

$\Sigma$ -admixture doorway state:

$$|{}^{10}_{\Lambda}Li\rangle = \alpha |{}^9\text{Li} \otimes \Lambda\rangle + \beta |{}^9\text{Be} \otimes \Sigma^-\rangle$$
$$\pi^- p \rightarrow K^+ \Sigma^-$$

Tretyakova, Lanskoy Phys. At. Nucl. 66 (2003) 1651



# Neutron-rich hypernuclei

## Study by using DCX reaction: ${}^6_{\Lambda}\text{H}$

- **FINUDA:** M. Agnello et al. PhysRevLett 108 (2012) 042501

- Study of the  ${}^6\text{Li}(K_{\text{stop}}^-, \pi^+)$  reaction

$${}^6\text{Li}(K_{\text{stop}}^-, \pi^+) {}^6_{\Lambda}\text{H} \quad {}^6_{\Lambda}\text{H} \rightarrow {}^6\text{He} + \pi^-$$

- Reported 3 candidate events of  ${}^6_{\Lambda}\text{H}$  production

$$B_{\Lambda}({}^6_{\Lambda}\text{H}) = (4.0 \pm 1.1)\text{MeV}$$

$$\text{BR}(\text{DCX}, {}^6_{\Lambda}\text{H}) / \text{BR}(\text{NCX}, {}^{12}\text{C}) \approx 6 \times 10^{-3}$$

$$\text{BR}(\text{DCX}, {}^6_{\Lambda}\text{H}) / \text{BR}(\text{NCX}, {}^4\text{He}) \approx 3 \times 10^{-4}$$

- **J-PARC-E10:** H. Sugimura et al., PhysLettB 729 (2014) 39

- Missing-mass spectrum of the  ${}^6\text{Li}(\pi^-, K^+)$  reaction

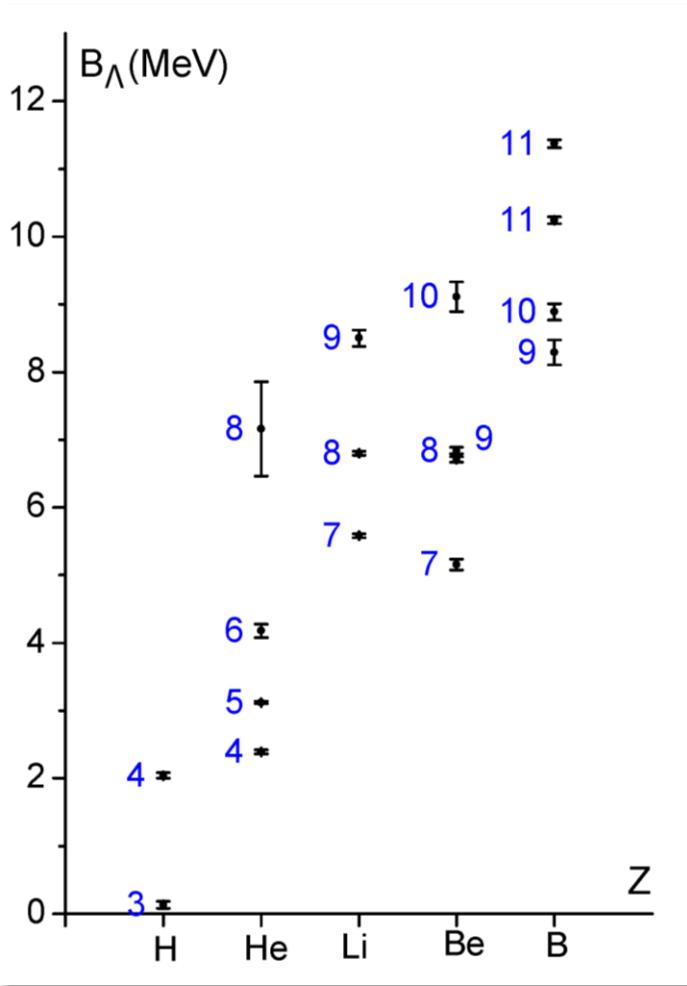
$$\frac{d\sigma}{d\Omega}(\text{DCX}) / \frac{d\sigma}{d\Omega}(\text{NCX}) < 1.5 \times 10^{-4}$$

DCX:  $(\pi^-, K^+)$  NCX:  $(\pi^+, K^+)$  for  ${}^{12}_{\Lambda}\text{C}$

No clear peak of  ${}^6_{\Lambda}\text{H}$  production in threshold region

cross section is extremely smaller than it was expected

# Neutron-rich $\Lambda$ hypernuclei



Proposal  ${}^8_{\Lambda}\text{H}$

L. Majling Nucl Phys A 585 (1995) 211c



$$S_{2n}({}^6_{\Lambda}\text{H}) = S_{2n}({}^5\text{H}) + B_{\Lambda}({}^6_{\Lambda}\text{H}) - B_{\Lambda}({}^4_{\Lambda}\text{H})$$

$$\sim -2 \quad (4.0)?? \quad 2.1$$



$$S_{4n}({}^8_{\Lambda}\text{H}) = S_{4n}({}^7\text{H}) + B_{\Lambda}({}^8_{\Lambda}\text{H}) - B_{\Lambda}({}^4_{\Lambda}\text{H})$$

$$-0.57 \quad ?? \quad 2.1$$

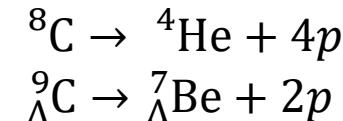
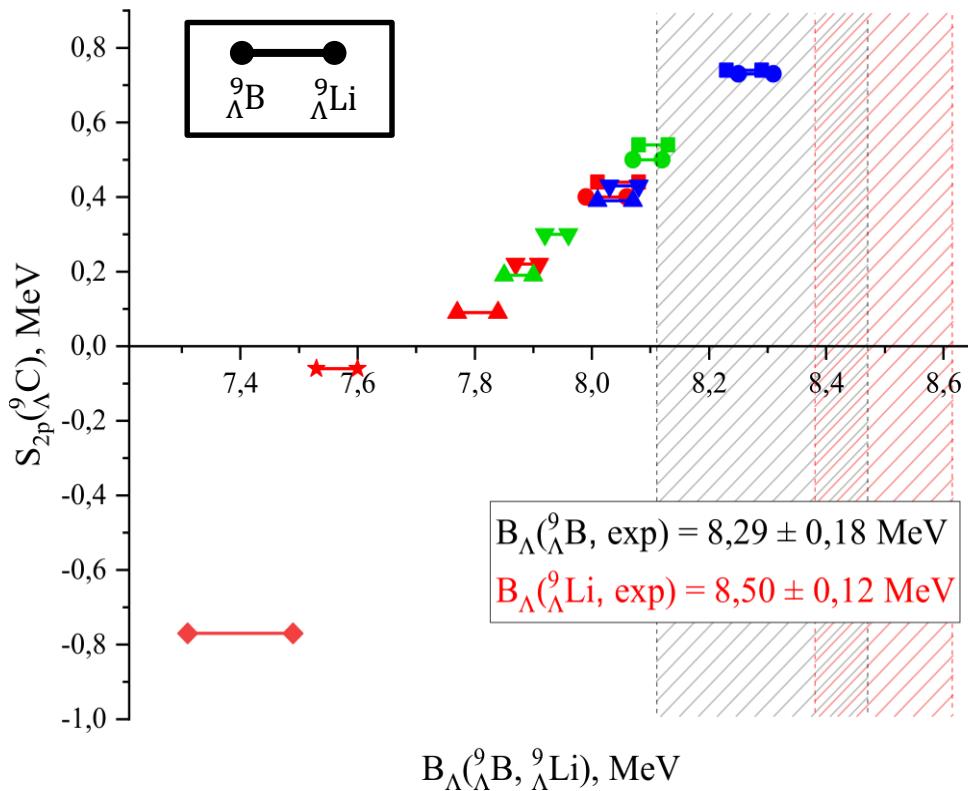
$$B_{\Lambda}({}^8_{\Lambda}\text{H}) \sim 7\text{-}8 \text{ MeV} ?$$

Hydrogen isotopes

	${}^4\text{H}$	${}^5\text{H}$	${}^6\text{H}$	${}^7\text{H}$
Decay mode	$n$	$2n$	$3n$	$4n$
$E_{\text{res}}$ [MeV]	3.2	$1.7\div 2.4$	$2.3\pm 0.5$	$0.57^{+42}_{-21}$

# Proton-rich $\Lambda$ hypernuclei

## 2p separation energy in ${}^9\Lambda C$



calc ↘

$$S_{2p}({}^9\Lambda C) = S_{2p}({}^8C) + B_{\Lambda}({}^9C) - B_{\Lambda}({}^7Be)$$

exp: -2,14 MeV ↗ exp: 5,16 MeV ↗

Different NN and  $\Lambda N$  interactions  
 The better the description of  $B_{\Lambda}({}^9B)$  and  $B_{\Lambda}({}^9Li)$ , the greater 2p separation energy in  ${}^9\Lambda C$ .

$$S_{2p}({}^9\Lambda C) > 0.$$

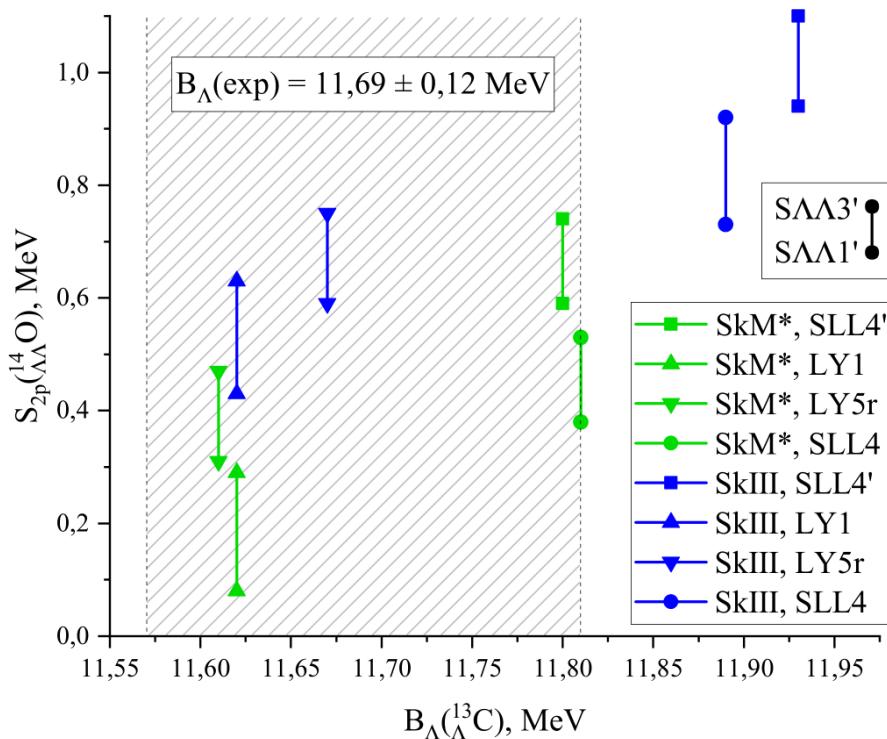
${}^9\Lambda C$  should be bound

Isotope	$S_p$ or $S_{2p}$ , MeV	$\delta B_{\Lambda}$ , MeV
${}^{16}F$	$S_p = -0.531 \pm 0.005$	$\delta B_{\Lambda}^p = 0.37 \div 1.17$
${}^{19}Na$	$S_p = -0.323 \pm 0.011$	$\delta B_{\Lambda}^p = 0.30 \div 0.36$
${}^{19}Mg$	$S_{2p} = -0.76 \pm 0.06$	$\delta B_{\Lambda}^{2p} = 0.48 \div 0.72$

Whether  ${}^{17}\Lambda F$ ,  ${}^{20}\Lambda N$  and  ${}^{20}\Lambda Mg$  hypernuclei are bound remains questionable.

# Proton-rich $\Lambda$ hypernuclei

Double-strangeness hypernuclei. 2p separation energy in  $^{14}_{\Lambda\Lambda}\text{O}$



$$S_{2p}(^{14}_{\Lambda\Lambda}\text{O}) = S_{2p}(^{12}\text{O}) + B_{\Lambda\Lambda}(^{14}_{\Lambda\Lambda}\text{O}) - B_{\Lambda\Lambda}(^{12}_{\Lambda\Lambda}\text{C})$$

$\text{exp}$  ↓  
 $\text{calc}$  ↑ ↑

as function  $B_\Lambda(^{13}\text{C})$  for different NN and  $\Lambda\text{N}$  Skyrme parameter sets. Hypernucleus  $^{13}_{\Lambda}\text{O}$  is unbound; a second hyperon addition completes the binding of the hypernucleus.

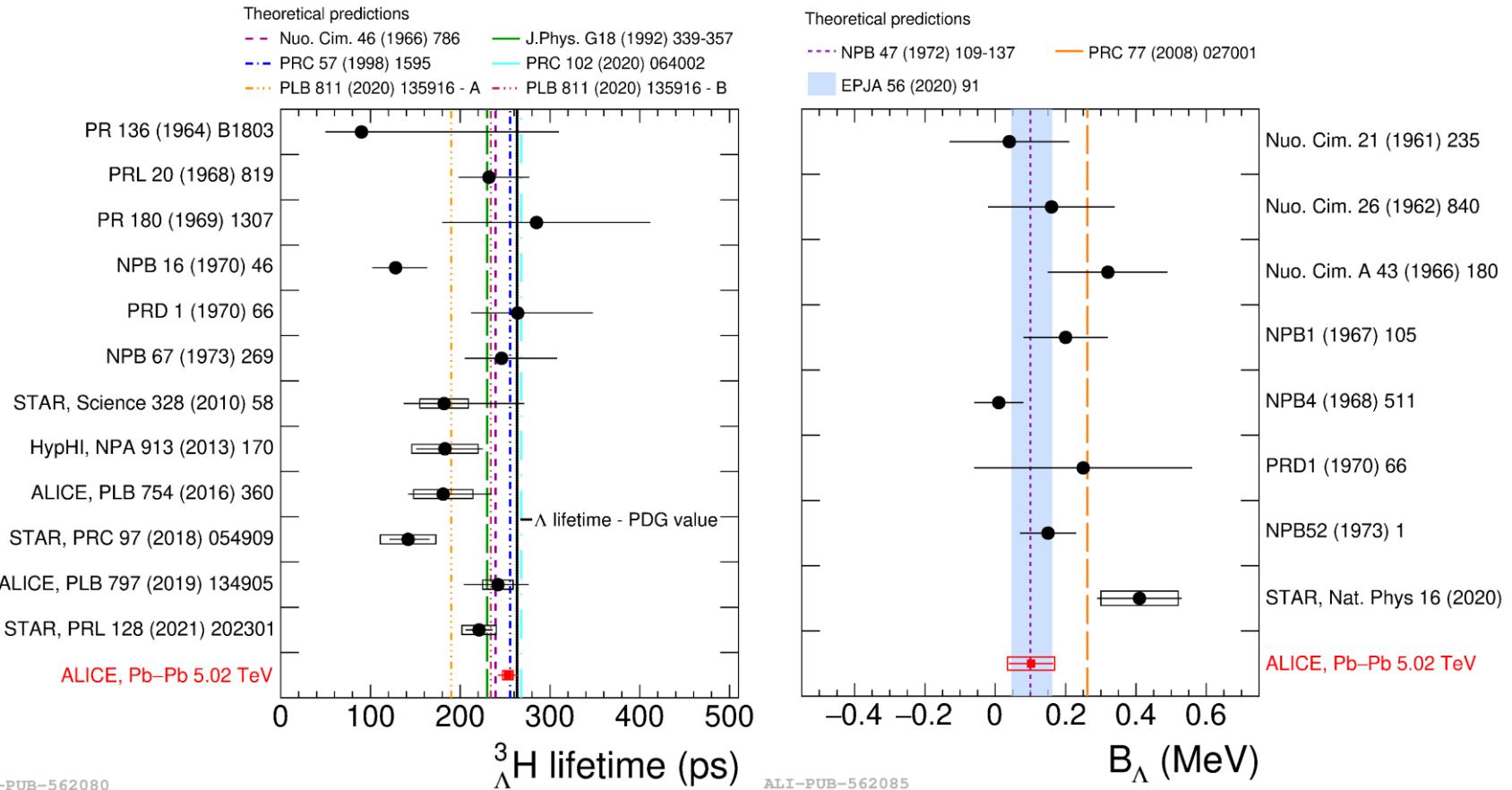
$^{14}_{\Lambda\Lambda}\text{O}$  should be bound

Lanskoy, Sidorov, Tretyakova EPJ A 58 (2022) 203

# Lightest hypernuclei

## Hyperhydrogen and hyperhelium

# Hypertriton ${}^3_{\Lambda}\text{H}$



$$\tau = [253 \pm 11(\text{stat}) \pm 6(\text{syst})] \text{ ps}$$

$$B_{\Lambda} = [102 \pm 63(\text{stat}) \pm 67(\text{syst})] \text{ keV}$$

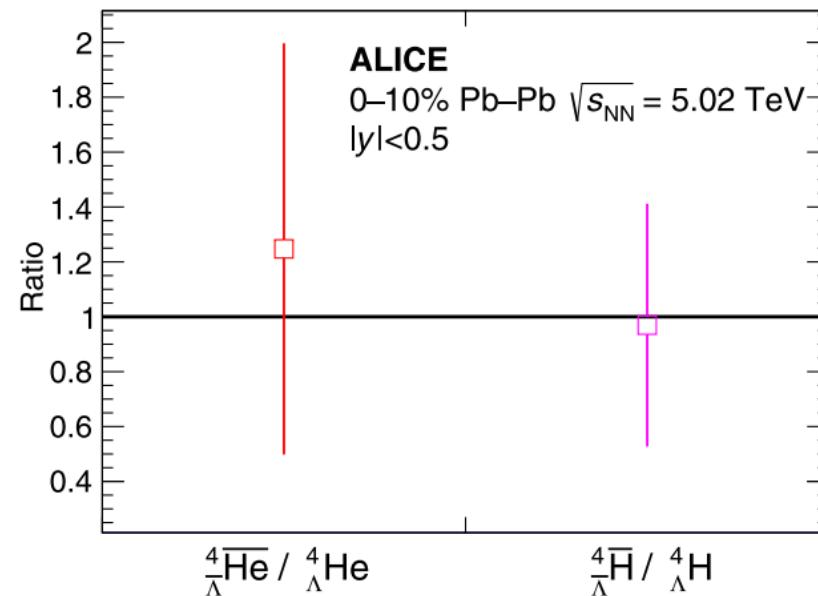
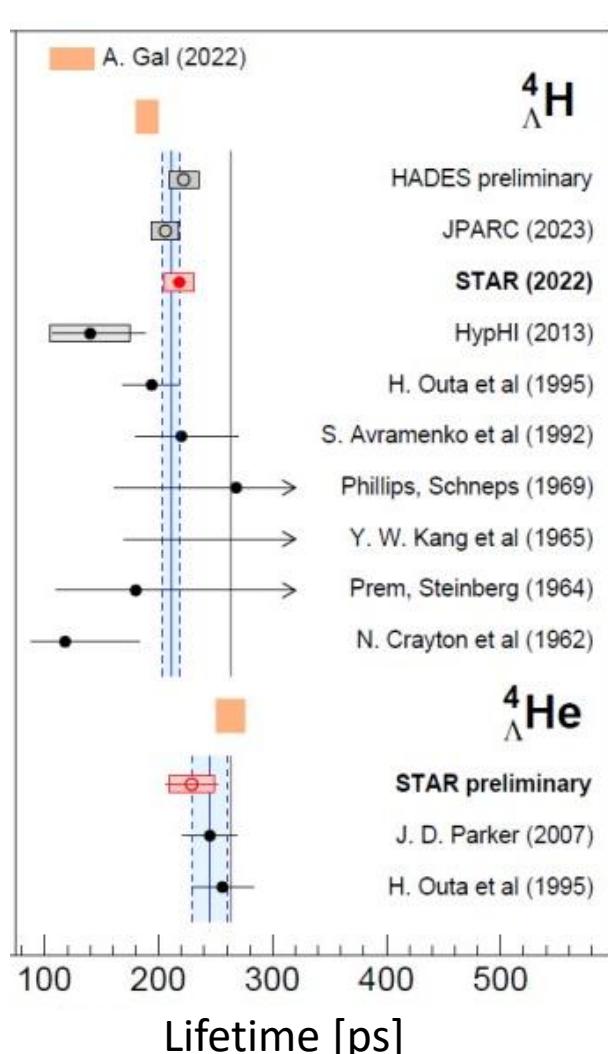
$$\frac{\tau({}^3_{\Lambda}\text{H}) - \tau({}^3_{\bar{\Lambda}}\text{H})}{\tau({}^3_{\Lambda}\text{H})} = [3 \pm 7(\text{stat}) \pm 4(\text{sys})] \times 10^{-2}$$

$$\tau({}^3_{\Lambda}\text{H}) \approx 0.96\tau_{\Lambda}$$



ALICE PhysRevLett 131 (2023) 102302

# $\Lambda$ hypernuclei A=4

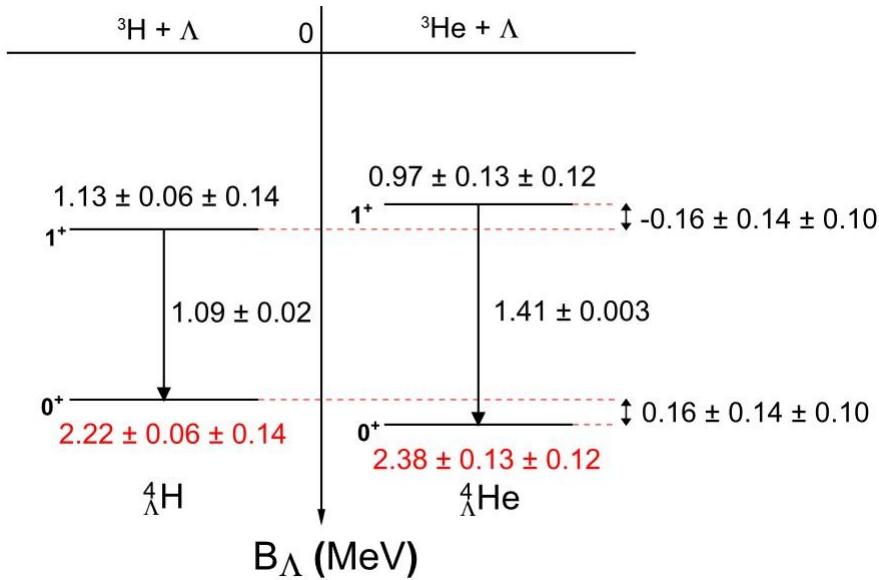


ALICE PhysRevLett 134 (2025) 162301

# $\Lambda$ hypernuclei A=4

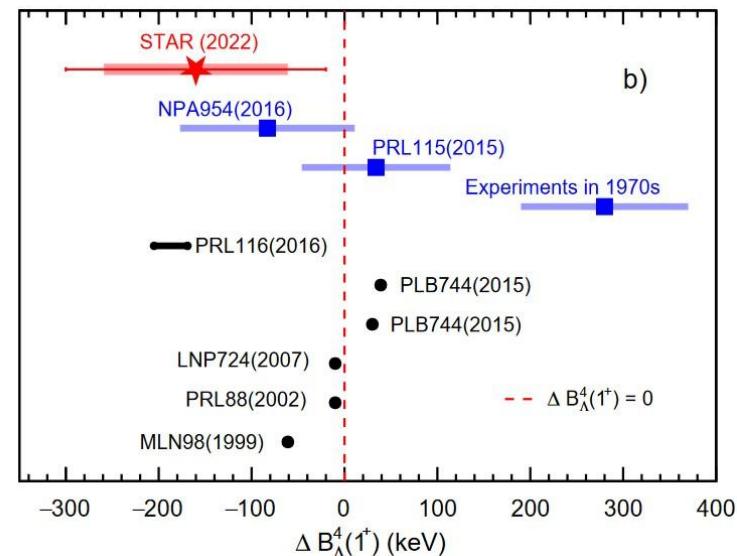
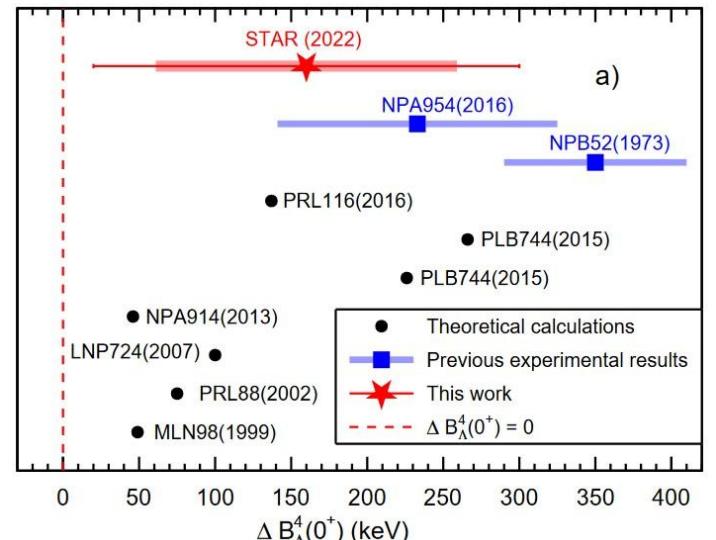
## Charge Symmetry Breaking (CSB) in $\Lambda N$ -interaction

- The difference between  $pp$ - and  $nn$ -interaction, between  $\Lambda p$ - and  $\Lambda n$ -interaction
- Different character of CSB in the singlet and triplet  $\Lambda N$ -pair states



STAR, PhysLettB 834 (2022) 137449

$$\Delta B_\Lambda^4(J^\pi) = B_\Lambda(^4\text{He}) - B_\Lambda(^4\text{H})$$



# Double-strangeness hypernuclei



BNL-AGS E906  ${}^9Be$  ( $K^-, K^+$ ) (Ahn et al, PRL 87 (2001) 132504)

evidence

Reevaluation of the reported observation of the  ${}^4_{\Lambda\Lambda}H$  hypernucleus  
(Randeniya and Hungerford PRC 76, 064308 (2007))

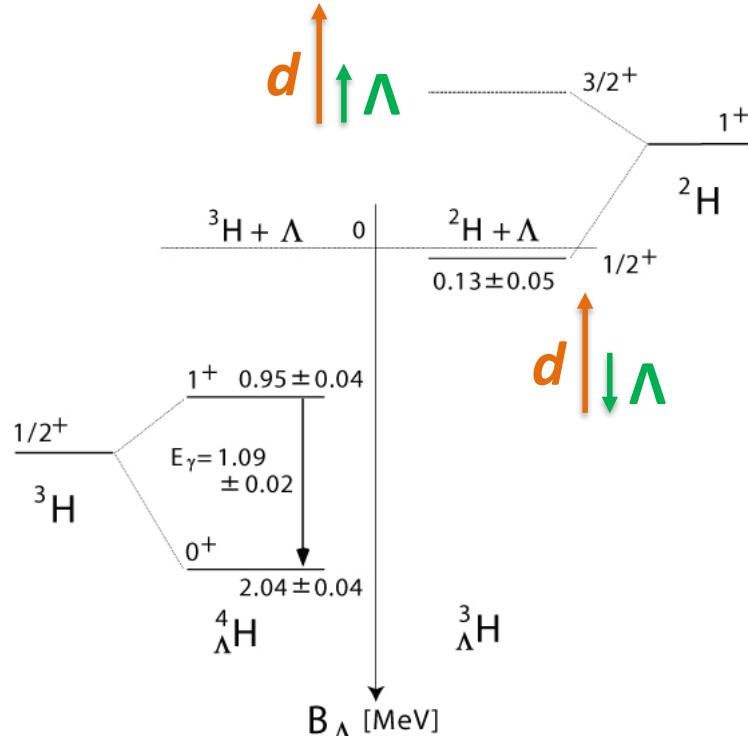
serious doubt

Few-body calculations: Filikhin, Gal 2002 -

No 4H-LL bound state

Nemura et al, 2005 -

stable bound state of 4H-LL



Without  $\Lambda\Lambda$ -interaction:

$$B_{\Lambda\Lambda}^0({}^4_{\Lambda\Lambda}H) = \frac{2}{3}B_\Lambda({}^3H_{gS}) + \frac{4}{3}B_\Lambda({}^3H^*)$$

${}^4_{\Lambda\Lambda}H$  bound if  $B_{\Lambda\Lambda} > B_\Lambda$

$$4B_\Lambda^* > B_\Lambda$$

$\Lambda\Lambda$ -attraction:

$$B_{\Lambda\Lambda}^0({}^4_{\Lambda\Lambda}H) = \frac{2}{3}B_\Lambda({}^3H_{gS}) + \frac{4}{3}B_\Lambda({}^3H^*) + \delta B$$

$$4B_\Lambda^* > B_\Lambda - 3\delta B$$

$\delta B = 0.2$  MeV (compatible with Nagara event)

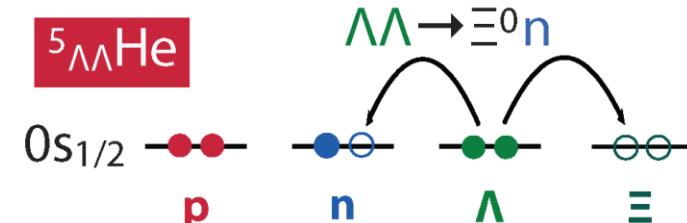
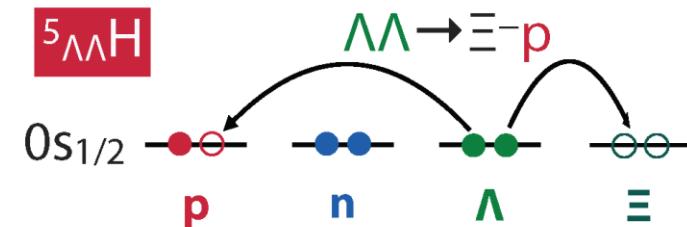
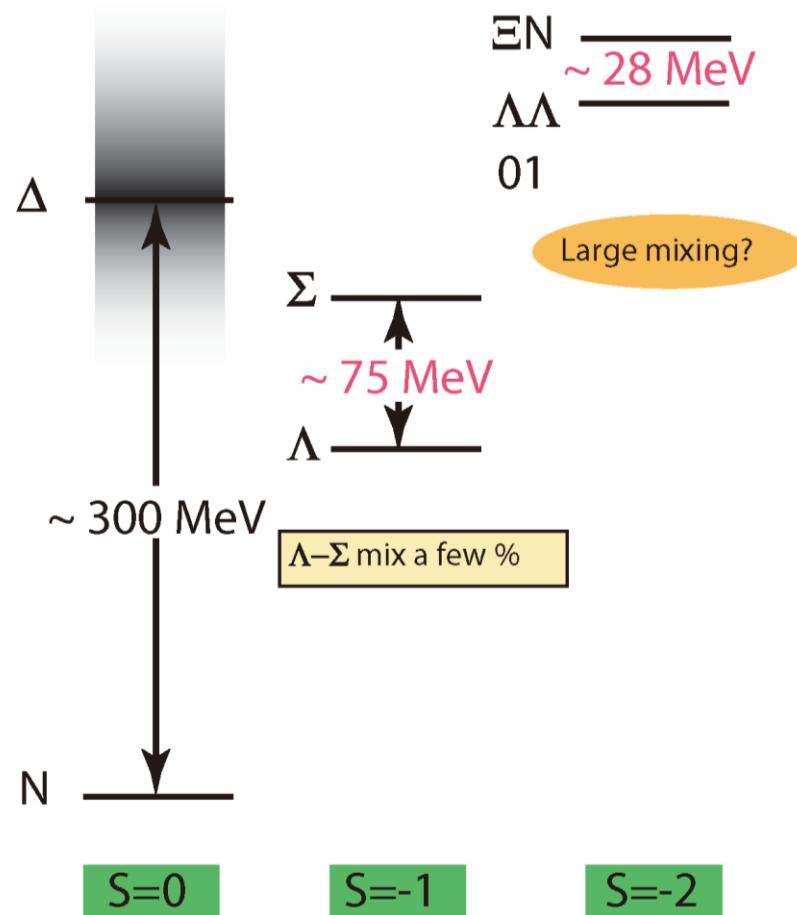
$$B_\Lambda^* > -0.1 \text{ MeV}$$

4H-LL is bound

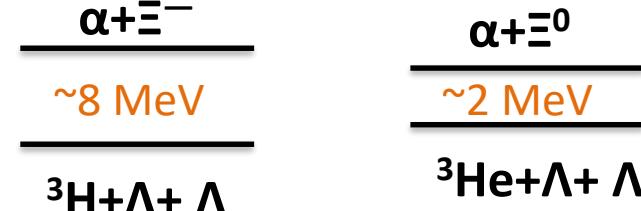
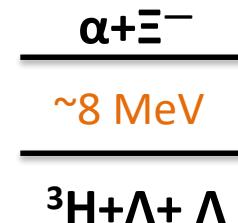
Predictions: Au+Au,  $\sqrt{s_{NN}} = 3$  GeV – yield per event  $\sim 10^{-5}\text{--}10^{-4}$  [Buyukcizmeci EPJ A61(2025) 23]

# Double-strangeness hypernuclei

## $\Lambda\Lambda - \Xi N$ mixing



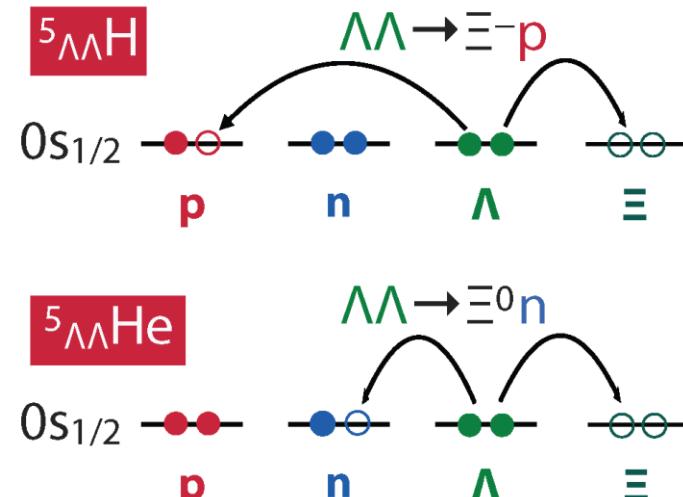
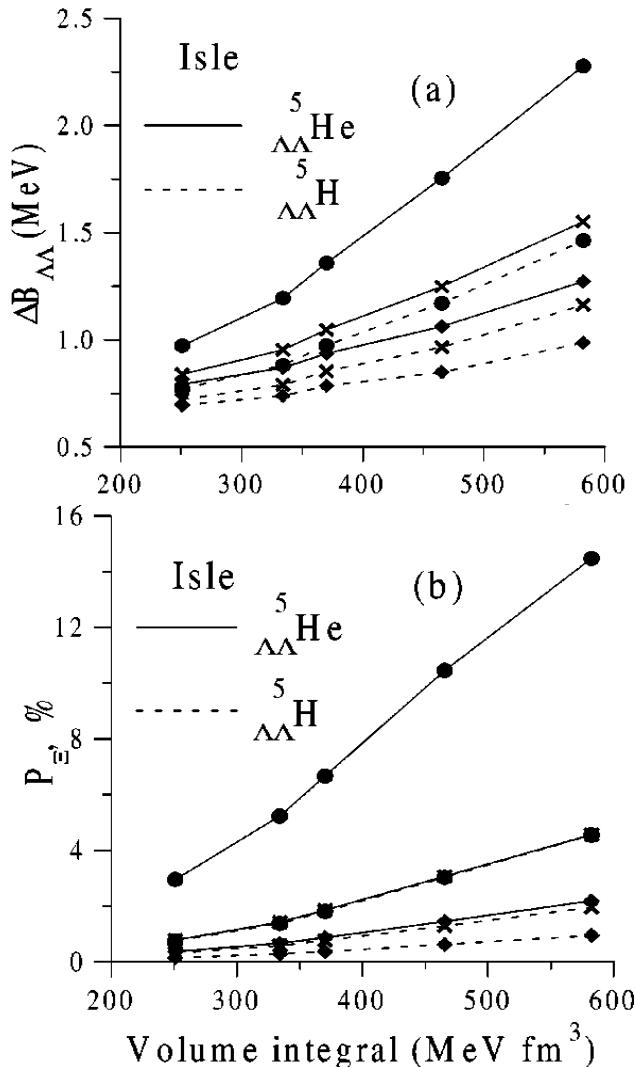
$$\Delta B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^5H) < \Delta B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^5He)$$



$$m_{\Xi^-} - m_{\Xi^0} = 6,85 \pm 0,21 \text{ MeV} \text{ (PDG 2024)}$$

# Double-strangeness hypernuclei

D. E. LANSKOY AND Y. YAMAMOTO PRC **69**, 014303 (2004)



$$m_{\Xi^-} - m_{\Xi^0} = 6,85 \pm 0,21 \text{ MeV (PDG 2024)}$$

Five-baryons wave function:

$$\begin{aligned} |{}^5_{\Lambda\Lambda}\text{H}\rangle &= \alpha_1 |{}^3\text{H} \otimes \Lambda\Lambda\rangle + \beta_1 |{}^4\text{He} \otimes \Xi^- p\rangle \\ |{}^5_{\Lambda\Lambda}\text{He}\rangle &= \alpha_2 |{}^3\text{He} \otimes \Lambda\Lambda\rangle + \beta_2 |{}^4\text{He} \otimes \Xi^0 n\rangle \\ P_\Xi &= \beta^2 \end{aligned}$$

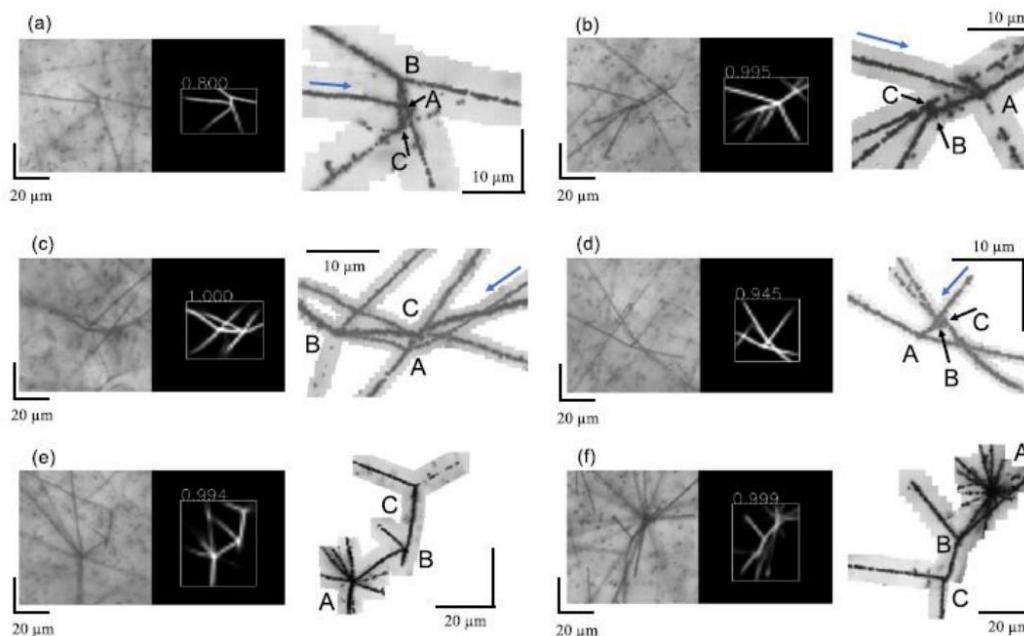
FIG. 1.  $\Delta B_{\Lambda\Lambda}$  (a) and  $\Xi$  admixture probabilities  $P_\Xi$  (b) as functions of volume integral  $\int V_{\Lambda\Lambda, \Xi} d^3r$  in  ${}^5_{\Lambda\Lambda}\text{H}$  and  ${}^5_{\Lambda\Lambda}\text{He}$  for  $\Xi\alpha$  Isle-type potentials and the Isle-type  $\Lambda$ -core potentials.



## Full Length Article

A novel application of machine learning to detect double- $\Lambda$  hypernuclear events in nuclear emulsions

Yan He <sup>a,b,\*</sup>, Vasyl Drozd <sup>b,c</sup>, Hiroyuki Ekawa <sup>b,d</sup>, Samuel Escrig <sup>b,d</sup>, Yiming Gao <sup>b,e,f</sup>, Ayumi Kasagi <sup>b,g</sup>, Enqiang Liu <sup>b,e,f</sup>, Abdul Muneem <sup>b</sup>, Manami Nakagawa <sup>b</sup>, Kazuma Nakazawa <sup>b,h</sup>, Christophe Rappold <sup>d</sup>, Nami Saito <sup>b</sup>, Takehiko R. Saito <sup>a,b,i,j</sup>, Shohei Sugimoto <sup>b,j</sup>, Masato Taki <sup>g</sup>, Yoshiki K. Tanaka <sup>b</sup>, He Wang <sup>b,e,f</sup>, Ayari Yanai <sup>b,j</sup>, Junya Yoshida <sup>b,k</sup>, Hongfei Zhang <sup>a,l</sup>



ML for  $\Lambda\Lambda$

# Conclusions

- Hypernuclei remain the main source of information on hyperonic interactions (but: density is proportional to nuclear one, nuclear cores are from valley of stability)
- Extending the hypernuclear map up to drip-lines provides data on fine interaction features (density dependence, CSB and so on)
- Information on  $\Lambda\Lambda$ ,  $\Xi N$  and  $\Sigma N$  interactions is very much needed – we are waiting for data on the corresponding hypernuclei
- New player in the experiment: Heavy Ion collisions – data on the lightest systems (the clearest information on interactions)

# **THANK YOU FOR YOUR ATTENTION!**

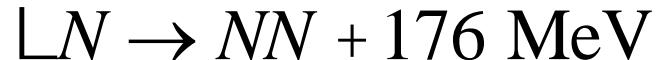
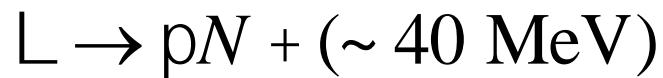
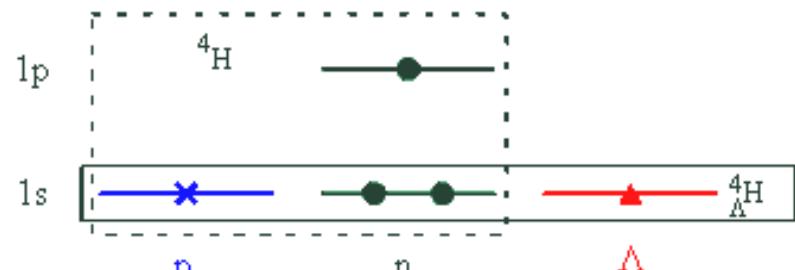
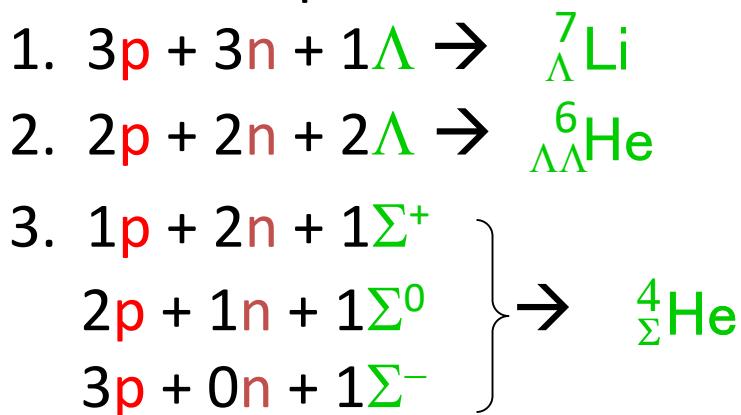
# Back-up

# Notation

$A_Z^{\Lambda}$

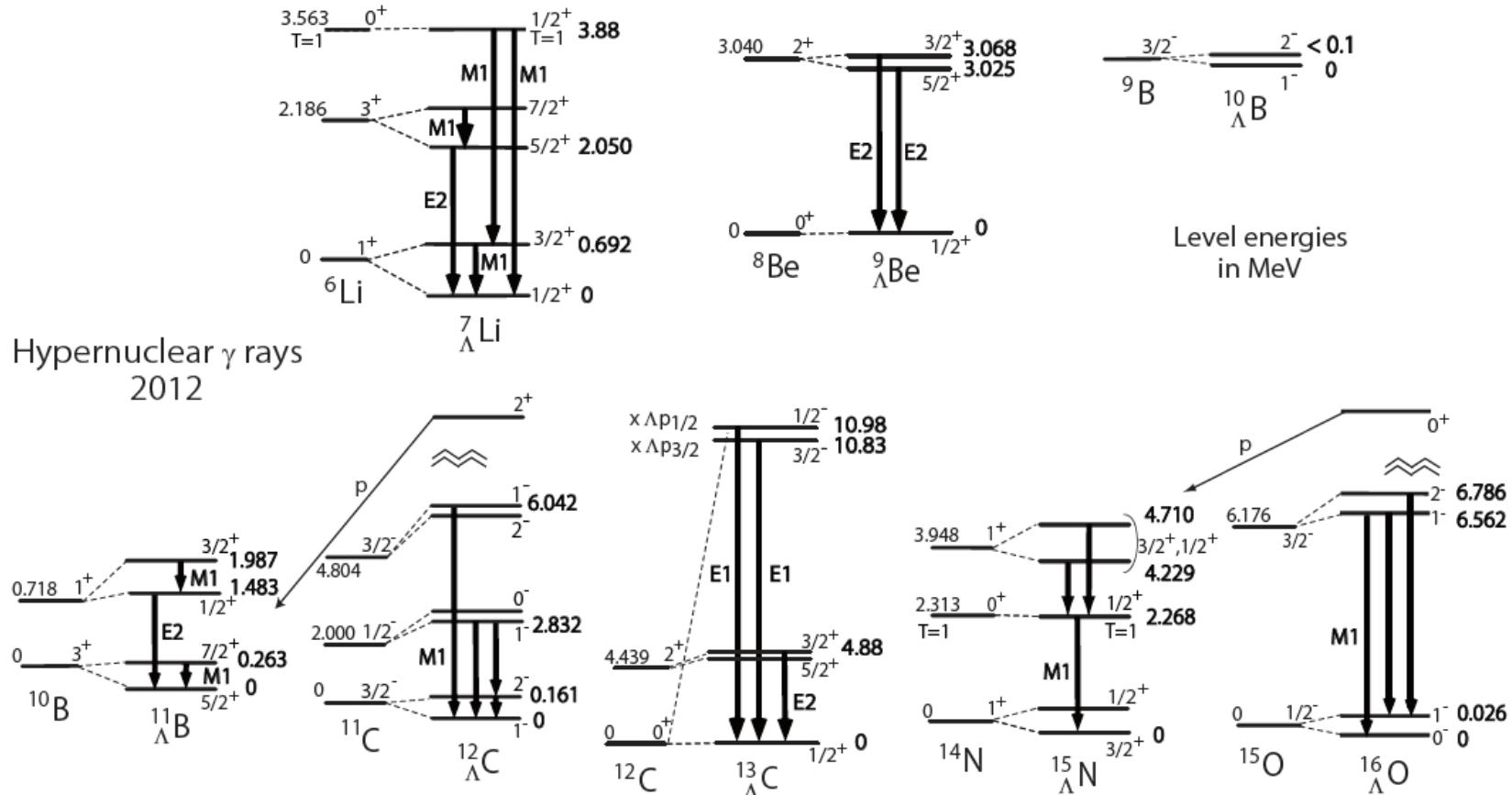
- $A$ : Total number of baryons (nucleon & hyperon)
- $Z$ : Total charge
- $\Lambda$ : hyperon (other examples --  $\Sigma$ ,  $\Xi$ , ...)

- Some examples:



# $\Lambda$ -hypernuclei

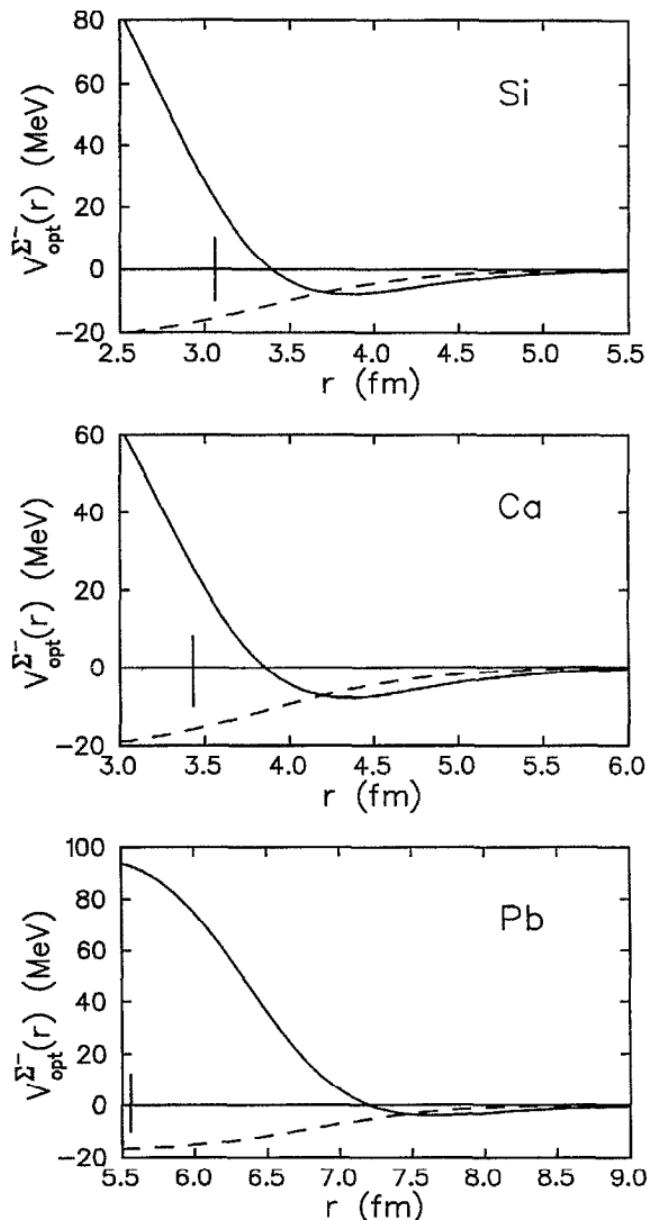
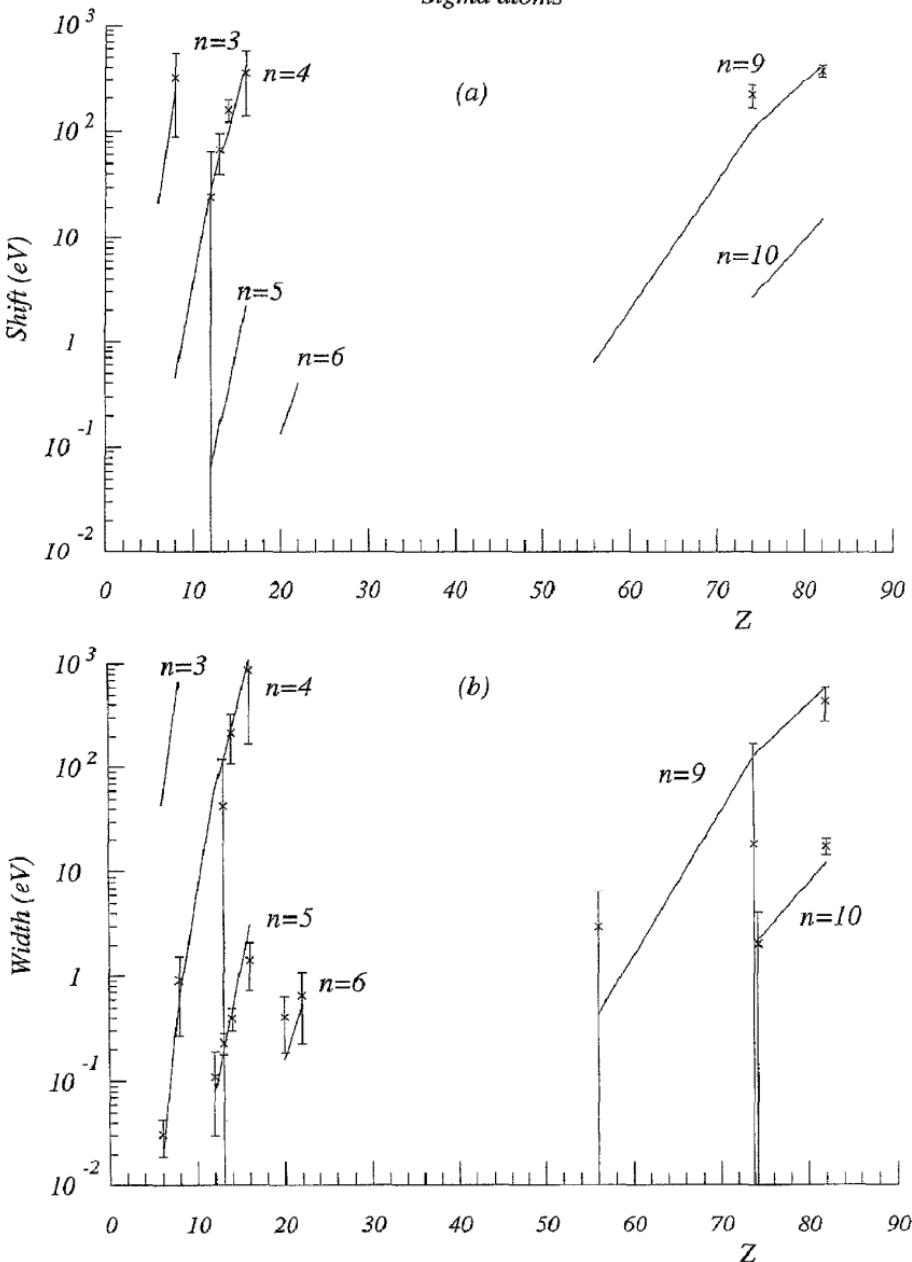
$\Lambda$  spin-orbit splitting (keV): 150 in  $^{13}\Lambda\text{C}$  & related 43 in  $^9\Lambda\text{Be}$



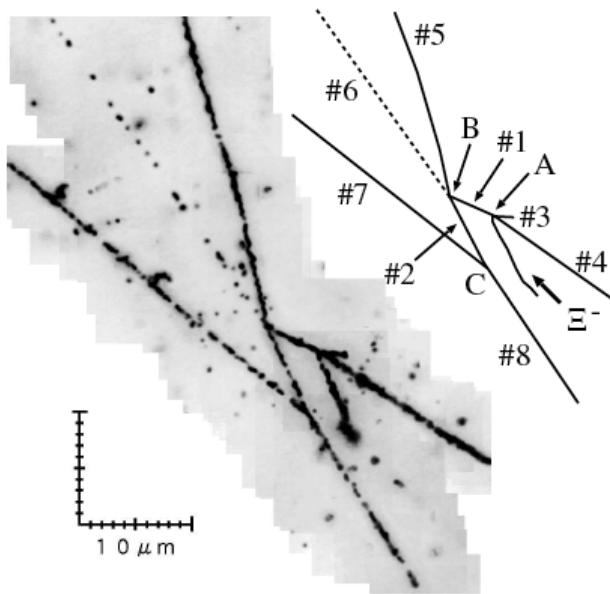
H. Tamura, in HandBook in Nuclear Physics. Springer 2023

# $\Sigma^-$ Atoms

Sigma atoms



# Double-strangeness hypernuclei



Nagara event,  $\Lambda\Lambda^6\text{He}$ , (KEK-E373) PRL 87 (2001) 212502

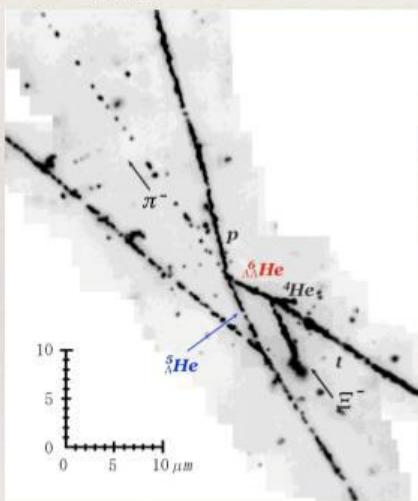
$B_{\Lambda\Lambda}(\Lambda\Lambda^6\text{He}_{\text{g.s.}}) = 6.91 \pm 0.16 \text{ MeV}$ , unambiguously determined.

- A:  $\Xi^-$  capture  $\Xi^- + {}^{12}\text{C} \rightarrow \Lambda\Lambda^6\text{He} + t + \alpha$
- B: weak decay  $\Lambda\Lambda^6\text{He} \rightarrow {}^5_\Lambda\text{He} + p + \pi^-$  (no  $\Lambda\Lambda^6\text{He} \rightarrow {}^4\text{He} + H$ )
- C:  ${}^5_\Lambda\text{He}$  nonmesic weak decay to 2  $Z=1$  recoils + n.

# Double-strangeness hypernuclei

KEK E373

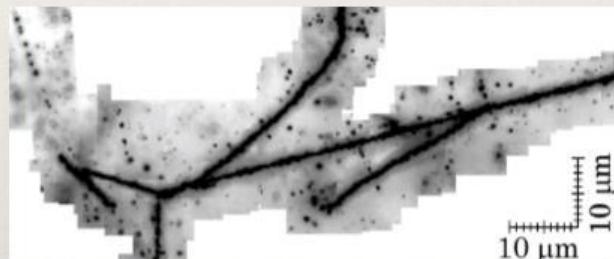
- ❖ “Nagara” event;  $\Lambda\Lambda^6\text{He}$
- ❖  $\Delta B_{\Lambda\Lambda} = 0.67 \pm 0.17 \text{ MeV}$



J.K. Ahn et al., PRC 88 (2013)  
014003.

KEK E373

- ❖ “Kiso” event;  $\Xi^{-14}\text{N}$
- ❖  $\Xi^{-} + ^{14}\text{N} \rightarrow ^{10}\Lambda\text{Be} + ^5\Lambda\text{He}$



K. Nakazawa et al., PTEP  
(2015) 033D02

- ❖  $B_\Xi = 1.03 \text{ or } 3.87 \text{ MeV } \pm \Gamma/2$
- ❖ Well beyond the atomic binding of 0.17 MeV

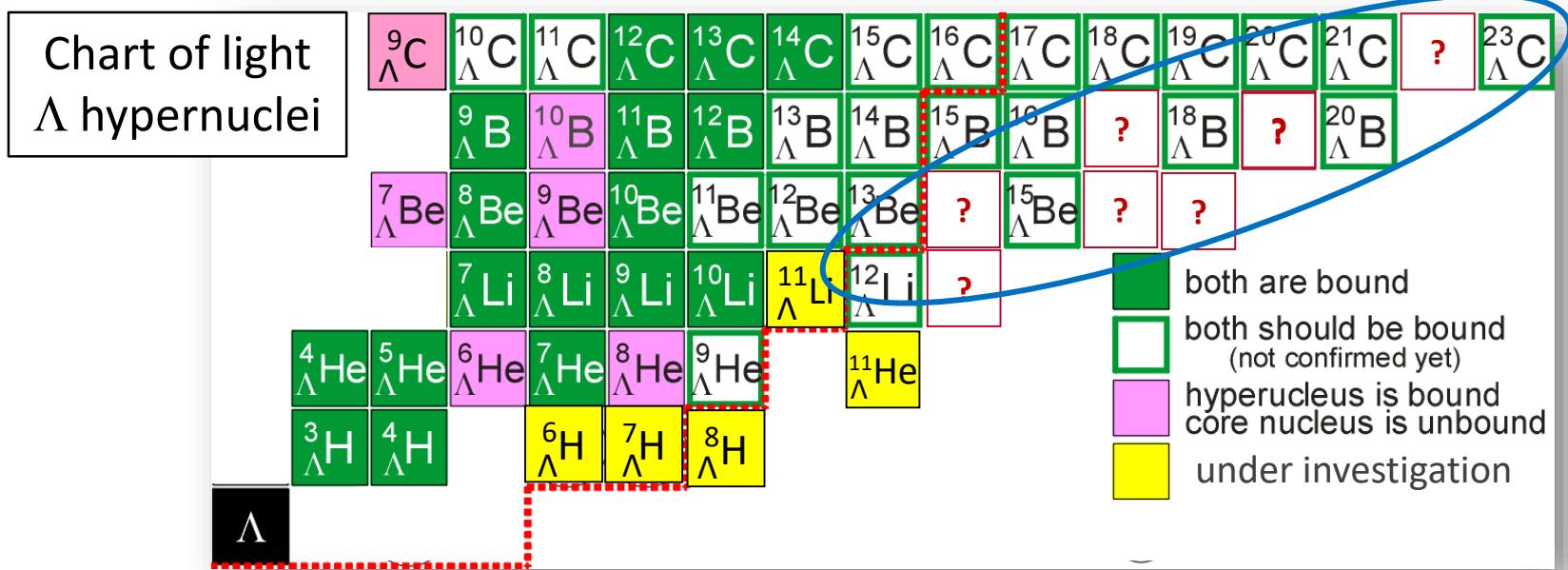
# Tools to access n-rich $\Lambda$ hypernuclei

## heavy-ion collisions vs meson- and electron- induced reaction

- Old emulsion experiments with stopped- $K^-$  beams
  - Hypernuclear species were limited and yield was low
- **Charge-exchange reactions**
  - SCX:  $(e, e' K^+)$ ,  $(K^-, \pi^0)$  DCX:  $(\pi^-, K^+)$ ,  $(K^-, \pi^+)$
- **Relativistic heavy-ion collisions**

SCX: Single Charge-eXchange  
DCX: Double Charge-eXchange

L. Majling, Nucl. Phys. A585 (1995) 211c

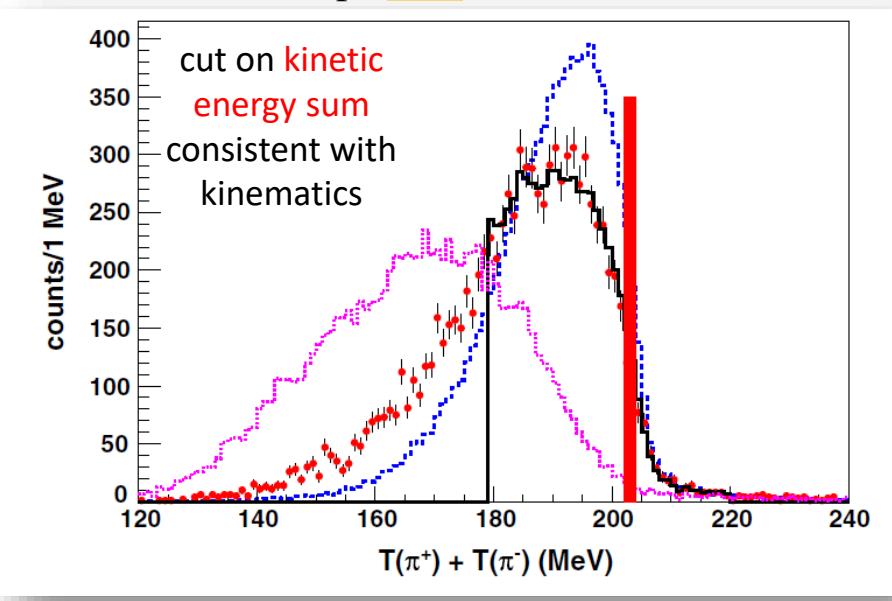


# Neutron-rich hypernuclei

## Study by using DCX reaction: ${}^6_{\Lambda}\text{H}$ (1)

- **FINUDA:** M. Agnello et al. PRL 108 (2012) 042501

- Study of the  ${}^6\text{Li}(K_{\text{stop}}^-, \pi^+){}^6_{\Lambda}\text{H}$  reaction



$$B_{\Lambda}({}^6_{\Lambda}\text{H}) = (4.0 \pm 1.1)\text{MeV}$$

- Reported 3 candidate events of  ${}^6_{\Lambda}\text{H}$  production

$$\text{BR}(\text{DCX}, {}^6_{\Lambda}\text{H}) / \text{BR}(\text{NCX}, {}^{12}_{\Lambda}\text{C}) \approx 6 \times 10^{-3}$$

$$\text{BR}(\text{DCX}, {}^6_{\Lambda}\text{H}) / \text{BR}(\text{NCX}, {}^4_{\Lambda}\text{He}) \approx 3 \times 10^{-4}$$

Tretyakova Dubna, May 2025

# Neutron-rich hypernuclei

## Study by using DCX reaction: ${}^6\Lambda\text{H}$ (2)

- **J-PARC-E10:** H. Sugimura et al., PLB 729 (2014) 39

- Missing-mass spectrum of the  ${}^6\text{Li}(\pi^-, \text{K}^+)$  reaction

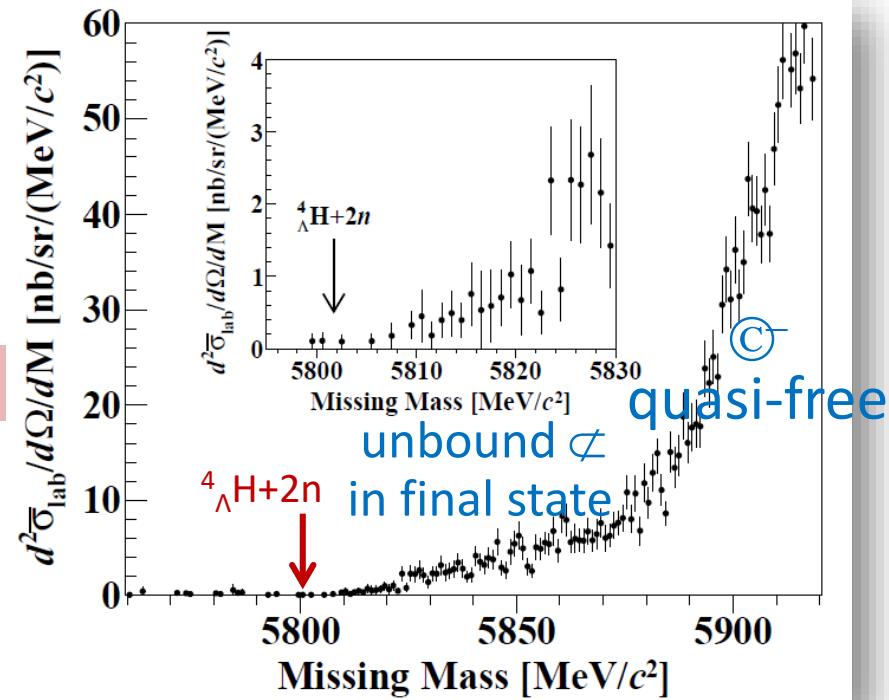
No clear peak of  ${}^6\Lambda\text{H}$  production  
in threshold region

cross section is extremely smaller  
than it was expected

$$\frac{d\sigma}{d\Omega}(\text{DCX}) / \frac{d\sigma}{d\Omega}(\text{NCX}) < 1.5 \times 10^{-4}$$

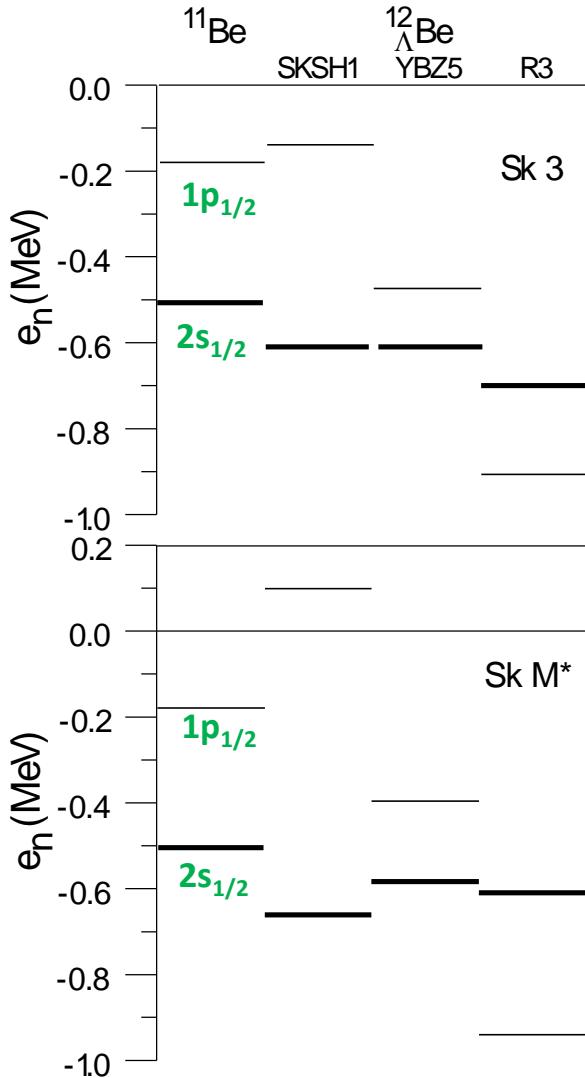
DCX:  $(\pi^-, \text{K}^+)$  NCX:  $(\pi^+, \text{K}^+)$  for  ${}^{12}\Lambda\text{C}$

${}^6\text{Li}(\pi^-, \text{K}^+)X$   
 $\theta_{\text{LAB}} = 2\text{-}14 \text{ deg.}$



# Neutron-rich hypernuclei

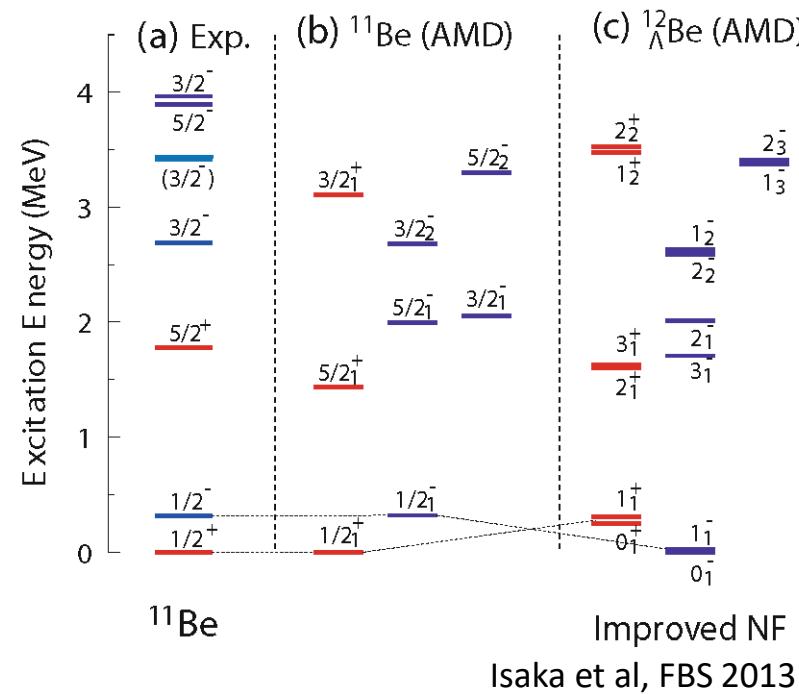
Tretyakova, Lanskoy EPJ A 5, 391 (1999)



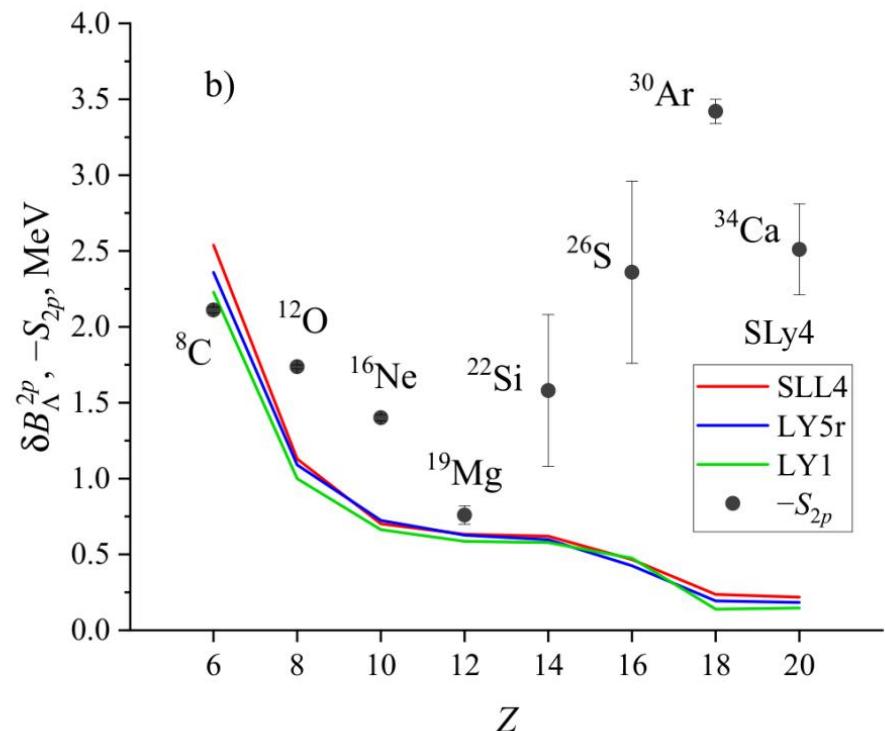
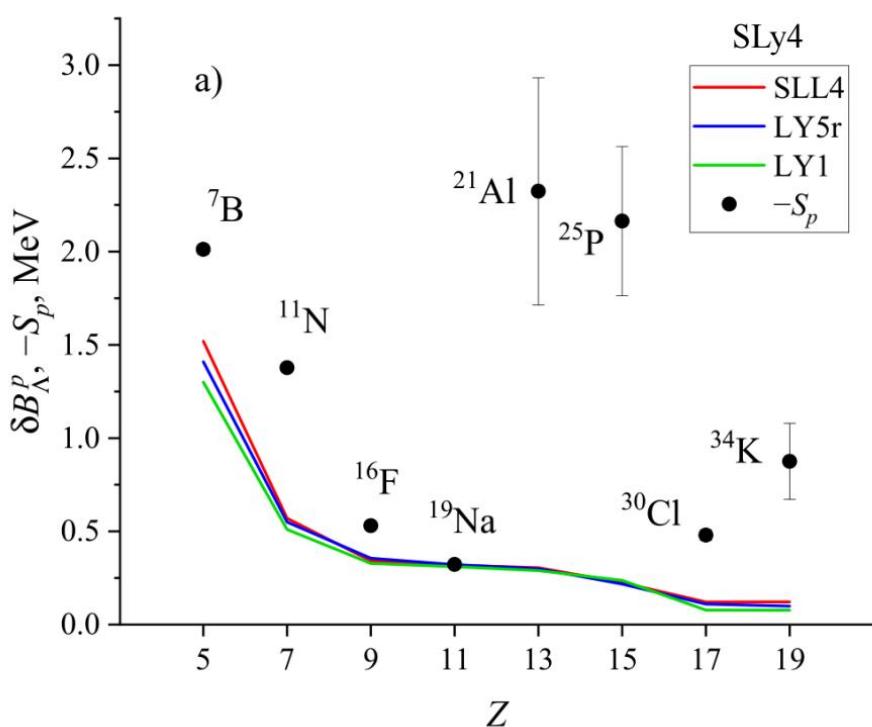
Structure  $^{12}\text{Be-L}$   
SkHF, AMD

$^{12}\Lambda\text{Be} : I=3/2$

Parity inversion in  $^{11}\text{Be}$ . Ground state is  $1/2^+$  instead for  $1/2^-$ . What's happening in  $^{12}\Lambda\text{Be}$ ? Measurement of low-lying  $0^-$ ,  $1^-$ ,  $0^+$  and  $1^+$  states may be possible.



# Proton-rich $\Lambda$ hypernuclei



Lanskoy, Sidorov, Tretyakova EPJ A. 2022