

Капли Ван-дер-Ваальса, балансирующие между жидкостью и газом

INFINUM25

Фазовая диаграмма
Область высоких температур
Методы исследований

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van der Waals droplets balancing between liquid and vapor

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van der Waals EoS -> Phase diagram
Hot region -- Analytical tools

V.N.Kondratyev

BLTP, JINR

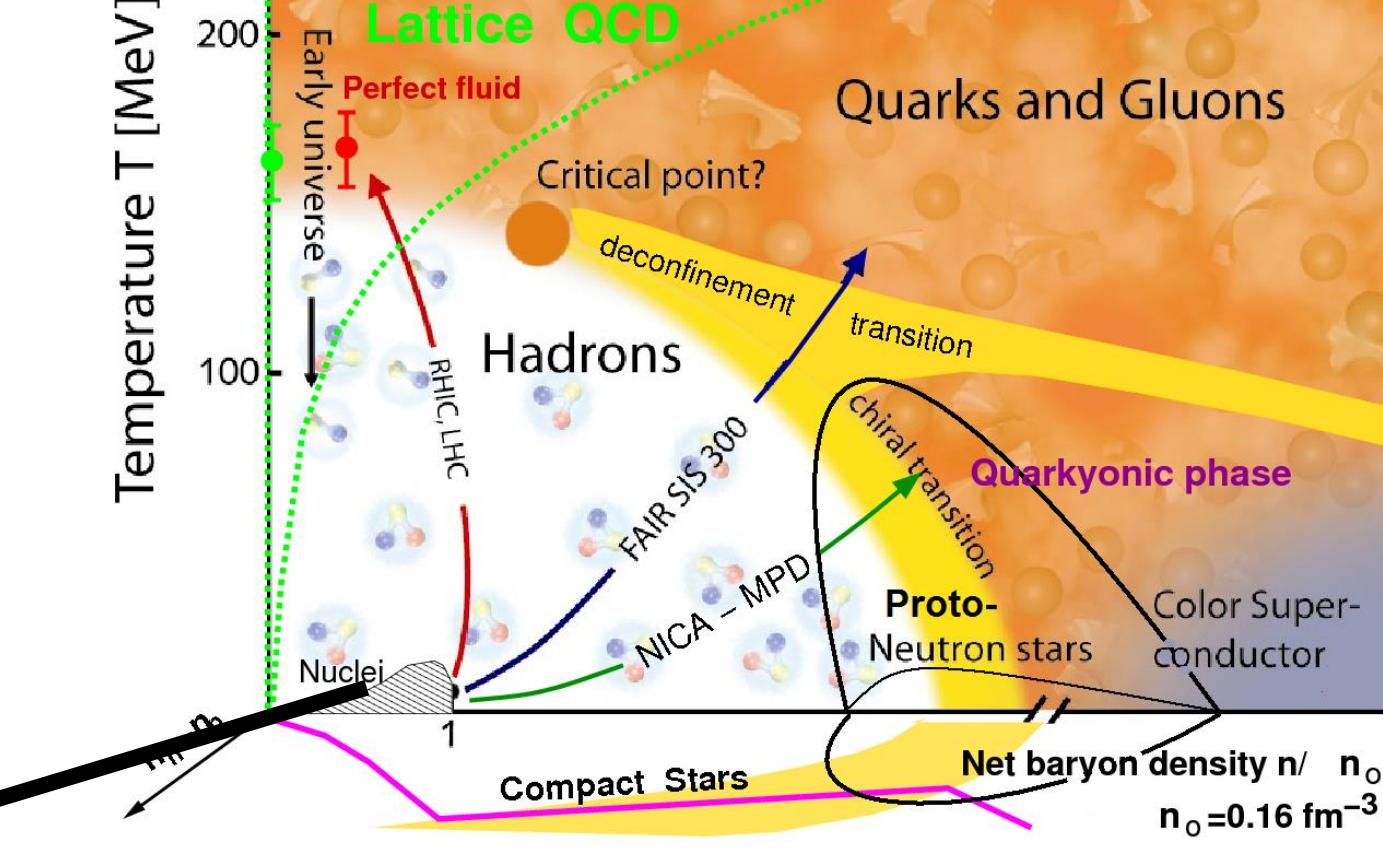
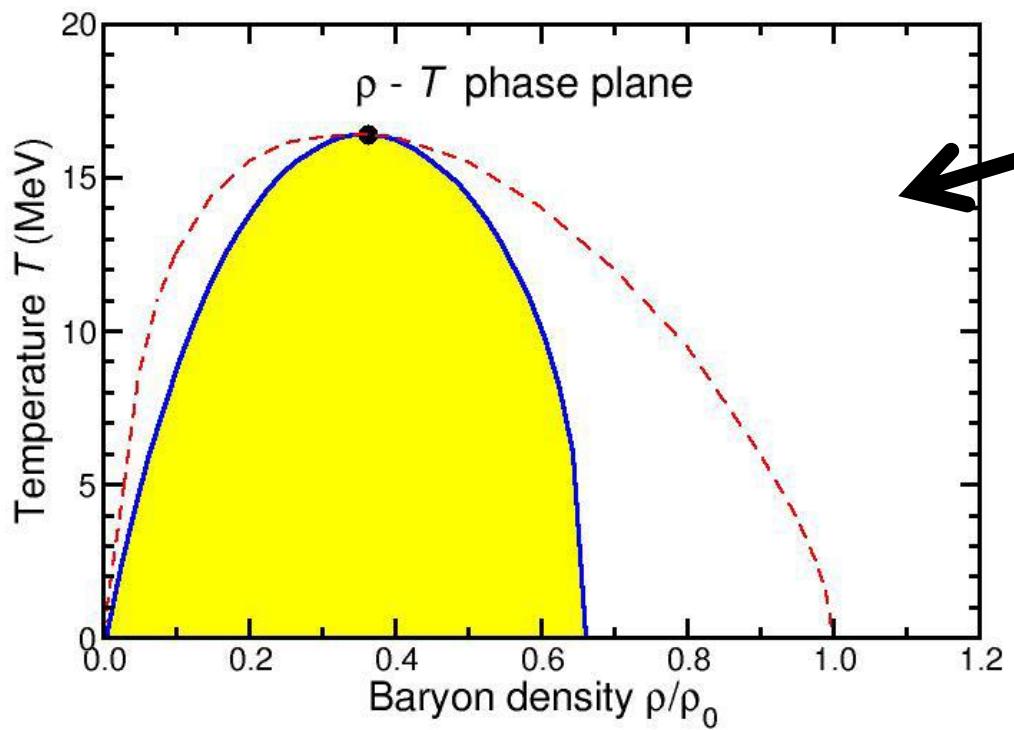
Liquid van der Waals State Equation



Droplet properties

- ...
- FEMTO`-`Nuclear Matter State Equation
- NANO – Device Thermal Stability
- ...

Hot region Phase diagram Liquid Gas phase transition

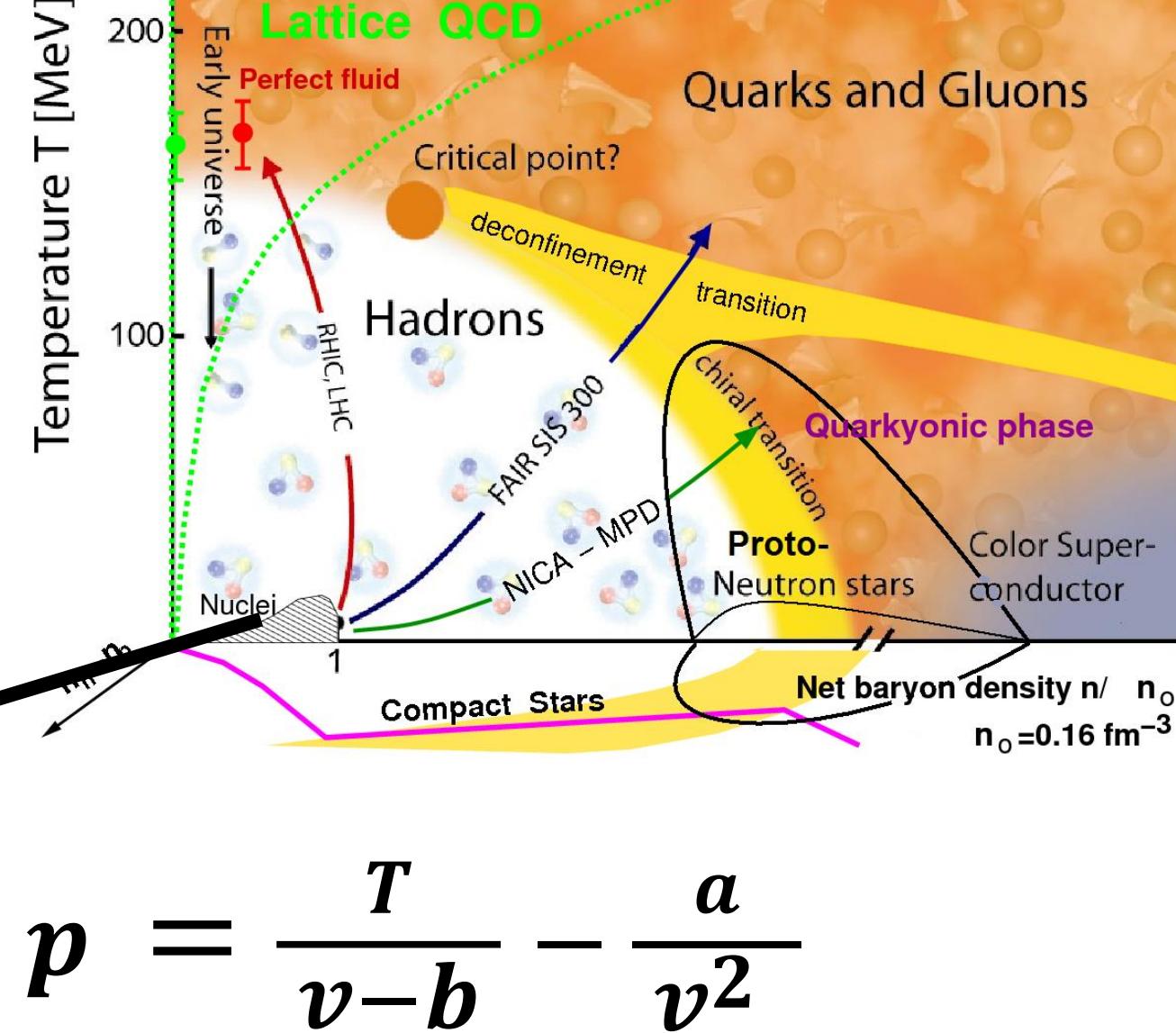
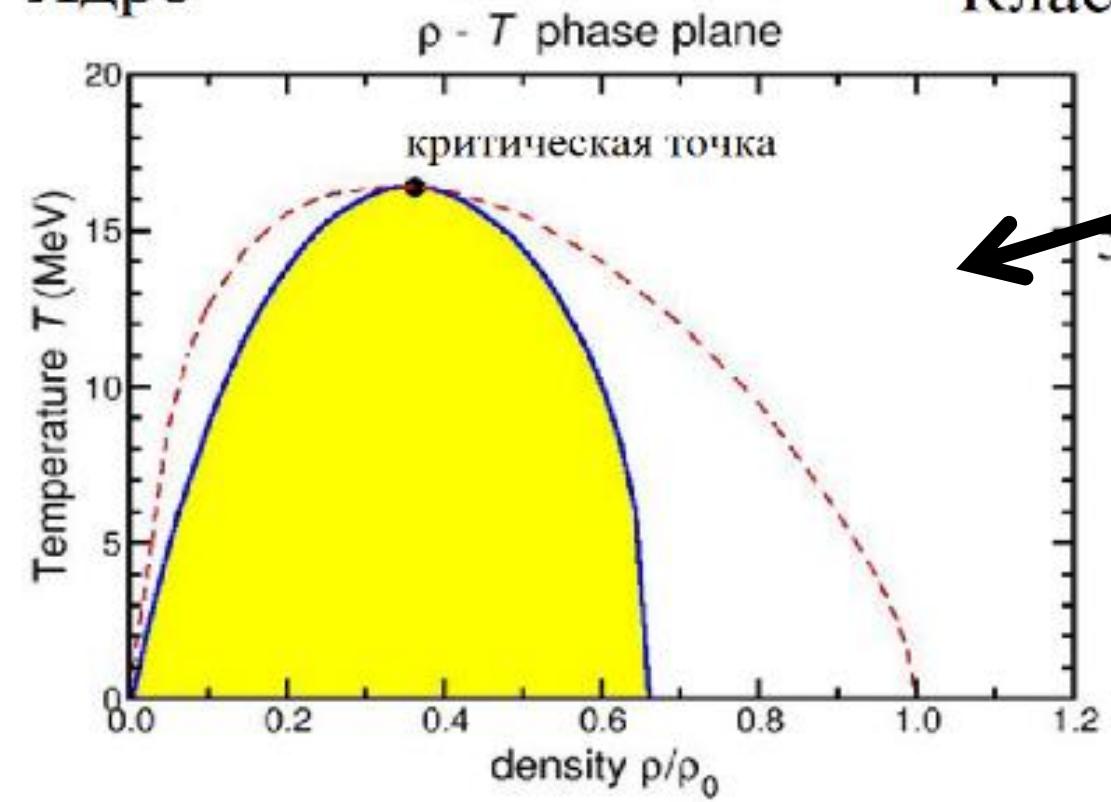


$$p = \frac{T}{v-b} - \frac{a}{v^2}$$

van der Waals EoS

Hot region Phase diagram Liquid Gas phase transition

Ядро Кластер



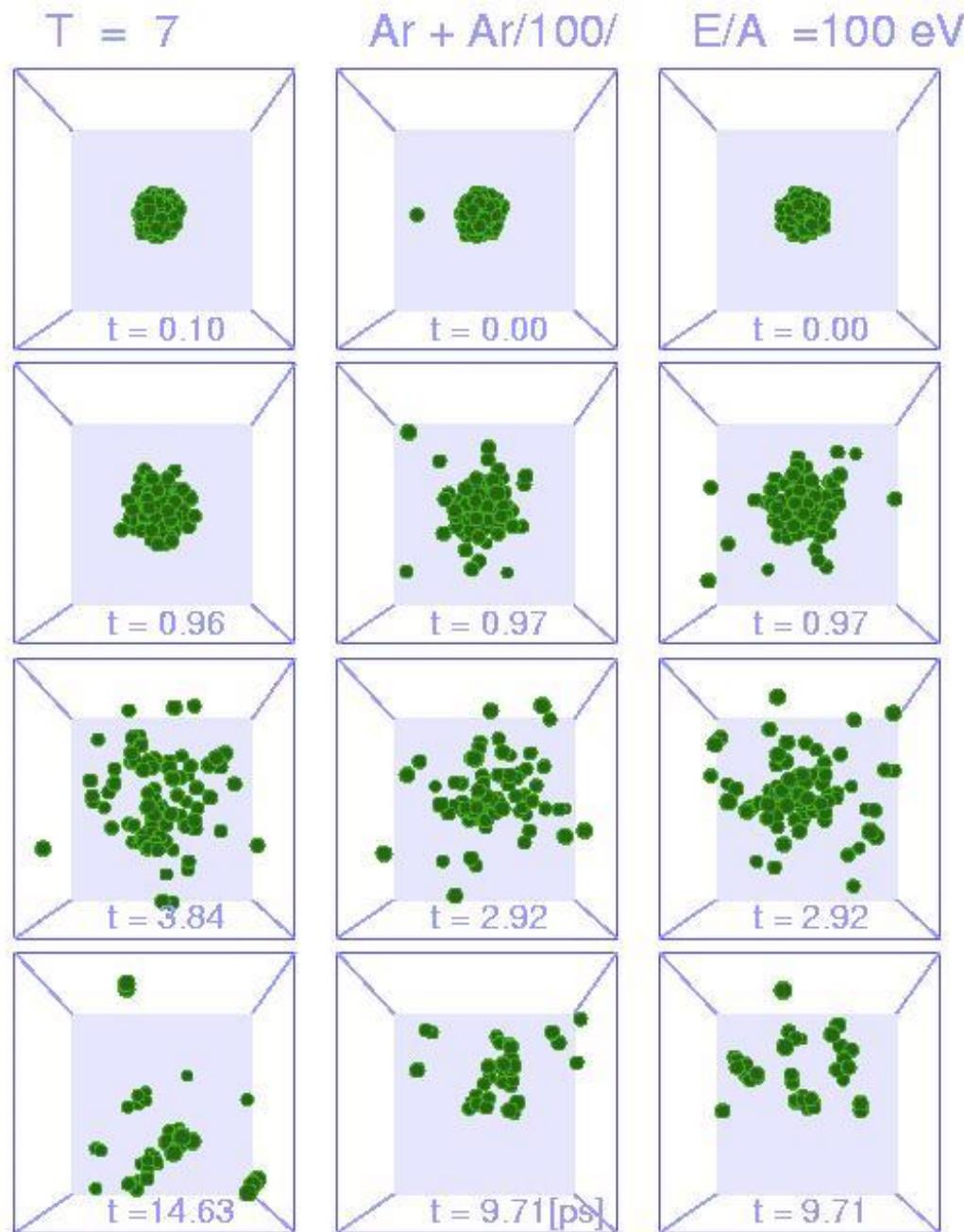
van der Waals EoS

$$p = \frac{T}{v-b} - \frac{a}{v^2}$$



- Д.И. Менделеев: открыл критическую температуру T_c для фазового перехода жидкость-газ (1860)
- вода: $T_c = 374 \text{ } ^\circ\text{C}$
спирт: $T_c = 243 \text{ } ^\circ\text{C}$

Collision *vs* Thermal expansion



classical molecular dynamics (CMD)

evolution of the system is described by
of a set classical Hamilton's equations

$$\frac{d\mathbf{r}_i}{dt} = \frac{\mathbf{p}_i}{m}; \quad \frac{d\mathbf{p}_i}{dt} = -\nabla_i \sum_{j \neq i} V(\mathbf{r}_i - \mathbf{r}_j).$$

combined two-body potential

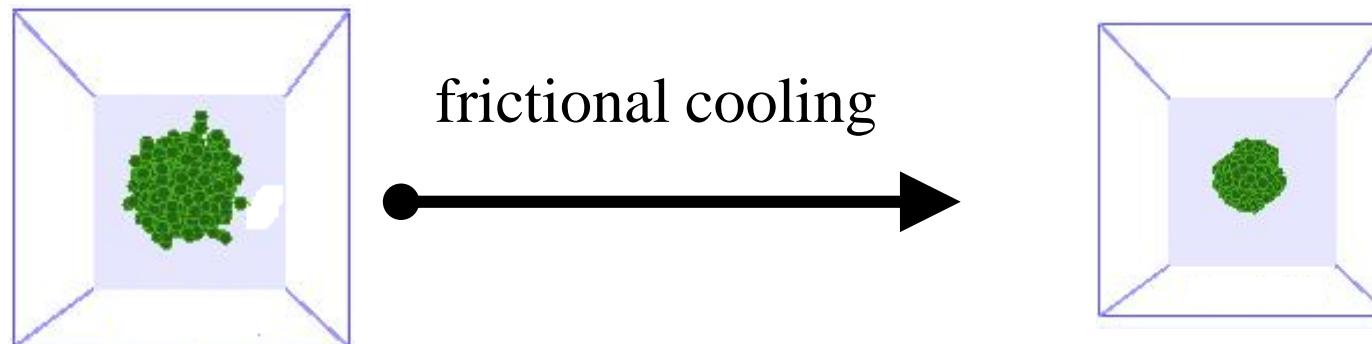
$$V(r) = \begin{cases} 0 & \text{for } r > r_c \\ \epsilon \left(\left(\frac{r_0}{r} \right)^{12} - 2 \left(\frac{r_0}{r} \right)^6 \right) - \left(\left(\frac{r_0}{r_c} \right)^{12} - 2 \left(\frac{r_0}{r_c} \right)^6 \right) & \text{for } r_c > r > r_1 \\ a_0 + a_1 r + a_2 r^2 + a_3 r^3 & \text{for } r_1 > r > r_2 \\ \Phi(r/a) \cdot Z_1 Z_2 e^{2/r} & \text{for } r < r_2 \end{cases}$$

6-12 Lennard-Jones potential

Ziegler, Biersack and Littmark
(ZBL) screening

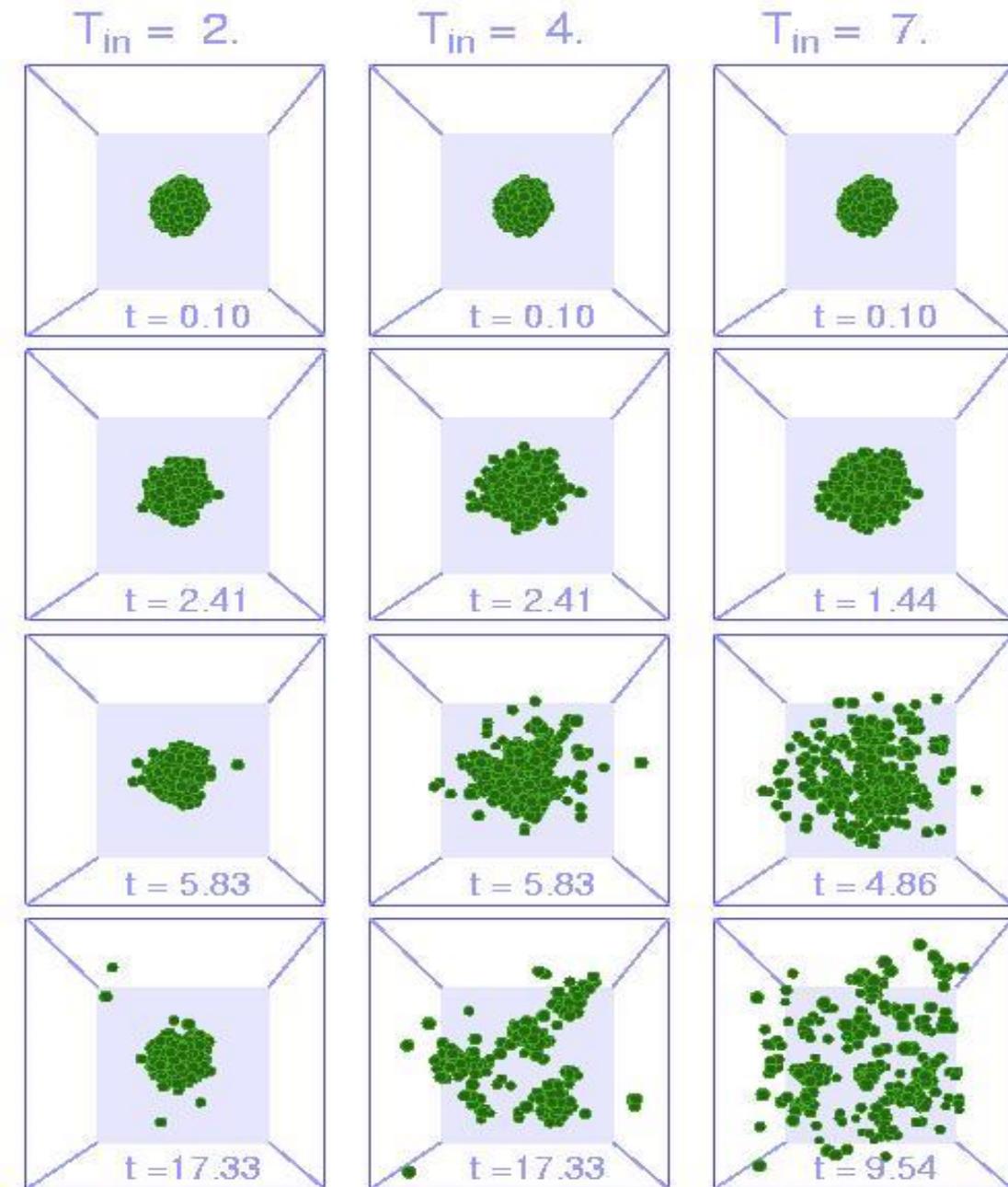
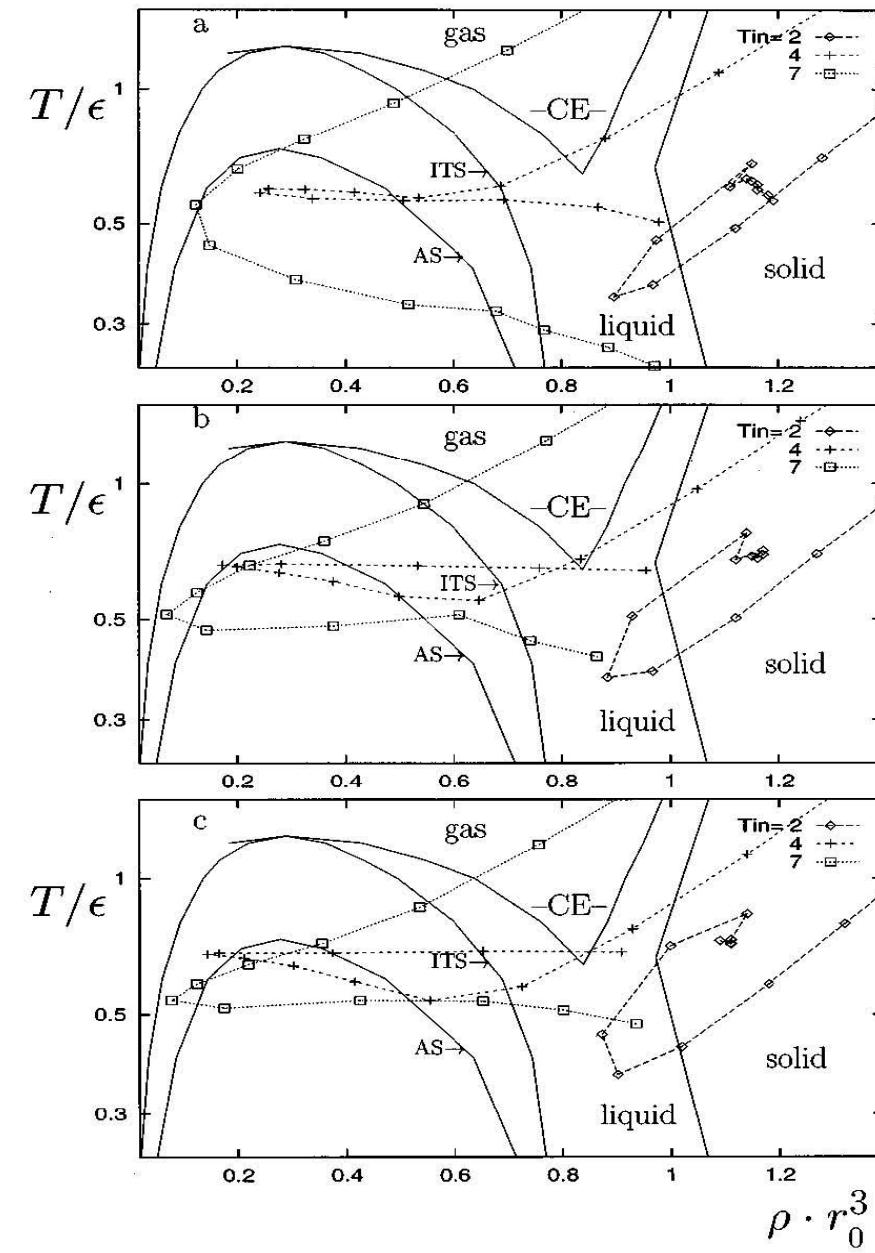
Initialization: microcanonical ensemble for the dynamical evolution

Particles are distributed randomly in a large sphere
the initial density is about $0.75/r_0^3$ and
propagated using the frictional cooling method to
a local minimum of the total potential energy.



Maxwell-Boltzmann distribution

Maxwell-Boltzmann distribution



CMD vs mean field treatment

One-body distribution function $f_1(\mathbf{r}, \mathbf{p}, t)$

$$f_1(\mathbf{r}, \mathbf{p}, t) = \sum_{i=1}^{A_{\text{tot}}} \delta(\mathbf{r} - \mathbf{r}_i) \delta(\mathbf{p} - \mathbf{p}_i),$$

$$\partial_t f_1 + \frac{\mathbf{p}}{m} \cdot \partial_{\mathbf{r}} f_1 = \int \partial_{\mathbf{r}} V(\mathbf{r}, \mathbf{r}_2) \partial_{\mathbf{p}} f_2 d\mathbf{r}_2 d\mathbf{p}_2$$

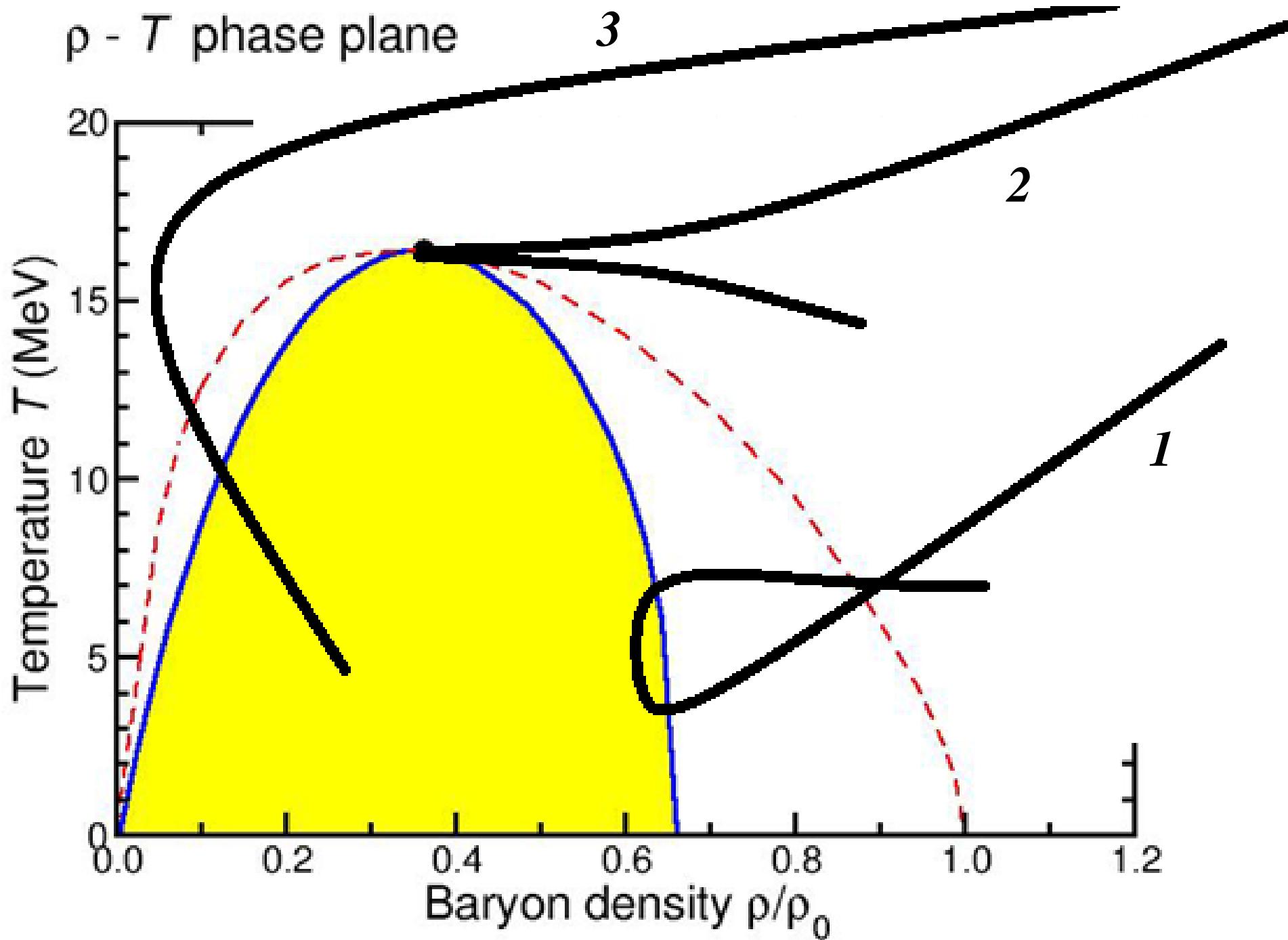
$$f_2(\mathbf{r}, \mathbf{r}_2, \mathbf{p}, \mathbf{p}_2, t) = \sum_{i \neq j} \delta(\mathbf{r} - \mathbf{r}_i) \delta(\mathbf{p} - \mathbf{p}_i) \delta(\mathbf{r}_2 - \mathbf{r}_j) \delta(\mathbf{p}_2 - \mathbf{p}_j)$$

$$f_1 = \overline{f_1} + \delta f_1; \quad U = \overline{U} + \delta U$$

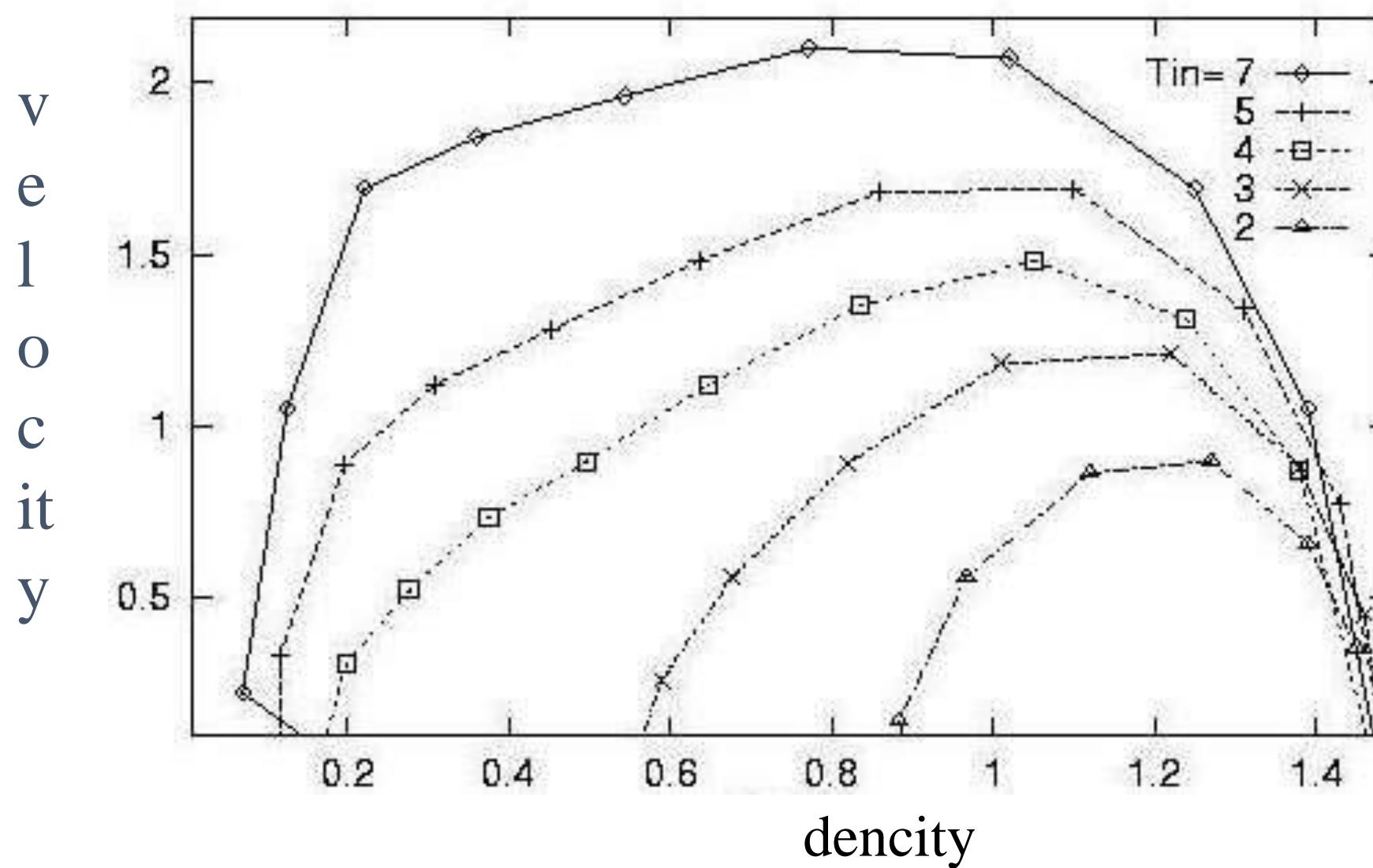
$$\partial_t \overline{f_1} + \frac{\mathbf{p}}{m} \cdot \partial_{\mathbf{r}} \overline{f_1} - \partial_{\mathbf{r}} \overline{U} \partial_{\mathbf{p}} \overline{f_1} = \langle \partial_{\mathbf{r}} \delta U \partial_{\mathbf{p}} \delta f_1 \rangle.$$

Vlasov, mean field

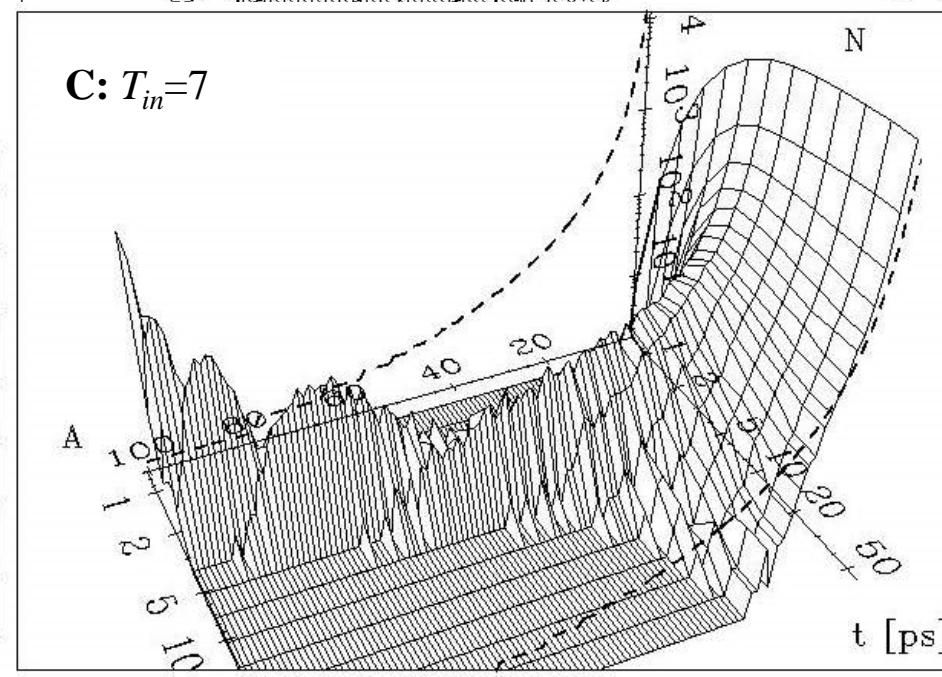
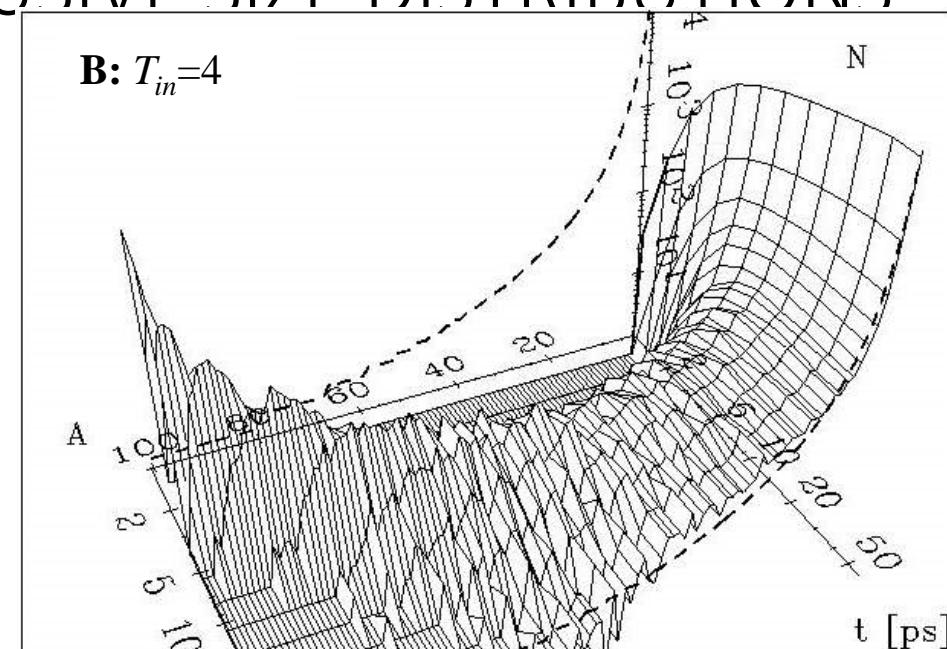
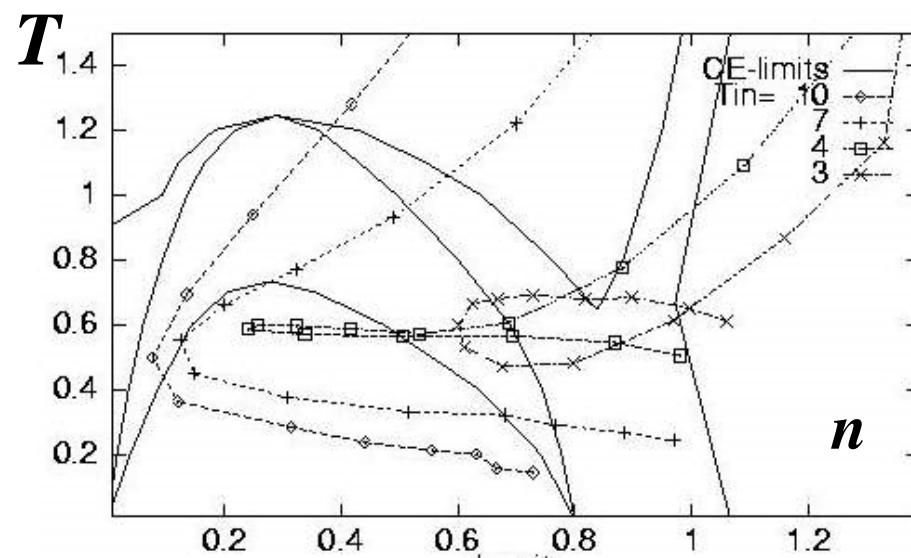
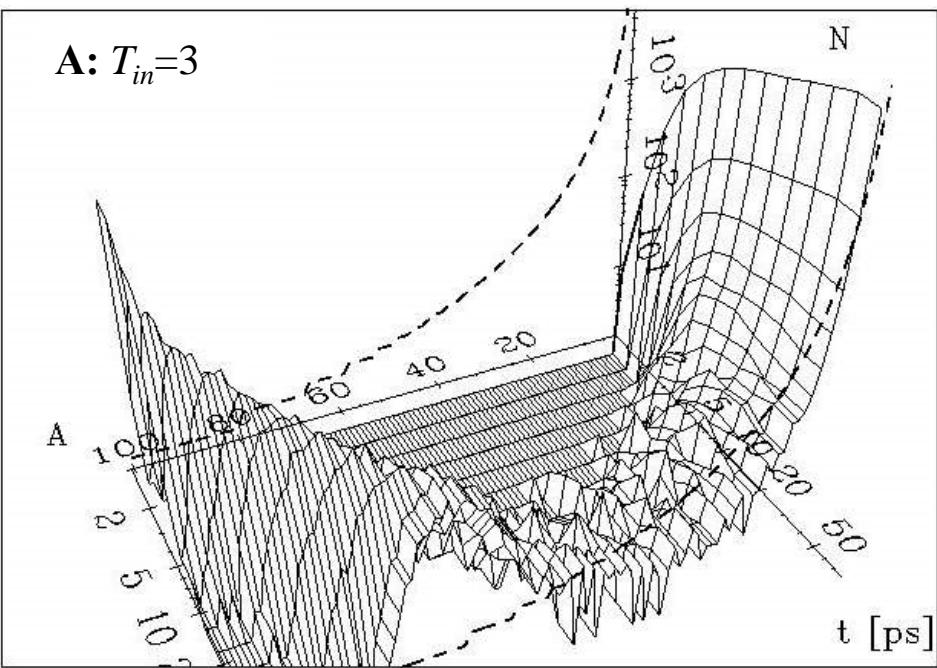
Collision term



Flow velocity

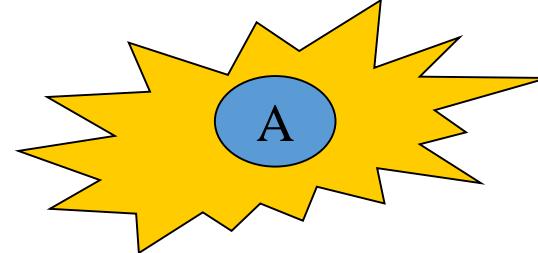


STATISTICAL PROPERTIES OF INCLUSIVE SIZE DISTRIBUTIONS



FISHER'S DROPLET MODEL

$$G_{\text{no drop}} = \mu_g(A + B)$$



$$G_{\text{with drop}} = \mu_g A + \mu_g B + 4\pi R^2 \sigma + k_B T \tau \ln A$$

the fragment mass distribution $\sim \exp\{-\Delta G/\kappa T\}$

$$N(A) = \left[Y_0 \exp\left(\frac{\Delta\mu}{k_B T} A - \frac{4\pi r_0^2 \sigma}{k_B T} A^{2/3} - \tau \ln A\right) \right].$$

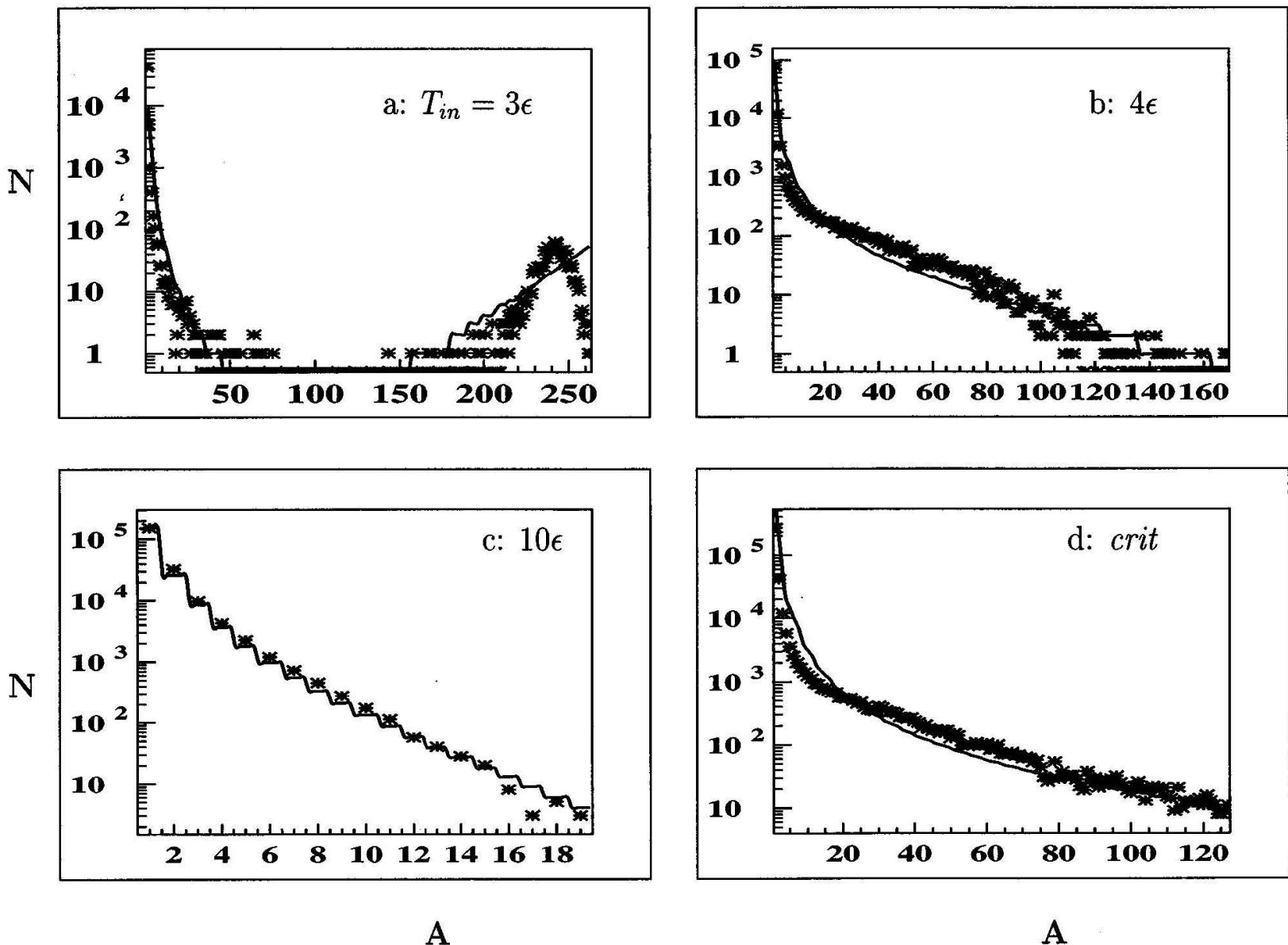
difference in the gas and liquid chemical potentials

$$N(A) = \left[Y_0 \exp\left(\frac{\Delta\mu}{k_B T} A - \tau \ln A\right) \right]; \quad T \geq T_c.$$

$$N(A) = [Y_0 A^{-\tau}]; \quad T = T_c$$

Fragment size distributions fit

$T=2.23$



conditional moments

$$M_k^{(j)} = \sum_A A^k n^{(j)}(A)$$

At critical point

$$N(A) = [Y_0 A^{-\tau}]; \quad T = T_c$$

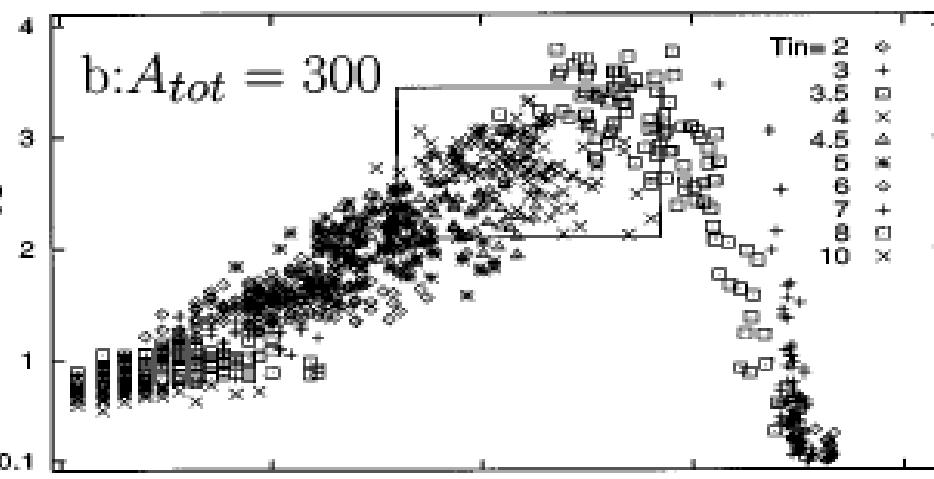
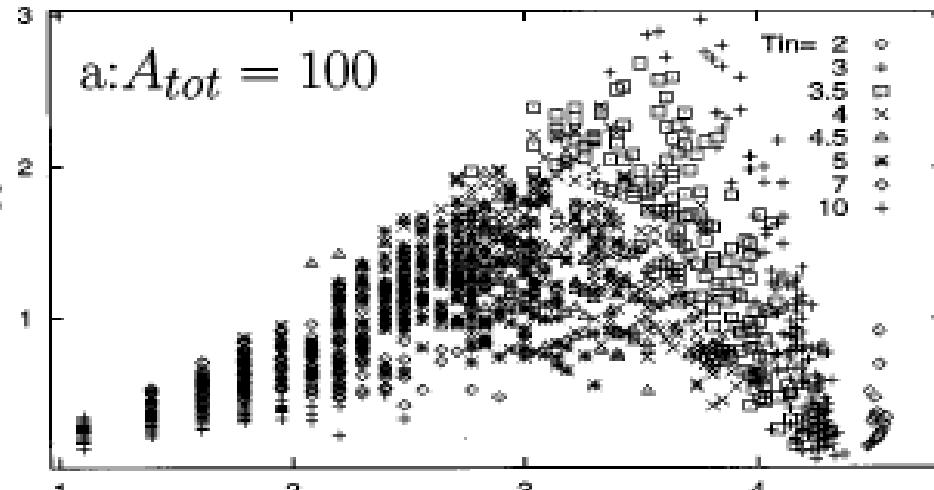
$$\begin{aligned} M_k &\sim \int_1^\infty \text{Infinity} A^{(\kappa-\tau)} dA \sim \\ &\sim A^{(\kappa+1-\tau)} \quad \int_1^\infty \text{Infinity} \end{aligned}$$

~Const at $k=0,1$

~Infinity at $k>1$

Campi scatter plot

$\ln S_2$

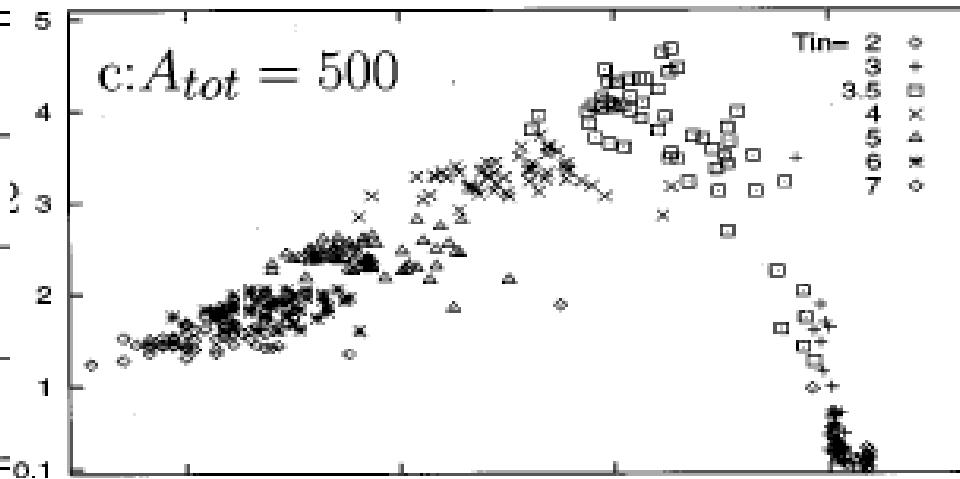
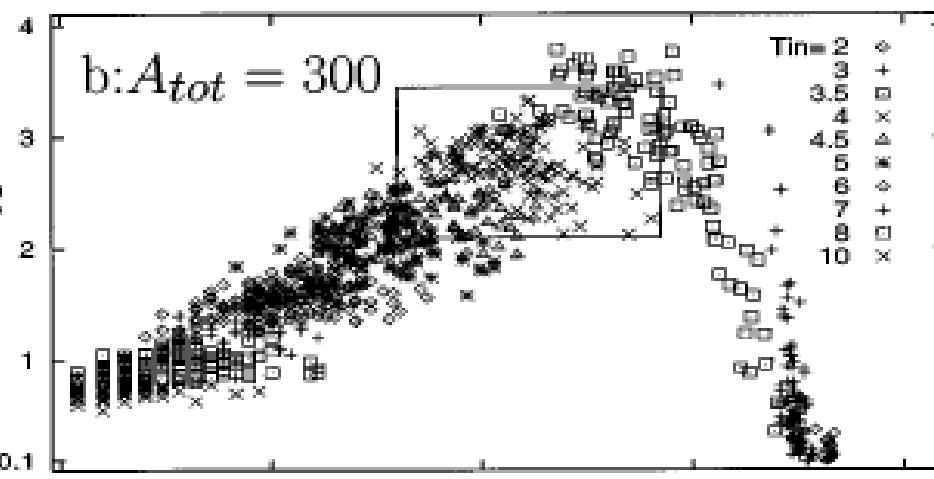


conditional moments

$$M_k^{(j)} = \sum_A A^k n^{(j)}(A)$$

$$S_k^{(j)} = M_k^{(j)} / M_1^{(j)}$$

higher moments ($k > 1$)
diverge at the critical point

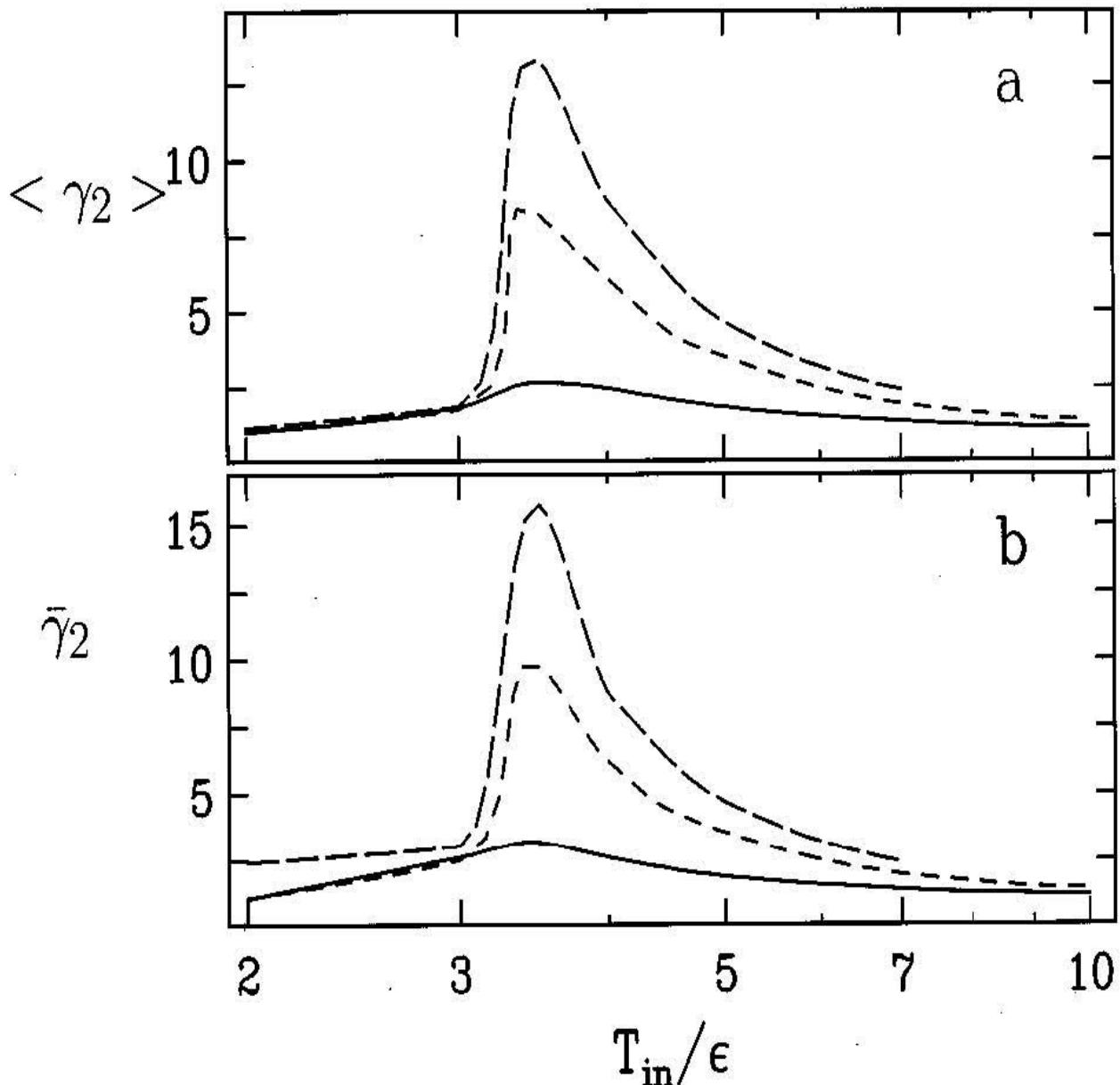


$\ln A_b$

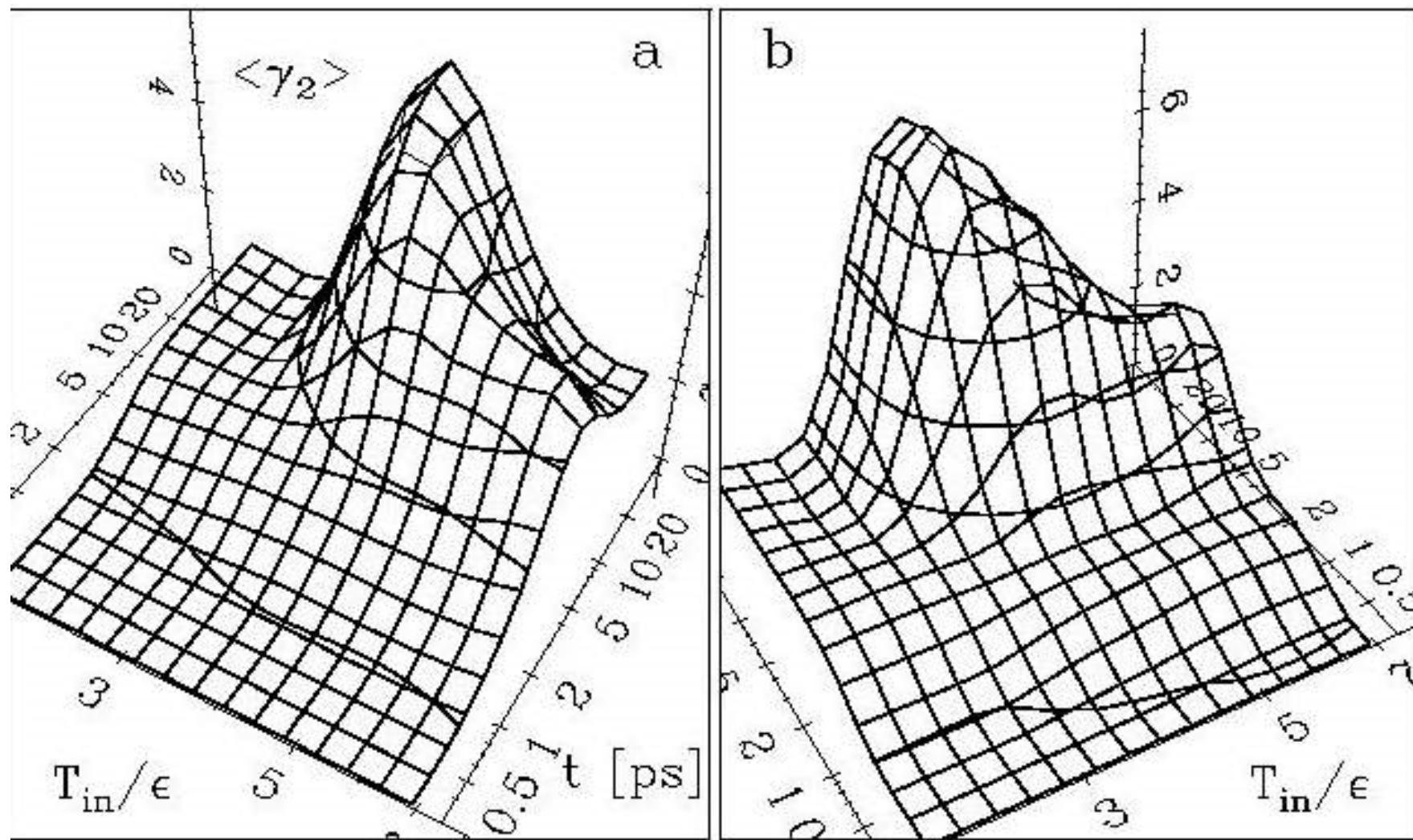
$\ln A_b$

Reduced variance

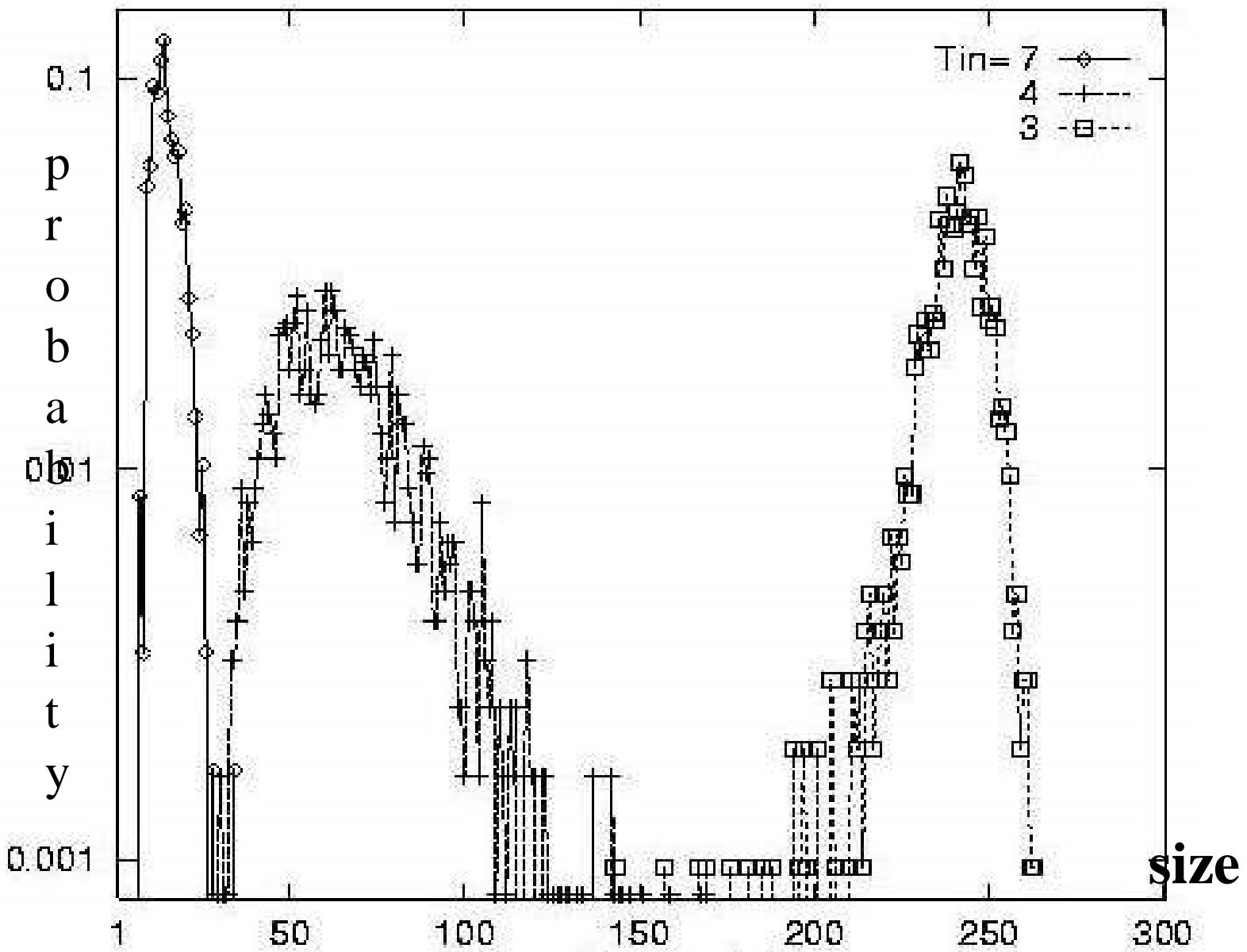
$$\gamma_2 = \frac{M_2 M_0}{M_1^2}.$$



Reduced variance vs time



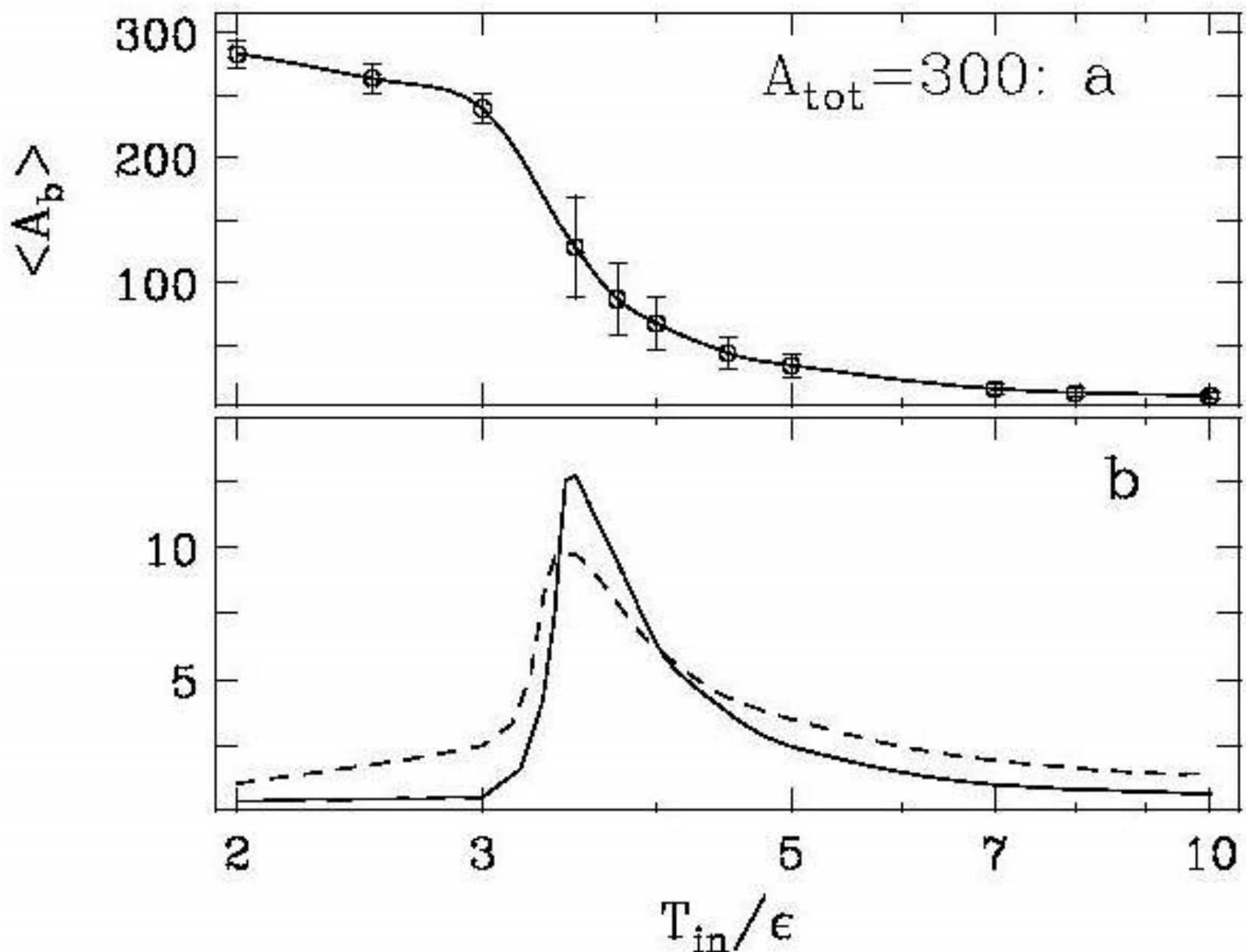
Biggest fragment



normalized variance of the size of the biggest fragment, NVB

$$\Delta_{A_b}^2 = \langle A_b^2 \rangle - \langle A_b \rangle^2$$

$$\gamma_{\text{NVB}} = \frac{\Delta_{A_b}^2}{\langle A_b \rangle}$$



Summary

- **Critical evolution of hot van der Waals droplets**
- Regimes
 - isentropic expansion
 - Fragmentation (4 - 6 units)
 - Cooling of fragments
- Critical behavior become visible by the use of different analytical tools
 - statistics, correlations, fluctuations
- droplet thermal stability changes sharply at critical point

Thank you

Magnetic field B

$$p = \frac{T}{v-b} - \frac{a}{v^2} + \frac{h}{v^{2/3}}$$

$$h = \frac{B^2}{2\mu} = 15 \text{keV} \frac{B^2}{T T^2}$$

matter:

Equation of state: $pT(\rho)$

