

The Pomeron, Odderon, and N^* resonances in ϕ -meson photoproduction

Sang-Ho Kim (金相鎬)
Pukyong National University (PKNU)



Contents based on
arXiv: 1904.05133 [hep-ph]

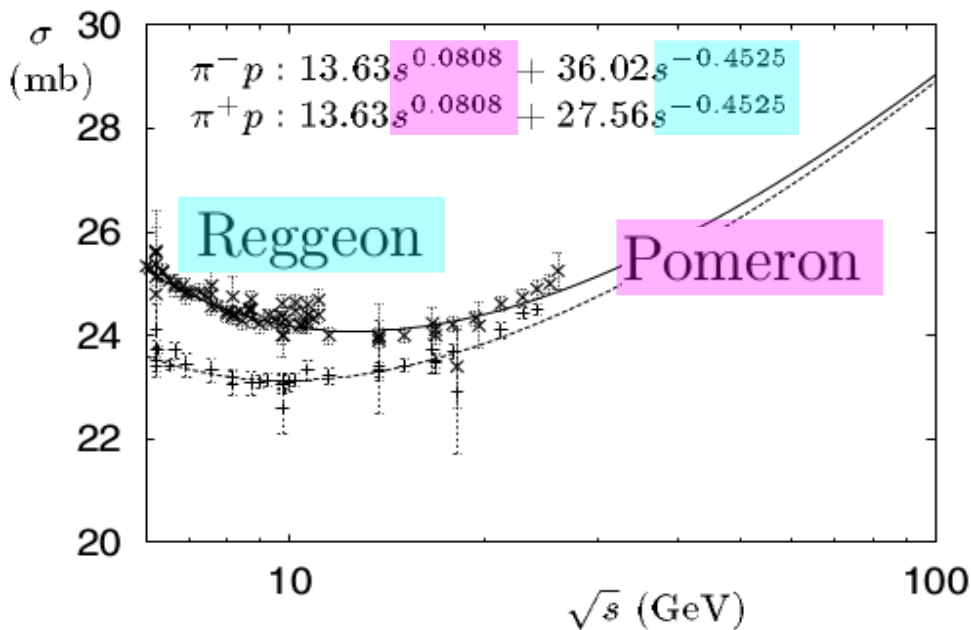
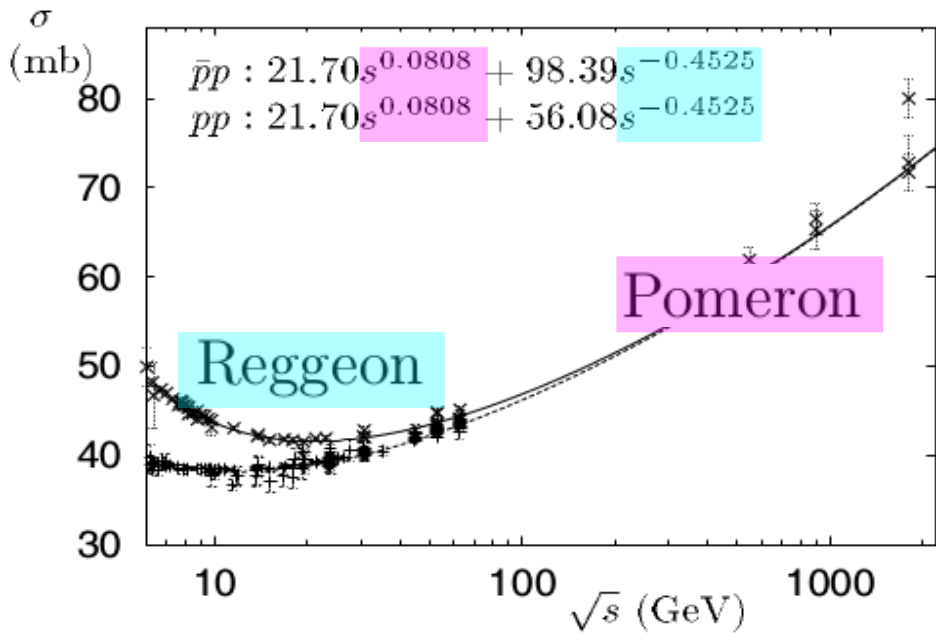
In collaboration with
Seung-il Nam (PKNU)

Contents

$$\gamma p \rightarrow \phi p$$

- ◆ Background
- ◆ Formalism
- ◆ Numerical Results
- ◆ Summary

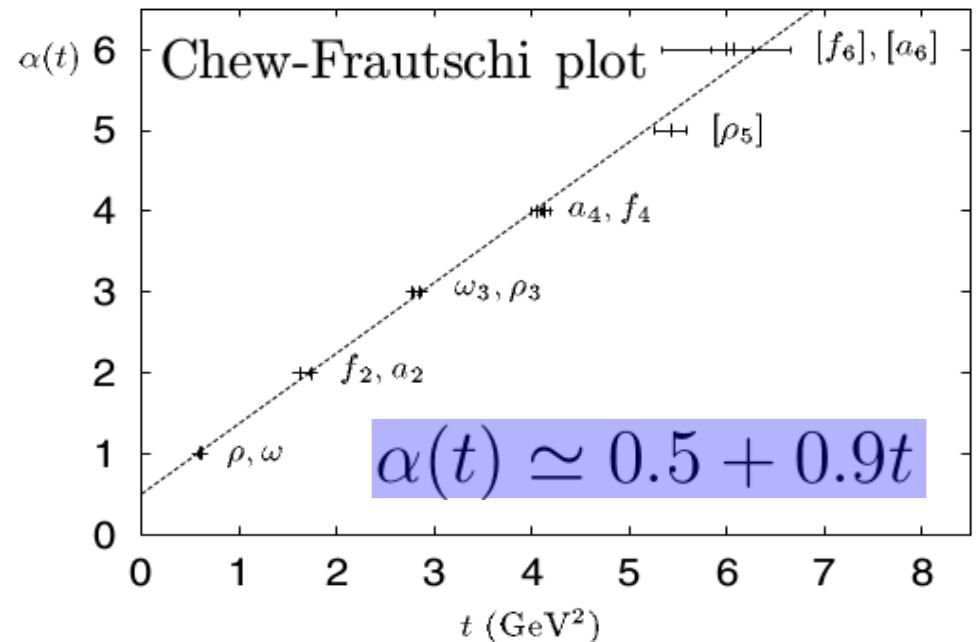
Background



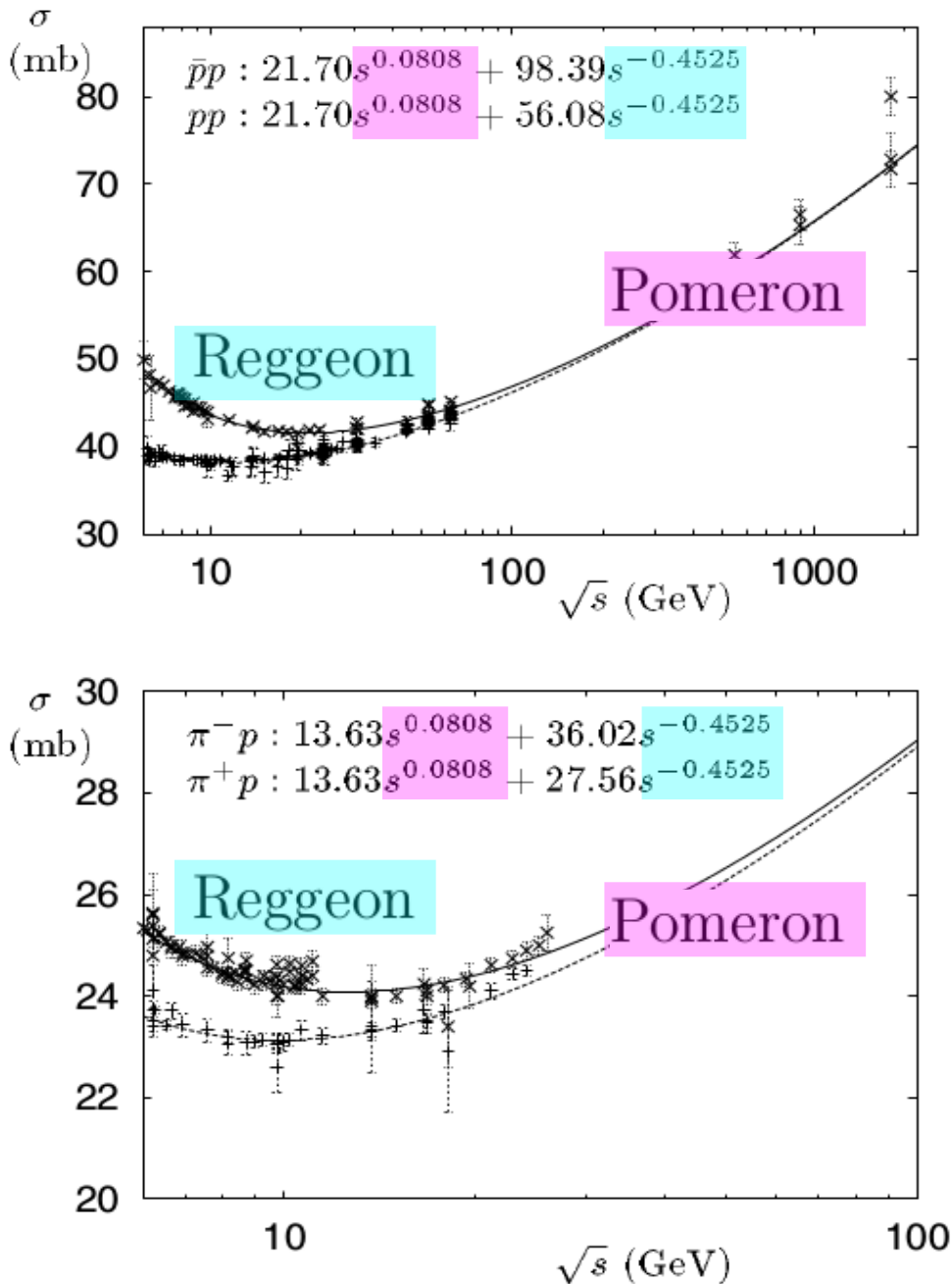
Donnachie, Pomeron Physics and QCD (2002)

Reggeon (Meson exchange)

- Describes an exchange of a family of ordinary mesons.
- Governs relatively low energy regions.
- (ρ, ω) trajectories ($C=-1$, natural parity) & (f_2, a_2) trajectories ($C=+1$, natural parity) are all degenerate.



$$\sigma \propto s^{\alpha(0)-1} = s^{-0.5}$$



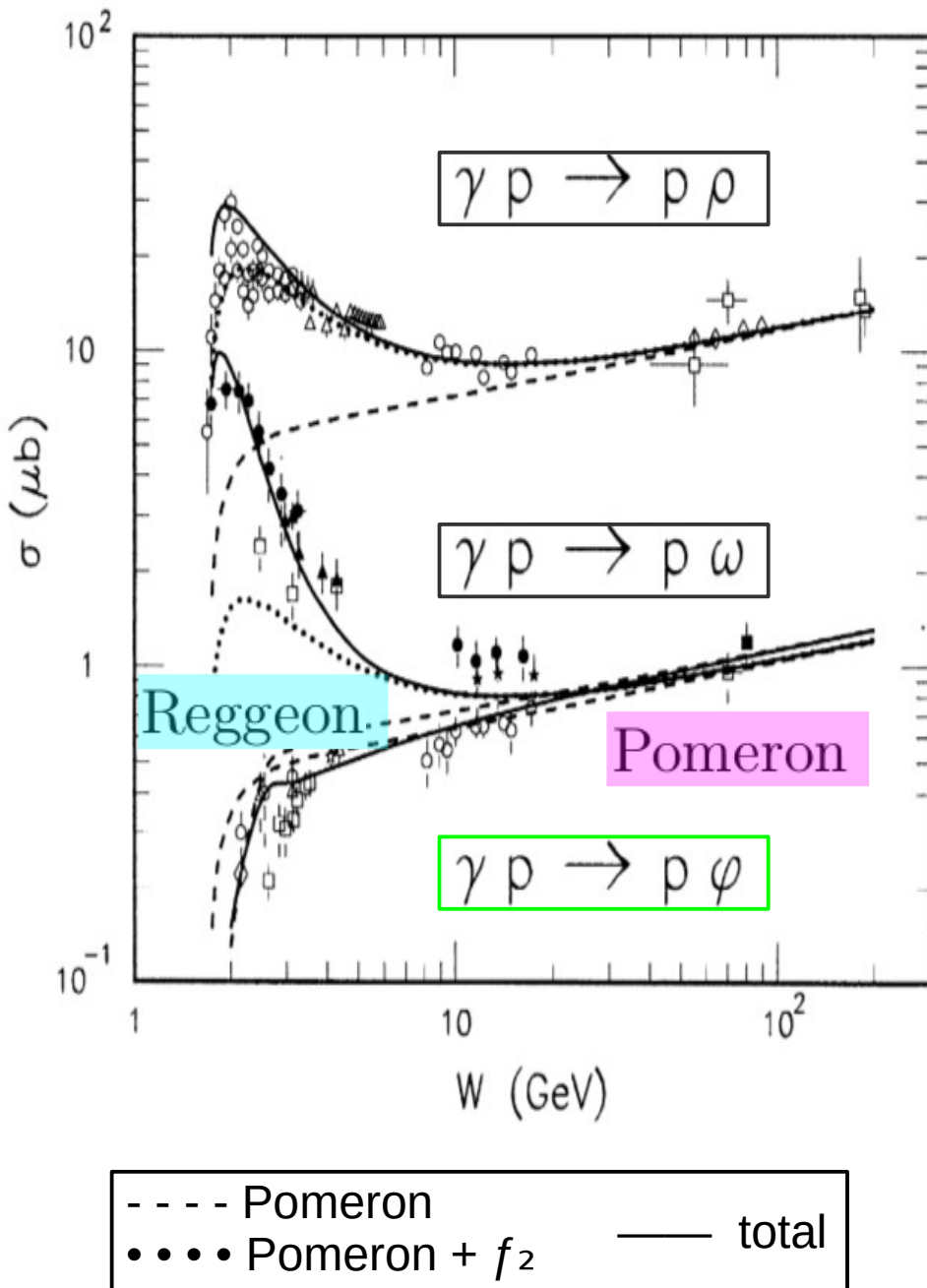
Donnachie, Pomeron Physics and QCD (2002)

Pomeron

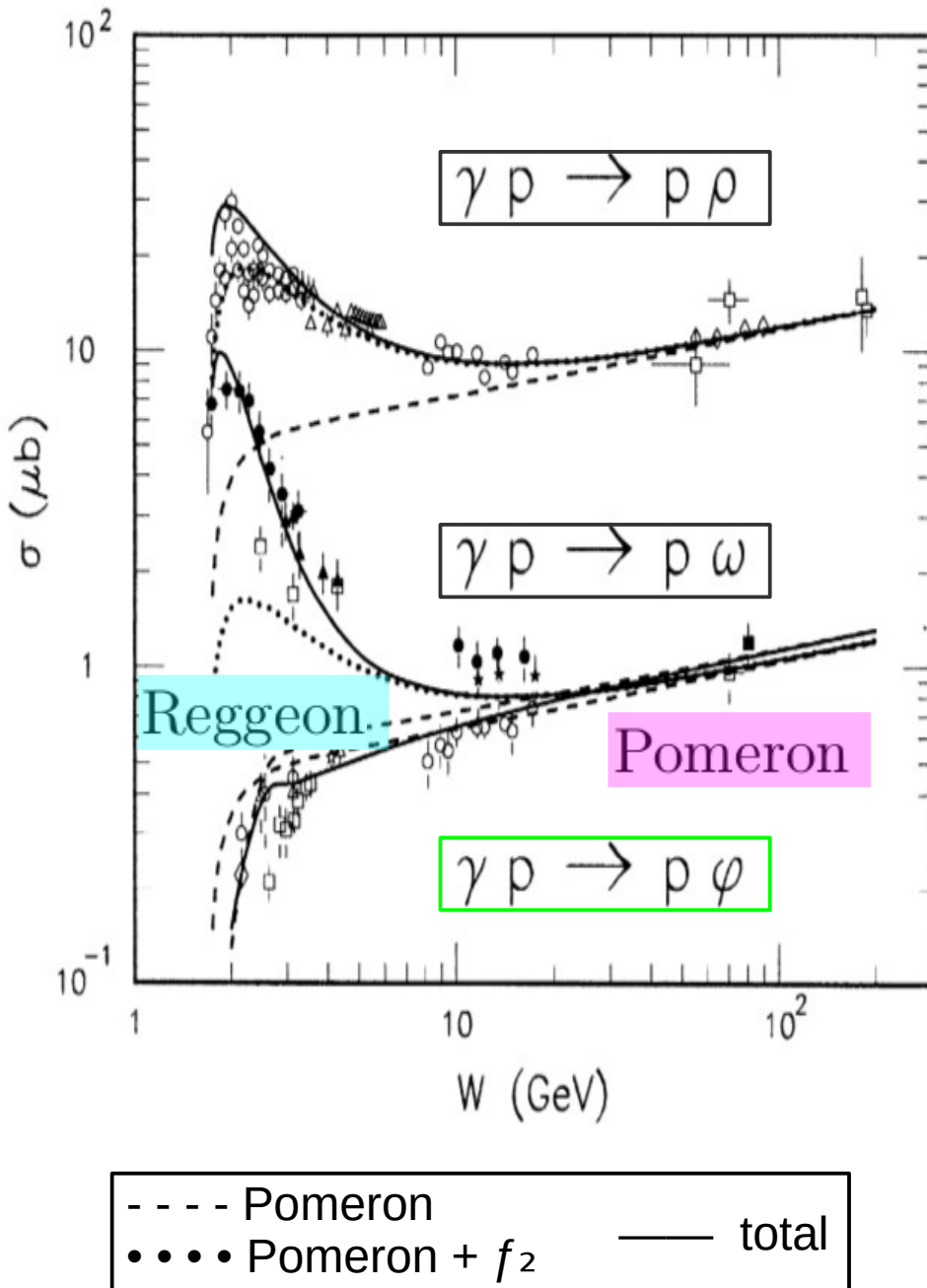
- Is not associated with meson trajectories.
 - Is known as a gluon-rich Regge trajectory with vacuum quan. number, ($J^{PC} = 0^{++}$).
 - Governs relatively high energy regions.
-
- There is no deep theory reason for the Pomeron hypothesis, but the phenomenology based on which turns out to be very successful.
 - Pomeron trajectory:

$$\alpha_P(t) \simeq 1.08 + 0.25t$$

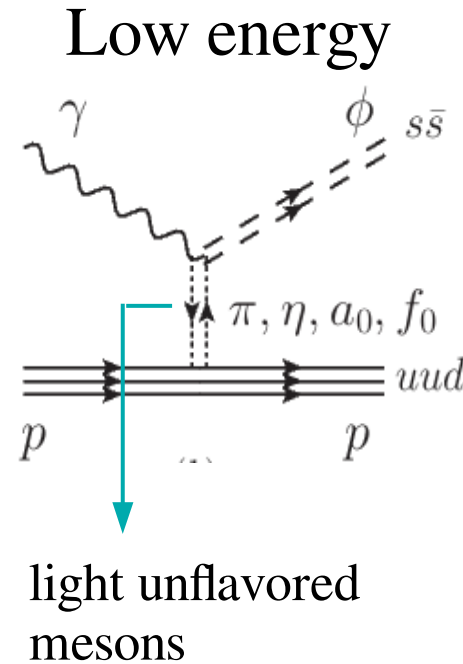
$$\sigma \propto s^{\alpha(0)-1} = s^{0.08}$$



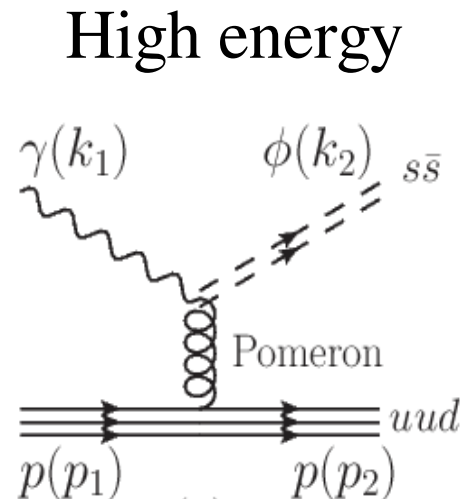
Laget, PLB.489.313(2000)



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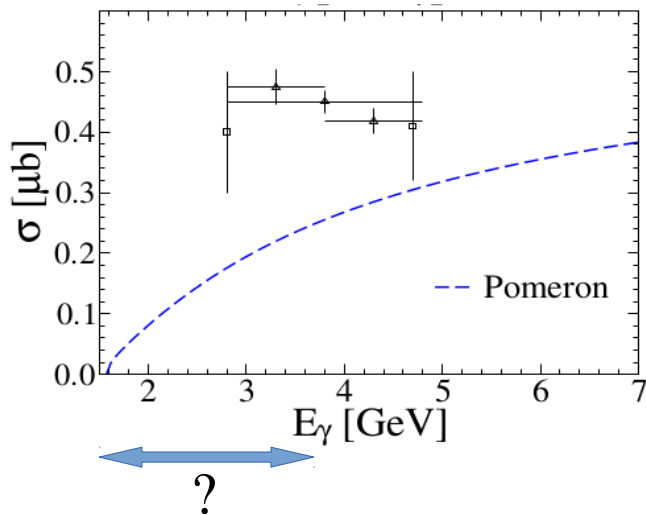


- The dynamics of **Reggeon** is related to non-perturbative QCD in q-q̄ sector.
- OZI suppressed.
- PS(0⁻) π & η exchange
- S(0⁺) a_0 & f_0 exchange

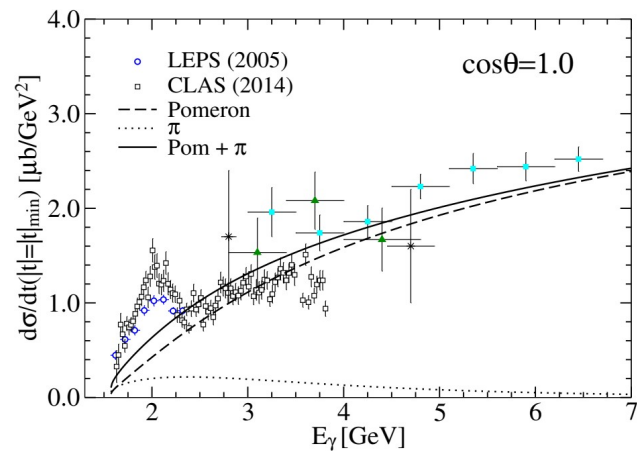


- **Pomeron** is the result of non-perturbative QCD interaction in gluon sector.
- Natural parity (+1).

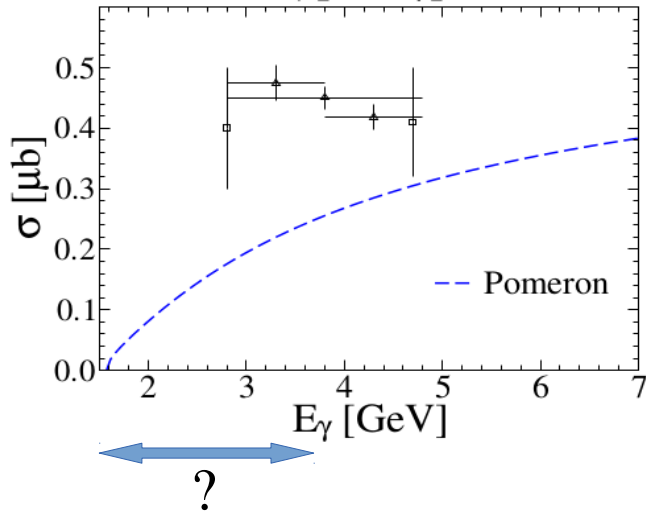
- Pomeron alone is not sufficient to describe low energy regions.



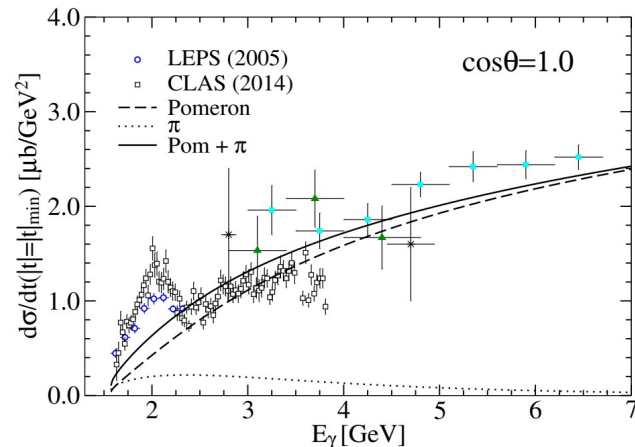
- Only forward angle data existed before.



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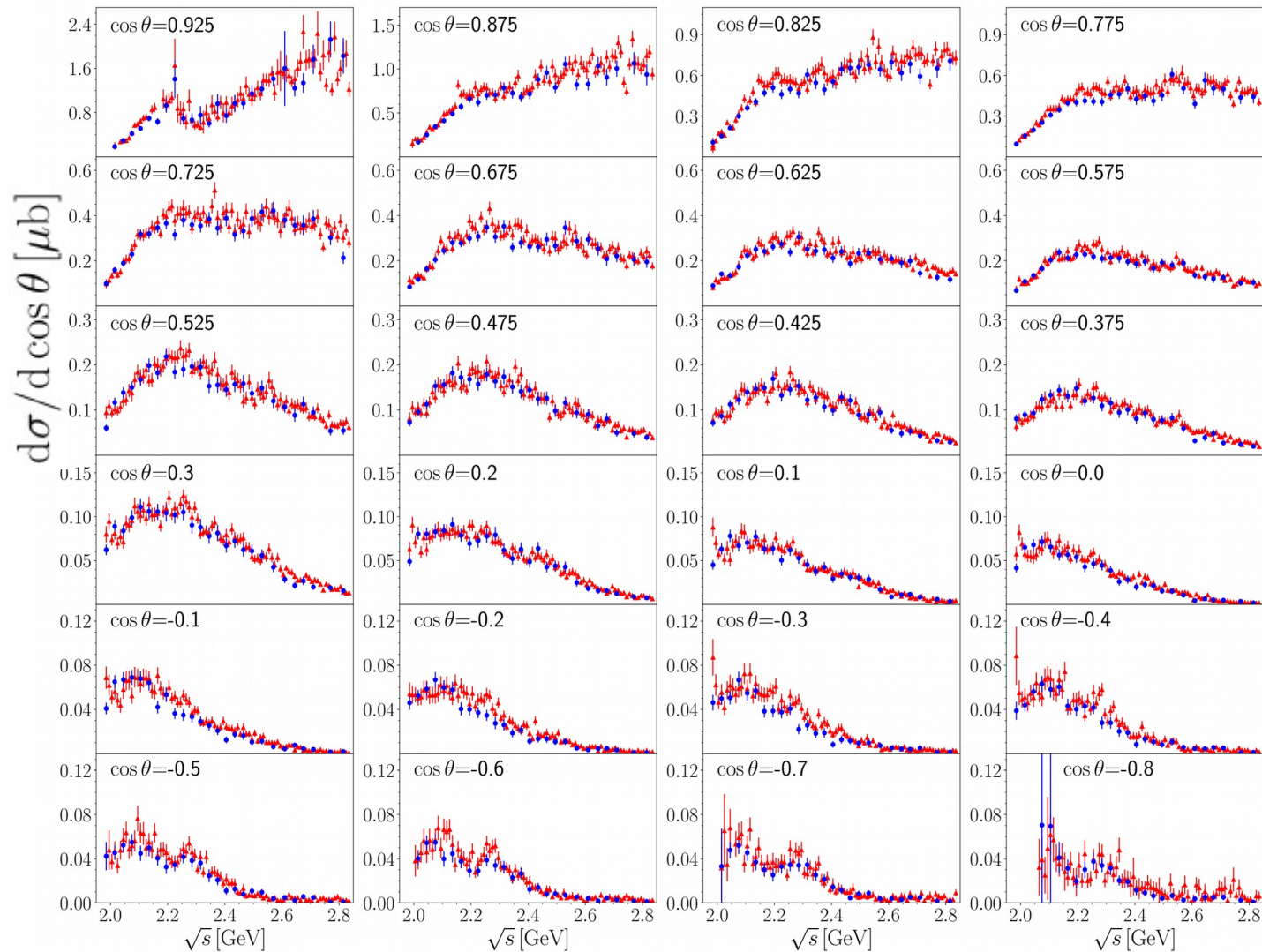


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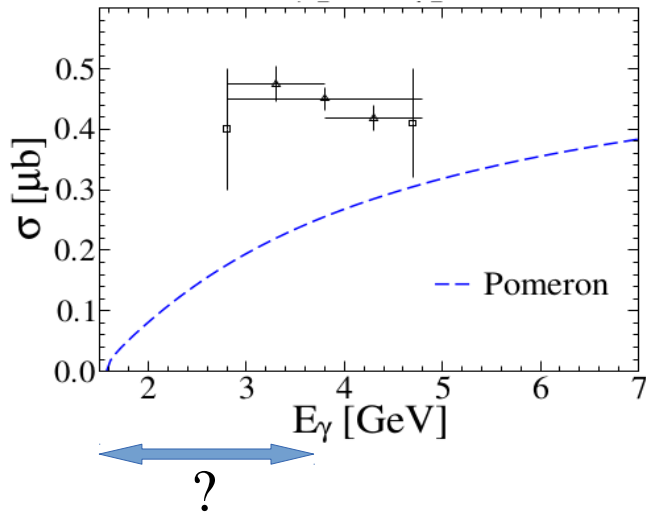


- Abundant data are reported at CLAS at full scattering angles & low energies ($\sqrt{s} = 1.9-2.8$ GeV).

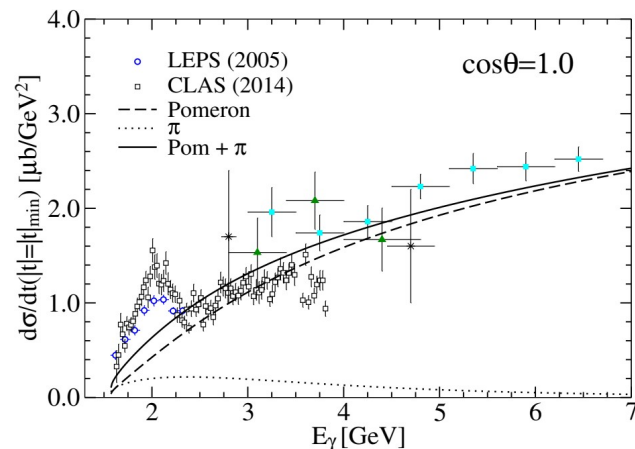
[Seraydaryan, PRC.89.055206] & [Dey, PRC.89.055208] (2014)



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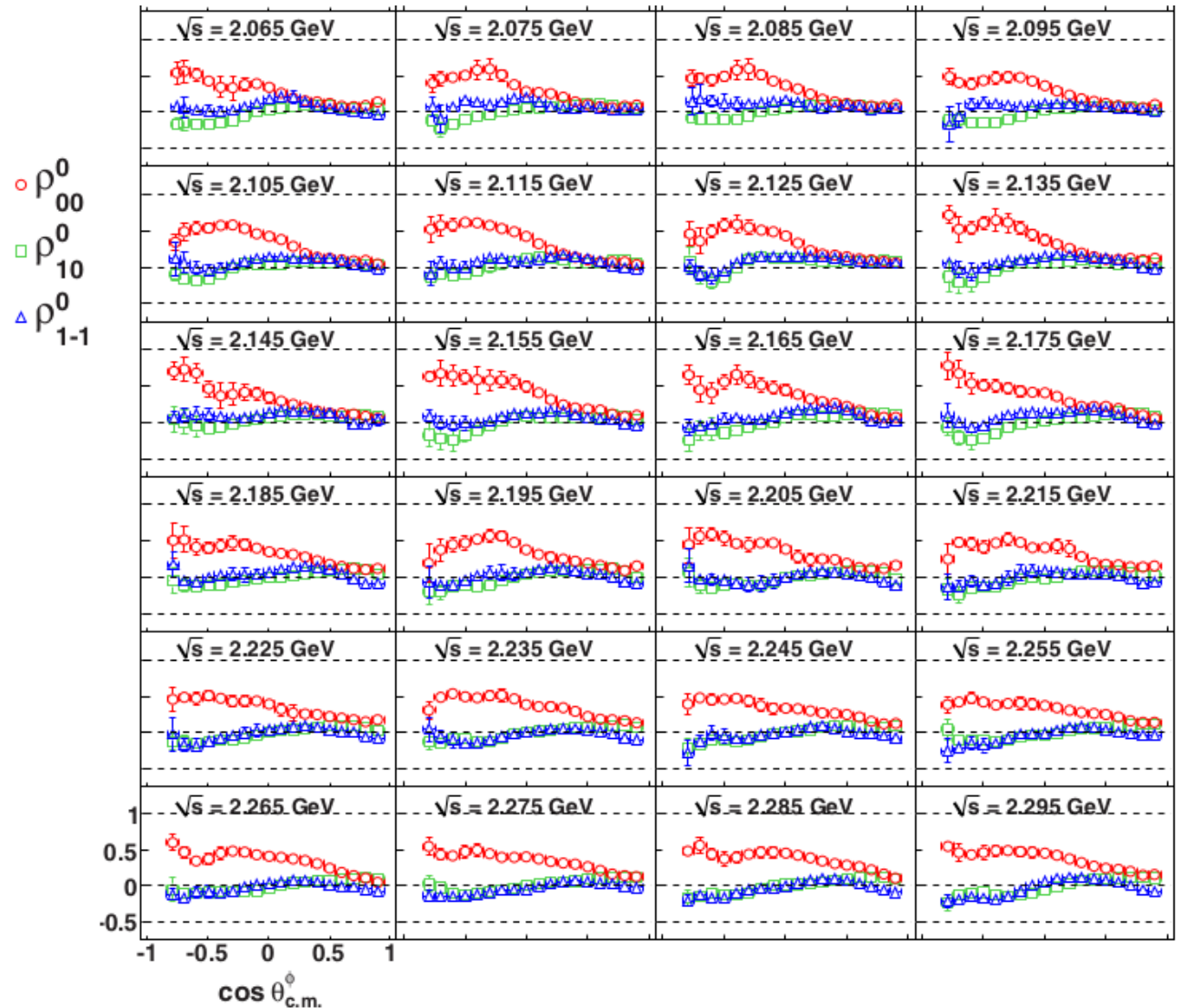


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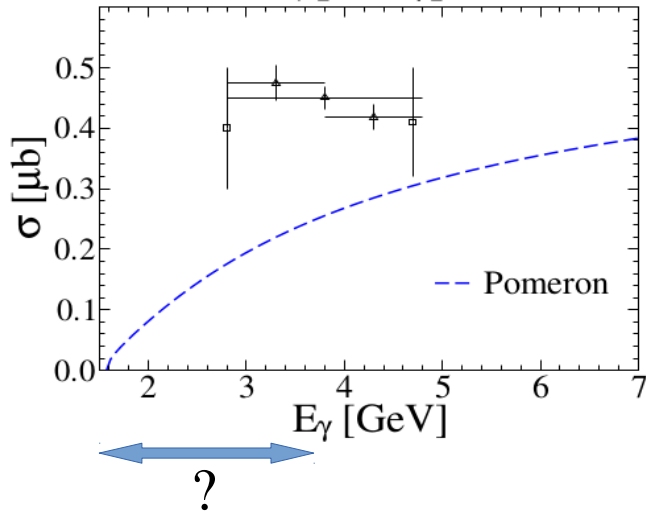


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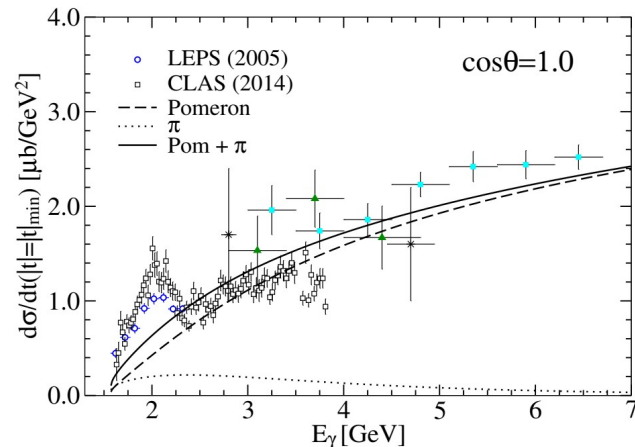
[Seraydaryan, PRC.89.055206] & [Dey, PRC.89.055208] (2014)



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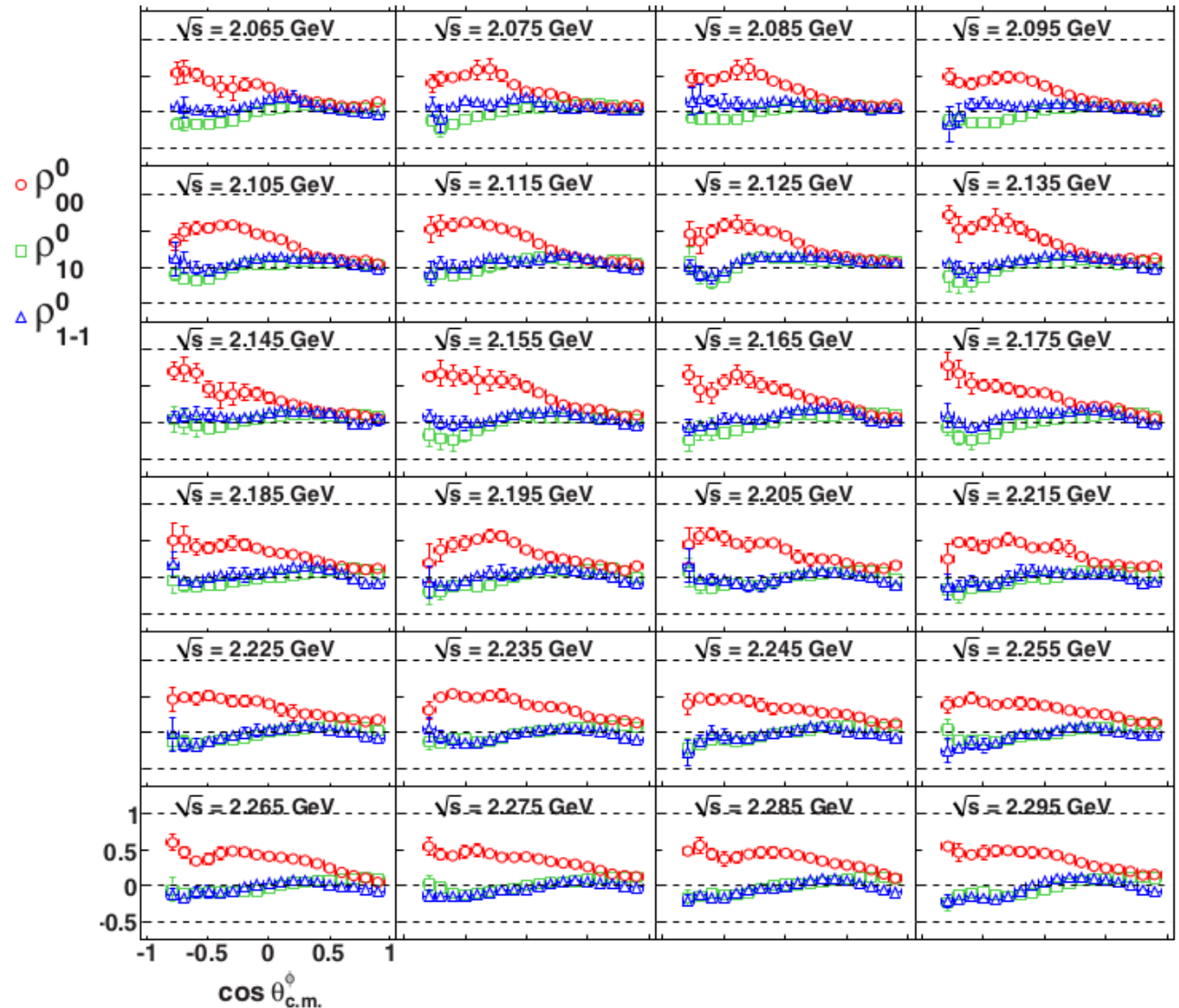


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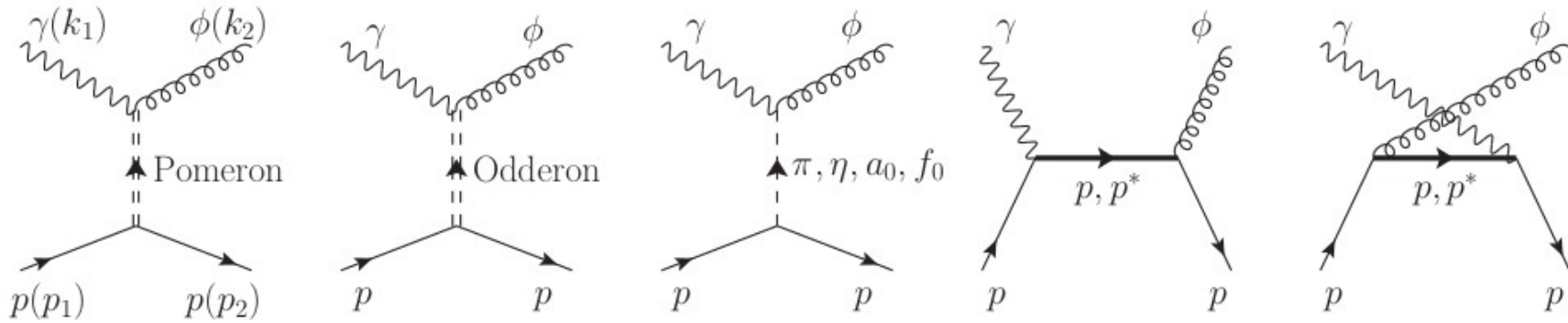
[Seraydaryan, PRC.89.055206] & [Dey, PRC.89.055208] (2014)



- We need a systematic analysis on ϕ photoproduction.

Formalism

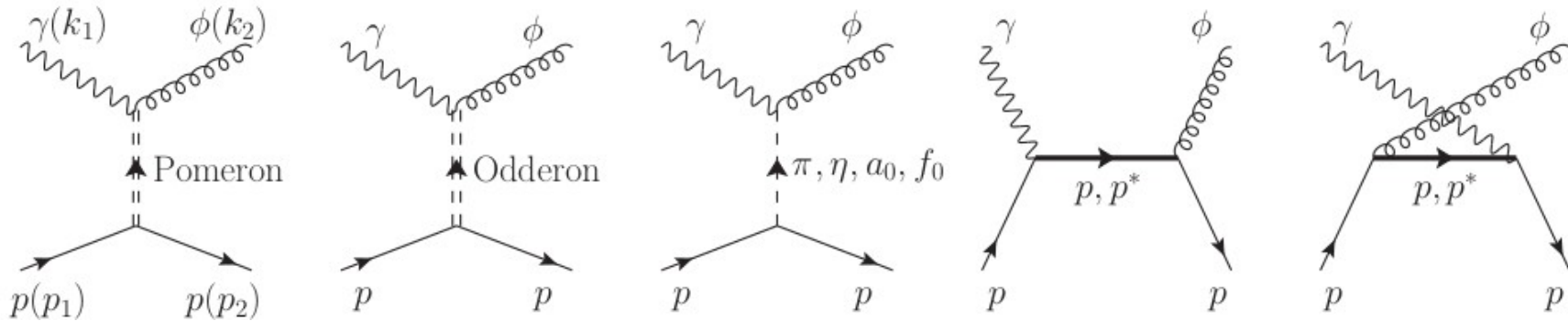
- Feynman diagrams for $\gamma p \rightarrow \phi(1020)p$



Previous work: Pomeron + PS(π, η) + N + assumed N^*

Our work: Pomeron + PS(π, η) + N + Odderon + S(a_0, f_0) + PDG N^*

• Feynman diagrams for $\gamma p \rightarrow \phi(1020)p$



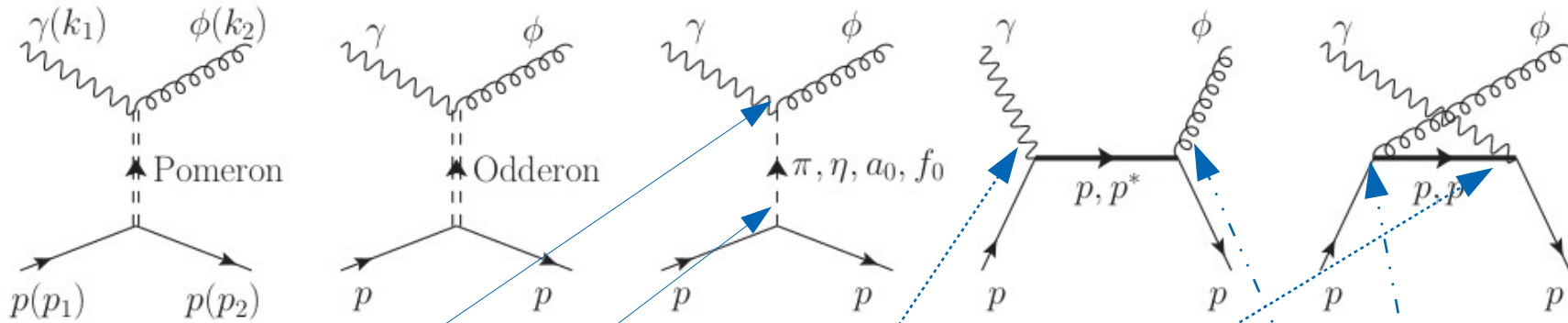
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• Effective Lagrangians

$$\left\{ \begin{array}{l} \mathcal{L}_{\gamma\Phi\phi} = \frac{eg_{\gamma\Phi\phi}}{M_\phi} \epsilon^{\mu\nu\alpha\beta} \partial_\mu A_\nu \partial_\alpha \phi_\beta \Phi, \\ \mathcal{L}_{\gamma S\phi} = \frac{eg_{\gamma S\phi}}{M_\phi} A^{\mu\nu} \phi_{\mu\nu} S, \\ \mathcal{L}_{\Phi NN} = -ig_{\Phi NN} \bar{N} \gamma_5 N \Phi, \\ \mathcal{L}_{SNN} = -g_{SNN} \bar{N} N S, \end{array} \right. \quad \begin{array}{l} \mathcal{L}_{\gamma NN} = -e\bar{N} \left[\gamma_\mu - \frac{\kappa_N}{2M_N} \sigma_{\mu\nu} \partial^\nu \right] N A^\mu, \\ \mathcal{L}_{\phi NN} = -g_{\phi NN} \bar{N} \left[\gamma_\mu - \frac{\kappa_{\phi NN}}{2M_N} \sigma_{\mu\nu} \partial^\nu \right] N \phi^\mu \end{array}$$

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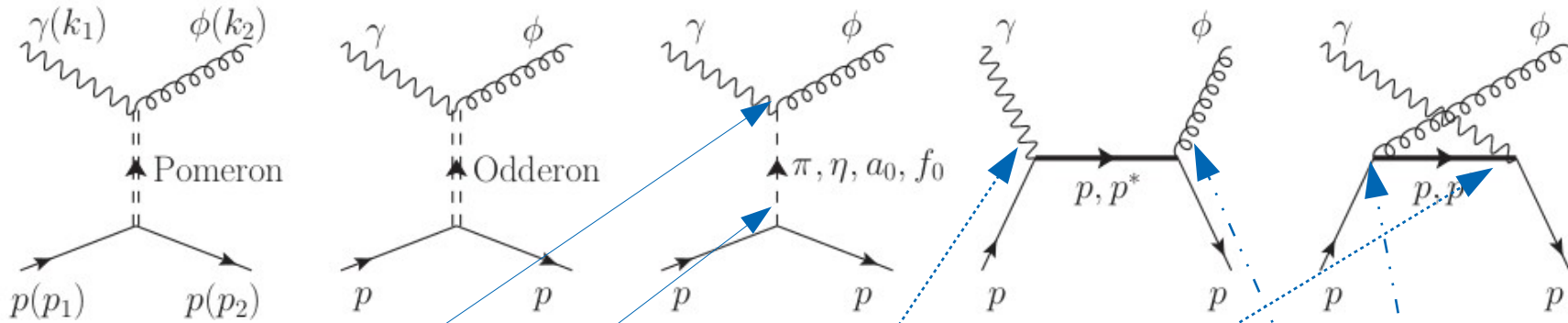
• Effective Lagrangians

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$$\mathcal{L}_{\gamma NN} = -e\bar{N} \left[\gamma_\mu - \frac{\kappa_N}{2M_N} \sigma_{\mu\nu} \partial^\nu \right] N A^\mu,$$

$$\mathcal{L}_{\phi NN} = -g_{\phi NN} \bar{N} \left[\gamma_\mu - \frac{\kappa_{\phi NN}}{2M_N} \sigma_{\mu\nu} \partial^\nu \right] N \phi^\mu$$

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- Effective Lagrangians

$$\begin{cases}
 \mathcal{L}_{\gamma\Phi\phi} = \frac{eg_{\gamma\Phi\phi}}{M_\phi} \epsilon^{\mu\nu\alpha\beta} \partial_\mu A_\nu \partial_\alpha \phi_\beta \Phi, & \mathcal{L}_{\gamma NN} = -e\bar{N} \left[\gamma_\mu - \frac{\kappa_N}{2M_N} \sigma_{\mu\nu} \partial^\nu \right] N A^\mu, \\
 \mathcal{L}_{\gamma S\phi} = \frac{eg_{\gamma S\phi}}{M_\phi} A^{\mu\nu} \phi_{\mu\nu} S, & \\
 \mathcal{L}_{\Phi NN} = -ig_{\Phi NN} \bar{N} \gamma_5 N \Phi, & \mathcal{L}_{\phi NN} = -g_{\phi NN} \bar{N} \left[\gamma_\mu - \frac{\kappa_{\phi NN}}{2M_N} \sigma_{\mu\nu} \partial^\nu \right] N \phi^\mu, \\
 \mathcal{L}_{SNN} = -g_{SNN} \bar{N} N S, &
 \end{cases}$$

- Form factors are considered to dress the interaction vertices.

meson exchange

$$F_{\Phi,S}(t) = \frac{\Lambda_{\Phi,S}^2 - M_{\Phi,S}^2}{\Lambda_{\Phi,S}^2 - t}$$

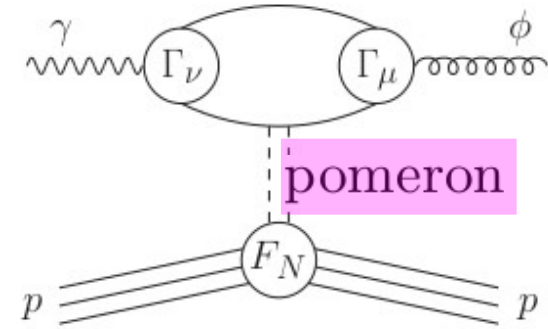
N exchange

$$F_N(x) = \frac{\Lambda_N^4}{\Lambda_N^4 + (x - M_N^2)^2}$$

N^* exchange (Gaussian form)

$$F_{N^*}(x) = \exp \left[-\frac{(x - M_{N^*}^2)^2}{\Lambda_{N^*}^4} \right]$$

We employ a Donnachie-Landshoff (DL) model.



- scattering amplitude:

$$\mathcal{M} = \varepsilon_\nu^* \bar{u}_{N'} \mathcal{M}^{\mu\nu} u_N \epsilon_\mu \quad \mathcal{M}^{\mu\nu} = -M(s, t) \Gamma^{\mu\nu}$$

- transition operator:

$$\Gamma^{\mu\nu} = \not{k}_1 \left(g^{\mu\nu} - \frac{k_2^\mu k_2^\nu}{k_2^2} \right) - \gamma^\mu \left(k_1^\nu - \frac{k_1 \cdot k_2 k_2^\nu}{k_2^2} \right) - \left[k_2^\mu - \frac{k_1 \cdot k_2 (p_1^\mu + p_2^\mu)}{k_1 \cdot (p_1 + p_2)} \right] \left(\gamma^\nu - \frac{\not{k}_2 k_2^\nu}{k_2^2} \right)$$

- scalar function: $M(s, t) = C_P F_1(t) F_2(t) \frac{1}{s} \left(\frac{s - s_{\text{th}}}{s_P} \right)^{\alpha_P(t)} \exp \left[-\frac{i\pi}{2} \alpha_P(t) \right]$

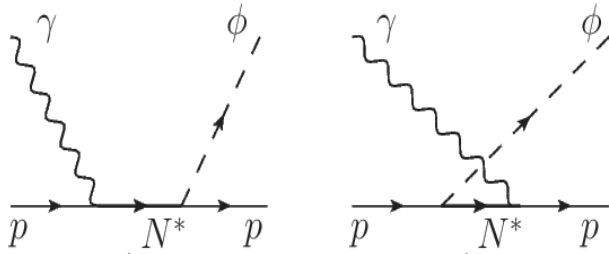
- form factors: $F_1(t) = \frac{4M_N^2 - a_N^2 t}{(4M_N^2 - t)(1 - t/t_0)^2}$, $F_2(t) = \frac{2\mu_0^2}{(1 - t/M_\phi^2)(2\mu_0^2 + M_\phi^2 - t)}$

	$\alpha_P(t)$	s_P [GeV ²]	s_{th} [GeV ²]	C_P	a_N^2	μ_0^2	t_0 [GeV ²]
Titov(2003)	1.08+0.25t	4	0	3.65	2.8	1.1	0.7
Titov(2007)	"	"	"	3.20	4	"	"
Kiswandhi(2012)	"	$(M_N + M_\phi)^2$	1.3	3.65	2.8	"	"
In this work	"	"	0	3.0	6.0	"	"

- Pomeron & Odderon trajectories:

$$\alpha_P(t) = 1.08 + (0.25 \text{ GeV}^{-2})t, \quad \alpha_O(t) = 0.95 + (0.25 \text{ GeV}^{-2})t$$

- We choose N(2100), N(2120) & N(2300) from “PDG 2018” to describe two bump structures at backward angles.



- Effective Lagrangians

$$\mathcal{L}_{\gamma NN^*} = \frac{eg_{\gamma NN^*}}{2M_N} \bar{N}^* (\sigma \cdot F) N + \text{h.c.}$$

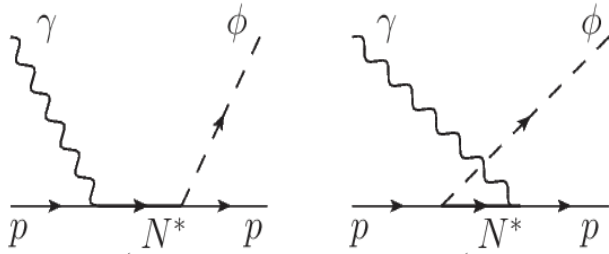
$$\mathcal{L}_{\phi NR} = g_{\phi NN^*} \bar{N} \phi N^* + \text{h.c.}$$

- $\Gamma_{N^*} = (200-300) \text{ MeV}$

PDG 2018

	N(2000)	5/2 ⁺	**
	N(2040)	3/2 ⁺	*
	N(2060)	5/2 ⁻	***
→	N(2100)	1/2 ⁺	***
→	N(2120)	3/2 ⁻	***
	N(2190)	7/2 ⁻	****
	N(2220)	9/2 ⁺	****
	N(2250)	9/2 ⁻	****
→	N(2300)	1/2 ⁺	**
	N(2570)	5/2 ⁻	**
	N(2600)	11/2 ⁻	***
	N(2700)	13/2 ⁺	**

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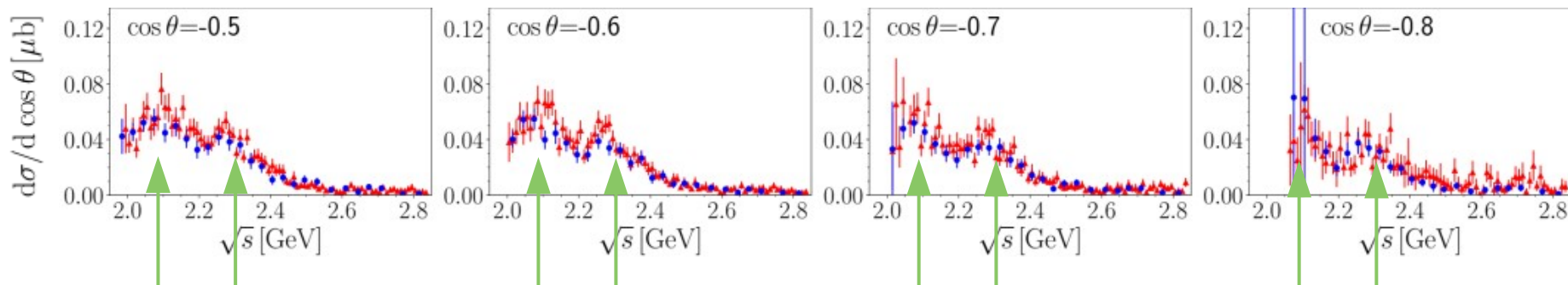
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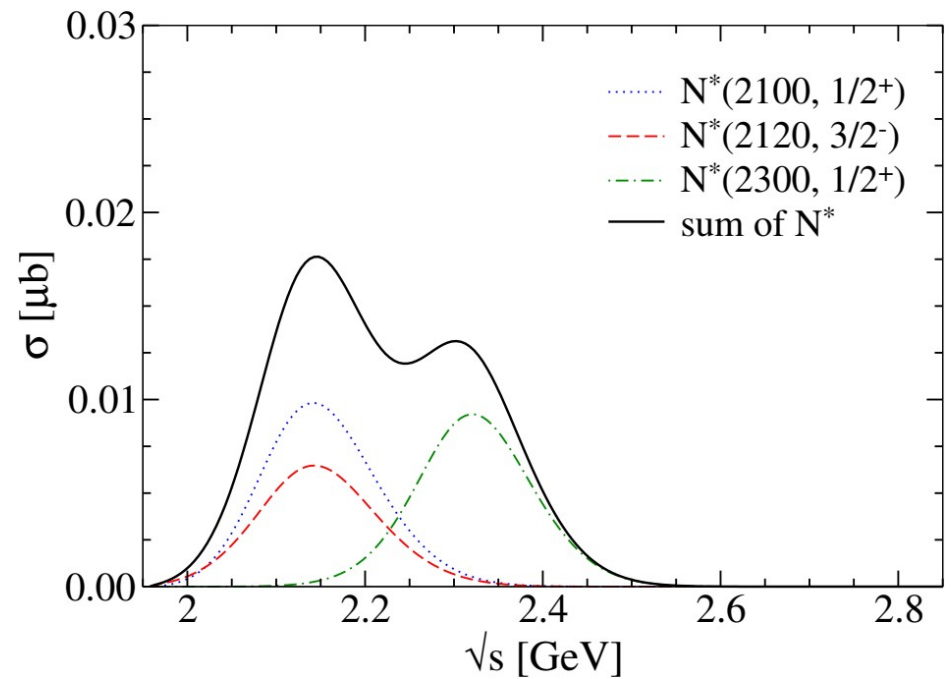
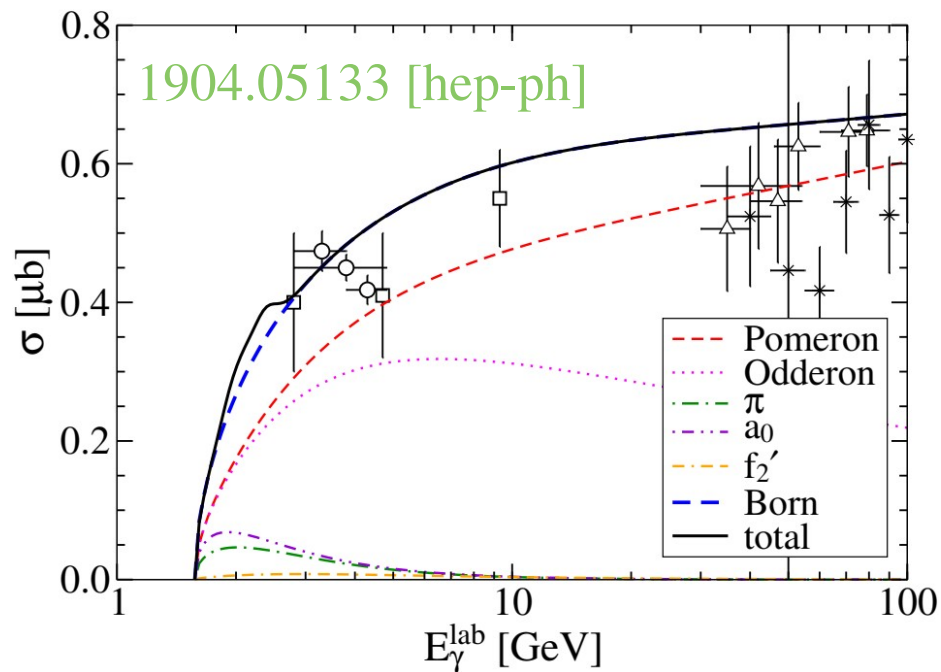
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	N(2570)	5/2 ⁻	**
	N(2600)	11/2 ⁻	***
	N(2700)	13/2 ⁺	**

1. Two bump structures are located near their pole positions, i.e. $\sqrt{s} \approx 2.1 \text{ \& } 2.3 \text{ GeV}$.
2. We expect only lower partial waves would be important.



Numerical Results



$$\mathcal{M}_{\text{total}} = \sum_i \mathcal{M}_i^{\text{Born}} + \sum_j c_j \mathcal{M}_j^{N^*}$$

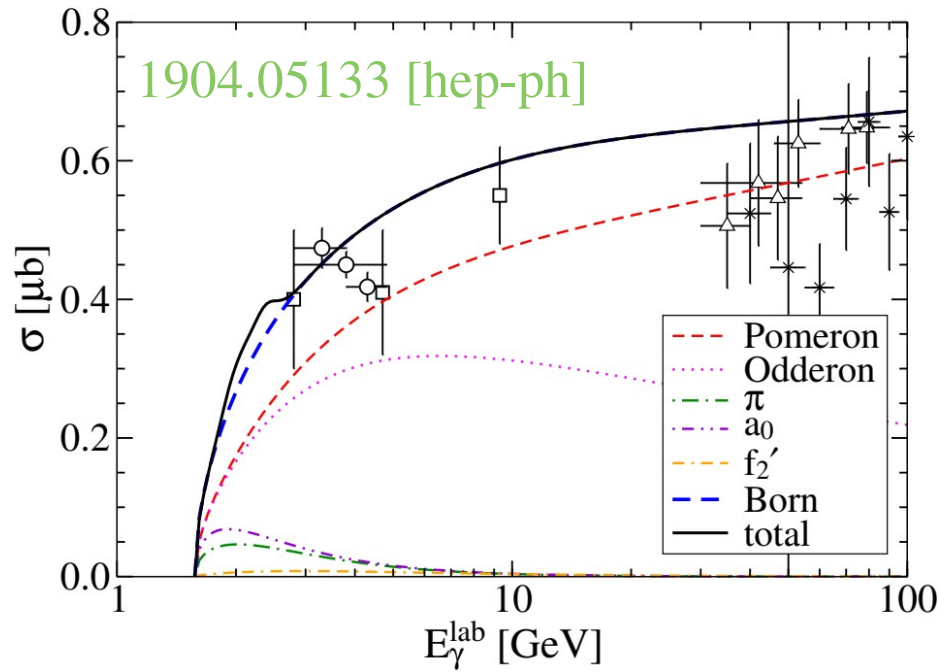
$$i = (\mathbb{P}, \mathbb{O}, \pi, \eta, a_0, f_0, f_2')$$

$$j = (N^*(2100, 1/2^+),$$

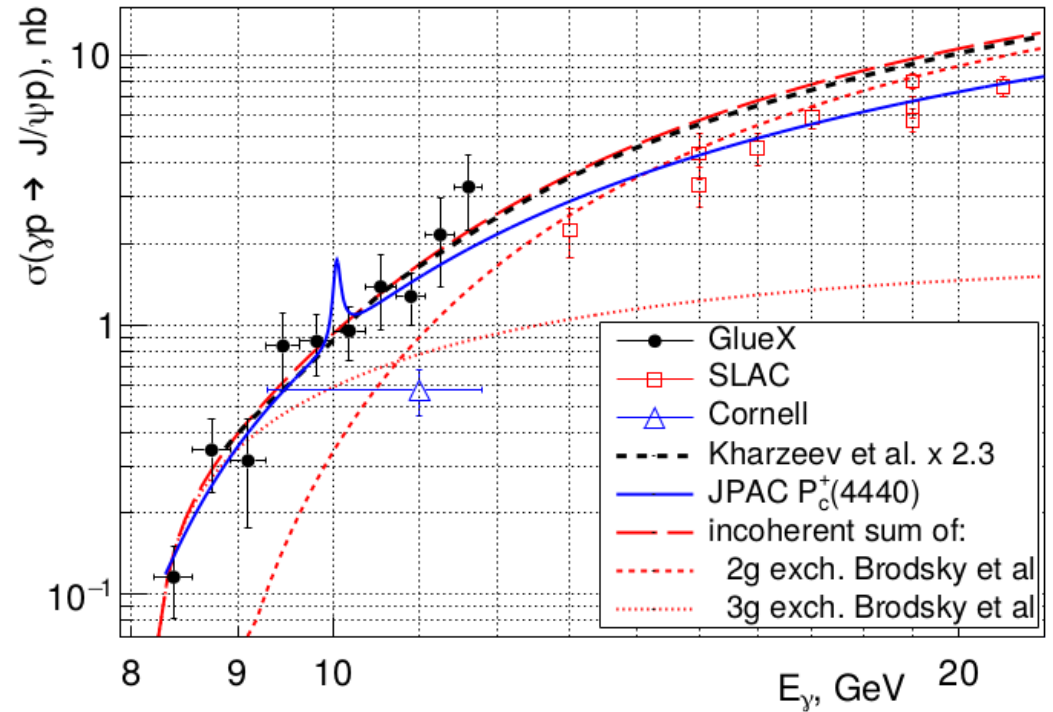
$$N^*(2120, 3/2^-),$$

$$N^*(2300, 1/2^+))$$

Total cross section



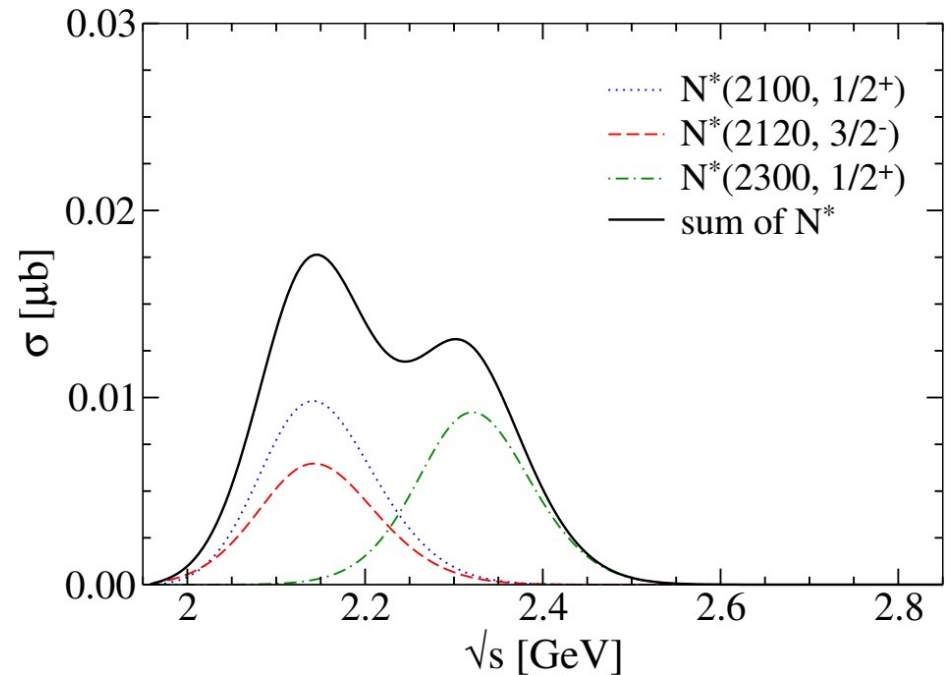
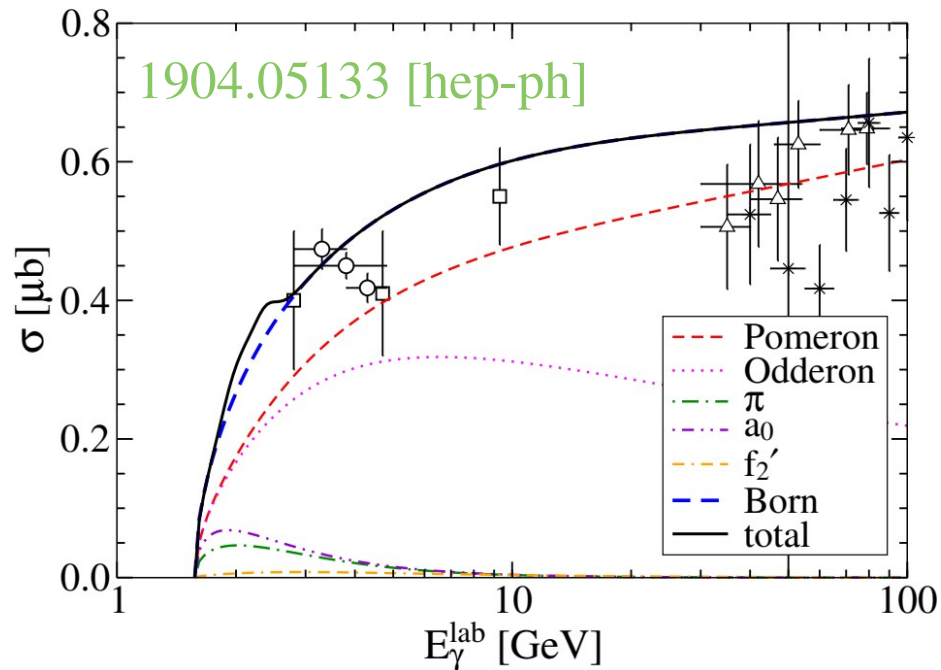
“First measurement of near-threshold J/ψ exclusive photoproduction off the proton”
[GLUEX Collaboration]
1905.10811 [nucl-ex]



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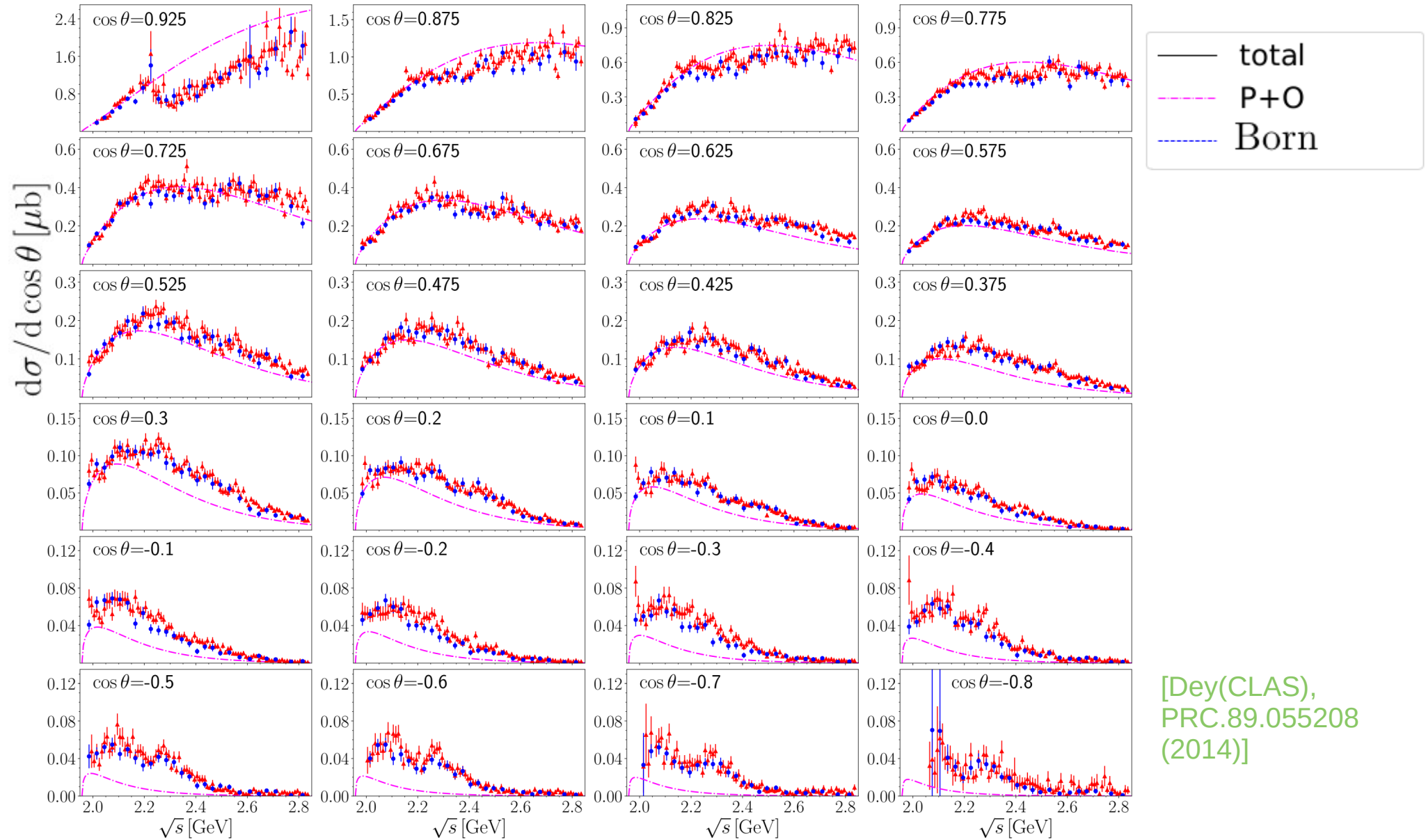
$$\mathcal{M}_{\text{total}} = \sum_i \mathcal{M}_i^{\text{Born}} + \sum_j \mathcal{C}_j \mathcal{M}_j^{N^*}$$

$$i = (\mathbb{P}, \mathbb{O}, \pi, \eta, a_0, f_0, f_2')$$

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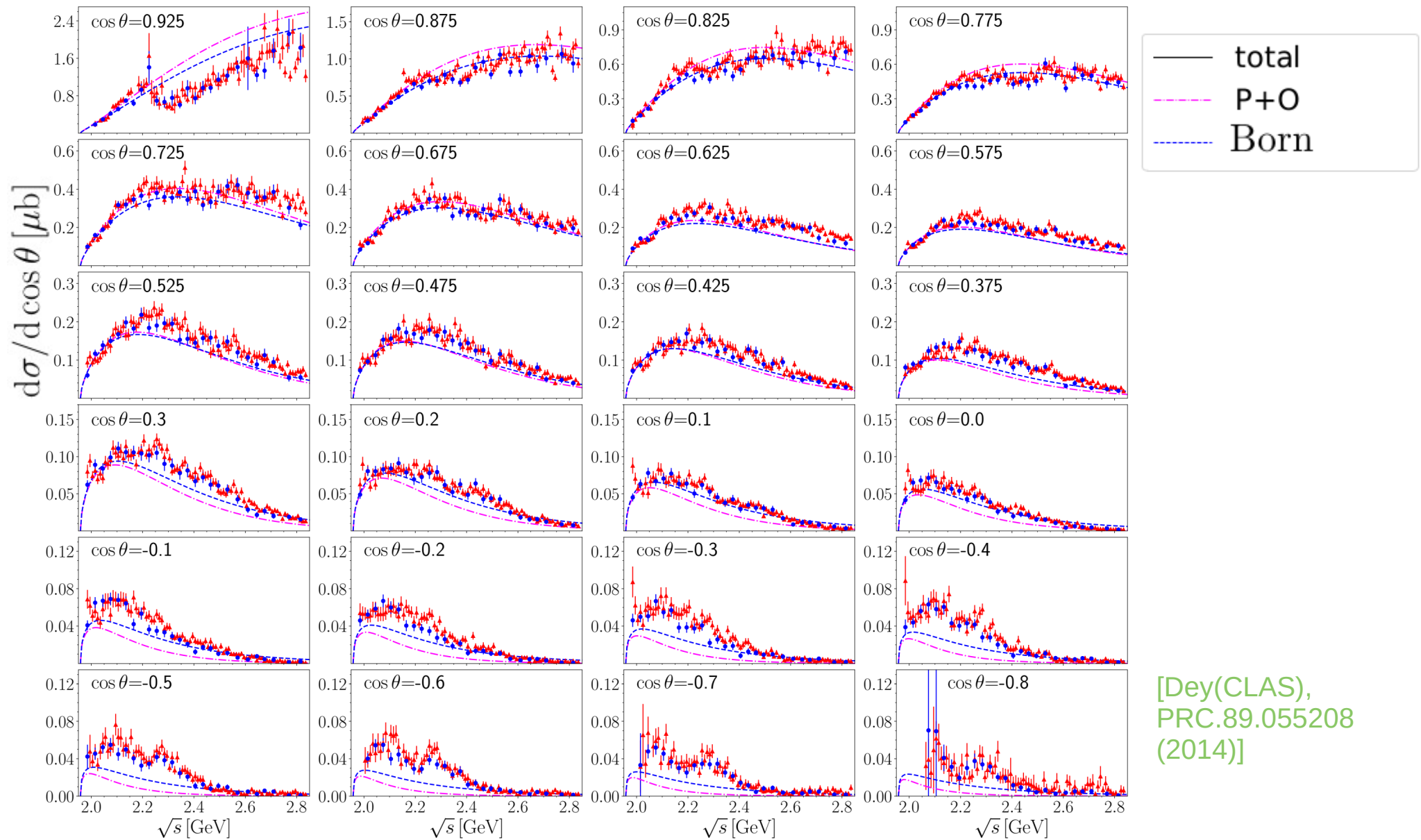
- The total cross section is almost governed by Pomeron and Odderon exchanges.
- Other contributions are small to the total cross section but come into play significantly for the “differential cross sections” and “spin-density matrices”.

Differential cross sections (1-1)



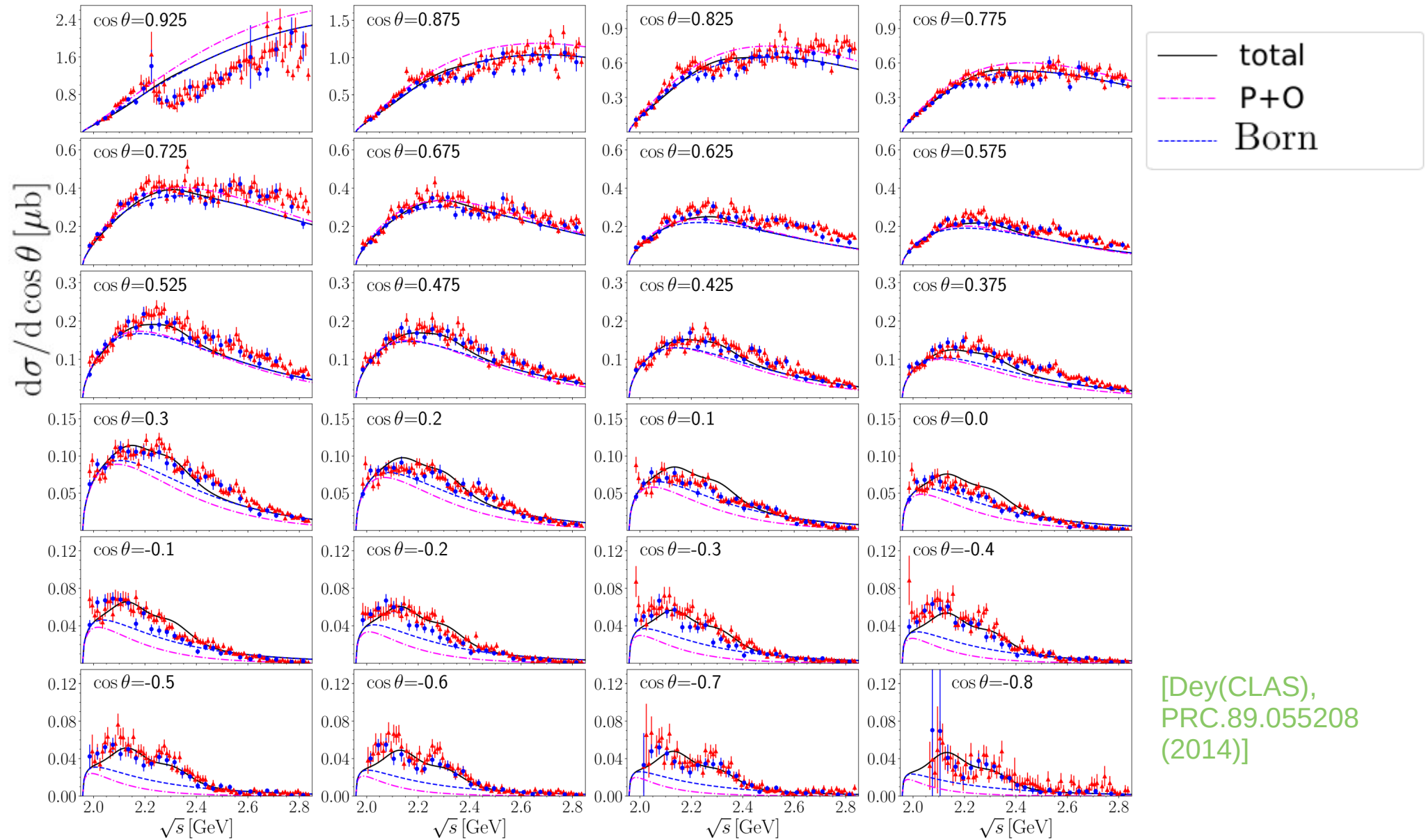
- PS- and S-meson exchanges, respectively, make constructive and destructive interference effects with the dominant Pomeron and Odderon contributions.
- Three N^* contributions improve the results at backward angles remarkably.

Differential cross sections (1-2)



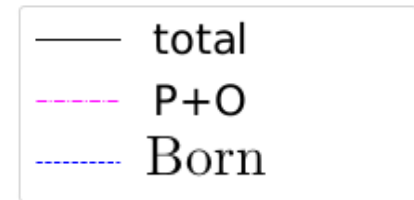
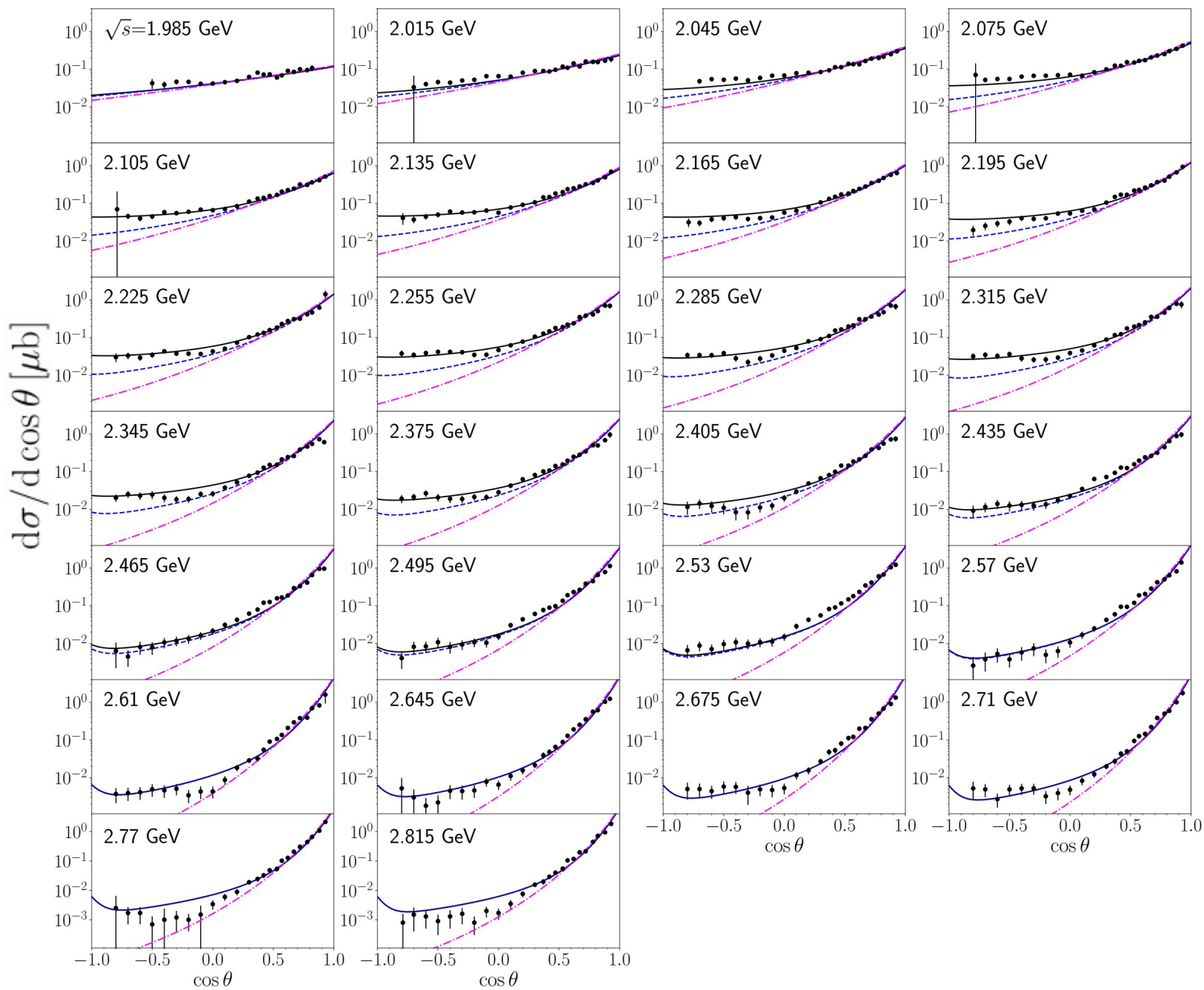
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Differential cross sections (1-3)



- PS- and S-meson exchanges, respectively, make constructive and destructive interference effects with the dominant Pomeron and Odderon contributions.
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Differential cross sections (2)



[Dey(CLAS),
PRC.89.055208
(2014)]

- SDMEs in terms of the helicity amplitudes

$$\rho_{\lambda\lambda'}^0 = \frac{1}{N} \sum_{\lambda_\gamma, \lambda_i, \lambda_f} \mathcal{M}_{\lambda_f \lambda; \lambda_i \lambda_\gamma} \mathcal{M}_{\lambda_f \lambda'; \lambda_i \lambda_\gamma}^*$$

$$\rho_{\lambda\lambda'}^1 = \frac{1}{N} \sum_{\lambda_\gamma, \lambda_i, \lambda_f} \mathcal{M}_{\lambda_f \lambda; \lambda_i - \lambda_\gamma} \mathcal{M}_{\lambda_f \lambda'; \lambda_i \lambda_\gamma}^*$$

$$\rho_{\lambda\lambda'}^2 = \frac{i}{N} \sum_{\lambda_\gamma, \lambda_i, \lambda_f} \lambda_\gamma \mathcal{M}_{\lambda_f \lambda; \lambda_i - \lambda_\gamma} \mathcal{M}_{\lambda_f \lambda'; \lambda_i \lambda_\gamma}^*$$

$$\rho_{\lambda\lambda'}^3 = \frac{1}{N} \sum_{\lambda_\gamma, \lambda_i, \lambda_f} \lambda_\gamma \mathcal{M}_{\lambda_f \lambda; \lambda_i \lambda_\gamma} \mathcal{M}_{\lambda_f \lambda'; \lambda_i \lambda_\gamma}^*$$

- normalization factor

$$N = \sum |\mathcal{M}_{\lambda_f \lambda; \lambda_i \lambda_\gamma}|^2$$

- symmetry relation

$$\rho_{\lambda\lambda'}^\alpha = (-1)^{\lambda - \lambda'} \rho_{-\lambda - \lambda'}^\alpha \quad \text{for } (\alpha = 0, 1),$$

$$\rho_{\lambda\lambda'}^\alpha = -(-1)^{\lambda - \lambda'} \rho_{-\lambda - \lambda'}^\alpha \quad \text{for } (\alpha = 2, 3)$$

- SDMEs in terms of the helicity amplitudes

$$\rho_{\lambda\lambda'}^0 = \frac{1}{N} \sum_{\lambda_\gamma, \lambda_i, \lambda_f} \mathcal{M}_{\lambda_f \lambda; \lambda_i \lambda_\gamma} \mathcal{M}_{\lambda_f \lambda'; \lambda_i \lambda_\gamma}^*$$

$$\rho_{\lambda\lambda'}^1 = \frac{1}{N} \sum_{\lambda_\gamma, \lambda_i, \lambda_f} \mathcal{M}_{\lambda_f \lambda; \lambda_i - \lambda_\gamma} \mathcal{M}_{\lambda_f \lambda'; \lambda_i \lambda_\gamma}^*$$

$$\rho_{\lambda\lambda'}^2 = \frac{i}{N} \sum_{\lambda_\gamma, \lambda_i, \lambda_f} \lambda_\gamma \mathcal{M}_{\lambda_f \lambda; \lambda_i - \lambda_\gamma} \mathcal{M}_{\lambda_f \lambda'; \lambda_i \lambda_\gamma}^*$$

$$\rho_{\lambda\lambda'}^3 = \frac{1}{N} \sum_{\lambda_\gamma, \lambda_i, \lambda_f} \lambda_\gamma \mathcal{M}_{\lambda_f \lambda; \lambda_i \lambda_\gamma} \mathcal{M}_{\lambda_f \lambda'; \lambda_i \lambda_\gamma}^*$$

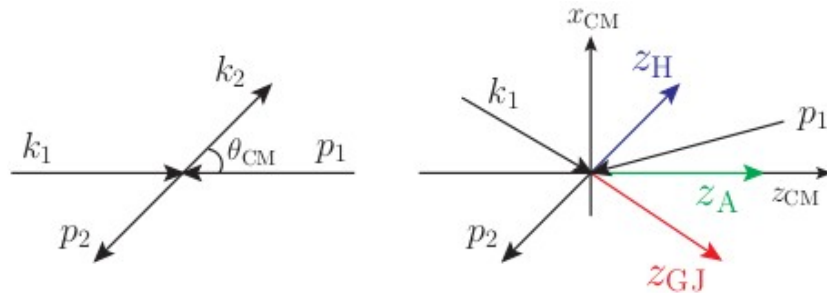
- normalization factor

$$N = \sum |\mathcal{M}_{\lambda_f \lambda; \lambda_i \lambda_\gamma}|^2$$

- symmetry relation

$$\rho_{\lambda\lambda'}^\alpha = (-1)^{\lambda-\lambda'} \rho_{-\lambda-\lambda'}^\alpha \quad \text{for } (\alpha = 0, 1),$$

$$\rho_{\lambda\lambda'}^\alpha = -(-1)^{\lambda-\lambda'} \rho_{-\lambda-\lambda'}^\alpha \quad \text{for } (\alpha = 2, 3)$$



- center of mass frame
- ϕ -meson rest frame

Adair frame: z axis is parallel to the incoming photon momentum in the CM frame.

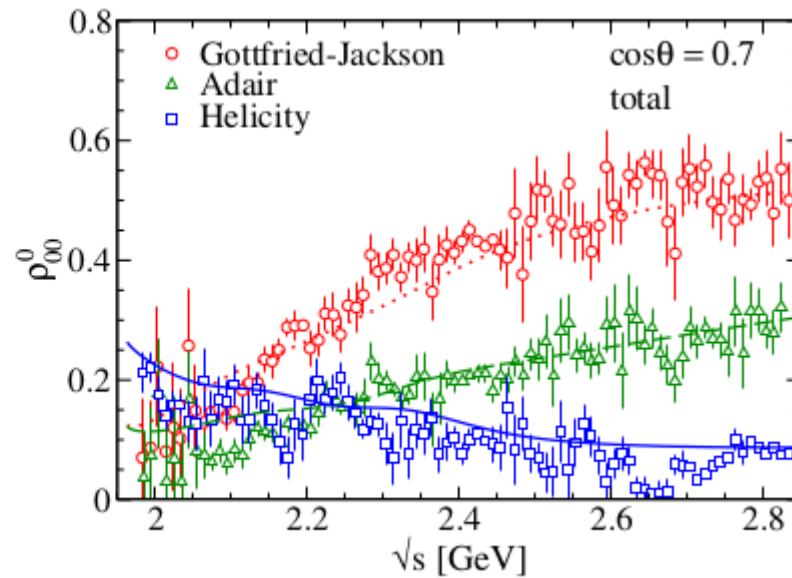
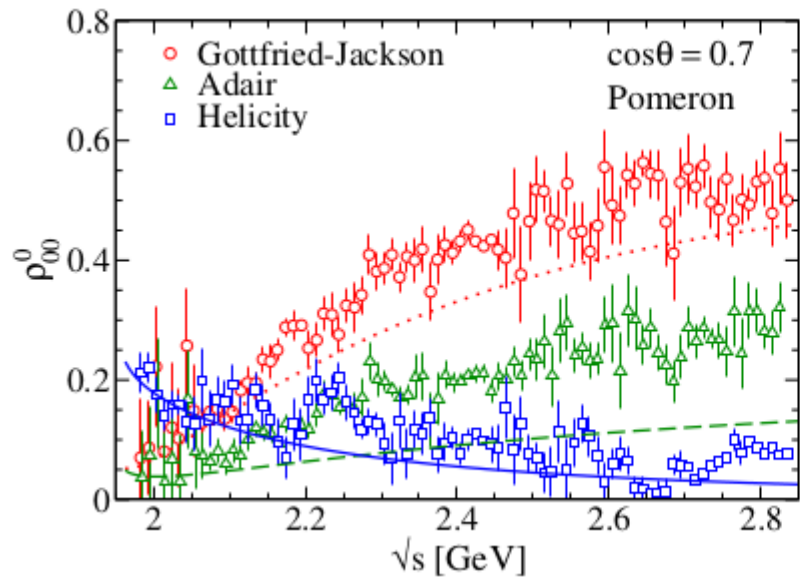
Helicity frame: z axis is antiparallel to the momentum of the outgoing nucleon.

It is in favor of s-channel helicity conservation (SCHC).

Gottfried-Jackson frame: z axis is parallel to the momentum of the incoming photon.

It is in favor of t-channel helicity conservation (TCHC).

Spin-density matrix elements (1)

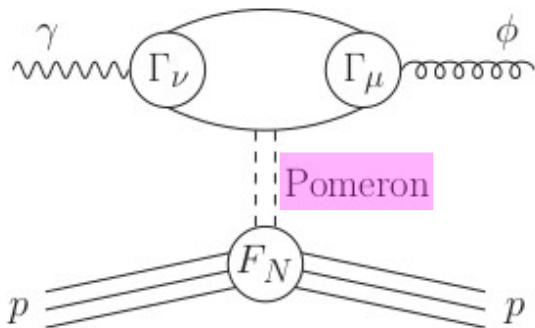


[Dey(CLAS),
PRC.89.055208
(2014)]

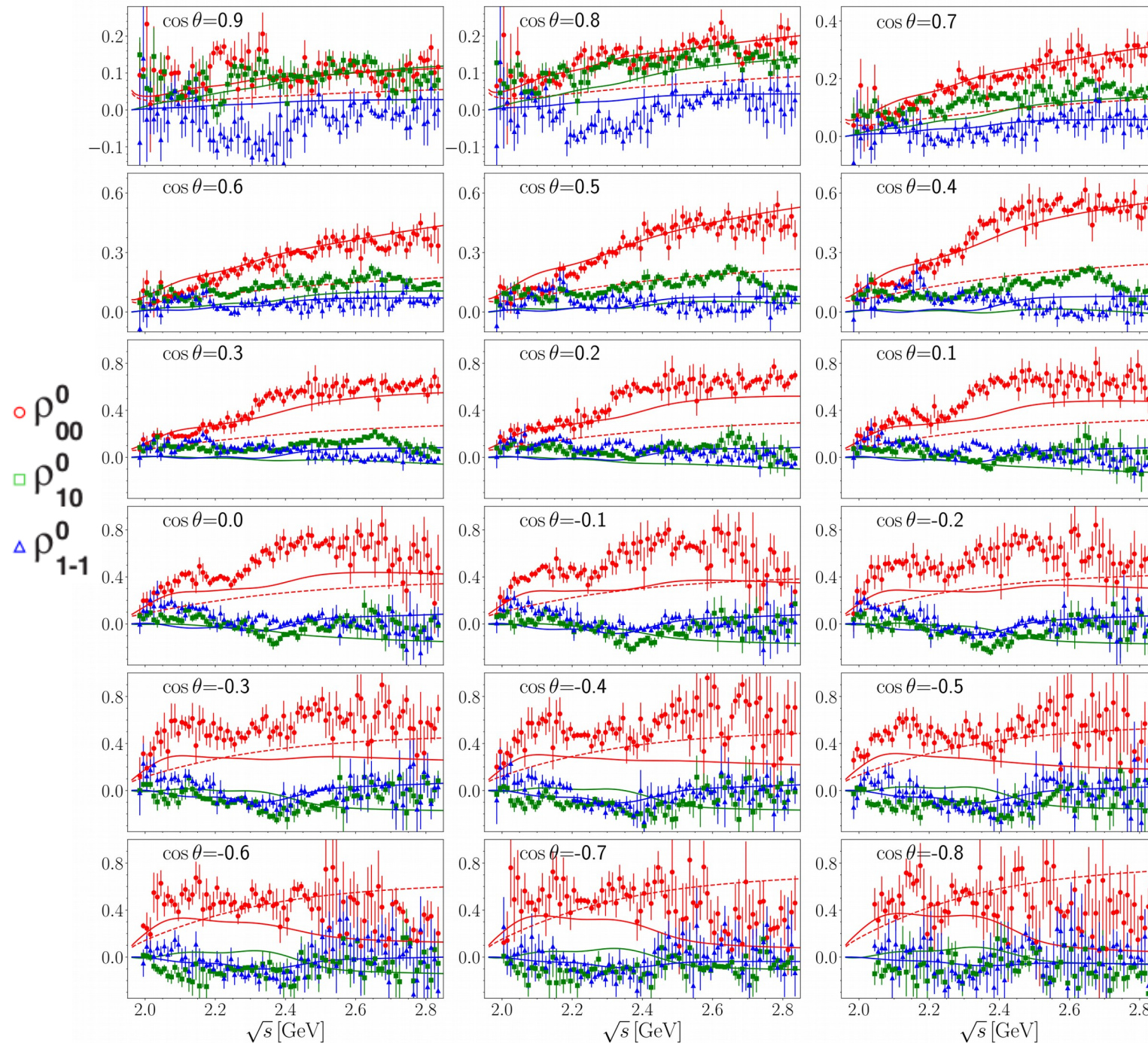
- ρ_{00}^0 is nonzero in all three frames and thus exhibits strong deviation from TCHC, implying nonzero helicity flip ($\rho_{00}^0 \propto |\mathcal{M}_{\lambda_\gamma=1, \lambda_\phi=0}|^2 + |\mathcal{M}_{\lambda_\gamma=-1, \lambda_\phi=0}|^2$).

- The inclusion of $S(a_0, f_0)$ -mesons is essential to improve the results.

- Pomeron alone is not sufficient.



Spin-density matrix elements (2)

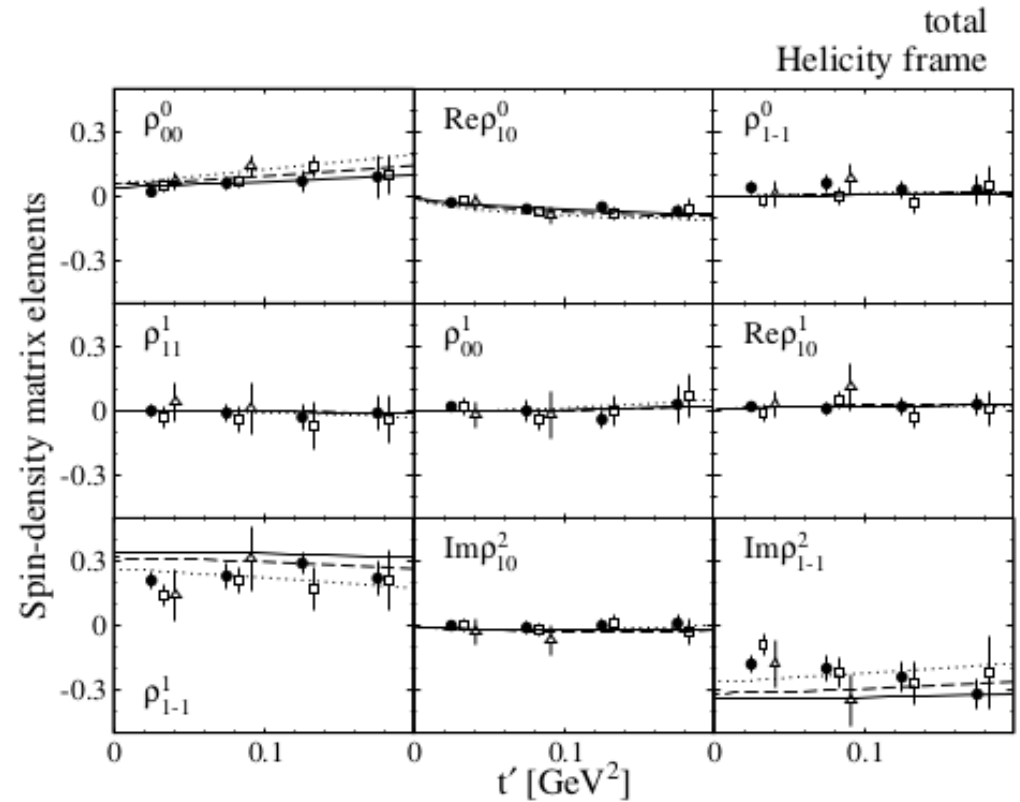
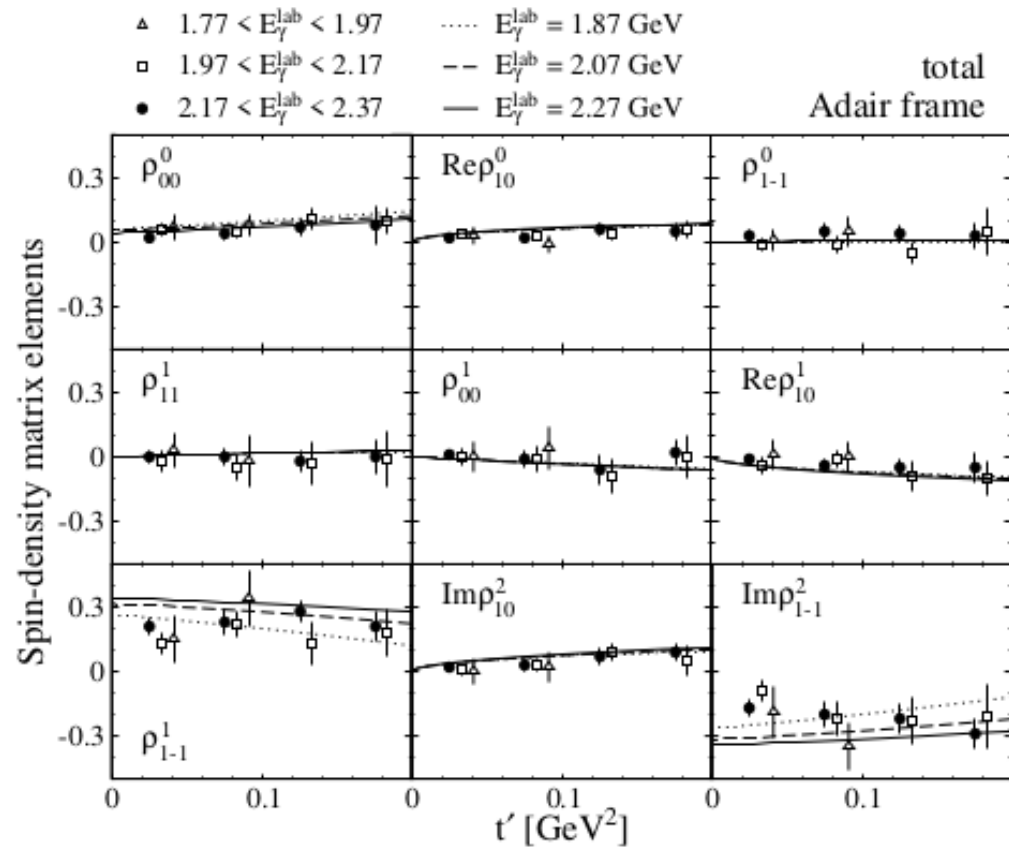


[Adair frame]

- forward angle: Pomeron alone is not enough.
- S(a₀,f₀)- mesons improves the results.
- backward angle: N* exchange describes the bump structure.

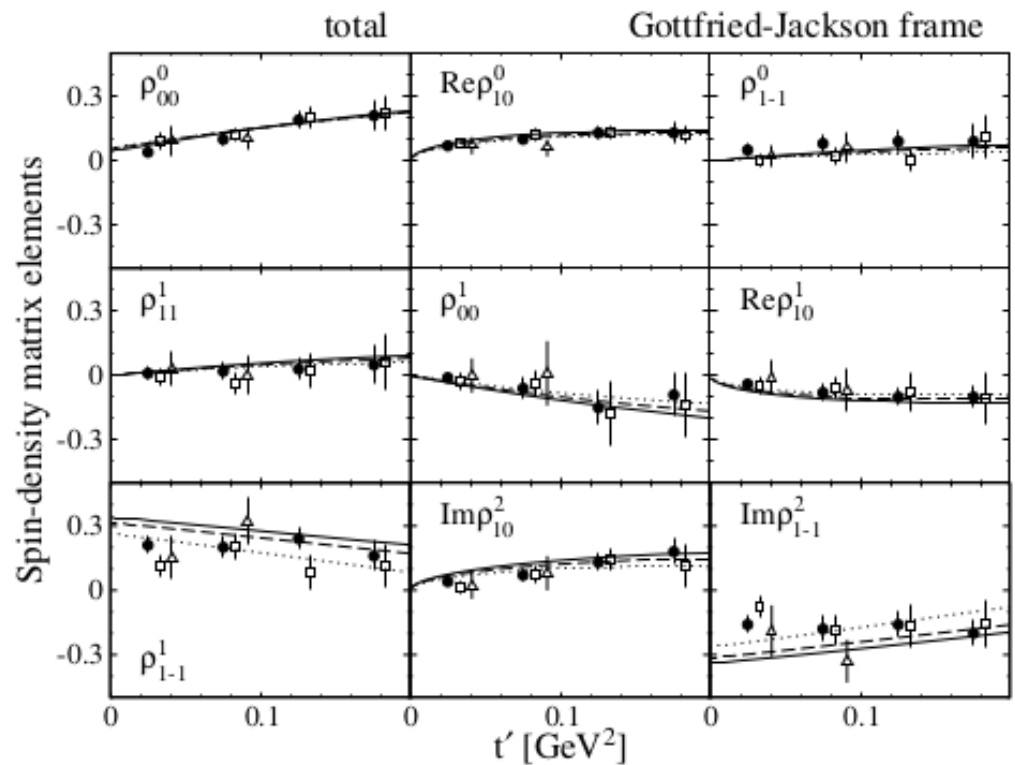
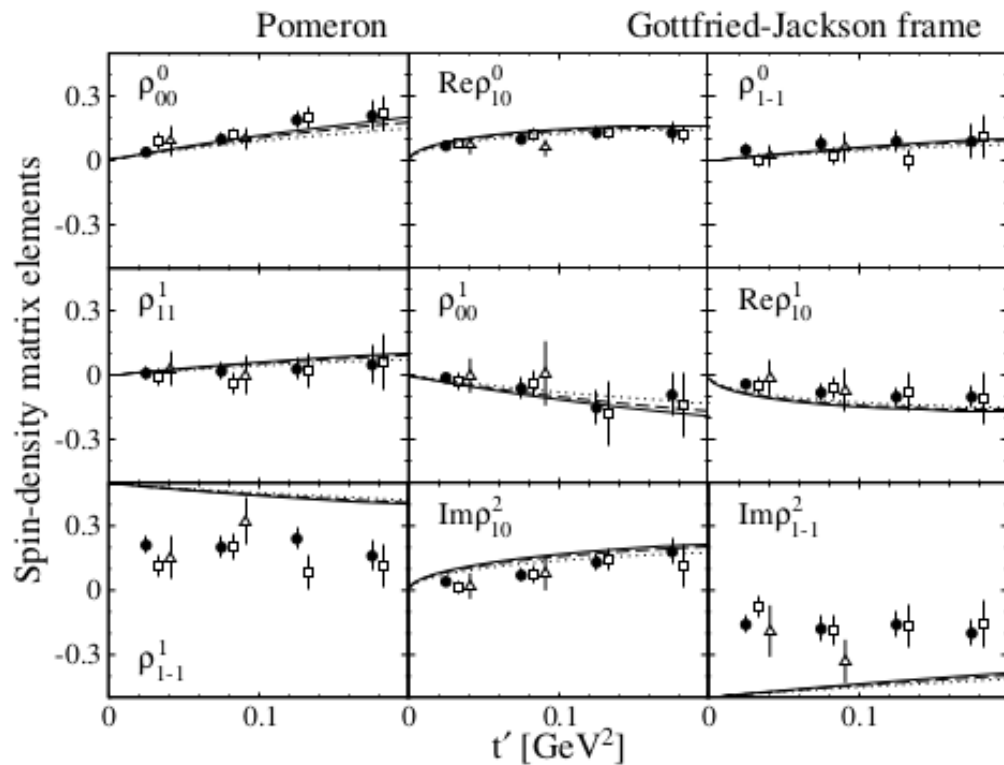
[Dey(CLAS),
PRC.89.055208
(2014)]

Spin-density matrix elements (3-1)



- Pomeron exchange:

$$\rho_{1-1}^1 \simeq \frac{1}{2}(1 - \rho_{00}^0)$$



- Pomeron exchange:

$$\rho_{1-1}^1 \simeq \frac{1}{2}(1 - \rho_{00}^0)$$

- GJ frame is useful to test TCHC.
- Relative strength of N & U parity exchange processes:

$$\rho_{1-1}^1 = \frac{1}{2} \frac{\sigma^N - \sigma^U}{\sigma^N + \sigma^U}$$

Summary

- ◇ φ photoproduction, $\gamma p \rightarrow \varphi(1020)p$, is reanalyzed with effective Lagrangians .
- ◇ Abundant CLAS(2014) data are reported at full angles & low energies.
- ◇ Various contributions from t-channel exchanges and N^* exchange are considered in addition to the dominant Pomeron exchange.
 - ⇒ Odderon ⇒ pseudoscalar meson (π, η) ⇒ scalar meson (a_0, f_0)
- ◇ Extension to other vector-meson (ρ, ω) photo- and electro-production mechanisms.

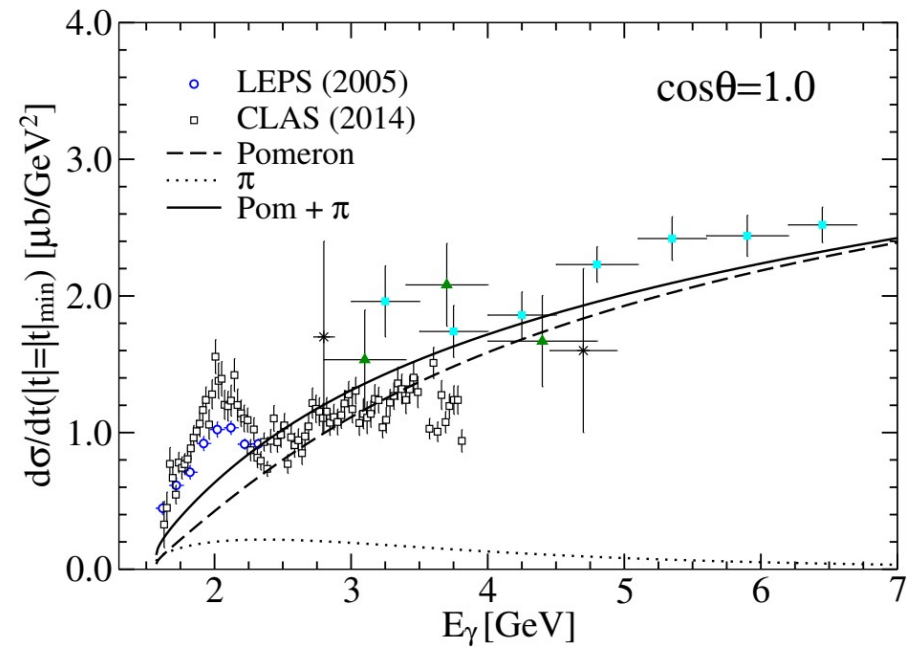
- ◇ φ photoproduction, $\gamma p \rightarrow \varphi(1020)p$, is reanalyzed with effective Lagrangians .
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 - \Rightarrow Odderon \Rightarrow pseudoscalar meson (π, η) \Rightarrow scalar meson (a_0, f_0)
- ◇ Extension to other vector-meson (ρ, ω) photo- and electro-production mechanisms.

Thank you very much

Back Up

- Nagano, Toki, Proceedings (1998)
: scalar glueball ($J^{\pi}=0^{+}$, $M_{gl}^2 \simeq 3 \text{ GeV}^2$).
- Williams, PRC, 57, 223 (1998)
: $s\bar{s}$ knockout, nonzero φ NN couplings.
- Titov et al., PRC, 60, 035205 (1999)
: scalar mesons (σ, a_0, f_0).
- Laget, PLB, 489, 313 (2000)
: $f_2(1270)$ meson, two gluon exchange.
- Titov, Lee, PRC, 67, 065205 (2003)
: $f_2(1270), f'_2(1525)$ mesons, N^* .
- ∴ Pomeron & pseudoscalar mesons (π^0, η)
in common.

t-channel contributions are widely studied.



Mibe(LEPS)PRL.95.182001(2005)

After an observation of the bump structure, most of works have moved on to the N^* scenario.

- Titov, Kampf, PRC, 76, 035202 (2007)
: Pomeron + (π, η) mesons.

- a. Ozaki, Hosaka, Nagahiro, Scholten, PRC, 80, 035201 (2009)
: coupled-channel effective-Lagrangian method based on the K-matrix approach.
Suggest the existence of a N^* , $J^P=1/2^-$ resonance ($M=2.250$, $\Gamma=0.100$ [GeV]).

- b. Kiswandhi, Xie, Yang, PLB, 691, 214 (2010)
: Assume a N^* resonance of $J^P=3/2^-$ ($M=2.10\pm 0.03$, $\Gamma=0.465\pm 0.141$ [GeV]).

- c. Kiswandhi, Yang, PRC, 86, 015203 (2012)
: N^* of $J^P=3/2^\pm$ ($M=2.08\pm 0.04$, $\Gamma=0.501\pm 0.117$ (P=+), 0.570 ± 0.159 (P=-) [GeV]).

- d. Ryu, Titov, Hosaka, Kim, PTEP, 2014, 023D03 (2014)
: various hadronic rescattering contributions, focusing on the $K\Lambda(1520)$ channel.

