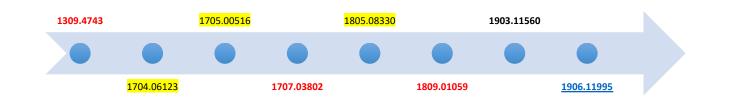
13th APCTP - BLTP JINR Joint Workshop "Modern problems in nuclear and elementary particle physics"





DK interaction as a doorway to manifestly exotic mesons Lisheng Geng @ Beihang U.



+some preliminary results

Contents

- Motivation: new types of clusters of color singlets in addition to nuclei
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- □ A K*(4307) with hidden charm as KX(3872)/Zc(3900) molecule
- □ Summary and outlook

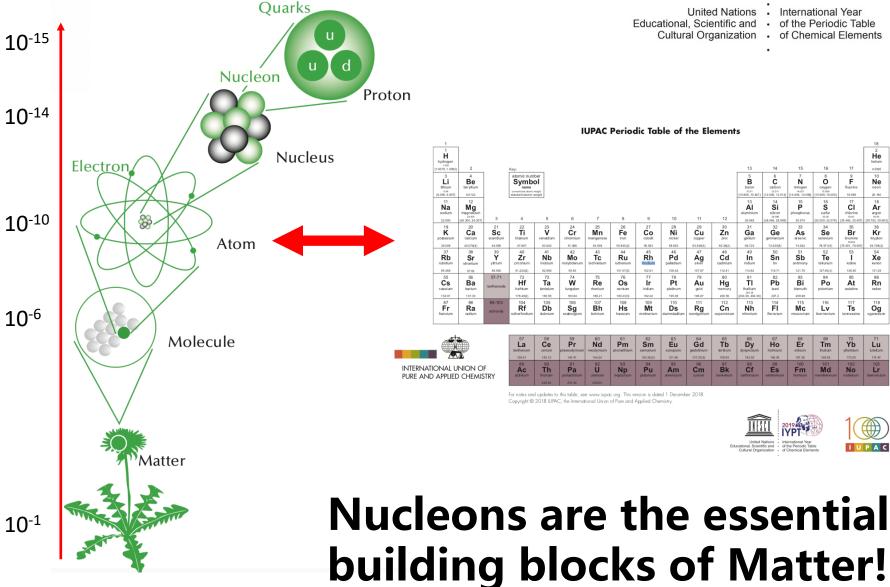
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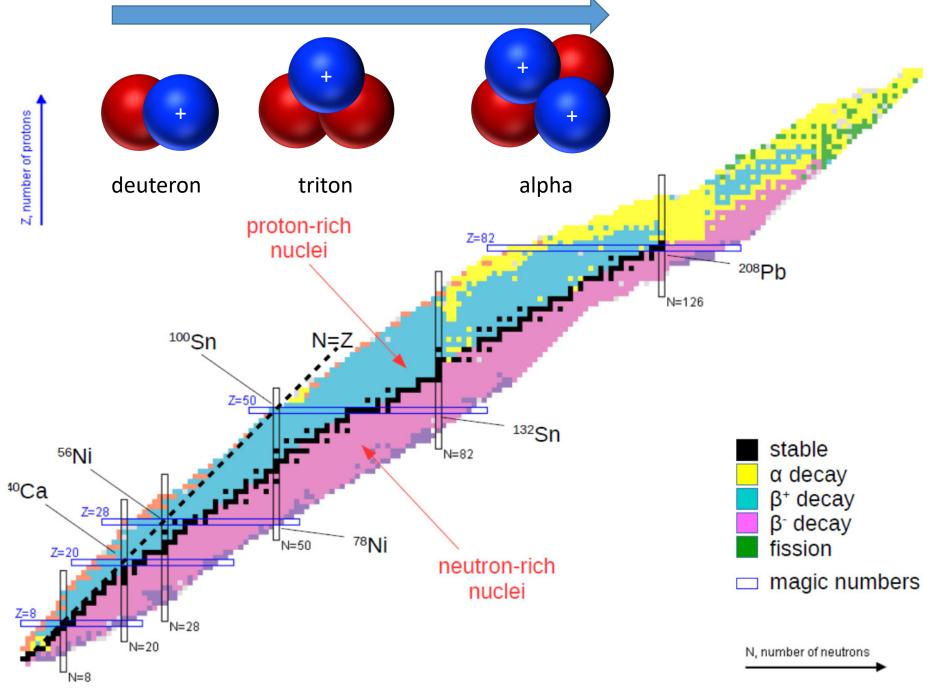




United Nations International Year . Cultural Organization .



Adapted from LHC the guide

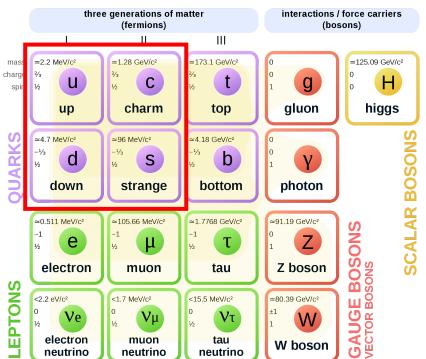


The existence of triton can be inferred from that of deuteron with reasonable confidence

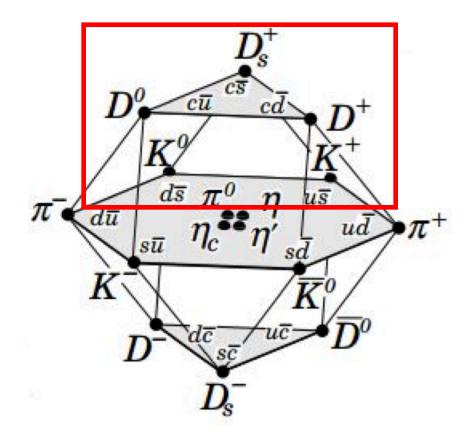
"In nature, are there other clusters of color singlet hadrons, similar to atomic nuclei, bound by the residual strong force???"



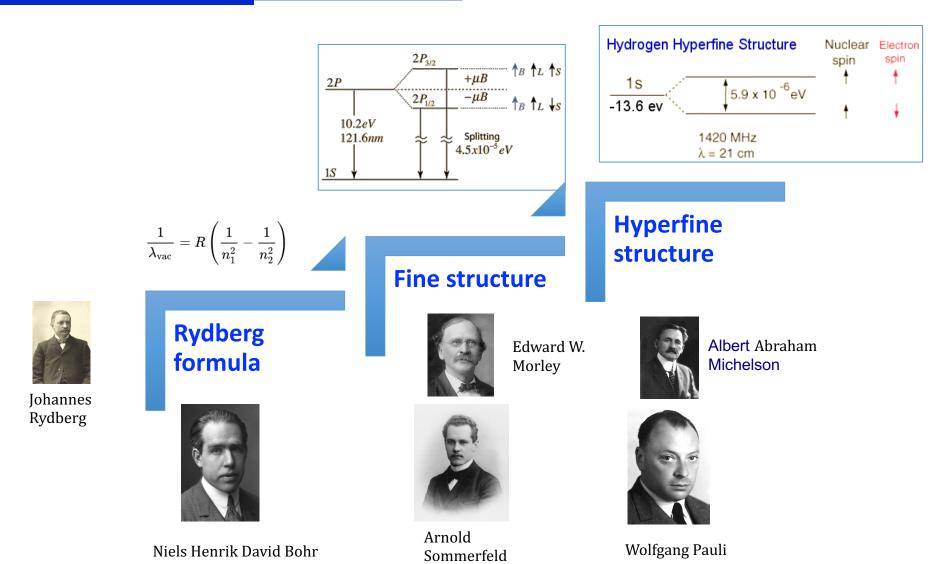
DK/DDK/DDDK molecules???



Standard Model of Elementary Particles three generations of matter interactions / force carriers

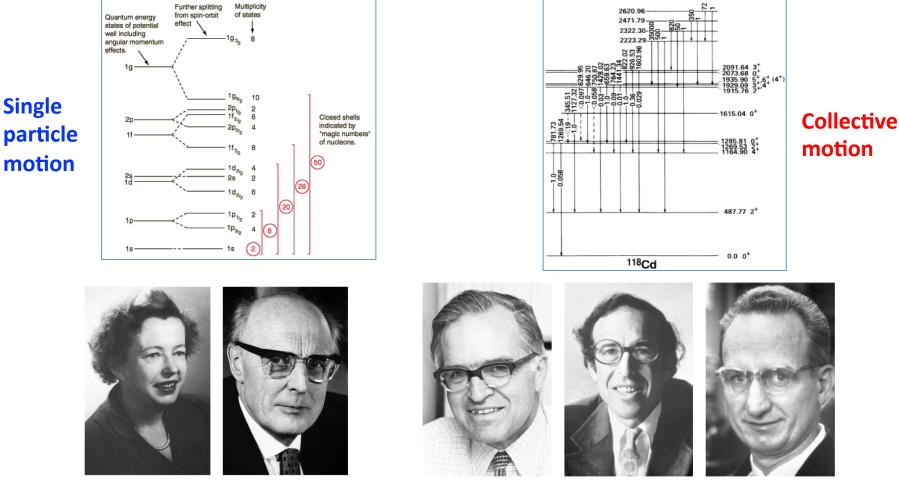


Why spectroscopy—Atomic



8

Why spectroscopy—Nuclear



Maria Goeppert Mayer J. Hans D. Jensen

Aage Niels Bohr, Ben Roy Mottelson Leo James Rainwater

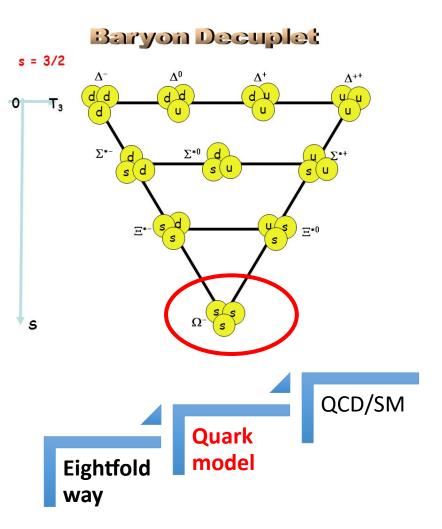
Why spectroscopy—particle/hadron

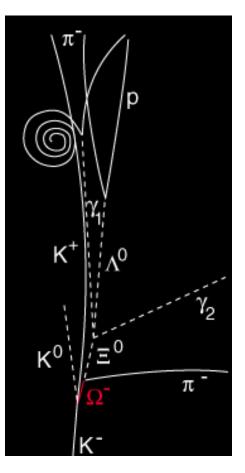


Murray Gell-Mann



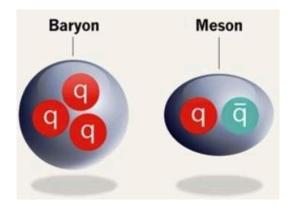
Yuval Ne'eman.





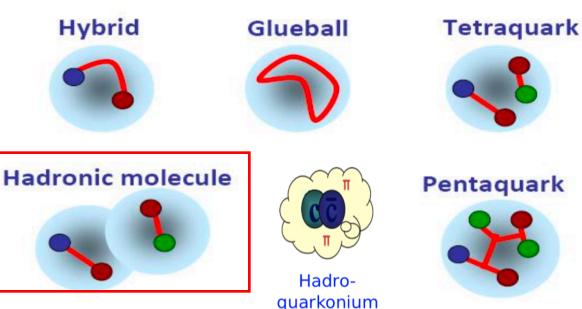
V. E. Barnes et al., Phys. Rev. Lett. 12, 204 (1964)

Why spectroscopy—particle/hadron



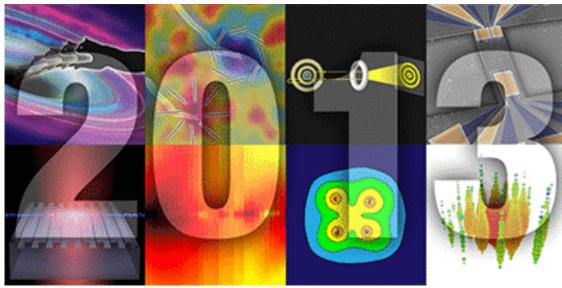
In the naïve quark model

In principle, QCD allows



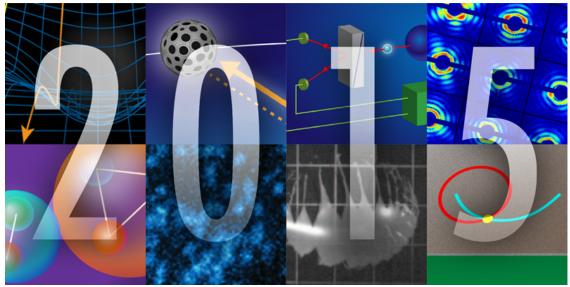
Highlights of the year

the research covered in Physics that **really made waves in and beyond the physics community.**



Four-Quark Matter

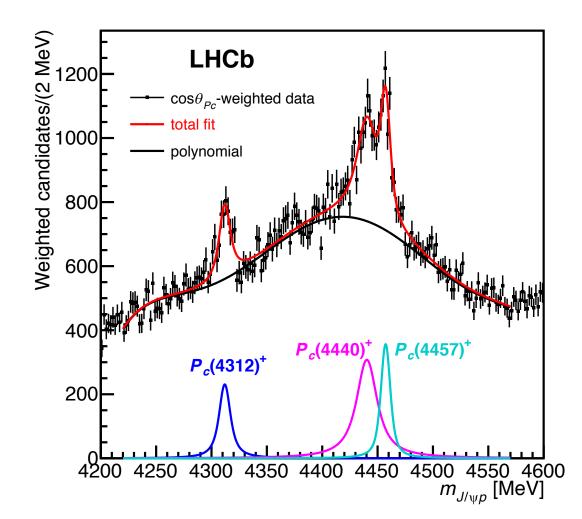
Particle High Five



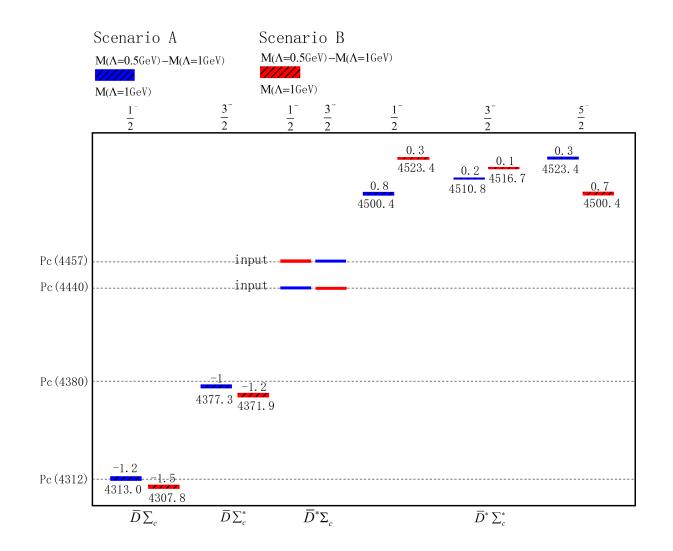
Latest LHCb discovery:

Fine structure observed by LHCb,1904.03947

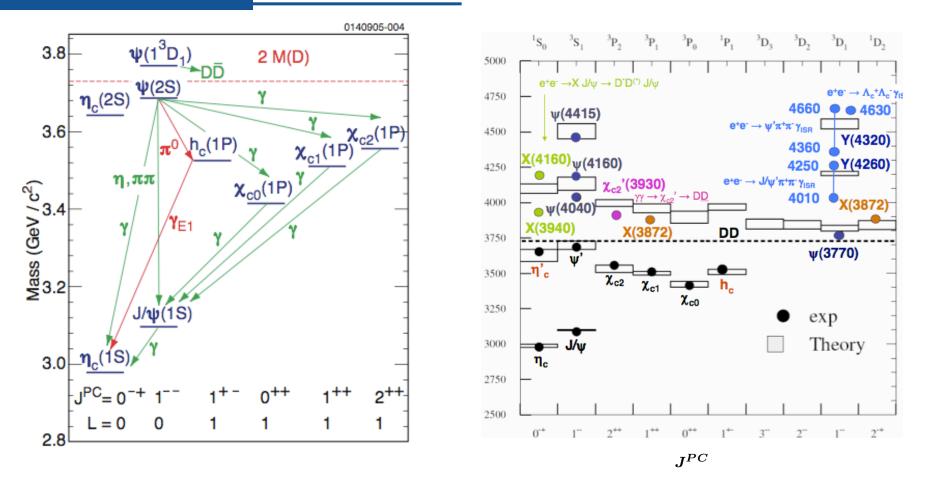




Emergence of a complete heavy-quark spin symmetry multiplet 1903.11560



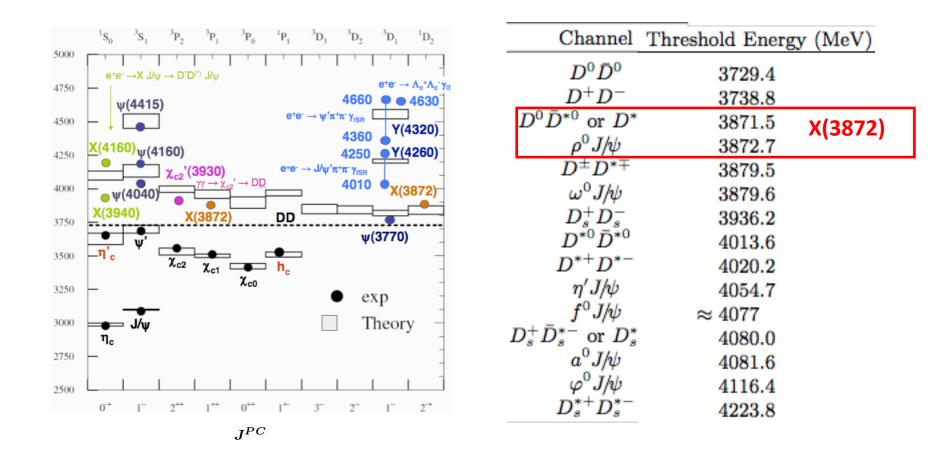
Charmonium spectroscopy before/after B factories



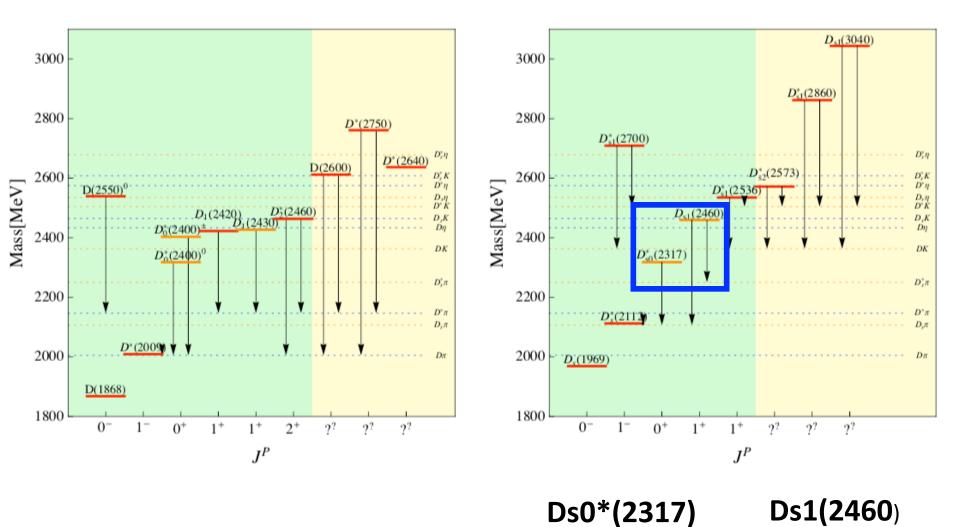
•A lot of new states, but the nature of some states are not well understood, e.g.Y(4260), X(3872), Zc(3900)

•In complete contrast to the before-B-factory period, when potential models worked quite well.

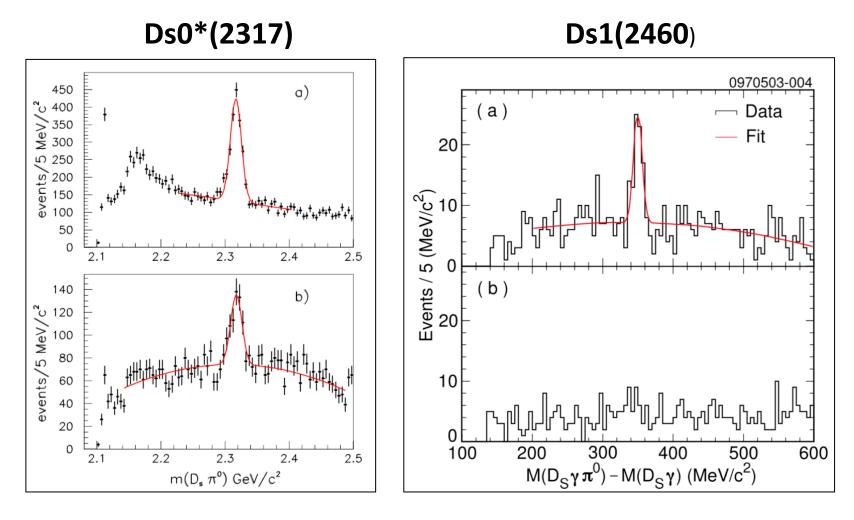
Coupled channel effects?



Open charm systems



Two peculiar states



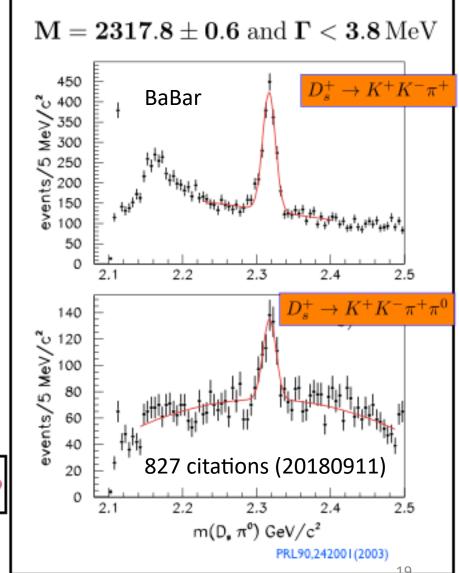
BaBar PRL90,242001(2003)

CLEO PRD68,032002(2003)

Two peculiar states

- $D_{s0}^{*}(2317), D_{s1}(2460)$
- 160/70 MeV lower than quark model predictions--difficult to be understood as conventional csbar states.
- "Dynamically generated" from strong DK interaction
 - ✓ E. E. Kolomeitsev 2004,
 - ✓ F. K. Guo 2006,
 - ✓ D. Gamermann 2007

 $m_{D_{s1}(2460)} - m_{D_{s0}^*(2317)} \approx m_{D^*} - m_D$

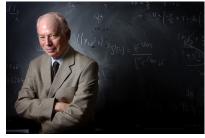


Feng-Kun Guo, EPJ Web of Conferences 202, 02001 (2019)

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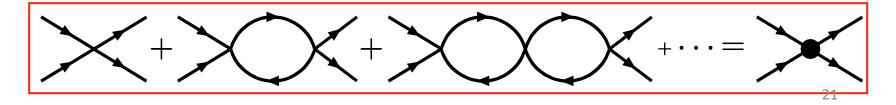
UChPT in Bethe-Salpeter equation



D Model independent DK interaction from ChPT

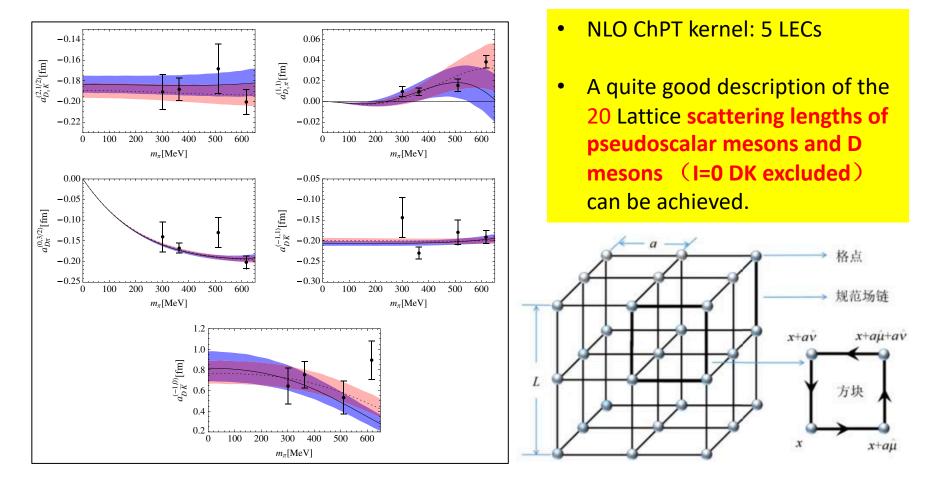
 $\mathcal{V}_{WT}(P(p_1)\phi(p_2) \to P(p_3)\phi(p_4)) = \frac{1}{4f_0^2} \mathcal{C}_{LO}(s-u) \quad \text{Weinberg-Tomazawa} \\
\mathcal{V}_{NLO}(P(p_1)\phi(p_2) \to P(p_3)\phi(p_4)) = -\frac{8}{f_0^2} C_{24} \left(c_2 \, p_2 \cdot p_4 - \frac{c_4}{m_P^2} \left(p_1 \cdot p_4 \, p_2 \cdot p_3 + p_1 \cdot p_2 \, p_3 \cdot p_4 \right) \right) \\
-\frac{4}{f_0^2} \mathcal{C}_{35} \left(c_3 \, p_2 \cdot p_4 - \frac{c_5}{m_P^2} \left(p_1 \cdot p_4 \, p_2 \cdot p_3 + p_1 \cdot p_2 \, p_3 \cdot p_4 \right) \right) \\
-\frac{4}{f_0^2} \mathcal{C}_6 \, \frac{c_6}{m_P^2} \left(p_1 \cdot p_4 \, p_2 \cdot p_3 - p_1 \cdot p_2 \, p_3 \cdot p_4 \right) \\
-\frac{8}{f_0^2} \mathcal{C}_0 \, c_0 + \frac{4}{f_0^2} \mathcal{C}_1 \, c_1 , \quad (11)$

Resumed in the Bethe-Salpeter equation (two-body elastic unitarity)



Fixing the LECs using latest LQCD* data

Liuming Liu et al., PRD87 (2013) 014508



Ds0 and Ds1 dynamically generated

Charm sector

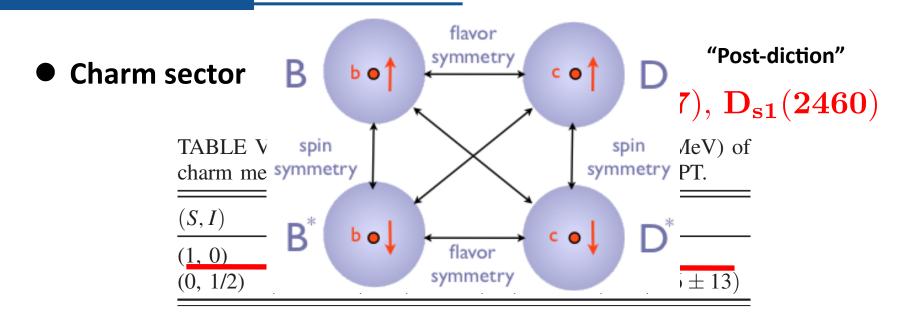
"Post-diction"

$\mathbf{D_{s0}^{*}(2317)},\,\mathbf{D_{s1}(2460)}$

TABLE V. Pole positions $\sqrt{s} = M - i\frac{\Gamma}{2}$ (in units of MeV) of charm mesons dynamically generated in the HQS UChPT.

$\overline{(S,I)}$	$J^P=0^+$	$J^{P} = 1^{+}$
(1, 0)	2317 ± 10	2457 ± 17
(0, 1/2)	$(2105 \pm 4) - i(103 \pm 7)$	$(2248 \pm 6) - i(106 \pm 13)$

Ds0 and Ds1 dynamically generated



Bottom Sector

TABLE VI. Pole positions $\sqrt{s} = M - i\frac{\Gamma}{2}$ (in units of MeV) of bottom mesons dynamically generated in the HQS UChPT.

(S, I)	$J^P=0^+$	$J^{P} = 1^{+}$		
(1, 0)	5726 ± 28	5778 ± 26		
(0, 1/2)	$(5537 \pm 14) - i(118 \pm 22)$	$(5586\pm16) - i(124\pm25)$		

Predicted Bs0 and Bs1 states

Physics Letters B 750 (2015) 17-21



Contents lists available at ScienceDirect

Physics Letters B



Predicting positive parity B_s mesons from lattice QCD



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^b Fermi National Accelerator Laboratory, Batavia, IL 60510-5011, USA

^c Department of Physics, University of Ljubljana, 1000 Ljubljana, Slovenia

^d Jozef Stefan Institute, 1000 Ljubljana, Slovenia

^e TRIUMF, 4004 Wesbrook Mall, Vancouver, BC V6T 2A3, Canada

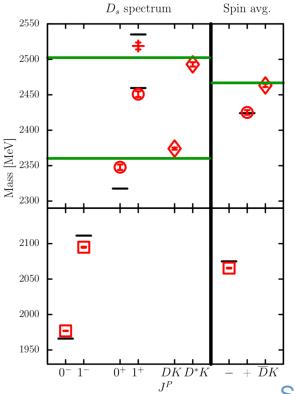
Table 5

Comparison of masses from this work to results from various model based calculations; all masses in MeV.

J^P	0+	1+	
Covariant (U)ChPT [24]	5726(28)	5778(26)	
NLO UHMChPT [19]	5696(20)(30)	5742(20)(30)	
LO UChPT [17,18]	5725(39)	5778(7)	
LO χ-SU(3) [16]	5643	5690	
HQET + ChPT [20]	5706.6(1.2)	5765.6(1.2)	
Bardeen, Eichten, Hill [15]	5718(35)	5765(35)	In agreement with IQCD
rel. quark model [5]	5804	5842	
rel. quark model [22]	5833	5865	
rel. quark model [23]	5830	5858	
HPQCD [30]	5752(16)(5)(25)	5806(15)(5)(25)	25
this work	5713(11)(19)	5750(17)(19)	23

Support from lattice QCD studies

- <u>G. S. Bali et al., arXiv:1706.01247 [hep-lat].</u>
- C. B. Lang et al., arXiv:1403.8103 [hep-lat].
- D. Mohler et al., arXiv:1308.3175 [hep-lat].



"DK components substantial"

FIG. 12. On the left, our final results for the lower lying D_s spectrum as detailed in Table VII. The short horizontal black lines indicate the corrected experimental values (see Section II) while the green horizontal lines give the positions of the DK and D^*K non-interacting thresholds. Our lattice results for the finite volume thresholds are labelled DKand D^*K , respectively. The errors indicated are statistical only. On the right, the negative parity spin-averaged 1S mass $m_- = \frac{1}{4} (m_{0^-} + 3m_{1^-})$ is shown and denoted -, while the same spin-average of the positive parity 0^+ and 1^+ states is labelled with + and the weighted average of the threshold is labelled as $\overline{D}K$.

See as well Miguel Albaladejo et al. arXiv:1805.07104

Further tests of the DK interaction

DExperiments, theory, and lattice QCD all show that *DK* or

- D^*K interaction is strong enough to form the Ds0*(2317) or Ds1(2460)
- **D**A natural question is: if we add one more $D(\overline{D})$ or $D^*(\overline{D^*})$, can they form molecules of three hadrons?
- □ This seems to be a rather straightforward and naive question, but remains unexplored until quite recently

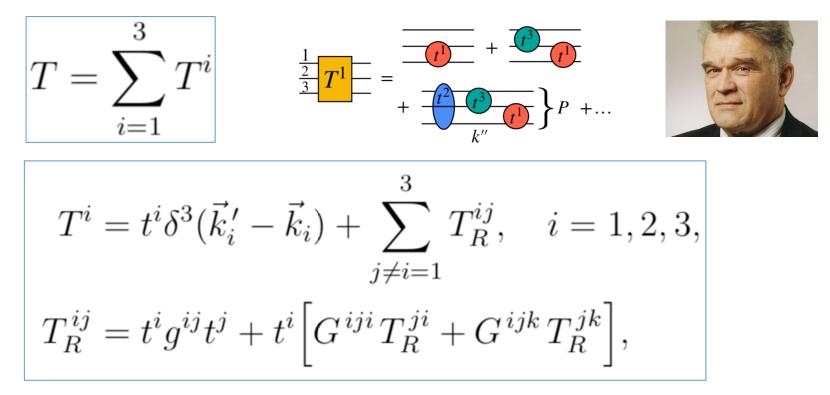
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An explicit three-body study of DDK

A. Mart' inez Torres, K. P. Khemchandani, and LSG 1809.01059

- Coupled-three-channel problem: $D(DK D_s \pi D_s \eta)$
- Three-body scattering matrix (Faddeev)



A. Martínez Torres, K. P. Khemchandani, and E. Oset PRC 77, 042203(R) A. Martinez Torres, K.P. Khemchandani, LSG, M. Napsuciale, E. Oset, PRD78 (2008) 074031

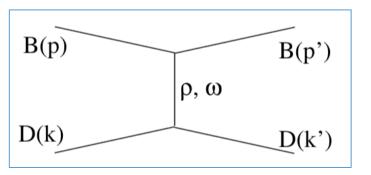
Two-body inputs

• DK: leading order UChPT DK, $D_s\eta$ and $D_s\pi$

$$V_{ij} = -\frac{C_{ij}}{4f^2}(s-u) \qquad \begin{array}{l} a(\mu) = -1.846, \mu \\ = 1000 \ \mathrm{MeV} \Rightarrow \\ \mathrm{Pole=2318} \ \mathrm{MeV} \end{array}$$

F.-K. Guo, P.-N. Shen, H.-C. Chiang, R.-G. Ping, and B.-S. Zou, PL B641, 278 (2006).

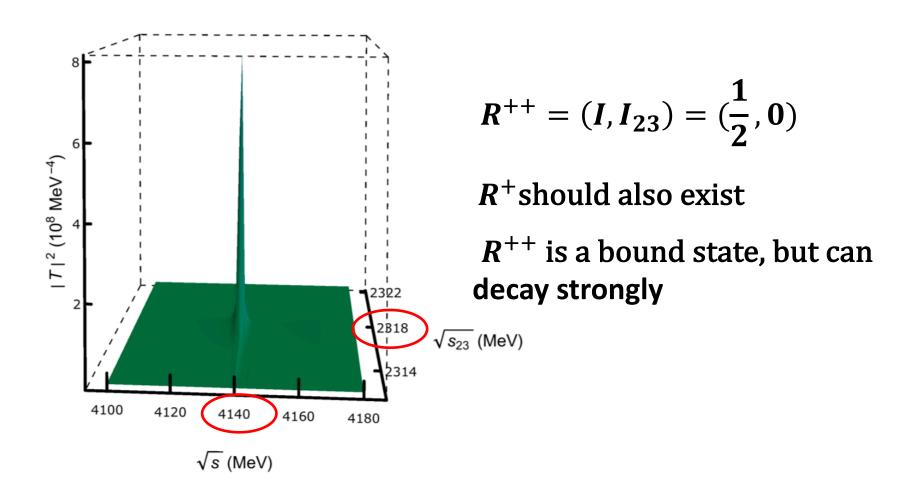
DD(Ds): local hidden gauge theory



 $a(\mu) = -1.3 \sim -1.5, \mu =$ 1500 *MeV* \leftarrow fixed from $D\overline{D}/D\overline{D^*}$ --X(3700) /X(3872)

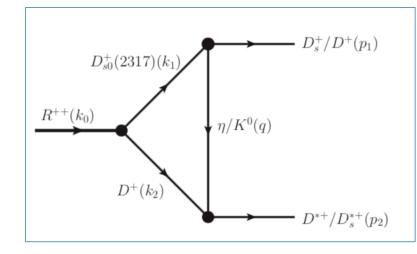
S. Sakai, L. Roca, and E. Oset, PRD96, 054023 (2017).

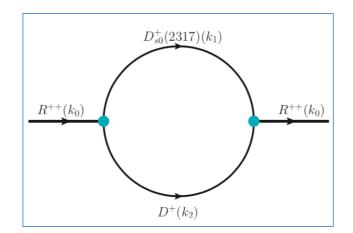
Three-body amplitudes

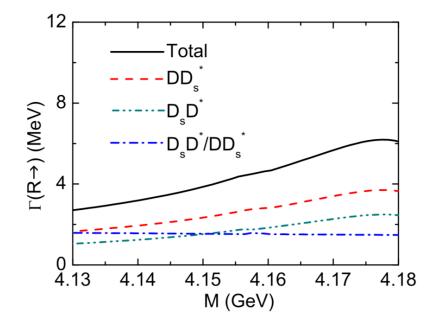


Two-body decay width

Yin Huang, LSG, et al., in preparation







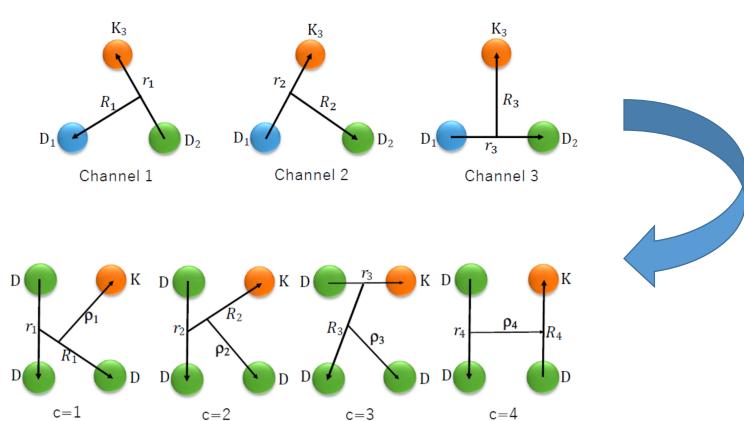
Preliminary result: $\Gamma \sim 10 \text{ MeV}$

A DDDK state

Tian-Wei Wu, LSG, et al., in preparation

1(0+)

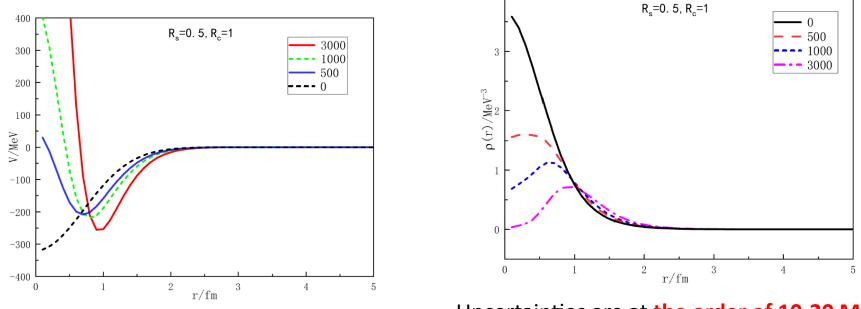
Gaussian Expansion Method



What if we add one more D?

Gaussian Expansion Method

What if we add one more D? Preliminary results show that such a state exists as well



Uncertainties are at the order of 10-20 MeV

$e^{-(r/R_S)^2}$	$e^{-(r/R_c)^2}$
$V_{DK}(\vec{r}; R_c) = C_S \frac{e^{-(r/R_S)^2}}{\pi^{3/2} R_S^3} + C$	$C(R_C) \frac{3}{\pi^{3/2} R_c^3},$

	DK*	DDK	DDDK
Binding	45 MeV	(67-71) MeV	91-107 MeV

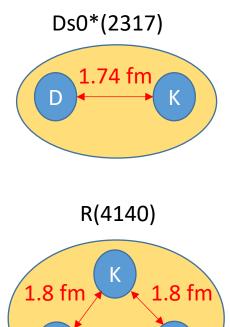
DD interactions play a minor role

$\frac{C_S}{\pi R_S^3} \frac{C(R_c)}{\pi R_c^3}$	E_2	$E_3(\text{only } V_{DK})$	$E_3(V_{DK}+V_{DD})$	$E_4(\text{only}V_{DK})$	$\overline{E_4(V_{DK}+V_{DD})}$
<u></u>	$R_S = 0.5 \text{fm}$	1	$R_c = 1 \mathrm{fm}$		
0 -320.1	-45.0	-65.8	-71.2	-89.4	-106.8
500 - 455.4	-45.0	-65.8	-70.4	-89.2	-103.5
1000 - 562.6	-45.0	-65.7	-69.7	-88.8	-101.4
3000 - 838.7	-45.0	-65.0	-68.4	-87.0	-97.3
	$R_S = 0.5 \mathrm{fm}$	1	$R_c = 2 \mathrm{fm}$		
0 -149.1	-45.0	-66.0	-68.8, -45.1	-88.7, -66.3	-97.6, -70.7
500 - 178.4	-45.0	-65.9	-68.2, -45.5	-88.5, -66.7	-95.5, -70.9
1000 - 195.0	-45.0	-65.8, -45.2	-67.9, -45.8	-88.2, -66.9	-94.5, -71.2
3000 - 225.9	-45.0	-65.3, -45.6	-67.2, -46.6	-87.0, -67.0	-92.6, -71.7
	$R_S = 0.5 \mathrm{fm}$	1	$R_c = 3 \mathrm{fm}$		
0 -107.0	-45.0	-66.2, -47.3	-68.0, -48.3	-88.8, -70.2	-94.4, -74.3
500 - 119.4	-45.0	-66.2, -48.2	-67.7, -49.3	-88.7, -71.0	-93.2, -74.8
1000 - 125.6	-45.0	-66.1, -48.7	-67.5, -49.8	-88.4, -71.3	-92.5, -75.2
3000 - 136.2	-45.0	-65.8, -49.4	-67.1, -50.7	-87.6, -71.7	-91.4, -75.7

35

Spatial distributions

$\frac{C_S}{\pi R_S^3}$	$\frac{C(R_c)}{\pi R_c^3}$	$r_2(DK)$	$r_3(DK)$	$r_3(DD)$	< T >	$\langle V_{DK} \rangle$	$< V_{DD} >$	
$R_S = 0.5 \text{fm} \ R_c = 1 \text{fm}$								
0	-320.1	1.28	1.32	1.36	124.37	-189.61	-5.98	
500	-455.4	1.39	1.44	1.47	99.51	-164.83	-5.03	
1000	-562.6	1.46	1.53	1.54	91.43	-156.67	-4.51	
3000	-838.7	1.61	1.69	1.68	93.24	-157.80	-3.82	
			$R_S = 0.5 \text{fm}$	$R_c = 2 \mathrm{fm}$				
0	-149.1	1.74	1.80	1.80	60.20	-125.74	-3.23	
500	-178.4	1.91	1.98	1.96	51.00	-116.59	-2.64	
1000	-195.0	1.99	2.07	2.04	50.63	-116.12	-2.43	
3000	-225.9	2.13	2.22	2.15	53.61	-118.59	-2.24	
	$R_S = 0.5 \text{fm} \ R_c = 3 \text{fm}$							
0	-107.0	2.13	2.19	2.17	39.49	-105.35	-2.13	
500	-119.4	2.31	2.38	2.34	34.80	-100.73	-1.77	
1000	-125.6	2.37	2.47	2.42	34.90	-100.77	-1.65	
3000	-136.2	2.53	2.61	2.53	36.66	-102.24	-1.54	



1.8 fm

D

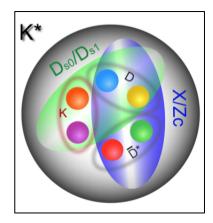
D

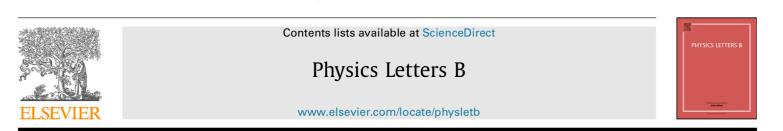
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Instead of a D, what happens if we add a $\overline{D^*}$ to the DK pair





Physics Letters B 785 (2018) 112-117

 K^* mesons with hidden charm arising from KX(3872) and $KZ_c(3900)$ dynamics



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^a Institut für Theoretische Physik II, Ruhr-Universität Bochum, D-44780 Bochum, Germany

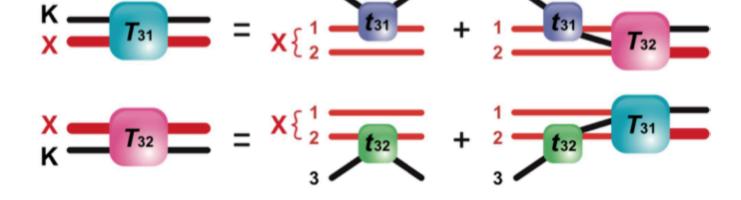
^b Instituto de Física, Universidade de São Paulo, C.P. 66318, 05389-970 São Paulo, São Paulo, Brazil

^c School of Physics and Nuclear Energy Engineering & Beijing Key Laboratory of Advanced Nuclear Materials and Physics, Beihang University, Beijing 100191, China

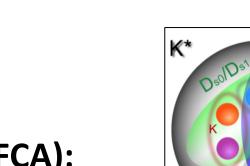
^d Beijing Advanced Innovation Center for Big Date-Based Precision Medicine, Beihang University, Beijing 100191, China

^e Universidade Federal de São Paulo, C.P. 01302-907, São Paulo, Brazil

Figure 2: Diagrams showing the scattering of the particle labeled "3" (K) on a cluster (X) made of particles 1 (D) and 2 (\overline{D}^*) .



• Fixed center approximation (FCA):

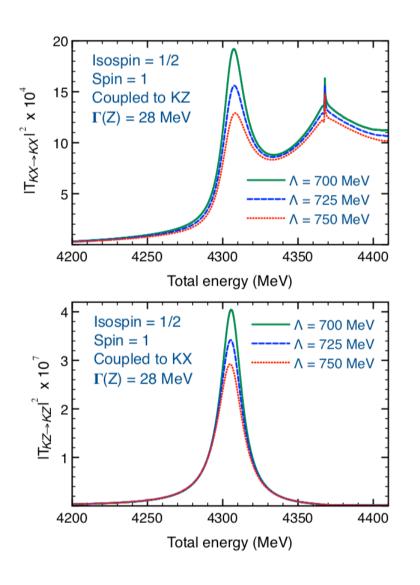


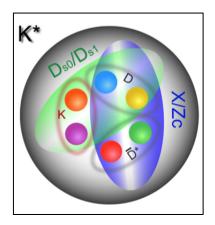




X/Zc

K*(4307)

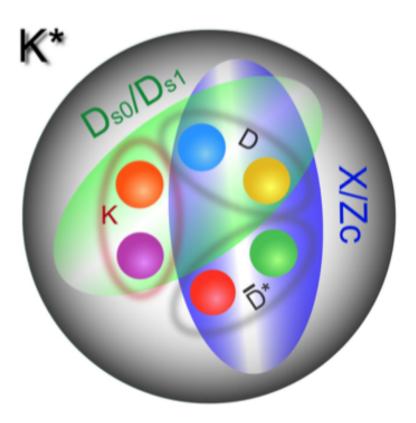


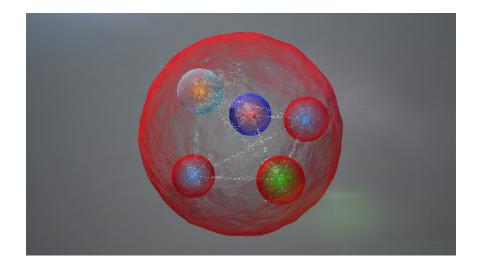


- Treating KX and KZ as coupled channel systems
- A resonance with M=(4307 \pm 2) i(9 \pm 2) MeV with I(J^P) = 1/2(1⁻)

In agreement with Li Ma, Qian Wang, Ulf-G. Meißner, 1711.06143, but with completely different dynamics

K*(4307)—bosonic counterpart of Pc





Pentaquark (N*) by LHCb

Phys.Rev.Lett. 115 (2015) 072001

Prediction of narrow N* and Λ * resonances with hidden charm above 4 GeV, Jia-Jun Wu, R. Molina, E. Oset, B.S. Zou, 1007.0573

Analogy between KD and Kbar N

$D_{s0}^{*}(2317)$

- DK bound state
- Dynamically generated--
 - Unitary heavy hadron chiral perturbation theory
- Coupled channels

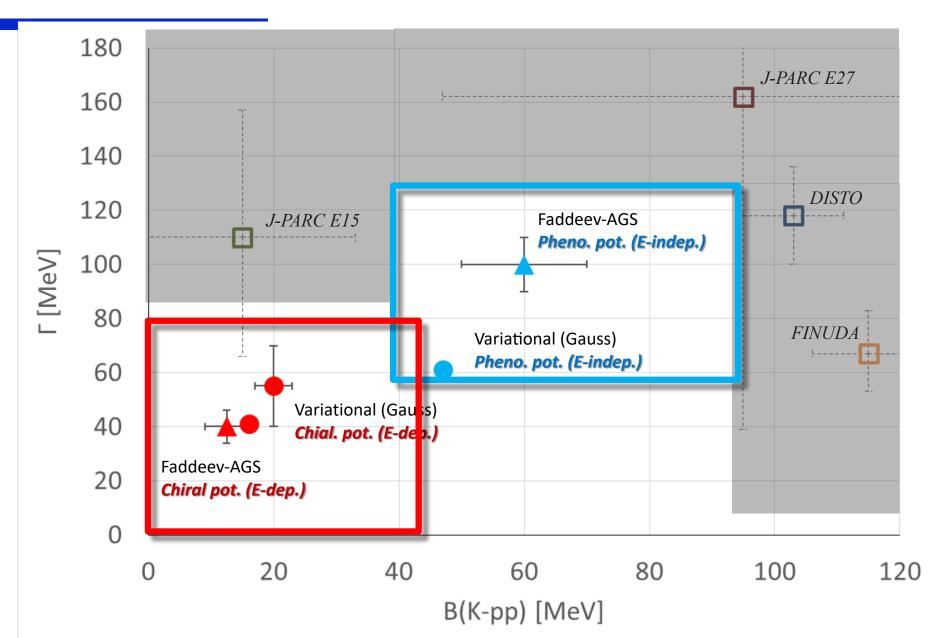
A(1405)

- N-Kbar bound state
- Dynamically generated- Unitary baryon chiral
 perturbation theory
- Coupled channels

The interaction between **a kaon and a heavy particle** seems to play an important role

Current status on "K⁻pp"

A. Dote, Menu2019



□From nucleons, we can build nuclei, based on which the whole visible universe is formed

□If the Ds0*(2317) is indeed a molecule of DK, then new forms of matter may be built upon them

- We have performed explicit few-body studies demonstrating that indeed both DDK and DDDK bound states exist
- Now we need experimental or lattice QCD confirmations and further theoretical studies on their production and decay mechanisms



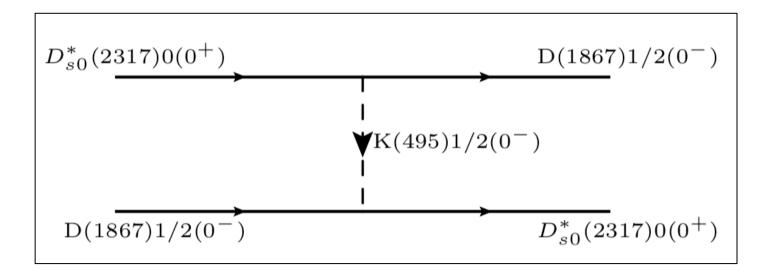


Thanks for your

attention !

July 18, 2019

Interestingly, the explicit three-body result is consistent with the quasi two body study, where one treats the DK pair as the Ds0* and describes the interaction between the Ds0* with the D using one-kaon exchange



Mario Sanchez Sanchez, LSG, Jun-Xu Lu, Tetsuo Hyodo, Manuel Pavon Valderrama. 1707.03802

