

Beyond the Standard Model and neutrino precision test

C.R. Das, J. Maalampi, J. Pulido and S. Vihonen

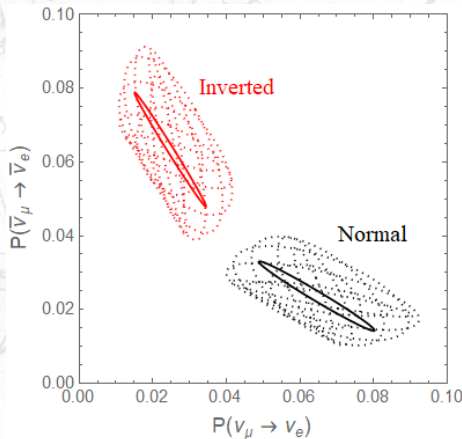
BLTP, JINR, Russia; University of Jyväskylä, Finland; CFTP, IST, Portugal and Sun Yat-sen University, PRC

13th APCTP - BLTP JINR Joint Workshop
“Modern Problems in Nuclear and Elementary Particle Physics”
July 14-20, 2019

**Although neutrinos are among the most abundant particles in the Universe,
many of their basic properties are still unknown.**

Gossip in the corridor

Neutrinos may have tipped the balance in favour of matter over anti-matter in the Universe!

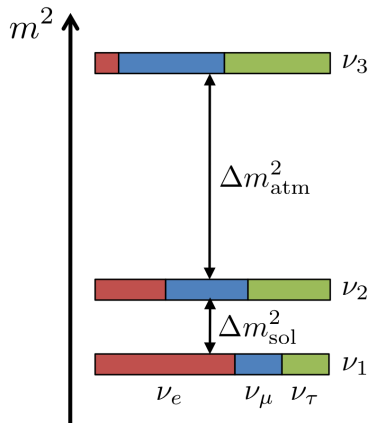


Detecting CP Violation in the Presence of Non-Standard Neutrino Interactions,
Jeffrey M. Hyde (Goucher Coll.), [arXiv: 1809.11128](https://arxiv.org/abs/1809.11128)

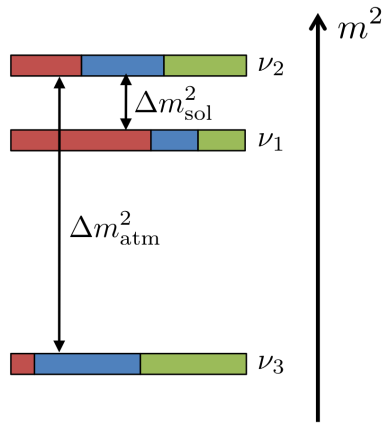
Gossip in the corridor

Which one is heaviest ν_2 or ν_3 ?

normal hierarchy (NH)

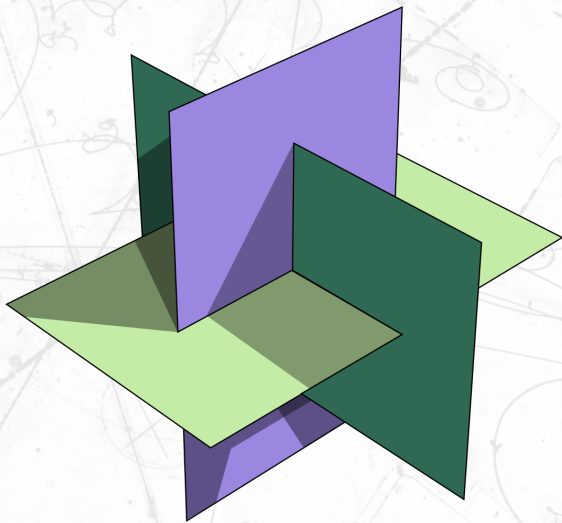


inverted hierarchy (IH)



No gossip in the corridor

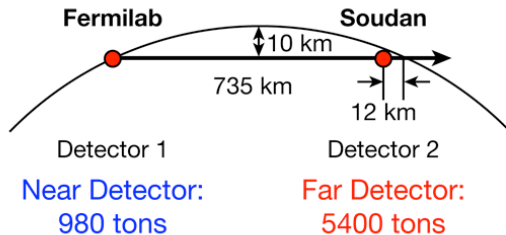
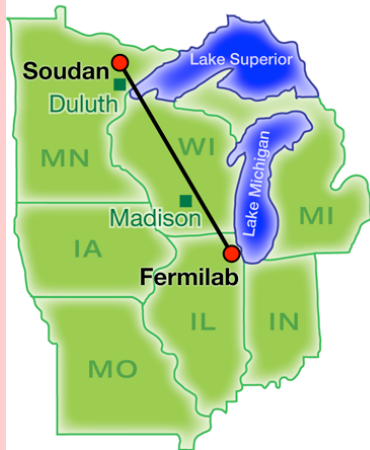
In which octant θ_{23} is sitting?



Preliminaries (Physics with long baseline)

MINOS and MINOS+ (Main injector neutrino oscillation search)

The MINOS Experiment



Preliminaries (Physics with long baseline)

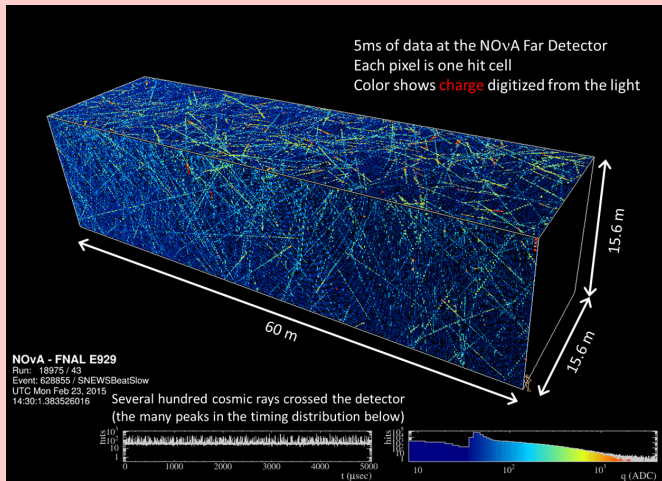
MINOS, MINOS+ and NOvA



Cross section of the earth showing Fermilab, MINOS and NOvA, to scale.
The red line is the central axis of the NuMI beam.

Preliminaries (Physics with long baseline)

NOvA (NuMI Off-Axis ν_e Appearance)



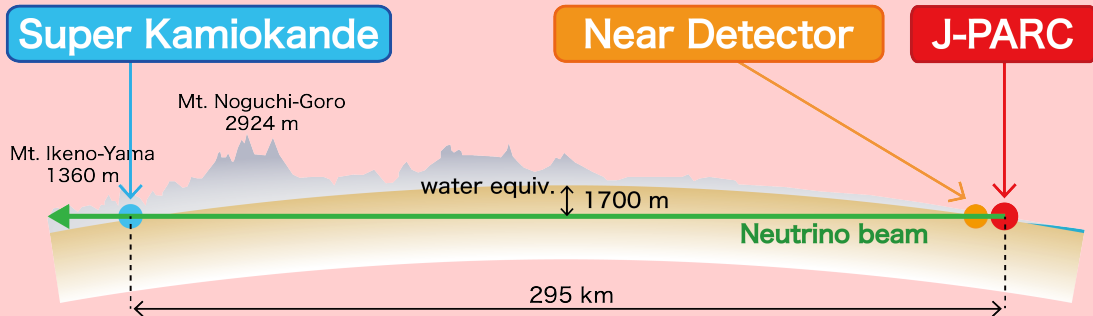
Preliminaries (Physics with long baseline)

NOvA (NuMI Off-Axis ν_e Appearance)



Preliminaries (Physics with long baseline)

T2K (Tokai to Kamioka, Japan)



DUNE (Deep Underground Neutrino Experiment)



	Normal Ordering (best fit)		Inverted Ordering ($\Delta\chi^2 = 4.14$)		Any Ordering
	bfp $\pm 1\sigma$	3σ range	bfp $\pm 1\sigma$	3σ range	3σ range
$\sin^2 \theta_{12}$	$0.307^{+0.013}_{-0.012}$	$0.272 \rightarrow 0.346$	$0.307^{+0.013}_{-0.012}$	$0.272 \rightarrow 0.346$	$0.272 \rightarrow 0.346$
$\theta_{12}/^\circ$	$33.62^{+0.78}_{-0.76}$	$31.42 \rightarrow 36.05$	$33.62^{+0.78}_{-0.76}$	$31.43 \rightarrow 36.06$	$31.42 \rightarrow 36.05$
$\sin^2 \theta_{23}$	$0.538^{+0.033}_{-0.069}$	$0.418 \rightarrow 0.613$	$0.554^{+0.023}_{-0.033}$	$0.435 \rightarrow 0.616$	$0.418 \rightarrow 0.613$
$\theta_{23}/^\circ$	$47.2^{+1.9}_{-3.9}$	$40.3 \rightarrow 51.5$	$48.1^{+1.4}_{-1.9}$	$41.3 \rightarrow 51.7$	$40.3 \rightarrow 51.5$
$\sin^2 \theta_{13}$	$0.02206^{+0.00075}_{-0.00075}$	$0.01981 \rightarrow 0.02436$	$0.02227^{+0.00074}_{-0.00074}$	$0.02006 \rightarrow 0.02452$	$0.01981 \rightarrow 0.02436$
$\theta_{13}/^\circ$	$8.54^{+0.15}_{-0.15}$	$8.09 \rightarrow 8.98$	$8.58^{+0.14}_{-0.14}$	$8.14 \rightarrow 9.01$	$8.09 \rightarrow 8.98$
$\delta_{\text{CP}}/^\circ$	234^{+43}_{-31}	$144 \rightarrow 374$	278^{+26}_{-29}	$192 \rightarrow 354$	$144 \rightarrow 374$
$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.40^{+0.21}_{-0.20}$	$6.80 \rightarrow 8.02$	$7.40^{+0.21}_{-0.20}$	$6.80 \rightarrow 8.02$	$6.80 \rightarrow 8.02$
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- Is there any CP violation among neutrinos?
- What is the order of neutrino masses?
- Which octant does θ_{23} belong to?

The problem of θ_{23} octant

The conversion probability formula is given by:

$$\begin{aligned} P_{\mu e} \approx & \sin^2 \theta_{23} \sin^2 2\theta_{13} \frac{\sin^2(\Delta_{31} - aL)}{(\Delta_{31} - aL)^2} \Delta_{31}^2 \\ & + \sin 2\theta_{23} \sin 2\theta_{13} \sin 2\theta_{12} \frac{\sin(\Delta_{31} - aL)}{\Delta_{31} - aL} \Delta_{31} \\ & \times \frac{\sin(aL)}{aL} \Delta_{21} \cos(\Delta_{31} + \delta_{\text{CP}}) \\ & + \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2(aL)}{(aL)^2} \Delta_{21}^2, \end{aligned}$$

where $\Delta_{ij} = \frac{L \Delta m_{ij}^2}{4E}$ and $a = \frac{G_F N_e}{\sqrt{2}}$.

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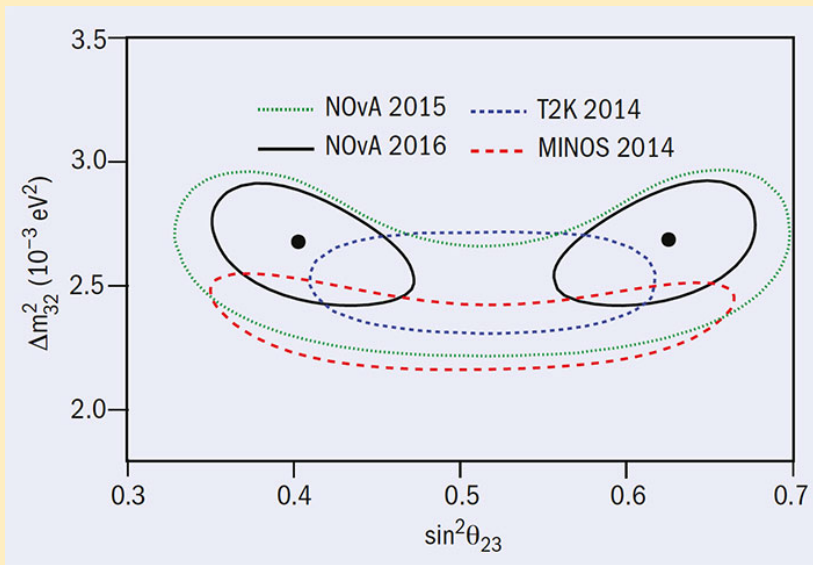
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Tests of three-flavour mixing in long-baseline neutrino oscillation experiments,
G.L. Fogli and E. Lisi, Phys. Rev. D **54**, 3667-3670 (1996); arXiv: hep-ph/9604415

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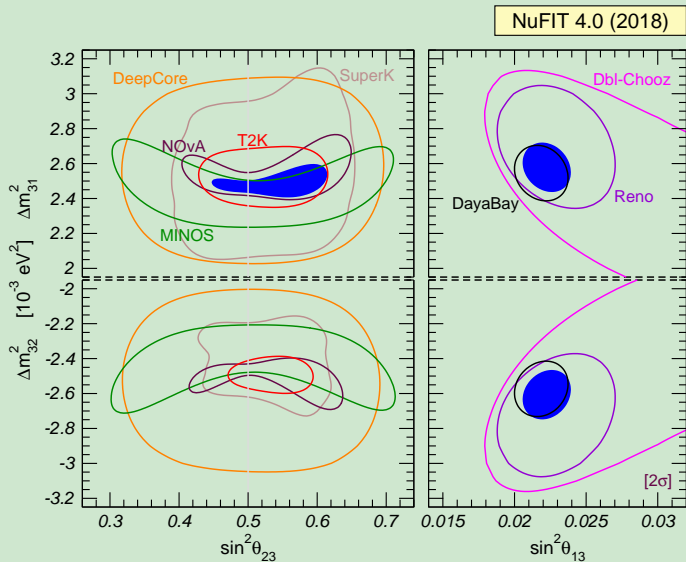
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The hint of normal hierarchy suggests the atmospheric mixing angle might reside in the high octant.

 I. Esteban, M.C. Gonzalez-Garcia, A. Hernandez-Cabezudo, M. Maltoni
and T. Schwetz, JHEP **01**, 106 (2019); arXiv: 1811.05487

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Matter effects and octant determination

Matter effects revisited:

$$\begin{aligned} P_{\mu\mu}^m \approx & 1 - \cos^2 \theta_{13}^m \sin^2 2\theta_{23} \sin^2 \left(C \frac{L}{E} \left(\frac{\Delta m_{31}^2 + A + (\Delta m_{31}^2)_m}{2} \right) \right) \\ & - \sin^2 \theta_{13}^m \sin^2 2\theta_{23} \sin^2 \left(C \frac{L}{E} \left(\frac{\Delta m_{31}^2 + A - (\Delta m_{31}^2)_m}{2} \right) \right) \\ & - \sin^4 \theta_{23} \sin^2 2\theta_{13}^m \sin^2 \left(C \frac{L}{E} (\Delta m_{31}^2)_m \right), \end{aligned}$$

where $A = 2 E V$, $C = 1.27$ and $V = 2\sqrt{2} G_F N_e$.

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$$(\Delta m_{31}^2)_m = \sqrt{(\Delta m_{31}^2 \cos 2\theta_{13} - A)^2 + (\Delta m_{31}^2 \sin 2\theta_{13})^2},$$

$$\sin 2\theta_{13}^m = \frac{\Delta m_{31}^2}{(\Delta m_{31}^2)_m} \sin 2\theta_{13},$$

and

$$\cos 2\theta_{13}^m = \frac{\Delta m_{31}^2}{(\Delta m_{31}^2)_m} (\cos 2\theta_{13} - A).$$

Matter effects and octant determination

Matter effects revisited:

Neglecting the last term, this expression is also octant-degenerate:

$$P_{\mu\mu}^m(\theta_{23}) = P_{\mu\mu}^m(\pi/2 - \theta_{23})$$

- The $P_{\mu\mu}^m$ expression derived for the survival probability, given here, does have a subleading term (the last term) that is octant sensitive, however.
- This term is also subject to matter resonant effects, and therefore could also contribute to the determination of the θ_{23} octant.

Matter effects and octant determination

The MSW resonance ...

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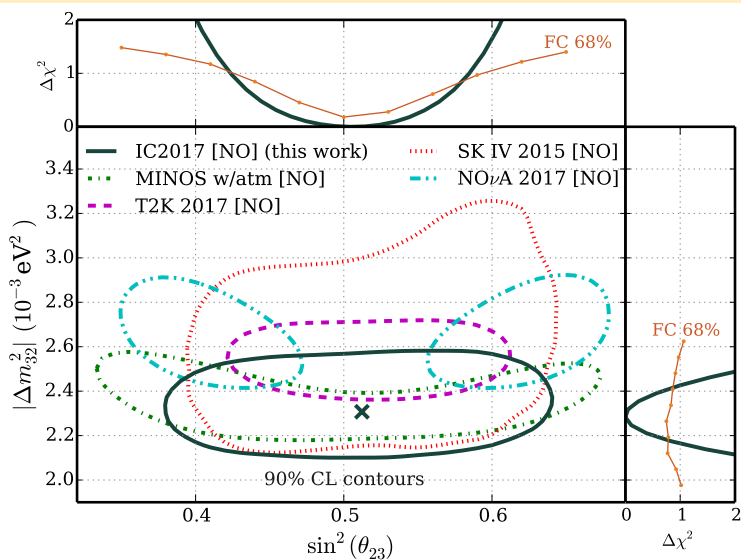


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A. Chatterjee, P. Ghoshal, S. Goswami and S.K. Raut,
JHEP **1306**, 010 (2013); arXiv: 1302.1370

This is Shrek!



How to free octants from its clutch!



Simulation examples:

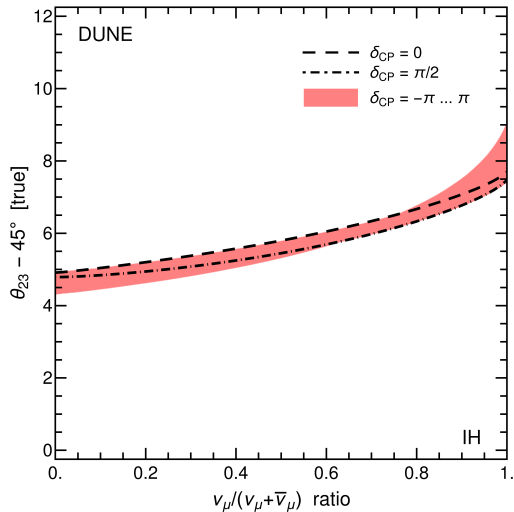
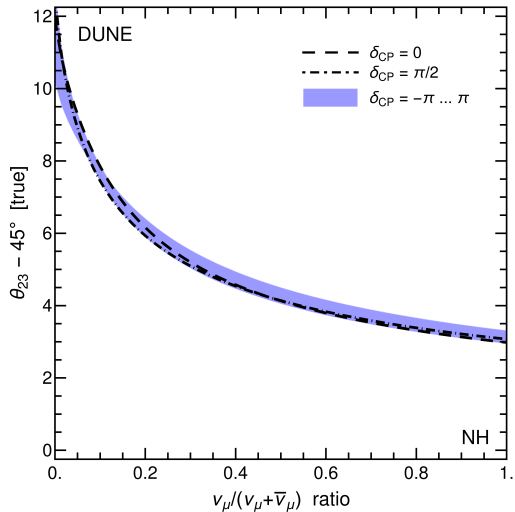
DUNE

- ① 1300 km baseline
- ② oscillation maximum
at ~ 2 GeV
- ③ wide-band beam

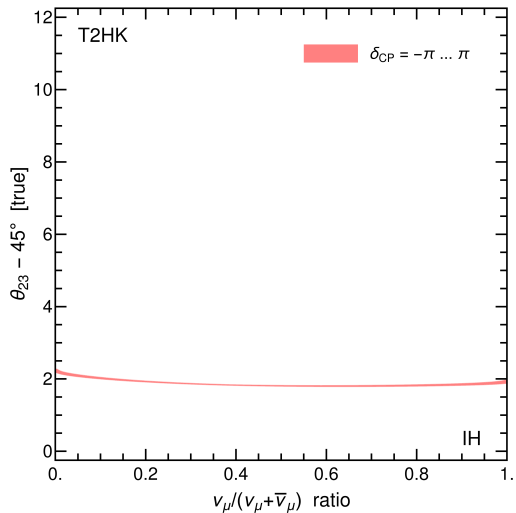
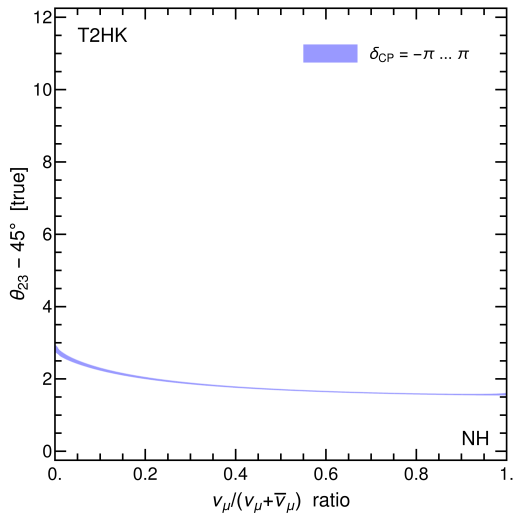
T2HK

- ① 295 km baseline
- ② oscillation maximum
at ~ 0.6 GeV
- ③ off-axis experiment

Octant determination in DUNE:



Octant determination in T2HK:



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This is because the $\nu_\mu \rightarrow \nu_\mu$ survival probability is mostly octant-degenerate and $\nu_\mu \rightarrow \nu_e$ is the one that tells us about the octant.

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If θ_{23} is very near to maximal, it will be very difficult to ascertain the octant through long-baseline experiments.

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The apparent conflict between T2K and NOvA results can also be an indication of new physics:

- Non-standard interactions, sterile neutrinos and decoherence effects are few examples.

Midpoint summary

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No!

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Beyond the Standard Model

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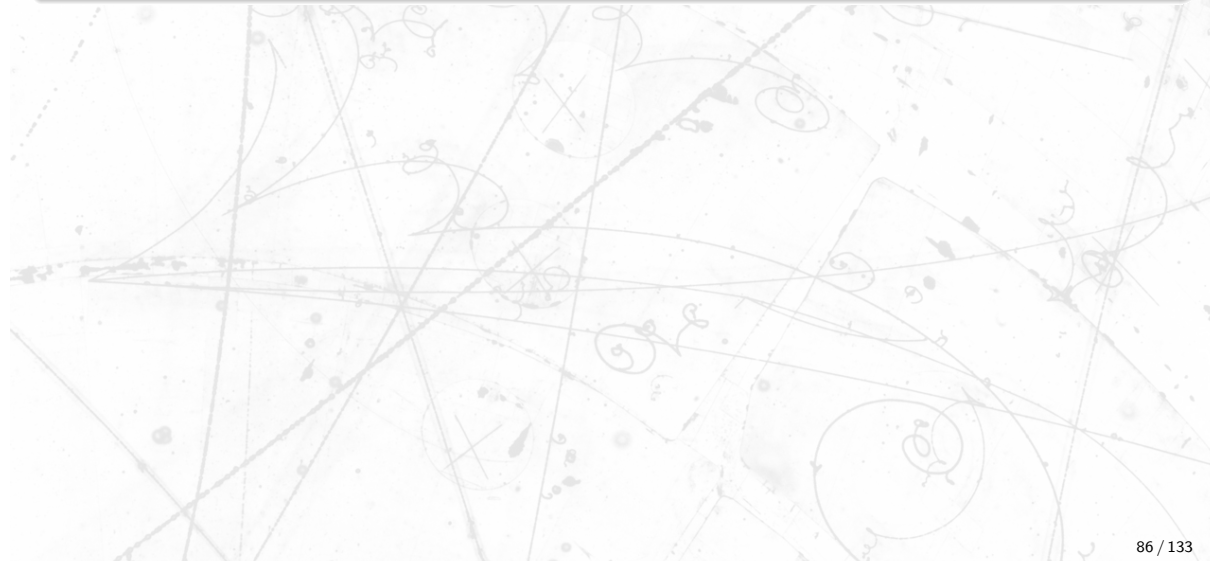
- Sterile neutrinos
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In case of one sterile neutrino

$$U_{4 \times 4} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{pmatrix}$$

the 3×3 matrix is no longer unitary.

Non-unitary mixing



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$$N = \begin{pmatrix} \alpha_{11} & 0 & 0 \\ \alpha_{21} & \alpha_{22} & 0 \\ \alpha_{31} & \alpha_{32} & \alpha_{33} \end{pmatrix} \times U_{PMNS}$$

$$H = \frac{1}{2E_\nu} \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix} + N^\dagger \times \begin{pmatrix} V_{CC} + V_{NC} & 0 & 0 \\ 0 & V_{NC} & 0 \\ 0 & 0 & V_{NC} \end{pmatrix} \times N$$

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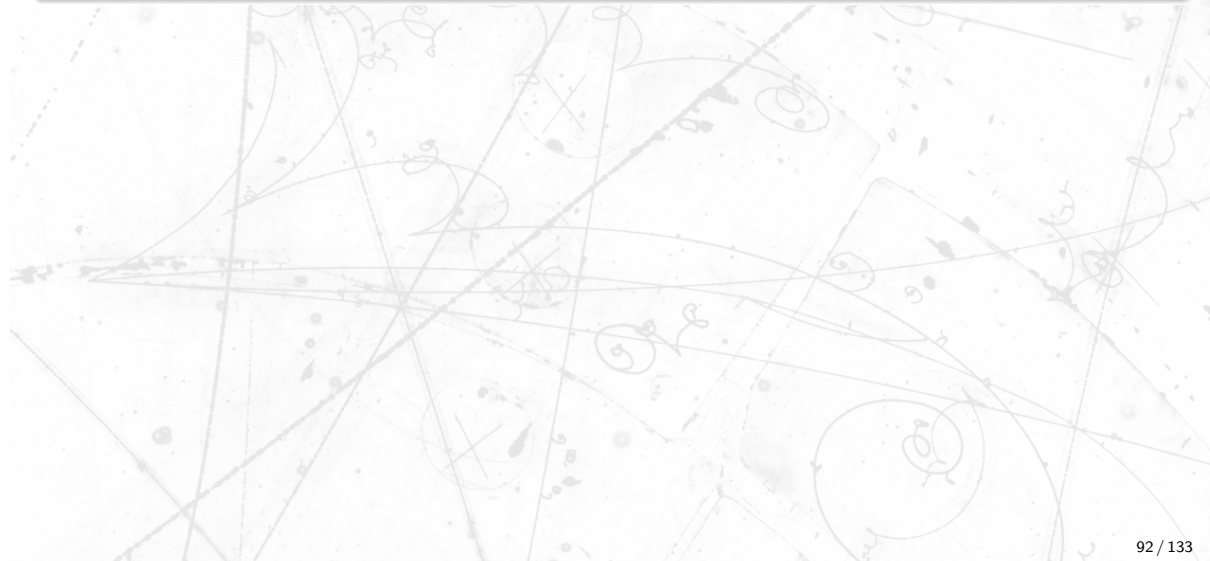
F.J. Escrihuela, D.V. Forero, O.G. Miranda, M. Tórtola and J.W.F. Valle,
Phys. Rev. **D92**, 053009 (2015) and New J. Phys. **19**, 093005 (2017)

- Non-unitary mixing bounds:
(Example from Escribuela et al.)

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Non-unitary parameter	Bound at 90% C.L.
α_{11}	0.9974
α_{22}	0.9994
α_{33}	0.9988
$ \alpha_{21} $	2.6×10^{-2}
$ \alpha_{31} $	2.0×10^{-3}
$ \alpha_{32} $	1.5×10^{-2}

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M. Blennow, P. Coloma, E. Fernandez-Martinez, J. Hernandez-Garcia and J. Lopez-Pavon, J. High Energ. Phys. **04**, 153 (2017); arXiv:1609.08637

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- Both notations are equivalent when calculating the Hamiltonian and oscillation probabilities.

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$\alpha_{\mu\mu}$	$2.2 \cdot 10^{-4}$	$2.2 \cdot 10^{-2}$	$1.4 \cdot 10^{-2}$
$\alpha_{\tau\tau}$	$2.8 \cdot 10^{-3}$	$1.0 \cdot 10^{-1}$	$1.0 \cdot 10^{-1}$
$ \alpha_{\mu e} $	$6.8 \cdot 10^{-4} (2.4 \cdot 10^{-5})$	$2.5 \cdot 10^{-2}$	$1.7 \cdot 10^{-2}$
$ \alpha_{\tau e} $	$2.7 \cdot 10^{-3}$	$6.9 \cdot 10^{-2}$	$4.5 \cdot 10^{-2}$
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- In this case, the average-out effect will be the same in both near and far detectors, and they will find no difference in the event rates that are measured in the far detector and extrapolated from the near detector.

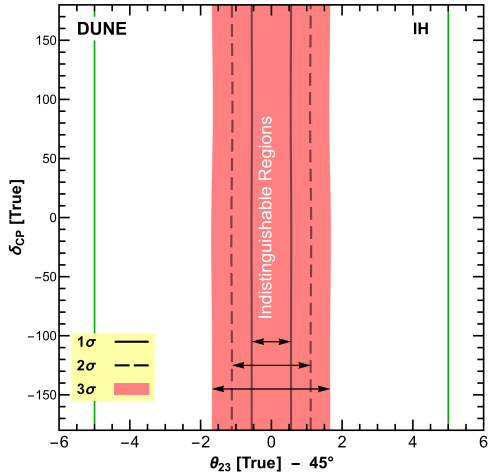
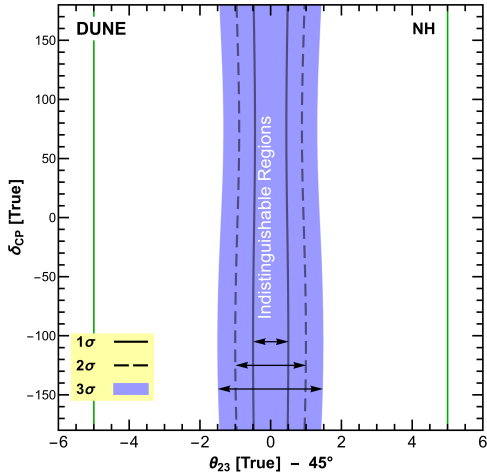
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- This is the reason why the bounds are calculated differently and sorted into two mass ranges.

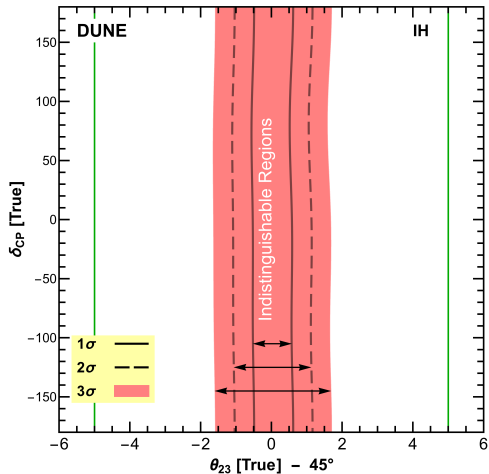
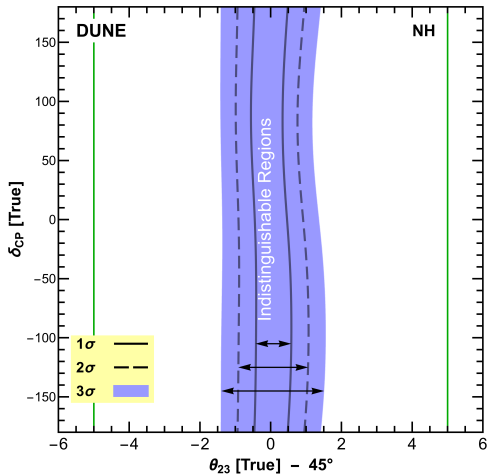
Standard Model case
(3 active neutrinos and nothing else)
(3.5 years + 3.5 years)



Non-unitary mixing

(3 active and 3 sterile neutrinos, Blennow et al. bound)

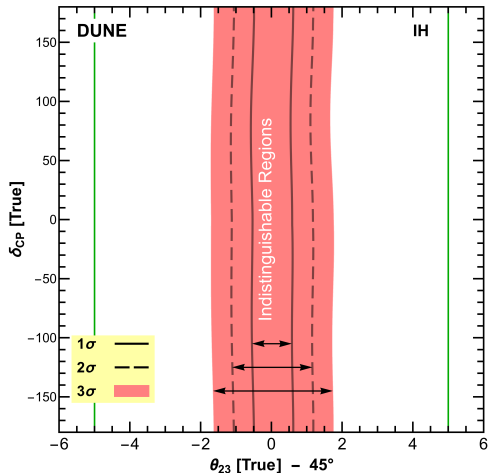
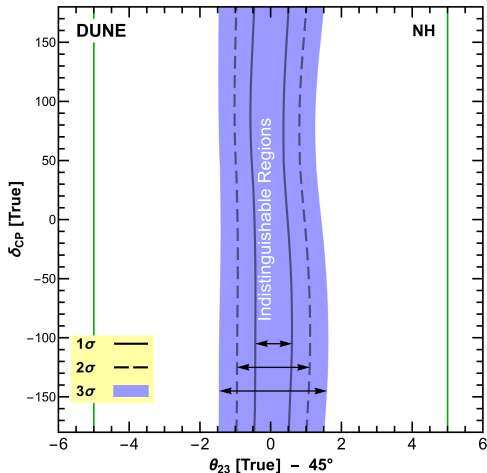
(3.5 years + 3.5 years)



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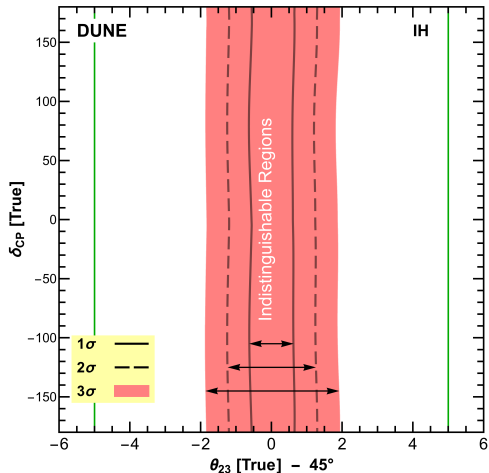
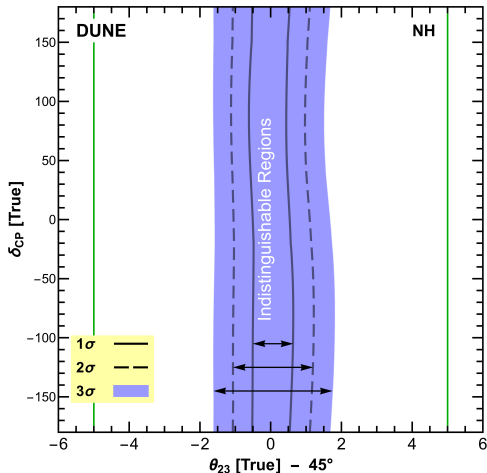
(3.5 years + 3.5 years)



Light sterile neutrino

(3 active and 3 sterile neutrinos, $0.1 \text{ eV}^2 < \Delta m_{41}^2 < 1 \text{ eV}^2$, Blennow et al. bound)

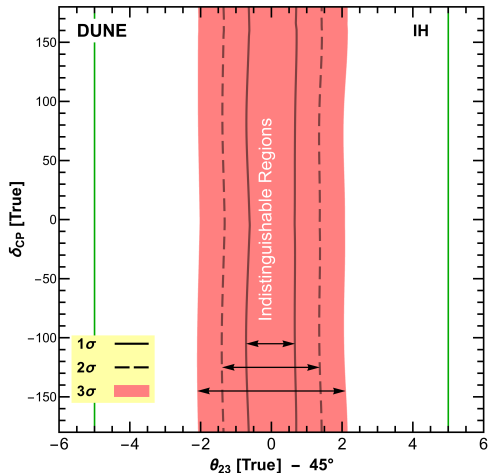
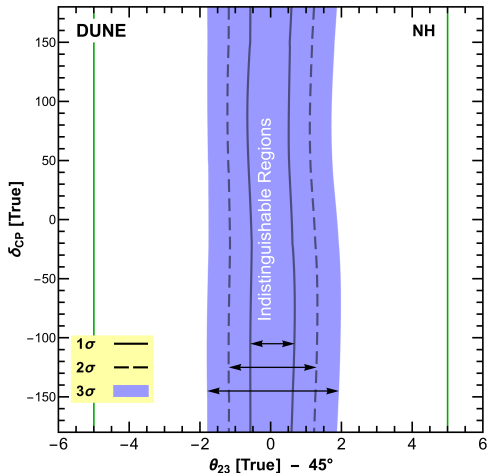
(3.5 years + 3.5 years)



Light sterile neutrino

(3 active and 3 sterile neutrinos, $\Delta m_{41}^2 > 100 \text{ eV}^2$, Blennow et al. bound)

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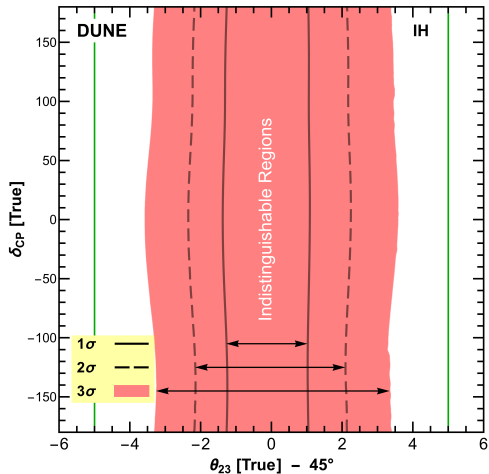
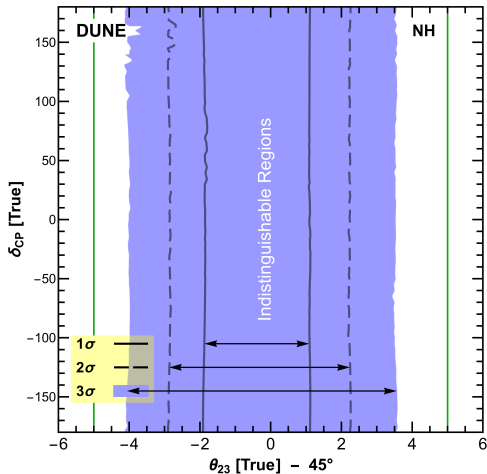
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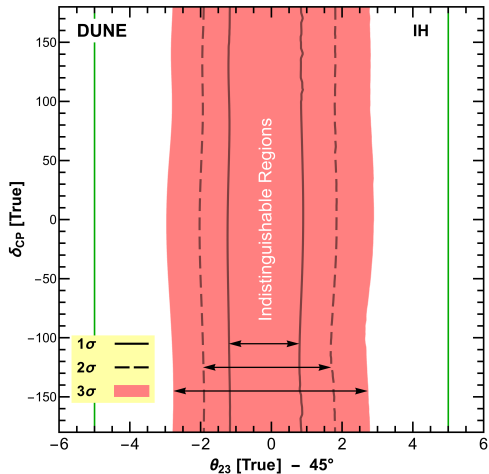
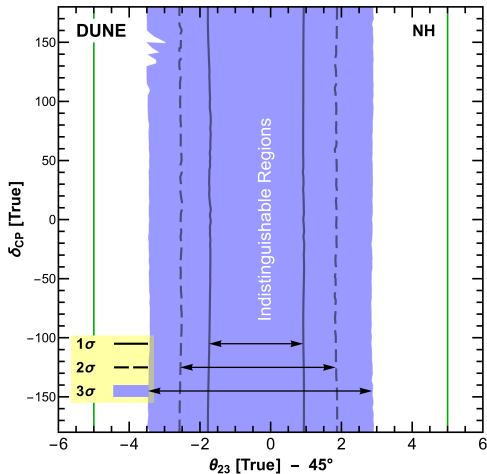
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What will happen if α s are unconstrained?

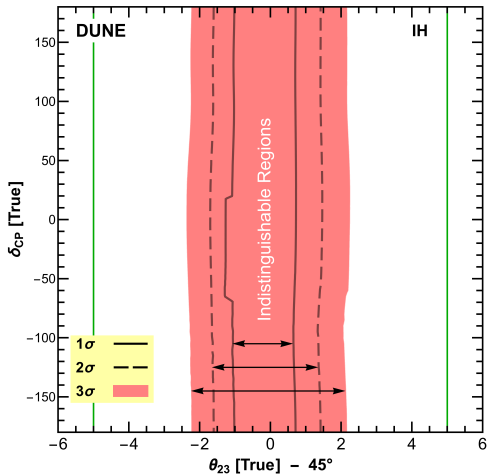
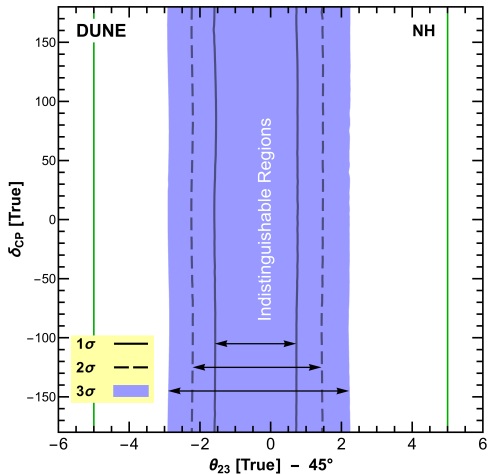
Non-unitary mixing
(Unconstrained α s)
(3.5 years + 3.5 years)



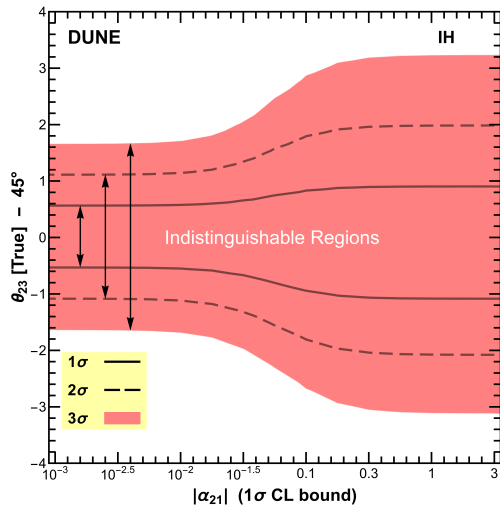
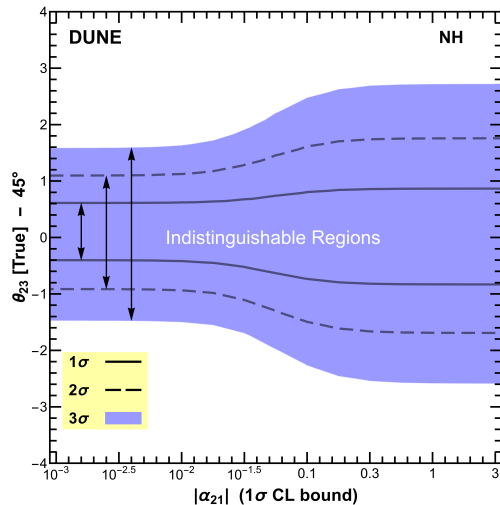
Non-unitary mixing
(Unconstrained α s)
(5 years + 5 years)



Non-unitary mixing
(Unconstrained α s)
(8 years + 8 years)



$|\alpha_{21}|$ dependency plot
(3.5 years + 3.5 years)



How new physics could potentially affect the octant measurement?

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- With non-unitarity, not at all.

How new physics could potentially affect the octant measurement?

- With non-unitarity, not at all.
- With light sterile neutrinos, a little.

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- And with an unconstrained model that has potentially more than just sterile neutrinos, a little more.

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If you don't know anything about BSMs,
don't worry, try to increase the events!

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- This non-unitarity do not appear yet in the leading order, so the effects turn out to be negligible. If one is to recalibrate the whole neutrino experimental data which is available today, the non-unitarity corrections would be so small that the new best-fits would easily fall within the current experimental bounds.

Summary

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Please see articles by **C.R. Das, J. Maalampi, J. Pulido and S. Vihonen:**

arXiv: 1712.07343

DOI: 10.1088/1742-6596/888/1/012219

DOI: 10.1103/PhysRevD.97.035023

DOI: 10.22323/1.283.0030

arXiv: 1606.02504

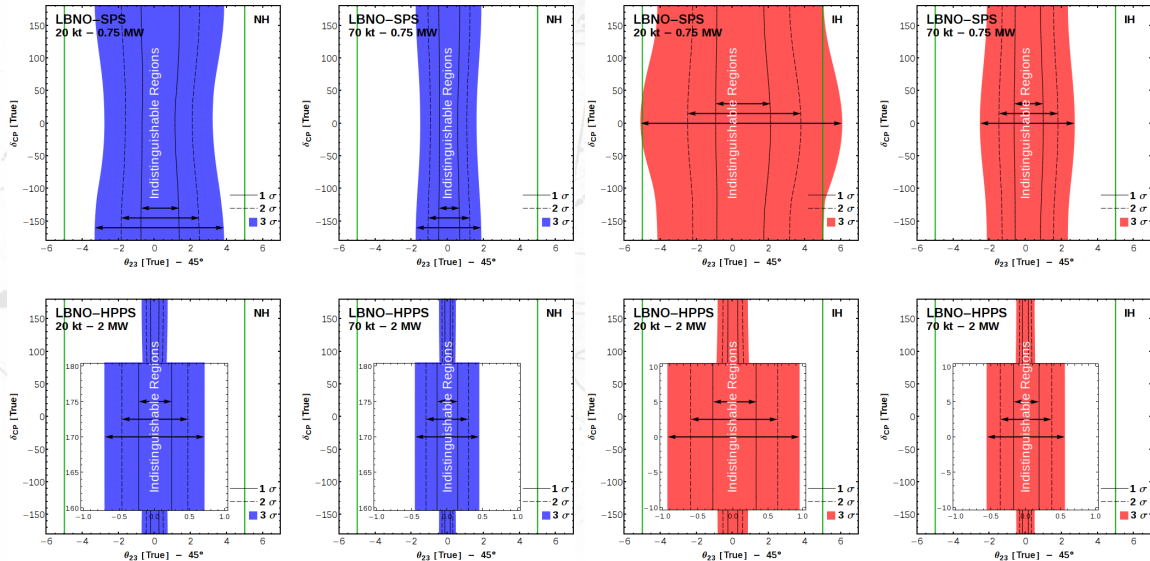
DOI: 10.1007/JHEP02(2015)048

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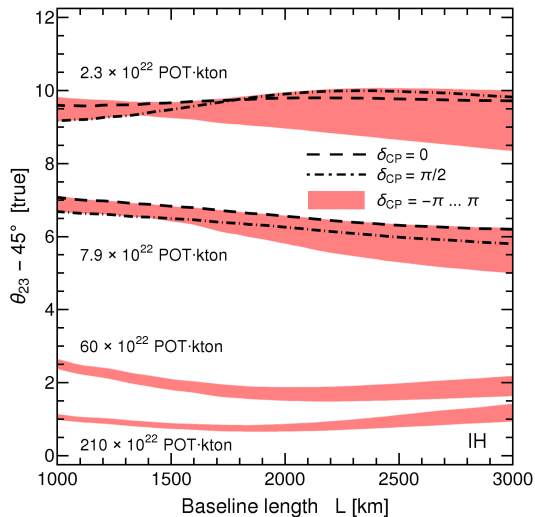
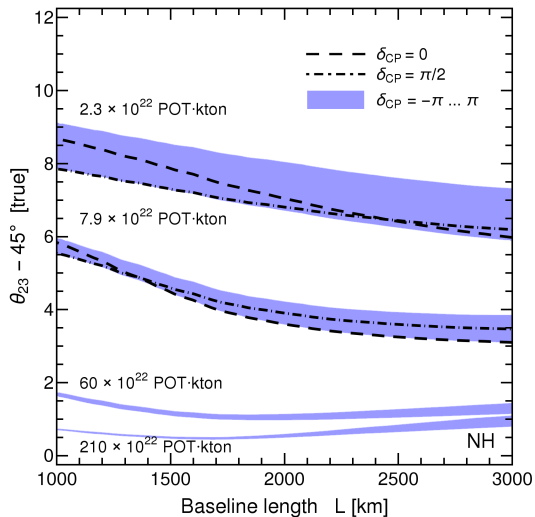
Experimental parameters:

Parameter	Value
Beam power [SPS] (10^{20} POT/yr)	1.125
Beam power [HPPS] (10^{21} POT/yr)	3.0
Baseline length (km)	2288
Running times (yr)	5+5
Detection efficiency (%)	90
ν_μ NC rejection (%)	99.5
ν_μ CC rejection (%)	99.5
Energy resolution (GeV)	$0.15 \times \sqrt{E}$
Energy window (GeV)	[0.1, 10.0]
Number of bins	80
Bin width (GeV)	0.125

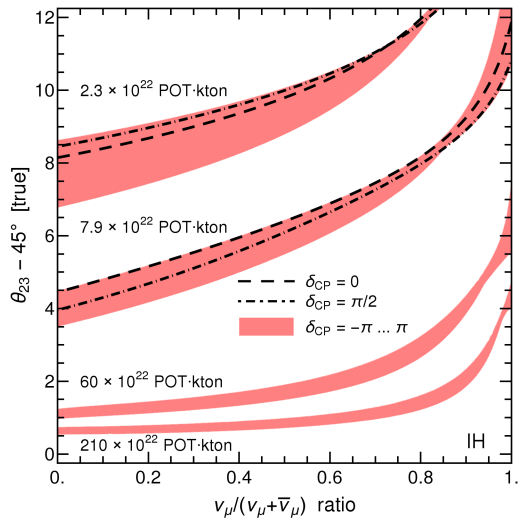
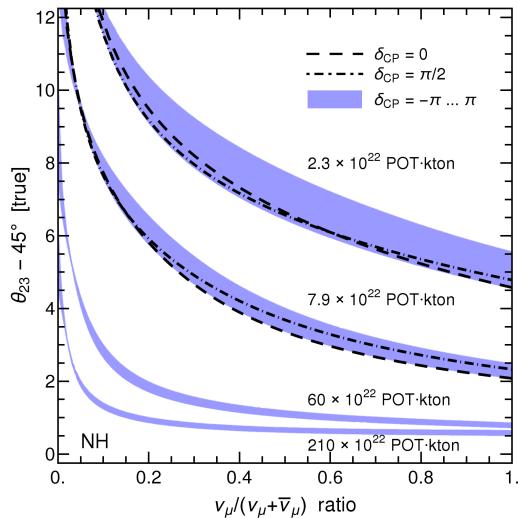
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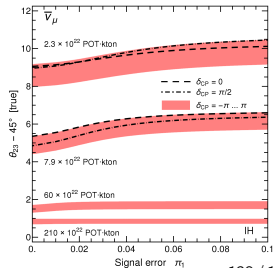
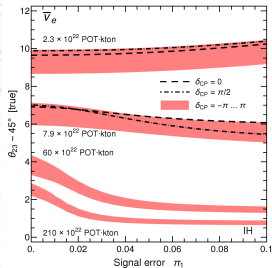
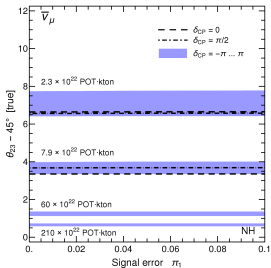
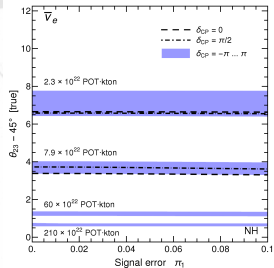
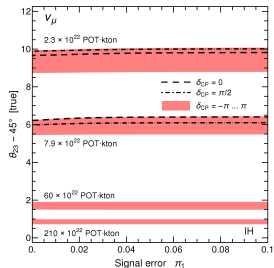
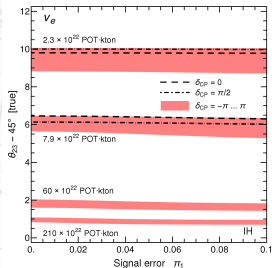
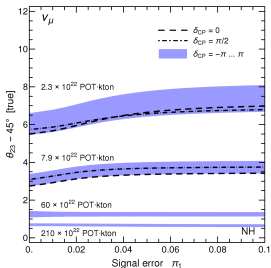
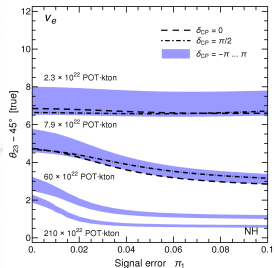
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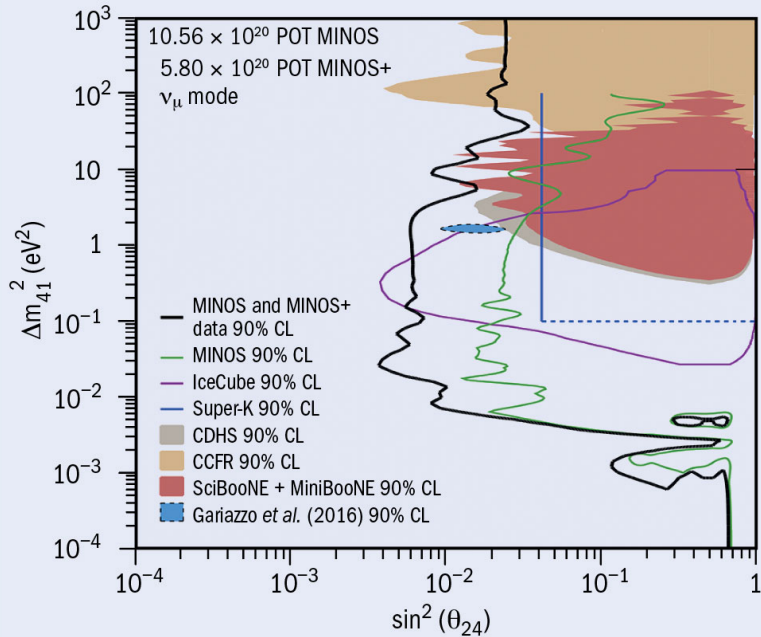


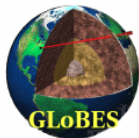
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GLOBES

General Long Baseline Experiment Simulator

GLOBES is a sophisticated software package for the simulation of long baseline neutrino oscillation experiments. Main features are:

- Full incorporation of correlations and degeneracies in the oscillation parameter space.
- Advanced routines for the treatment of arbitrary systematical errors
- AEDL, the **A**bstract **E**xperiment **D**efinition **L**anguage provides an easy way to define experimental setups.
- User-defined priors allow the inclusion of arbitrary external physical information
- Interface for the simulation of non-standard physics
- [Predefined setups](#) are available for many experiments: Superbeams, Beta Beams, Neutrino factories, Reactors, various detector technologies, ...
- Extensive documentation and examples are available for [download](#).

The latest stable release of GLOBES, version 3.0 is available for [download](#).

NEW: We now offer also the latest, frequently updated, development releases for [download](#).

NEW: A collection of [additional tools](#) for degeneracy finding, new physics simulation, etc. is now available for [download](#).

GLOBES is maintained by **Patrick Huber**, **Joachim Kopp**, **Manfred Lindner**, and **Walter Winter** (globes@mpi-hd.mpg.de).

How to say THANK YOU in various European languages

ETYMOLOGY

- From Latin *grātia* ('grace'), from PIE **gʷerh₂-* ('to welcome; to praise'; the same root as 'grace')
- From Latin *mercedem* ('pay; reward'), from Latin *merx* ('merchandise'; the same root as 'mercy', also see **)
- From Latin *obligo* ('bind in obligation'), from Latin *ob-* ('to') + *ligo* ('bind; untie'; the same root as 'obligation')
- From the Romanian verb *mulțumi* ('to thank'), from *la multi ani* (literally 'to/for many years', a birthday cheer)
- From Proto-Germanic **þankaz* ('thought; remembrance; gratitude'), from PIE **tong-* or **teng-* ('to think; to feel')
- via Old Norse *þökk*, from Proto-Germanic **þankaz*
- via Old High German *dankon*, from Proto-Germanic **þankaz*
- From Old Slavic *blago* ('good') + *dar* ('gift'), partially from PIE **deh₁-* ('to give'; the same root as 'donate')
- From Russian *spasi* ('save') + *bog* ('God'), from Proto-Russian **sūposi bogŭ* ('save (us) God')
- From Proto-Slavic **hvala* ('glory'), from Middle Persian **xwarənah* ('glory; prosperity; (good) fortune')
- From Albanian *falem* ('we pray') + *nderit* ('the honor'), partially borrowed from Serbo-Croatian *hvala*
- Equivalents in related languages, but origin is unclear; speculations about connection to Greek *kudos* ('praise')
- From Estonian *aitan*, which is a reduction of Proto-Finnic **aita* ('help') + **jumola* ('God')
- From a reduction of Latvian *palīdz Dievs* ('may God help'), compare Estonian and Russian
- Equivalents in related languages, but origin is unclear; possibly a clipping of multiple words
- From Ancient Greek *eukhōristos* ('pleasant; grateful'), from *eú* ('well, good') + *kharizomai* ('I show favor')
- From Hungarian *köszön* ('to thank') + *-öm* (suffix, from Old Turkic *kös* ('to wish; desire; long for'))
- From Georgian *madloba* ('thanks'), from Old Georgian *madli* ('benevolence; mercy')
- From Armenian *snorhakal* ('grateful') + *-ut* (enclitic suffix); from Middle Persian *snōhr* ('gratitude, contentment')
- From Arabic *talakkur* ('thank') + Turkish *ederim* ('I do'), also see †
- From Arabic *rahma* ('compassion; mercy')

* PIE = Proto-Indo-European

** *merci* has become part of the regular lexicon of multiple other languages (esp. Armenian, Bulgarian and Romanian)

- † from Basque *eder* ('appreciation') + *agur* ('hello')
- ‡ from Cornish *meur* ('great') + *gras* ('grace'), of Celtic origin
- § from Celtic *gragant* ('recognition; remembrance'), of Celtic origin
- ¶ from Irish *go raibí* ('may ... be') + *meadh* ('good') + *agat* ('at you') or 'may you have goodness', of Celtic origin
- ‡ from an earlier form of Italian *grà* ('I owe to you')
- § from Manx *gaa* ('may ... be') + *mea* ('good') + *eyd* ('at you', see and compare †, of Celtic origin)
- ¶ from Scottish Gaelic *spasadh* ('blessings') + *leat* ('with you'), of Celtic origin
- ‡ from Old Turkic *say* ('praise') + *olun* ('to'), variations widely used in Turkish and Azei as well

Any doubts?



**Any truth is better
than indefinite doubt.**

Arthur Conan Doyle

quote fancy

Any doubts?



Whenever there is any
doubt, there is no doubt.

Robert De Niro

 quote fancy

We have to learn many things about BSM in the future!

O friend, there is injustice and loyal in your love ...

There is also chance of death and life ...

There is also loss and profit ...

I am not daring to meet you, my heart becomes comfortless ...

Moving with difficulty in your pain, there is also remedy and happiness ...

Wondering how to hide this essence within me ...

The beauty is obvious, also visible and clear ...

Only the beloved of the lover is the target ...

You are the treatment of love, there is also healing and remedy ...

Wherever you live, in the ancient world, o clear foundation ...

There is also a glimpse of hope!

... Love for SM