

# **Hadron structure in soft-wall AdS/QCD at zero and finite temperature**

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# Plan of the Talk

- Introduction to AdS/QCD = Holographic QCD - novel approach based on correspondence between 5D theories including gravity and gauge 4D theories living on the boundary of AdS space.
- Applications:
  - Mass spectrum of hadrons
  - Electromagnetic structure of nucleon and Roper resonance  $N(1440)$
  - Tetraquarks
  - Extension to finite temperature
- Summary

# Introduction

- 1993 't Hooft Holographic Principle

Information about string theory contained in some region of space can be represented as “Hologram” (theory which lives on the boundary of that region)

- 1997 Maldacena AdS/CFT correspondence

Motivated by study of black holes and D-branes in string theories in  $\text{AdS}_5$

- AdS/CFT correspondence

Dynamics of the superstring theory in  $\text{AdS}_{d+1}$  background is encoded in  $d$  conformal field theory living on the AdS boundary.

- Parameter correspondence (matching partition functions)

Strings  $g_s$  – coupling,  $l_s$  – length,  $R$  – radius of AdS space

SU(N) YM  $g_{YM}$  – coupling, 't Hooft coupling  $\lambda = g_{YM}^2 N$

$$2\pi g_s = g_{YM}^2, \quad \frac{R^4}{l_s^4} = 2 g_{YM}^2 N = 2\lambda$$

- 't Hooft limit (large  $N$  at  $\lambda$  fixed)  $g_{YM}^2 = \lambda/N \ll 1$
- Strong coupling limit  $\lambda \gg 1$  means  $l_s \ll R$  small curvature  $\mathcal{R} = -20/R^2$

Supergravity limit (closed strings shrink to point-like particles)

- AdS/CFT  $\rightarrow$  ADS/QCD — breaking of conformal symmetry and confinement

# Introduction

- AdS/QCD  $\equiv$  Holographic QCD (HQCD) – approximation to QCD:  
attempt to model Hadronic Physics in terms of fields living in extra dimensions –  
**anti-de Sitter (AdS) space**
- HQCD models reproduce main features of QCD at low and high energies:  
chiral symmetry, confinement, power scaling of hadron form factors
- Symmetry arguments: Conformal group acting in boundary theory isomorphic to  
 $SO(4, 2)$  – the isometry group of **AdS<sub>5</sub>** space

# Introduction

- Conformal group contains 15 generators:

10 Poincaré (4 translations  $P_\mu$ , 6 Lorentz transformations  $M_{\mu\nu}$ ),  
5 conformal (4 conformal boosts  $K_\mu$ , 1 dilatation  $D$ ):

$M_{\mu\nu} = i(x_\mu \partial_\nu - x_\nu \partial_\mu)$	rotational symmetry
$D = i(x \partial)$	energy
$P_\mu = i\partial_\mu$	raising energy
$K_\mu = 2ix_\mu(x \partial) - ix^2\partial_\mu$	lowering energy

- Isomorphic to  $SO(4, 2)$  – the isometry group of  $\text{AdS}_5$  space
- Fields in  $\text{AdS}_5$  are classified by unitary, irreducible representations of  $SO(4, 2)$
- $SO(4, 2)$  is decomposed with respect to  $SO(4) \times SO(2)$   
 $SO(4)$  is isomorphic to  $SU(2) \times SU(2)$ : use spins  $J_1$  and  $J_2$  for classification
- Irreducible representations  $D(E_0, J_1, J_2)$  two spins  $J_1, J_2$  and energy  $E_0$   
(corresponds to  $\Delta$  – conformal dimension of operators in CFT)

# Introduction

- Scalar  $D(E_0, 0, 0)$

- Vector  $D\left(E_0, \frac{1}{2}, \frac{1}{2}\right)$

- Fermions of spin  $J = 1/2$

$$D\left(E_0, 0, \frac{1}{2}\right) \oplus D\left(E_0, \frac{1}{2}, 0\right)$$

- Fermions of spin  $J = 3/2$

$$D\left(E_0, 1, \frac{1}{2}\right) \oplus D\left(E_0, \frac{1}{2}, 1\right)$$

- Spin  $J$  totally symmetric tensor with  $J \geq 2$

$$D\left(E_0, \frac{J}{2}, \frac{J}{2}\right)$$

- Spin  $J$  totally symmetric spinor-tensor with  $J \geq 5/2$

$$D\left(E_0, \frac{J+1/2}{2}, \frac{J-1/2}{2}\right) \oplus D\left(E_0, \frac{J-1/2}{2}, \frac{J+1/2}{2}\right)$$

# Introduction

- **Top-down approaches** Low-energy approximation of string theory trying to find a gravitational background with features similar to QCD (e.g. Sakai-Sugimoto model)
- **Bottom-up approaches** More phenomenological use the features of QCD to construct 5d dual theory including gravity on AdS space
- **Towards to QCD:**
  - Break conformal invariance and generate mass gap
  - Tower of normalized bulk fields (Kaluza-Klein modes)  $\leftrightarrow$  Hadron wave functions
  - Spectrum of Kaluza-Klein modes  $\leftrightarrow$  Hadrons spectrum
- **Hard-wall:**

AdS geometry is cutted by two branes **UV** ( $z = \epsilon \rightarrow 0$ ) and **IR** ( $z = z_{\text{IR}}$ )  
Analogue of quark bag model, linear dependence on  $J(L)$  of hadron masses
- **Soft-wall:**

Soft cutoff of AdS space by dilaton field  $e^{-\varphi(z)}$   
Analytical solution of EOM, Regge behavior of hadron masses  $M^2 \sim J(L)$ ,  
correct power scaling of hadronic form factors at large  $Q^2$

# Introduction

- AdS metric Poincaré form

$$ds^2 = g_{MN}(z) dx^M dx^N = \frac{R^2}{z^2} (dx_\mu dx^\mu - dz^2) \quad R - \text{AdS radius}$$

- Metric Tensor  $g_{MN}(z) = \epsilon_M^a(z) \epsilon_N^b(z) \eta_{ab}$

- Vielbein  $\epsilon_M^a(z) = \frac{R}{z} \delta_M^a$  (relates AdS and Lorentz metric)

- Manifestly scale-invariant  $x \rightarrow \lambda x, z \rightarrow \lambda z.$

- $z$  – extra dimensional (holographic) coordinate;  
 $z = 0$  is UV boundary,  $z = \infty$  is IR boundary

- Five Dimensions: L = Length, W = Width, H = Height, T = Time, S = Scale

# Introduction

- Action for scalar field

$$S_\Phi = \frac{1}{2} \int d^d x dz \sqrt{g} e^{-\varphi(z)} \left( \partial_M \Phi(x, z) \partial^M \Phi(x, z) - m^2 \Phi^2(x, z) \right)$$

- Dilaton field  $\varphi(z) = \kappa^2 z^2$
- $g = |\det g_{MN}|$
- $m$  – 5d mass,  $m^2 R^2 = \Delta(\Delta - 4)$ ,  $\Delta$  = 3 conformal dimension
- Kaluza-Klein (KK) expansion  $\Phi(x, z) = \sum_n \phi_n(x) \Phi_n(z)$
- Tower of KK modes  $\phi_n(x)$  dual to 4-dimensional fields describing hadrons
- Bulk profiles  $\Phi_n(z)$  dual to hadronic wave functions

# Introduction

- Use  $-\partial_\mu \partial^\mu \phi_n(x) = M_n^2 \phi_n(x)$
- Substitute  $\Phi_n(z) = \left(\frac{R}{z}\right)^{1-d} \phi_n(z)$
- Identify  $\Delta = \tau = N + L$  (here  $N = 2$  – number of partons in meson)

Hete  $\tau$  is twist = Canonical dimension - Sum of spins

Examples: mesons  $\tau = 2 \times 3/2 - 2 \times 1/2 = 2$

baryons  $\tau = 3 \times 3/2 - 3 \times 1/2 = 3$

$$\left[ -\frac{d^2}{dz^2} + \frac{4L^2 - 1}{4z^2} + \kappa^4 z^2 - 2\kappa^2 \right] \phi_n(z) = M_n^2 \phi_n(z)$$

- Solutions:  
$$\phi_{nL}(z) = \phi_{n,\tau-2}(z) = \sqrt{\frac{2\Gamma(n+1)}{\Gamma(n+L+1)}} \kappa^{L+1} z^{L+1/2} e^{-\kappa^2 z^2/2} L_n^L(\kappa^2 z^2)$$
- $M_{nL}^2 = 4\kappa^2 \left( n + \frac{L}{2} \right) = 4\kappa^2 \left( n + \frac{\tau}{2} - 1 \right)$
- Massless pion  $M_\pi^2 = 0$  for  $n = L = 0$  Brodsky, Téramond

# Introduction

- “Positive dilaton”: Brodsky, Téramond

$$S_{\Phi}^+ = \frac{1}{2} \int d^d x dz \sqrt{g} e^{\varphi(z)} \left[ \partial_M \Phi_+ \partial^M \Phi_+ - m^2 \Phi_+^2 \right]$$

- “Negative dilaton”: Gutsche, Lyubovitskij, Schmidt, Vega PRD 85 (2012) 076003

$$S_{\Phi}^- = \frac{1}{2} \int d^d x dz \sqrt{g} e^{-\varphi(z)} \left[ \partial_M \Phi_- \partial^M \Phi_- - (m^2 + U(z)) \Phi_-^2 \right]$$

Potential

$$U(z) = \frac{z^2}{R^2} \left( \varphi''(z) + \frac{1-d}{z} \varphi'(z) \right)$$

- “No-wall”

$$S_{\Phi} = \frac{1}{2} \int d^d x dz \sqrt{g} \left[ \partial_M \Phi \partial^M \Phi - (m^2 + V(z)) \Phi^2 \right]$$

Potential

$$V(z) = \frac{z^2}{R^2} \left( \frac{1}{2} \varphi''(z) + \frac{1}{4} (\varphi'(z))^2 + \frac{1-d}{2z} \varphi'(z) \right)$$

- All 3 actions are equivalent upon field redefinition  $\Phi_{\pm} = e^{\mp\varphi(z)} \Phi_{\mp} = e^{\mp\varphi(z)/2} \Phi$

# Introduction

- Extension to AdS fermions (baryons)

$$S_\psi = \int d^d x dz \sqrt{g} \bar{\Psi}(x, z) \left( \not{\mathcal{D}} - \mu - \varphi(z)/R \right) \Psi(x, z)$$

- Field decomposition (left/right) and KK expansion

$$\Psi(x, z) = \Psi_L(x, z) + \Psi_R(x, z) \quad \Psi_{L/R} = \frac{1 \mp \gamma^5}{2} \Psi$$

$$\Psi_{L/R}(x, z) = \sum_n \Psi_{L/R}^n(x) F_{L/R}^n(z)$$

- EOM

$$\left[ -\partial_z^2 + \kappa^4 z^2 + 2\kappa^2 \left( \mu R \mp \frac{1}{2} \right) + \frac{\mu R(\mu R \pm 1)}{z^2} \right] F_{L/R}^n(z) = M_n^2 F_{L/R}^n(z)$$

Solutions (for  $d = 4$  and  $\mu R = L + 3/2$ )

- Bulk profiles

$$F_L^n(z) = \sqrt{\frac{2\Gamma(n+1)}{\Gamma(n+L+3)}} \kappa^{L+3} z^{L+9/2} e^{-\kappa^2 z^2/2} L_n^{L+2}(\kappa^2 z^2)$$

$$F_R^n(z) = \sqrt{\frac{2\Gamma(n+1)}{\Gamma(n+L+2)}} \kappa^{L+2} z^{L+7/2} e^{-\kappa^2 z^2/2} L_n^{L+1}(\kappa^2 z^2)$$

- Mass spectrum:  $M_{nL}^2 = 4\kappa^2(n + L + 2)$

# Introduction

- Extension to higher-spin AdS boson (mesons)

Vasilev, Buchbinder, Metzaev, Pashnev, ...

Fields  $\Phi \rightarrow \Phi_{M_1 M_2 \cdots M_J}$

5d mass  $m^2 R^2 \rightarrow m_J^2 R^2 = (\Delta - J)(\Delta + J - 4)$

Dilaton potential

$$U_J(z) = \frac{z^2}{R^2} \left( \varphi''(z) + \frac{1+2J-d}{z} \varphi'(z) \right)$$

## Solutions

- $\phi_{nL}(z) = \sqrt{\frac{2\Gamma(n+1)}{\Gamma(n+L)}} \kappa^{L+1} z^{L+1/2} e^{-\kappa^2 z^2/2} L_n^L(\kappa^2 z^2)$
- $M_{nLJ}^2 = 4\kappa^2 \left( n + \frac{L+J}{2} \right) \rightarrow 4\kappa^2 (n+J)$  at large  $J$

# Introduction

- Scattering problem for AdS field gives information about propagation of external field from  $z$  to the boundary  $z = 0$  — bulk-to-boundary propagator  $\Phi_{\text{ext}}(q, z)$   
[Fourier-transform of AdS field  $\Phi_{\text{ext}}(x, z)$ ]:

$$\Phi_{\text{ext}}(q, z) = \int d^d x e^{-iqx} \Phi_{\text{ext}}(x, z)$$

- Vector field as example

$$\partial_z \left( \frac{e^{-\varphi(z)}}{z} \partial_z V(q, z) \right) + q^2 \frac{e^{-\varphi(z)}}{z} V(q, z) = 0.$$

$$V(Q, z) = \Gamma\left(1 + \frac{Q^2}{4\kappa^2}\right) U\left(\frac{Q^2}{4\kappa^2}, 0, \kappa^2 z^2\right)$$

Consistent with GI, fulfills UV and IR boundary conditions :

$$V(Q, 0) = 1, \quad V(Q, \infty) = 0$$

- Hadron form factors

$$F_\tau(Q^2) = \langle \phi_\tau | \hat{V}(Q) | \phi_\tau \rangle = \int_0^\infty dz \phi_\tau^2(z) V(Q, z) = \frac{\Gamma(\tau) \Gamma(a+1)}{\Gamma(a+\tau)}$$

is implemented by a nontrivial dependence of AdS fields on 5-th coordinate

# Introduction

- Power scaling at large  $Q^2$

$$F_\tau(Q^2) \sim \frac{1}{(Q^2)^{\tau-1}}$$

Quark counting rules: Matveev-Muradyan-Tavhelidze-Brodsky-Farrar 1973

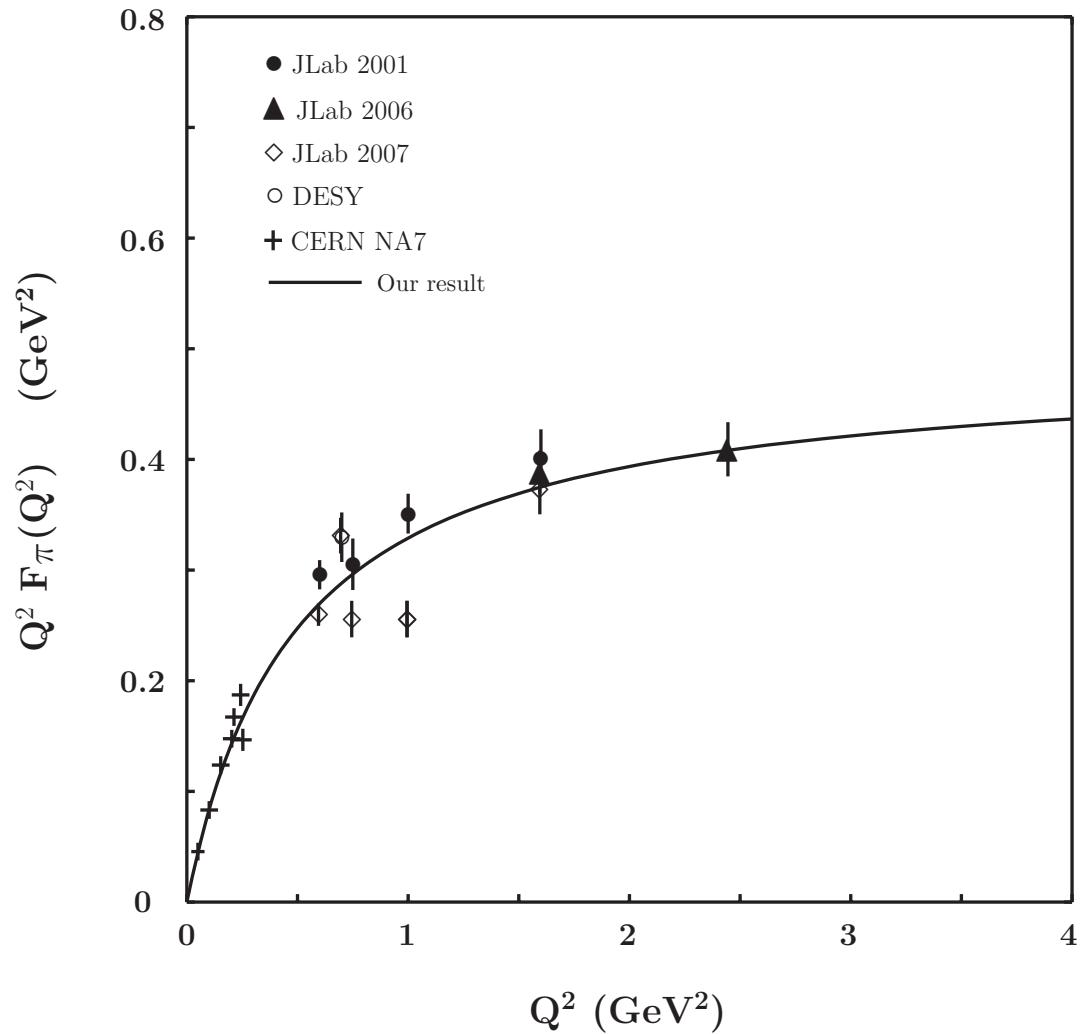
$$\text{Pion} : \frac{1}{Q^2}$$

$$\text{Nucleon(Dirac)} : \frac{1}{Q^4}$$

$$\text{Nucleon(Pauli)} : \frac{1}{Q^6}$$

$$\text{Deuteron(Charge)} : \frac{1}{Q^{10}}$$

# Mesons: pion form factor



# LFWFs motivated by holographic QCD

- Matching matrix elements (e.g. form factors) in HQCD and LF QCD
- Drell-Yan-West formula

$$F_\tau(Q^2) = \int_0^1 dx \int \frac{d^2 \mathbf{k}_\perp}{16\pi^3} \psi_\tau^\dagger(x, \mathbf{k}'_\perp) \psi_\tau(x, \mathbf{k}_\perp),$$

where  $\psi(x, \mathbf{k}_\perp) \equiv \psi(x, \mathbf{k}_\perp; \mu_0)$ ,  $\mathbf{k}'_\perp = \mathbf{k}_\perp + (1-x)\mathbf{q}_\perp$ , and  $Q^2 = \mathbf{q}_\perp^2$

- HQCD

$$F_\tau(Q^2) = \int_0^\infty dz V(Q, z) \varphi_\tau^2(z) = \frac{\Gamma(\frac{Q^2}{4\kappa^2} + 1) \Gamma(\tau)}{\Gamma(\frac{Q^2}{4\kappa^2} + \tau)}.$$

- Result for effective LFWF at the initial scale  $\mu_0$

$$\psi_\tau(x, \mathbf{k}_\perp) = \sqrt{\tau - 1} \frac{4\pi}{\kappa} \sqrt{\log(1/x)} (1-x)^{\frac{\tau-4}{2}} \exp\left[-\frac{\mathbf{k}_\perp^2}{2\kappa^2} \frac{\log(1/x)}{(1-x)^2}\right]$$

# Mesons: Light-Front Wave Function

- Mesonic WF longitudinal part and quark masses

$$\phi_{nJ}(z, x, m_1, m_2) = \phi_{nL}(z) f(x, m_1, m_2)$$

- Modified meson mass formula

$$M_{nJ}^2 = 4\kappa^2 \left( n + \frac{L+J}{2} \right) + \int_0^1 dx \left( \frac{m_1^2}{x} + \frac{m_2^2}{1-x} \right) f^2(x, m_1, m_2)$$

- Leptonic decay constants  $P^- \rightarrow \ell^- \bar{\nu}_\ell$

$$f_M = \kappa \frac{\sqrt{6}}{\pi} \int_0^1 dx \sqrt{x(1-x)} f(x, m_1, m_2)$$

- Find  $f(x, m_1, m_2)$  to fulfill the following constraints

- In sector of light quarks (consistency with ChPT):

$$\text{Gell-Mann-Oakes-Renner (GMOR)} \quad M_\pi^2 = 2\hat{m} B$$

$$\text{Gell-Mann-Okubo (GMO)} \quad 4M_K^2 = M_\pi^2 + 3M_\eta^2$$

# Mesons: Light-Front Wave Function

- In sector of heavy quarks (consistency with HQET)
- Leptonic decay constants

$$f_{Q\bar{q}} \sim 1/\sqrt{m_Q} \quad \text{heavy-light mesons}$$

$$f_{Q\bar{Q}} \sim \sqrt{m_Q} \quad \text{heavy quarkonia}$$

$$f_{c\bar{b}} \sim m_c/\sqrt{m_b} \quad \text{at } m_c \ll m_b$$

- Mass spectrum  
Expansion

$$M_{Q\bar{q}} = m_Q + \bar{\Lambda} + \mathcal{O}(1/m_Q)$$

$$M_{Q\bar{Q}} = 2m_Q + E + \mathcal{O}(1/m_Q)$$

Splitting

$$M_{Q\bar{q}}^V - M_{Q\bar{q}}^P \sim \frac{1}{m_Q}$$

# Light Mesons

- Following 't Hooft NPB 75 (1974) 461

$$f(x, m_1, m_2) = N x^{\alpha_1} (1 - x)^{\alpha_2}$$

where  $N$  is the normalization constant

$$1 = \int_0^1 dx f^2(x, m_1, m_2)$$

$\alpha_1, \alpha_2$  are parameters fixed in order to get consistency with QCD.

- Light quark sector  $\alpha_i = m_i/(2B)$

$$B = |\langle 0 | \bar{u}u | 0 \rangle| / F_\pi^2$$

is the quark condensate parameter

- Leptonic decay constants in chiral limit

$$f_\pi = f_K = f_\rho = 3f_\omega = \frac{3f_\phi}{\sqrt{2}} = \kappa \frac{\sqrt{6}}{8} .$$

# Heavy Mesons

- Heavy-light mesons  $\alpha_Q = \alpha = \mathcal{O}(1)$

$$\alpha_q = \frac{2\alpha_Q}{m_Q} \left( 1 + \frac{\bar{\Lambda}}{2m_Q} \right) - \frac{1}{2} .$$

Leds to

$$M_{Qq} = m_Q + \bar{\Lambda} + \mathcal{O}(1/m_Q)$$

$$M_{Q\bar{q}}^2 = 4\kappa^2 \left( n + \frac{L+J}{2} \right) + (m_Q + \bar{\Lambda})^2$$

$$f_{Q\bar{q}} = \frac{\kappa\sqrt{6}}{\pi} \frac{2\sqrt{\alpha}}{\alpha + \frac{3}{2}} \sqrt{\frac{\bar{\Lambda}}{m_Q}} \sim \sqrt{\frac{1}{m_Q}}$$

# Heavy Mesons

- Heavy Quarkonia

$$\alpha_{Q_i} = \frac{m_{Q_i}}{4E} \left( 1 - \frac{E}{2(m_{Q_1} + m_{Q_2})} \right) + \mathcal{O}\left(\frac{1}{m_{Q_i}}\right)$$

$$\kappa = \beta \left( \frac{\mu_{Q_1 Q_2}}{E} \right)^{1/4} \left( \frac{m_{Q_1} + m_{Q_2}}{E} \right)^{1/2},$$

where  $\beta = \mathcal{O}(1)$  and  $\mu_{Q_1 Q_2} = m_{Q_1} m_{Q_2} / (m_{Q_1} + m_{Q_2})$ .

$$M_{Q_1 \bar{Q}_2}^2 = 4\kappa^2 \left( n + \frac{L + J}{2} \right) + (m_{Q_1} + m_{Q_2} + E)^2$$

and

$$f_{Q \bar{Q}} \sim \sqrt{\frac{m_Q}{E}}.$$

# Mesons Masses: choice of parameters

- Dilaton parameter  $\kappa = 500 \text{ MeV}$
- Current quark masses

$$m_{u/d} = 7 \text{ MeV}, \quad m_s = 24m_{u/d} = 168 \text{ MeV}$$
$$m_c = 1.275 \text{ GeV}, \quad m_b = 4.18 \text{ GeV}$$

# Mesons Masses: Results

## Masses of light mesons

Meson	$n$	$L$	$S$	Mass [MeV]			
$\pi$	0,1,2,3	0	0	140	1010	1421	1738
$K$	0	0,1,2,3	0	495	1116	1498	1801
$\eta$	0,1,2,3	0	0	566	11494	1523	1822
$f_0[\bar{n}n]$	0,1,2,3	1	1	721	1233	1587	1876
$f_0[\bar{s}s]$	0,1,2,3	1	1	985	1404	1723	1993
$\rho(770)$	0,1,2,3	0	1	721	1233	1587	1876
$\omega(782)$	0,1,2,3	0	1	721	1233	1587	1876
$\phi(1020)$	0,1,2,3	0	1	985	1404	1723	1993
$a_1(1260)$	0,1,2,3	1	1	1010	1421	1738	2005

# Mesons Masses: Results

Masses of heavy-light mesons and heavy quarkonia

Meson	$J^P$	$n$	$L$	$S$	Mass [MeV]			
$D(1870)$	$0^-$	0	0,1,2,3	0	1870	2000	2121	2235
$D^*(2010)$	$1^-$	0	0,1,2,3	1	2000	2121	2235	2345
$D_s(1969)$	$0^-$	0	0,1,2,3	0	1970	2093	2209	2320
$D_s^*(2107)$	$1^-$	0	0,1,2,3	1	2093	2209	2320	2425
$B(5279)$	$0^-$	0	0,1,2,3	0	5280	5327	5374	5420
$B^*(5325)$	$1^-$	0	0,1,2,3	1	5336	5374	5420	5466
$B_s(5366)$	$0^-$	0	0,1,2,3	0	5370	5416	5462	5508
$B_s^*(5413)$	$1^-$	0	0,1,2,3	1	5416	5462	5508	5553

# Mesons Masses: Results

## Masses of heavy quarkonia

Meson	$J^P$	$n$	$L$	$S$	Mass [MeV]			
$\eta_c(2980)$	$0^-$	0,1,2,3	0	0	2975	3477	3729	3938
$\psi(3097)$	$1^-$	0,1,2,3	0	1	3097	3583	3828	4032
$\chi_{c0}(3415)$	$0^+$	0,1,2,3	1	1	3369	3628	3843	4038
$\chi_{c1}(3510)$	$1^+$	0,1,2,3	1	1	3477	3729	3938	4129
$\chi_{c2}(3555)$	$2^+$	0,1,2,3	1	1	3583	3828	4032	4219
$\eta_b(9390)$	$0^-$	0,1,2,3	0	0	9337	9931	10224	10471
$\Upsilon(9460)$	$1^-$	0,1,2,3	0	1	9460	10048	10338	10581
$\chi_{b0}(9860)$	$0^+$	0,1,2,3	1	1	9813	10110	10359	10591
$\chi_{b1}(9893)$	$1^+$	0,1,2,3	1	1	9931	10224	10471	10700
$\chi_{b2}(9912)$	$2^+$	0,1,2,3	1	1	10048	10338	10581	10808
$B_c(6277)$	$0^-$	0,1,2,3	0	0	6277	6719	6892	7025

# Electromagnetic structure of nucleons

Sachs Nucleon Form Factors in terms of Dirac and Pauli FF

$$G_E^N(Q^2) = F_1^N(Q^2) - \frac{Q^2}{4m_N^2} F_2^N(Q^2),$$

$$G_M^N(Q^2) = F_1^N(Q^2) + F_2^N(Q^2),$$

$$\langle r_E^2 \rangle^N = -6 \left. \frac{dG_E^N(Q^2)}{dQ^2} \right|_{Q^2=0},$$

$$\langle r_M^2 \rangle^N = -\frac{6}{G_M^N(0)} \left. \frac{dG_M^N(Q^2)}{dQ^2} \right|_{Q^2=0},$$

where  $G_M^N(0) \equiv \mu_N$  is the nucleon magnetic moment.

Decomposition of Dirac and Pauli FF in terms quark flavor form factors describing distribution of  $u$  and  $d$  in nucleons

$$F_i^{p(n)}(Q^2) = \frac{2}{3} F_i^{u(d)}(Q^2) - \frac{1}{3} F_i^{d(u)}(Q^2), \quad i = 1, 2.$$

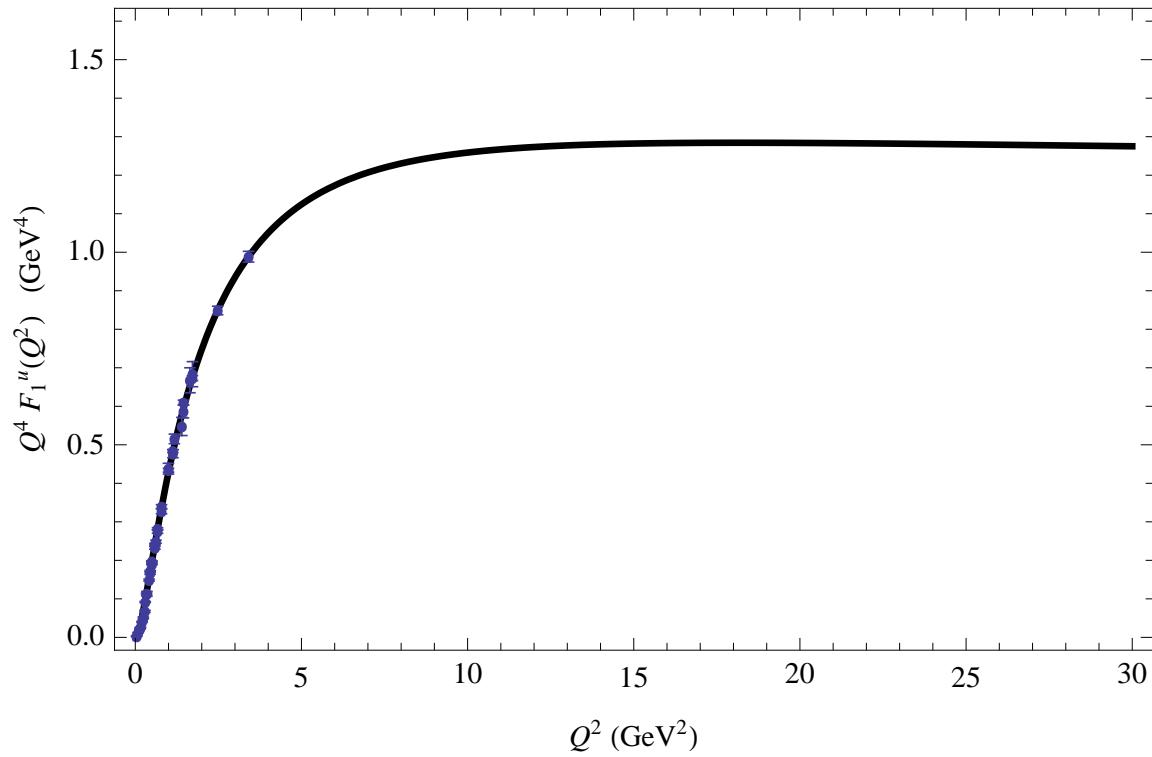
# Electromagnetic stucture of nucleons

Mass and electromagnetic properties of nucleons

Quantity	Our results	Data
$m_p$ (GeV)	0.93827	0.93827
$\mu_p$ (in n.m.)	2.793	2.793
$\mu_n$ (in n.m.)	-1.913	-1.913
$r_E^p$ (fm)	0.840	$0.8768 \pm 0.0069$
$\langle r_E^2 \rangle^n$ (fm $^2$ )	-0.117	$-0.1161 \pm 0.0022$
$r_M^p$ (fm)	0.785	$0.777 \pm 0.013 \pm 0.010$
$r_M^n$ (fm)	0.792	$0.862^{+0.009}_{-0.008}$
$r_A$ (fm)	0.667	$0.67 \pm 0.01$

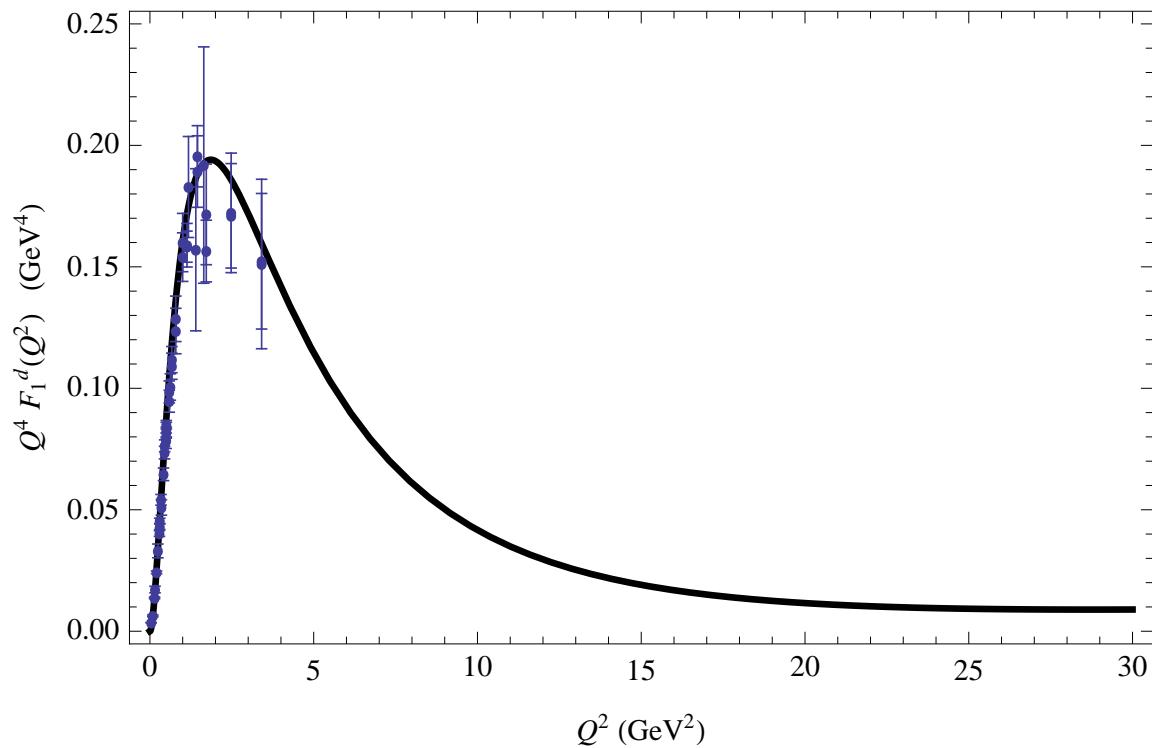
# Electromagnetic stucture of nucleons and Roper (1440)

Plot  $Q^4 F_1^u(Q^2)$



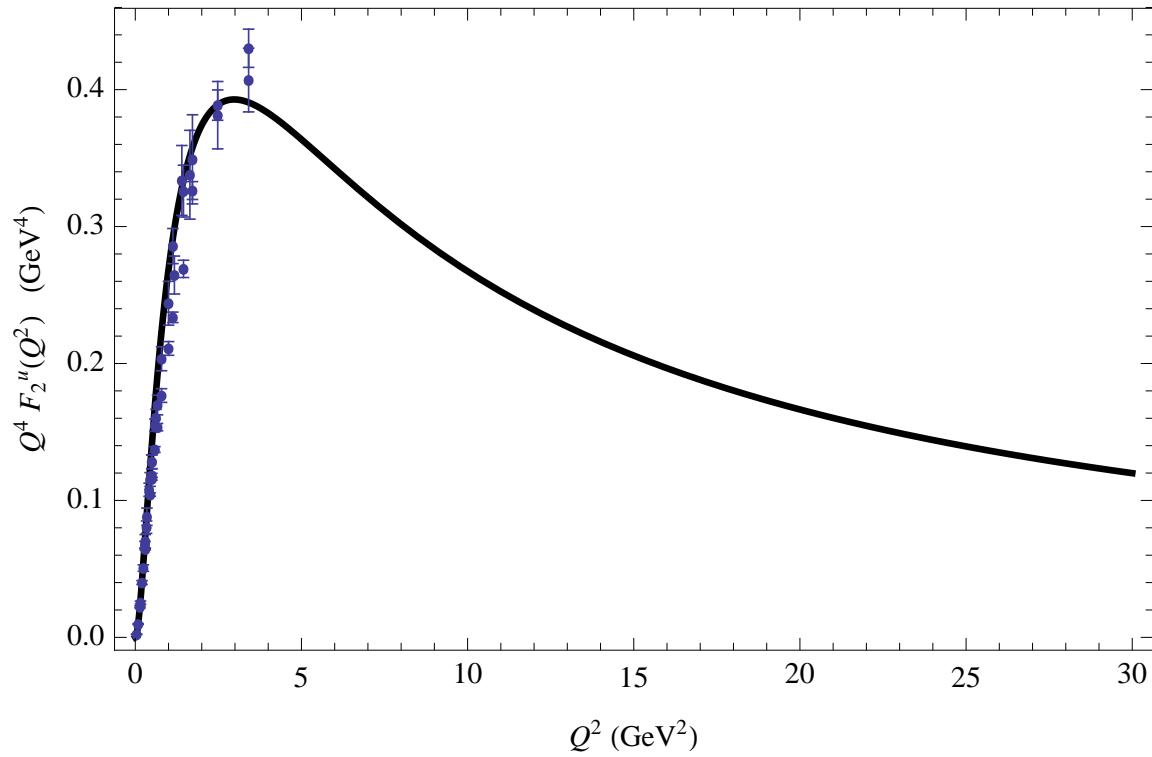
# Electromagnetic stucture of nucleons and Roper (1440)

Plot  $Q^4 F_1^d(Q^2)$



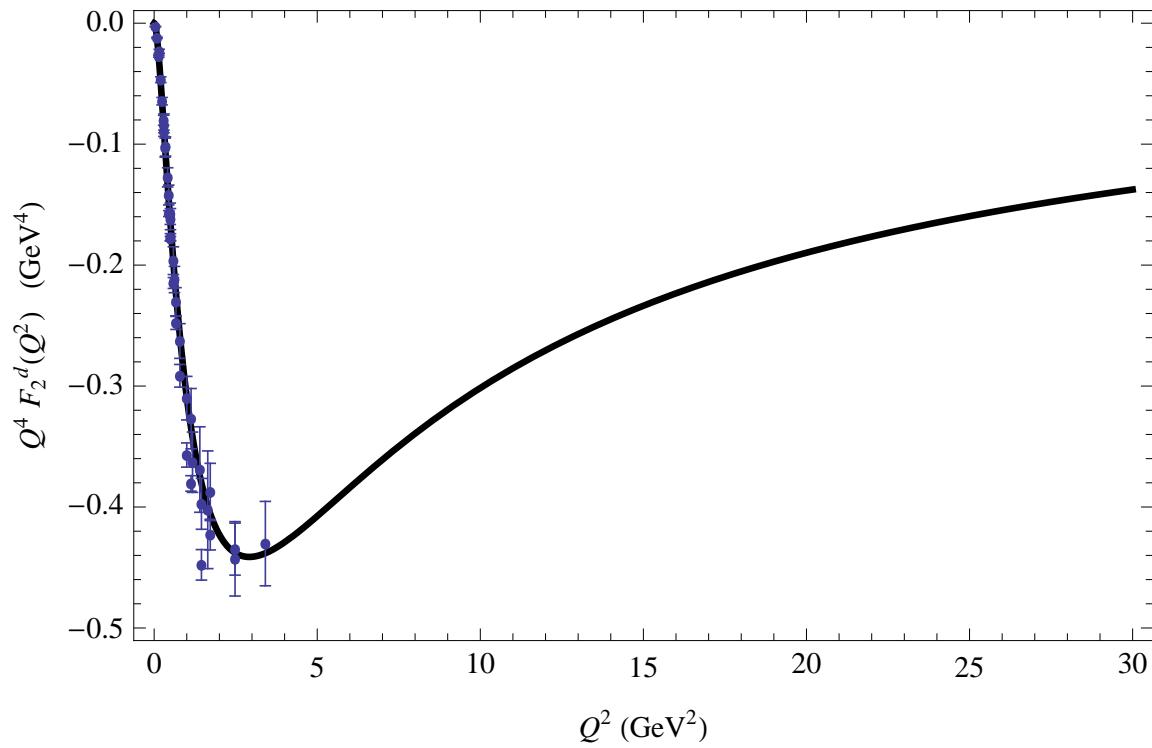
# Electromagnetic stucture of nucleons and Roper (1440)

Plot  $Q^4 F_2^u(Q^2)$

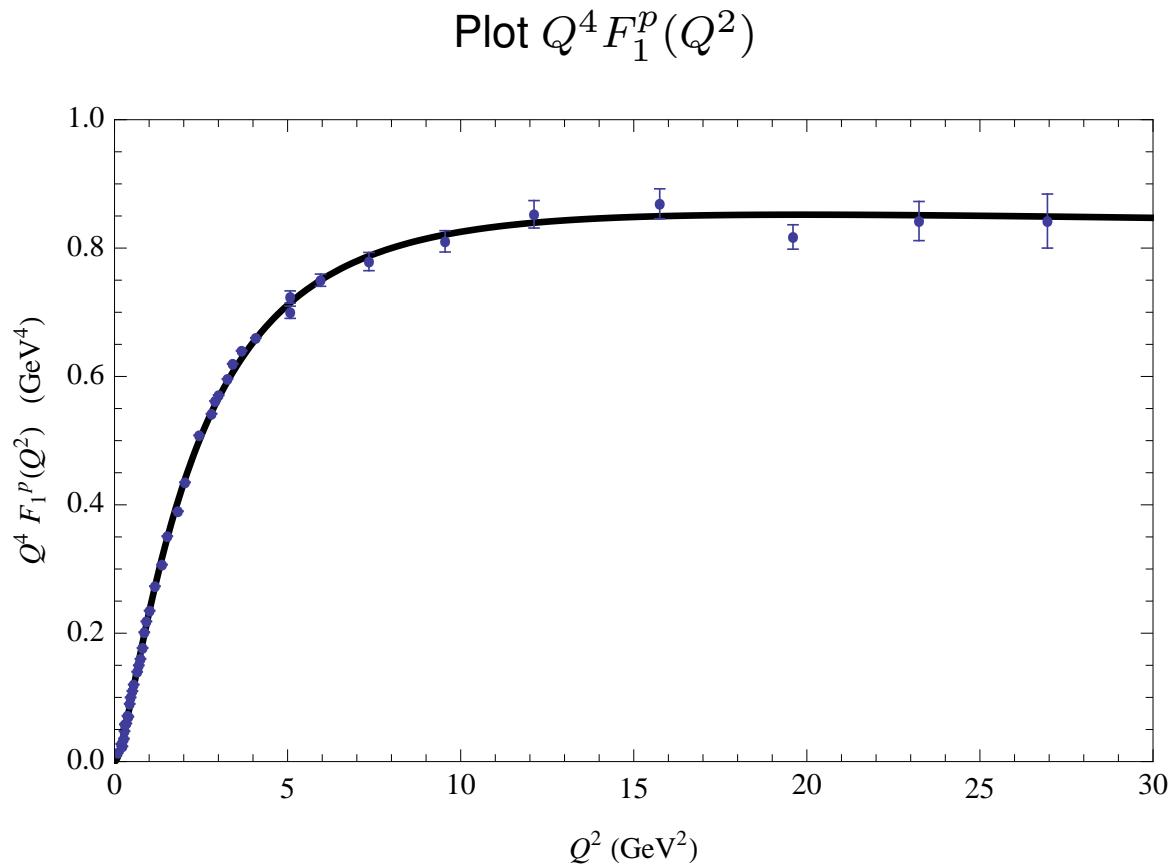


# Electromagnetic stucture of nucleons and Roper (1440)

Plot  $Q^4 F_2^d(Q^2)$

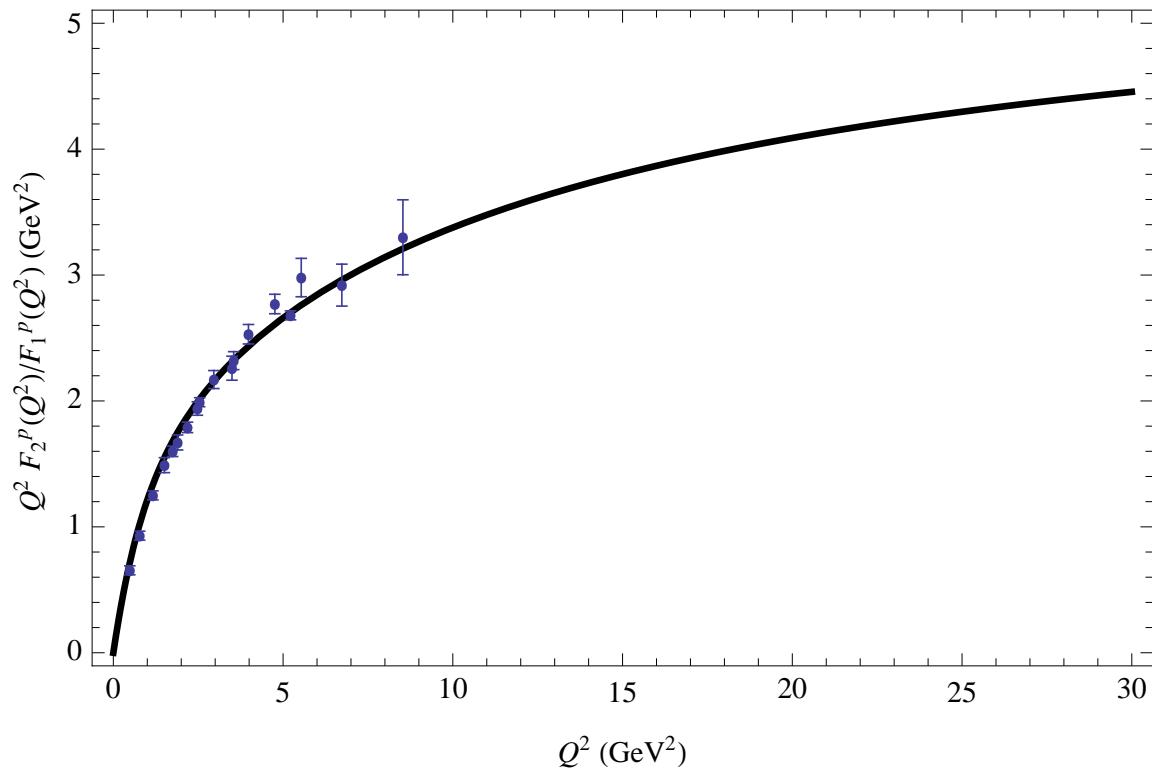


# Electromagnetic stucture of nucleons and Roper (1440)



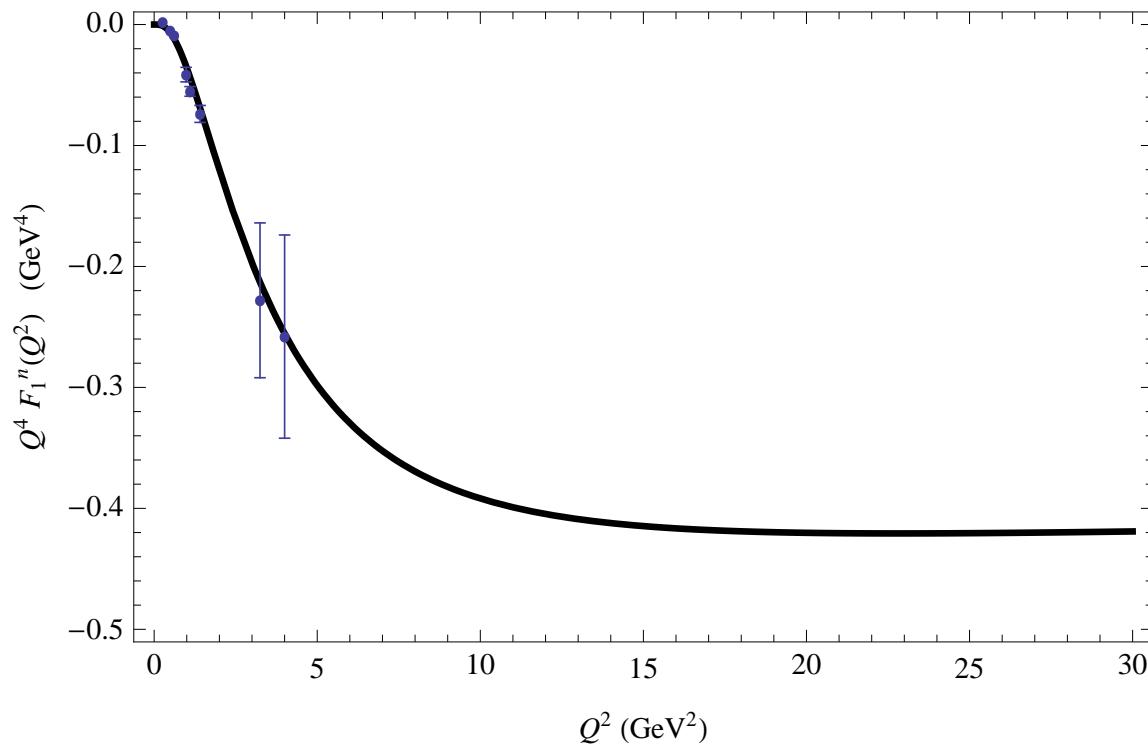
# Electromagnetic stucture of nucleons and Roper (1440)

Plot  $Q^2 F_2^p(Q^2)/F_1^p(Q^2)$

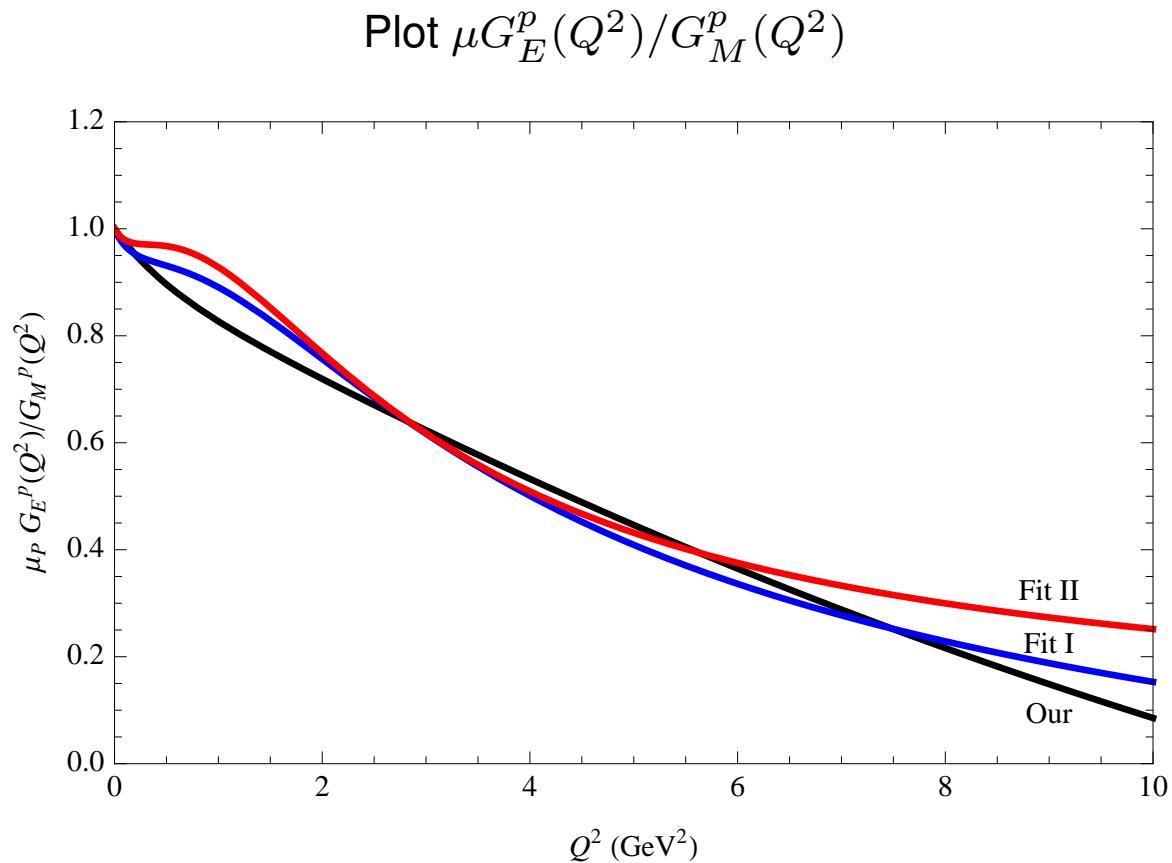


# Electromagnetic stucture of nucleons and Roper (1440)

Plot  $Q^4 F_1^n(Q^2)$

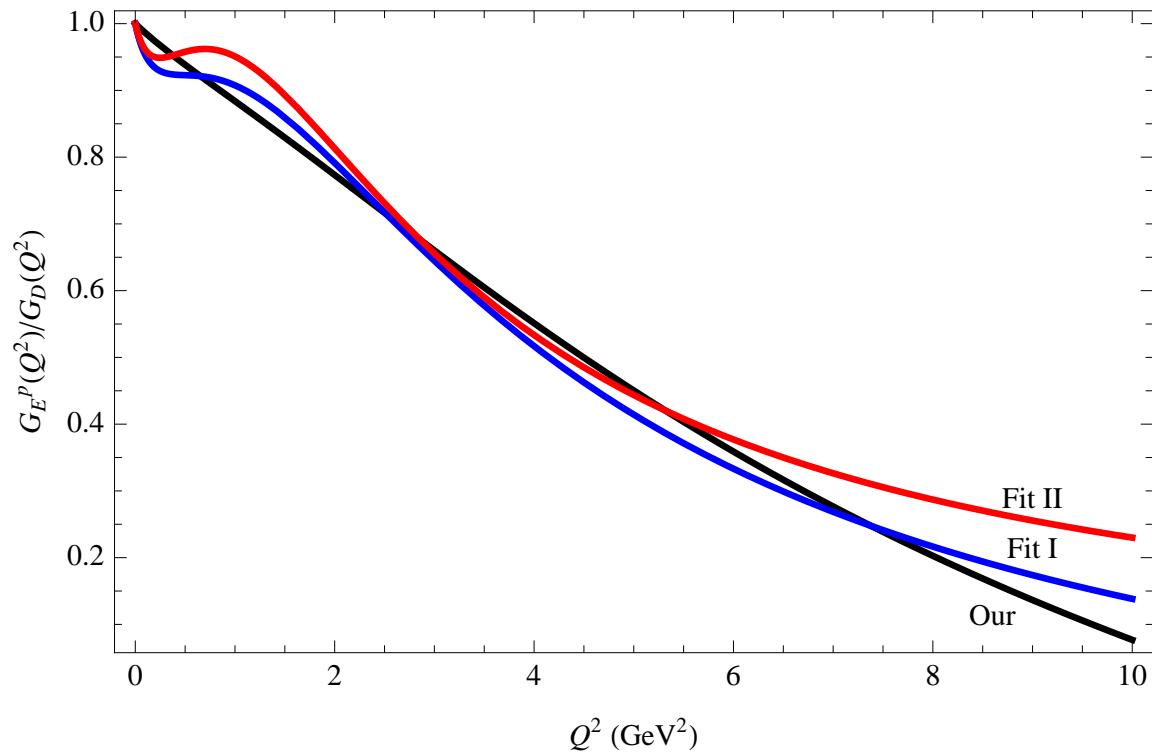


# Electromagnetic stucture of nucleons and Roper (1440)



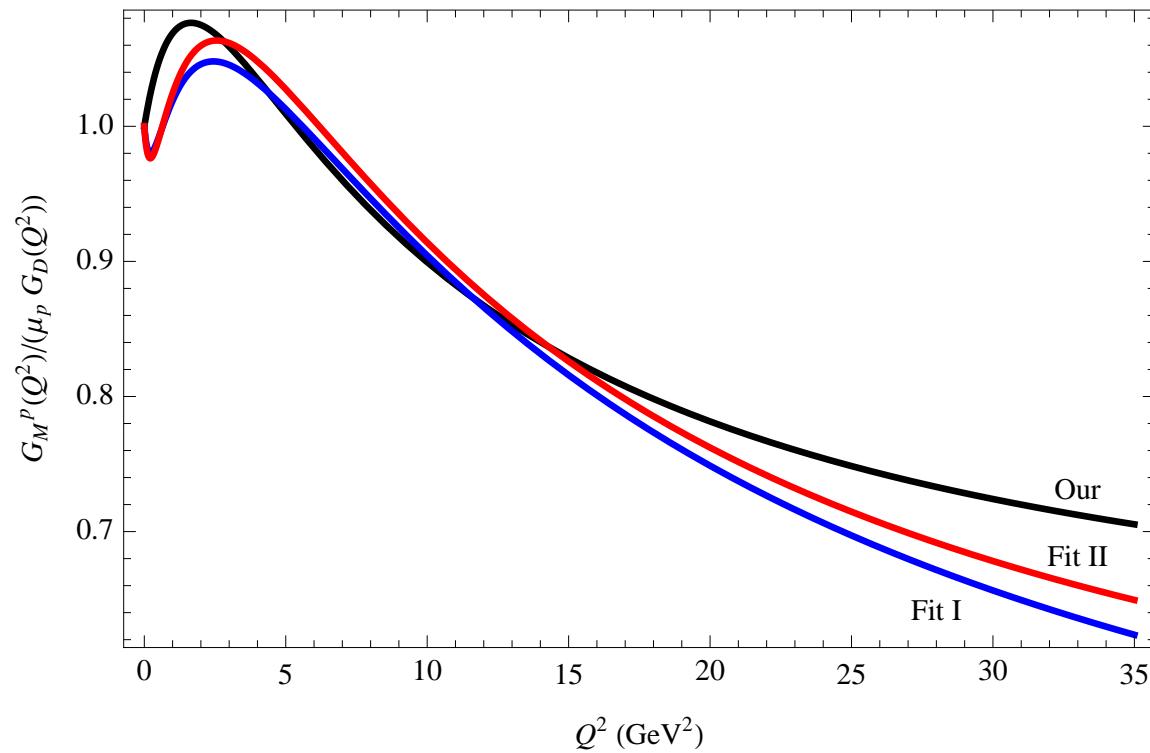
# Electromagnetic stucture of nucleons and Roper (1440)

Plot  $G_E^p(Q^2)/G_D(Q^2)$ , where  $G_D(Q^2) = 1/(1 + Q^2/\Lambda^2)^2$ ,  $\Lambda = 0.84 \text{ GeV}$ .

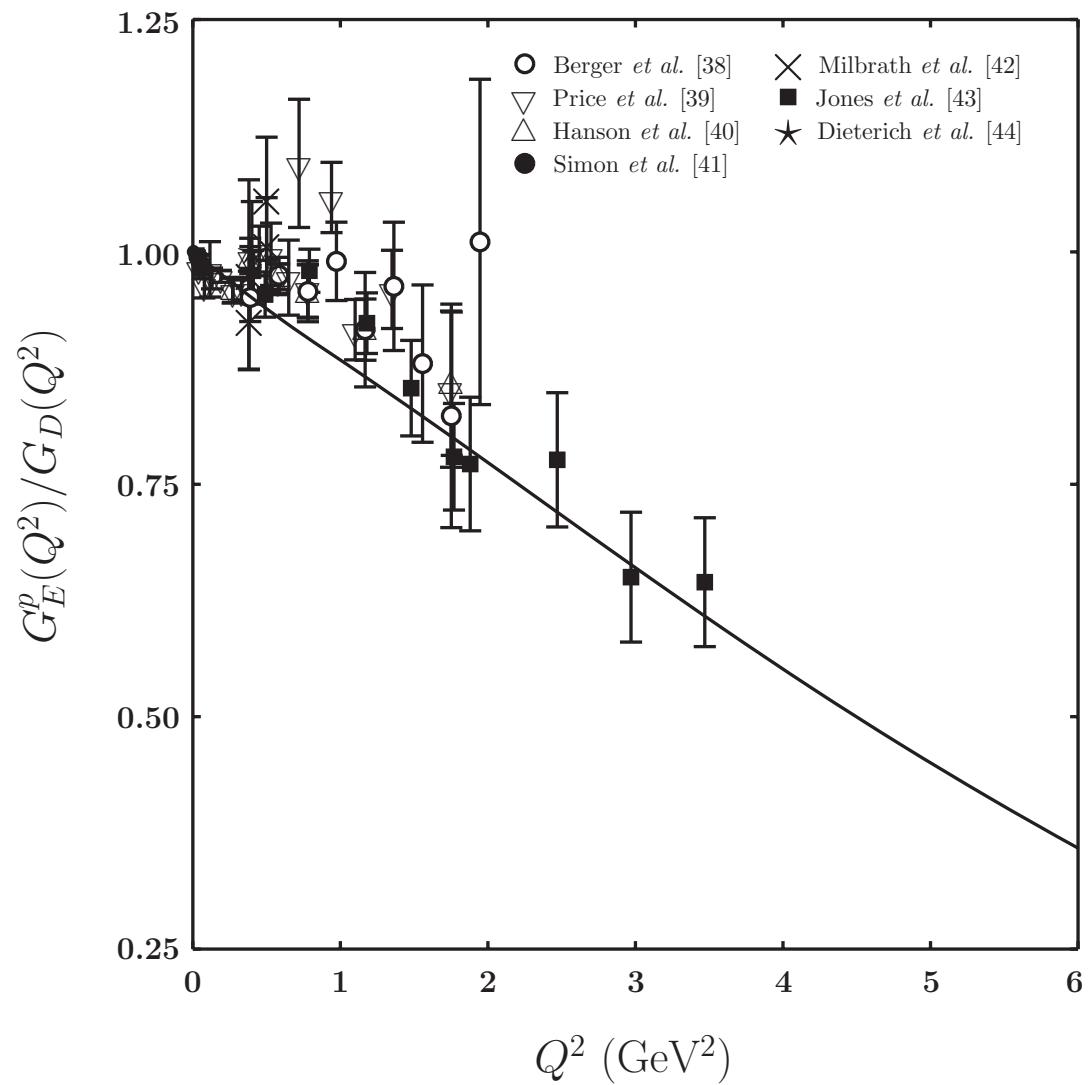


# Electromagnetic stucture of nucleons and Roper (1440)

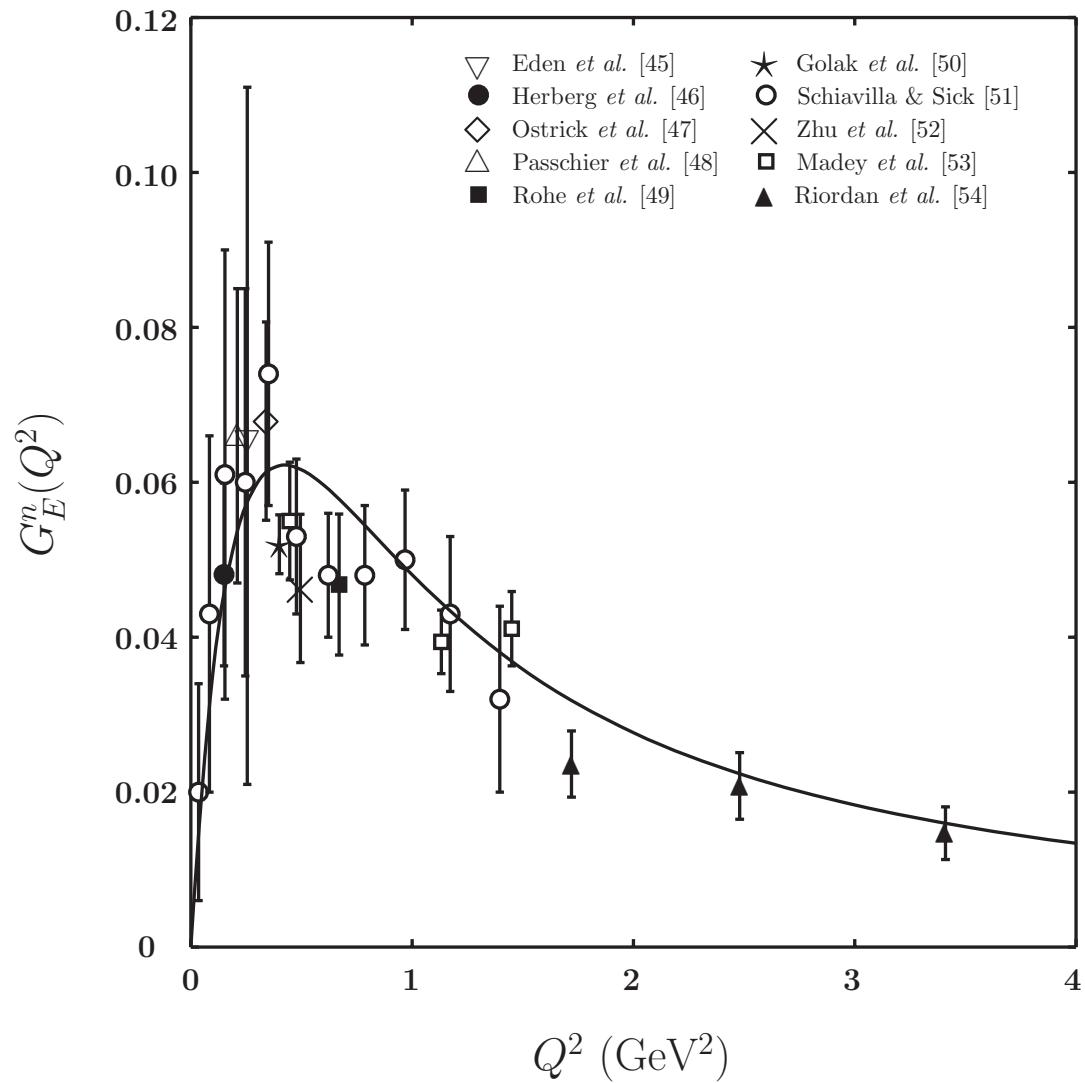
Plot  $G_M^p(Q^2)/G_D(Q^2)$ , where  $G_D(Q^2) = 1/(1 + Q^2/\Lambda^2)^2$ ,  $\Lambda = 0.84 \text{ GeV}$ .



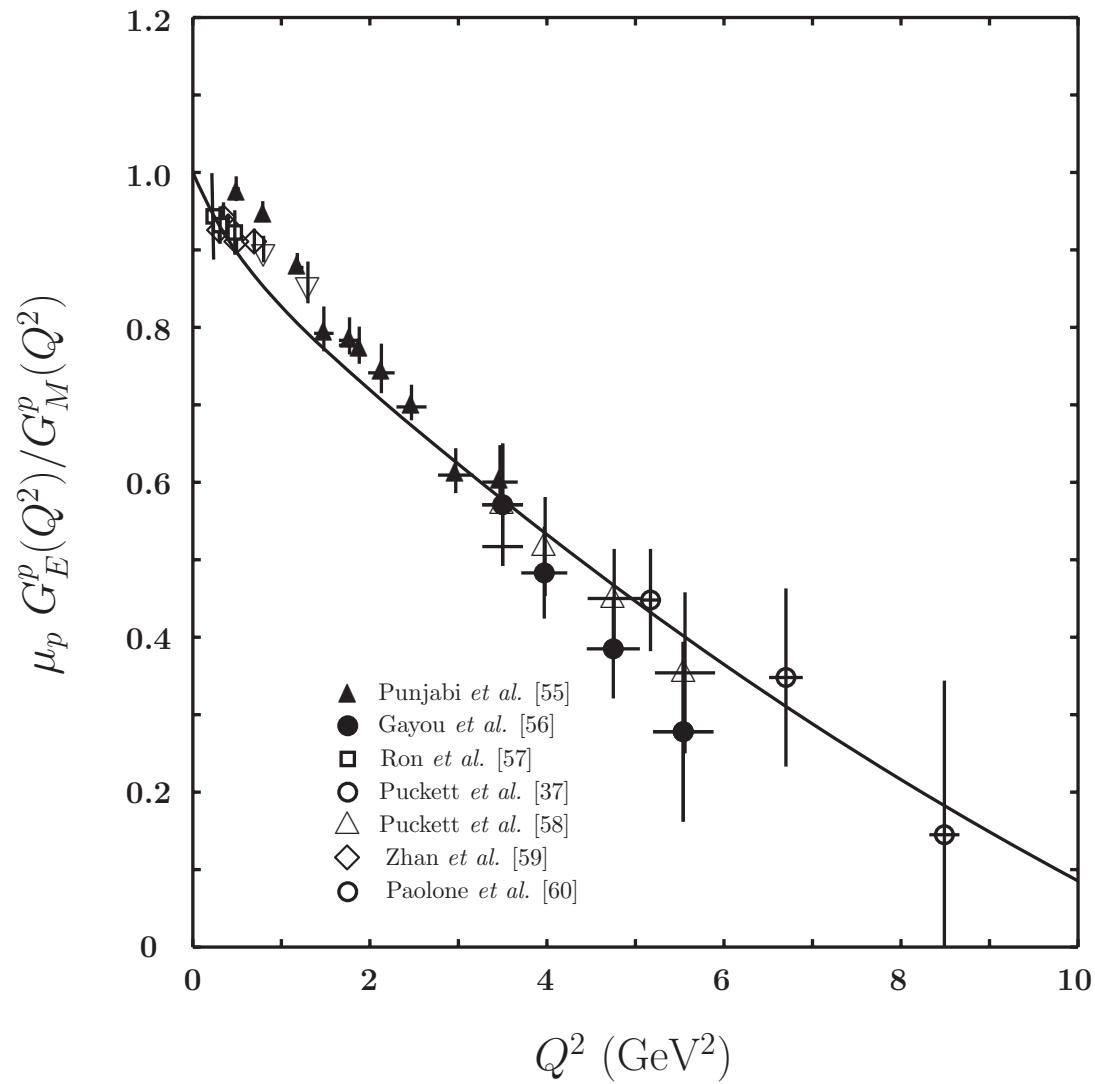
# Electromagnetic stucture of nucleons and Roper (1440)



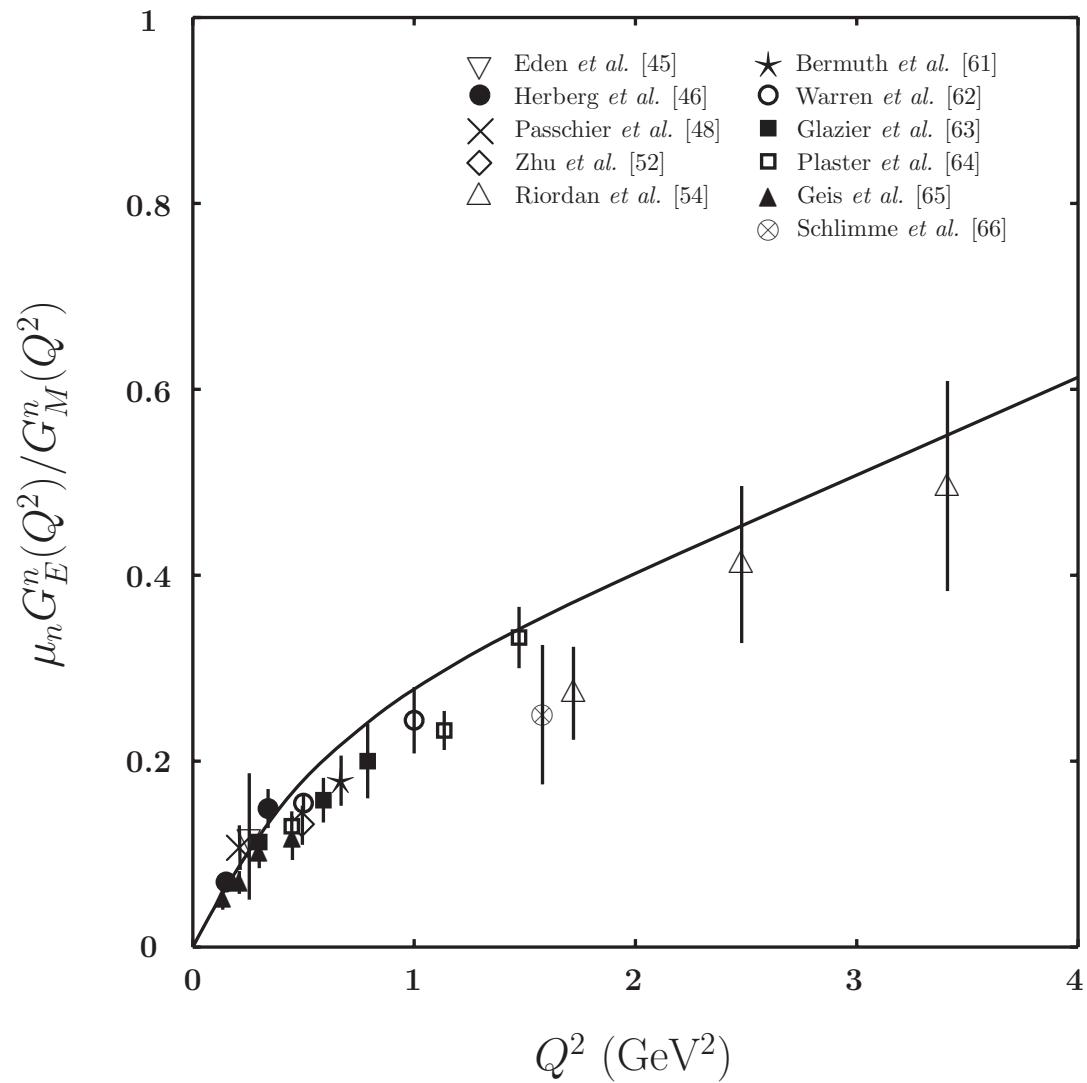
# Electromagnetic stucture of nucleons and Roper (1440)



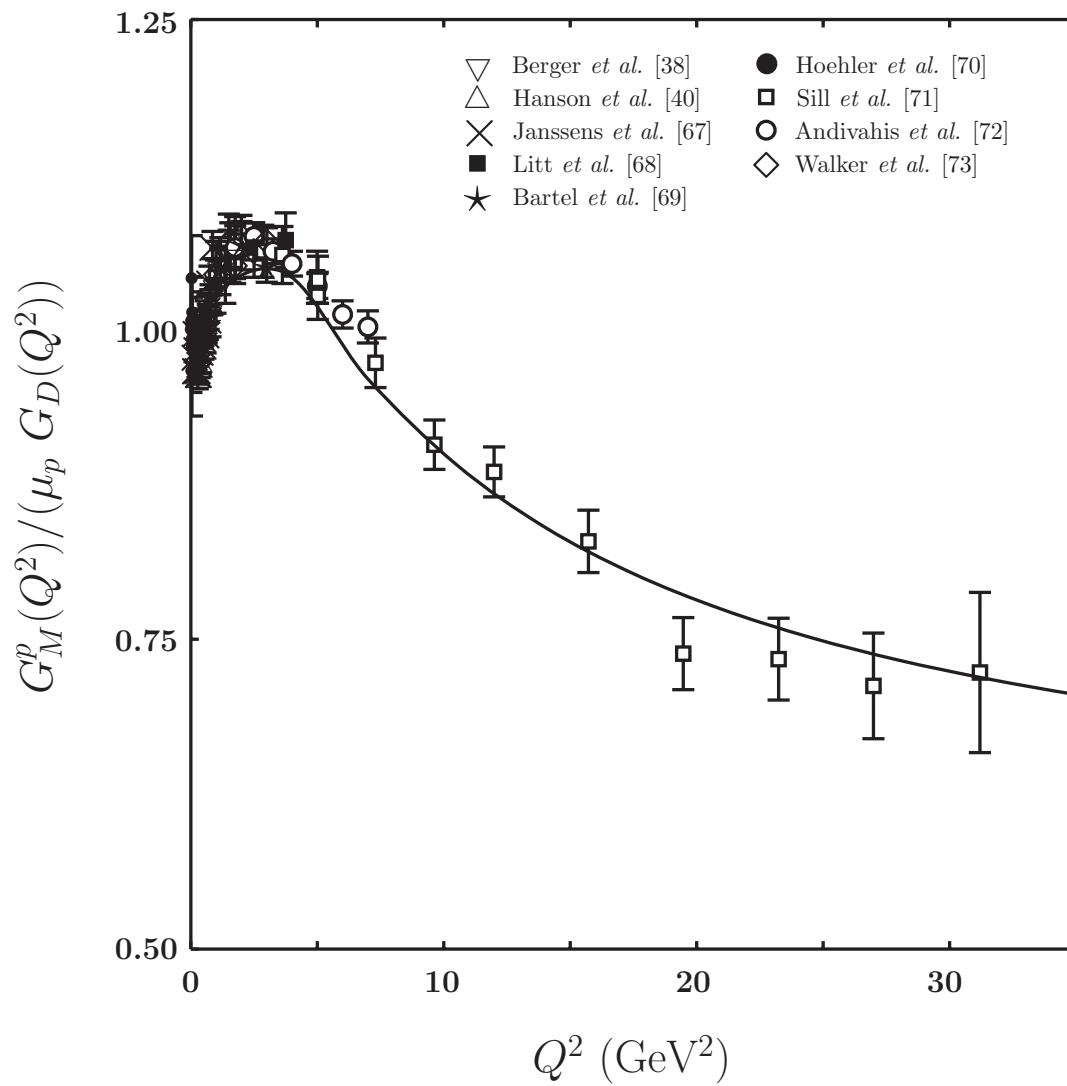
# Electromagnetic stucture of nucleons and Roper (1440)



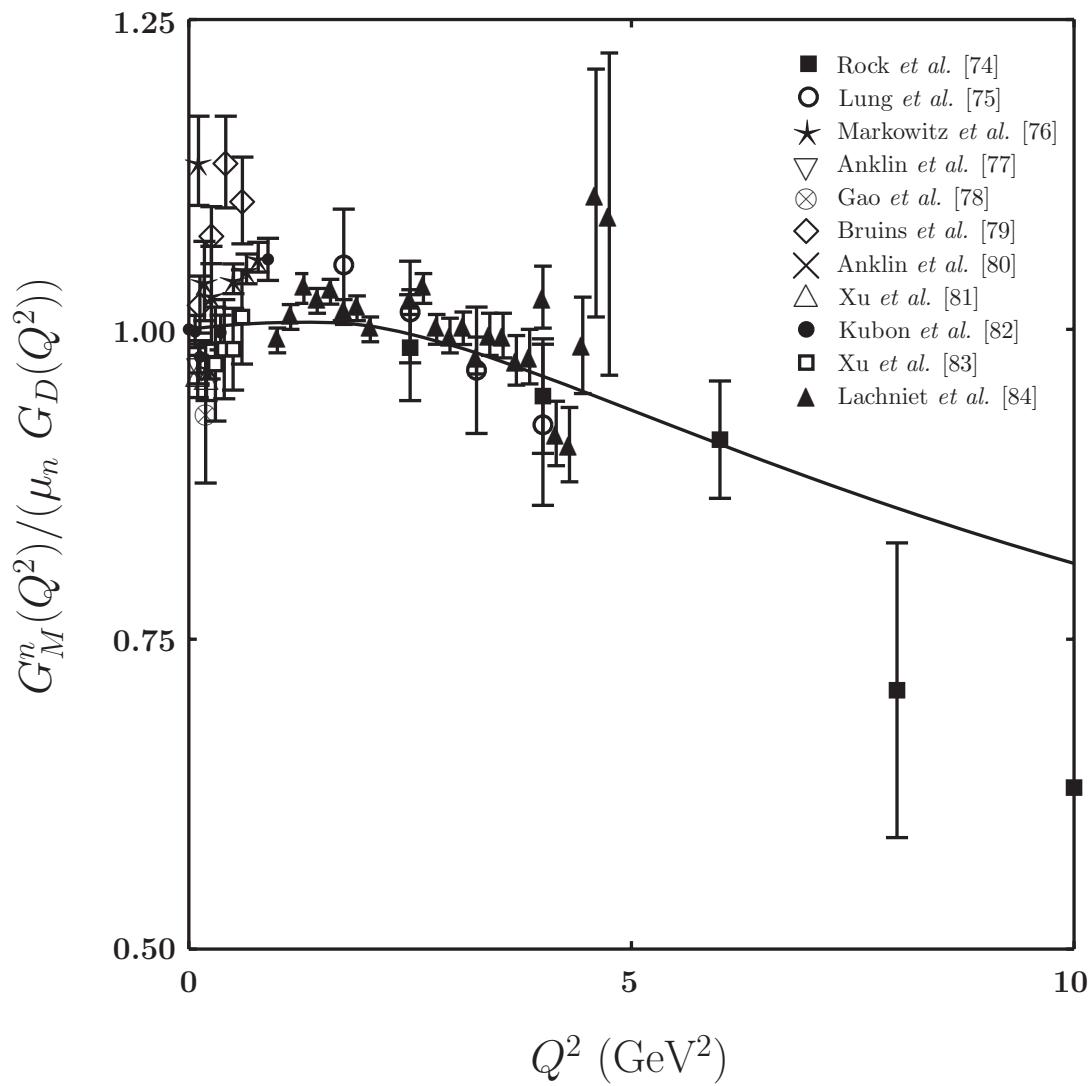
# Electromagnetic stucture of nucleons and Roper (1440)



# Electromagnetic stucture of nucleons and Roper (1440)



# Electromagnetic stucture of nucleons and Roper (1440)



# Electromagnetic structure of nucleons and Roper (1440)

- Put  $n = 1$  and get solutions dual to Roper:
- $N \rightarrow R + \gamma$  transition

$$M^\mu = \bar{u}_\mathcal{R} \left[ \gamma_\perp^\mu F_1(q^2) + i\sigma^{\mu\nu} \frac{q_\nu}{M_\mathcal{R}} F_2(q^2) \right] u_N, \quad \gamma_\perp^\mu = \gamma^\mu - q^\mu \frac{q}{q^2}$$

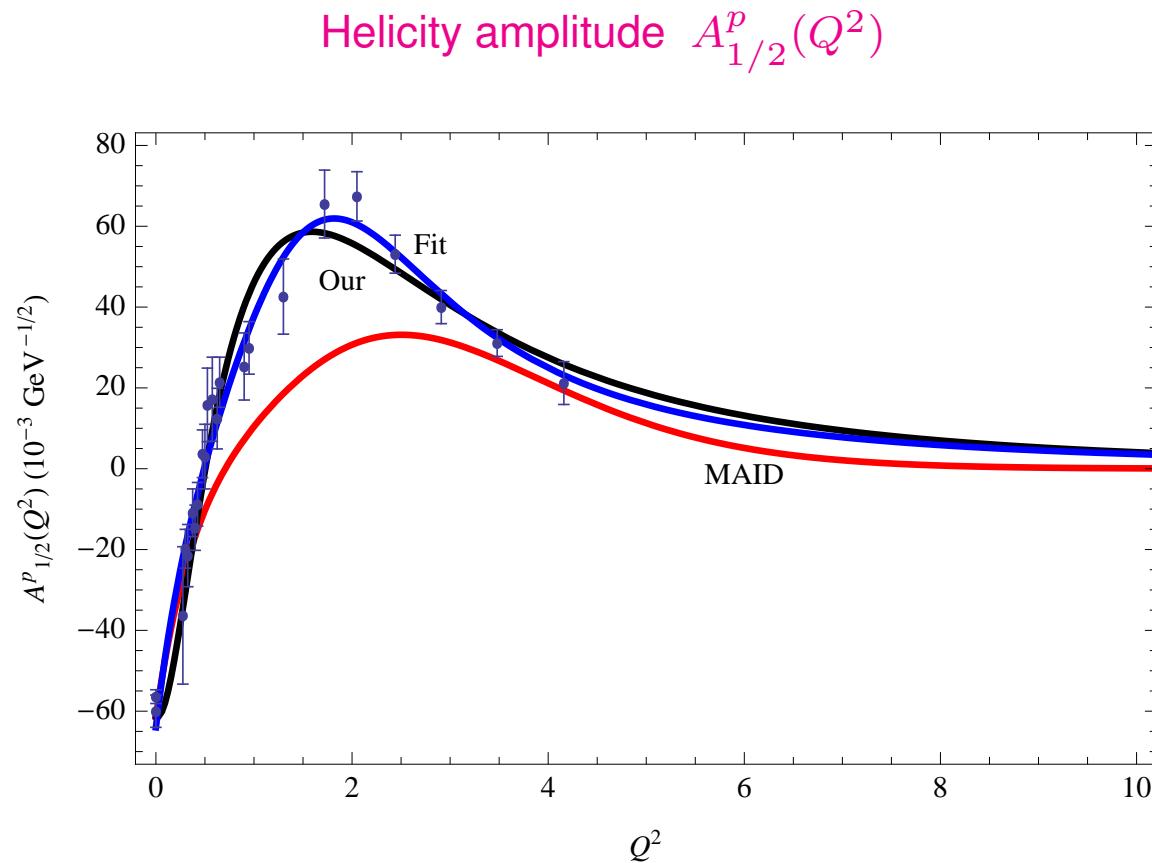
- Helicity amplitudes

$$\begin{aligned} H_{\pm \frac{1}{2}0} &= \sqrt{\frac{Q_-}{Q^2}} \left( F_1 M_+ - F_2 \frac{Q^2}{M_\mathcal{R}} \right) \\ H_{\pm \frac{1}{2}\pm 1} &= -\sqrt{2Q_-} \left( F_1 + F_2 \frac{M_+}{M_\mathcal{R}} \right) \end{aligned}$$

- Alternative set

$$\begin{aligned} A_{1/2} &= -b H_{\frac{1}{2}1}, \quad S_{1/2} = b \frac{|\mathbf{p}|}{\sqrt{Q^2}} H_{\frac{1}{2}0}, \\ Q_\pm &= M_\pm^2 + Q^2, \quad M_\pm = M_\mathcal{R} \pm M_N, \quad b = \sqrt{\frac{\pi\alpha}{2EM_\mathcal{R}M_N}} \end{aligned}$$

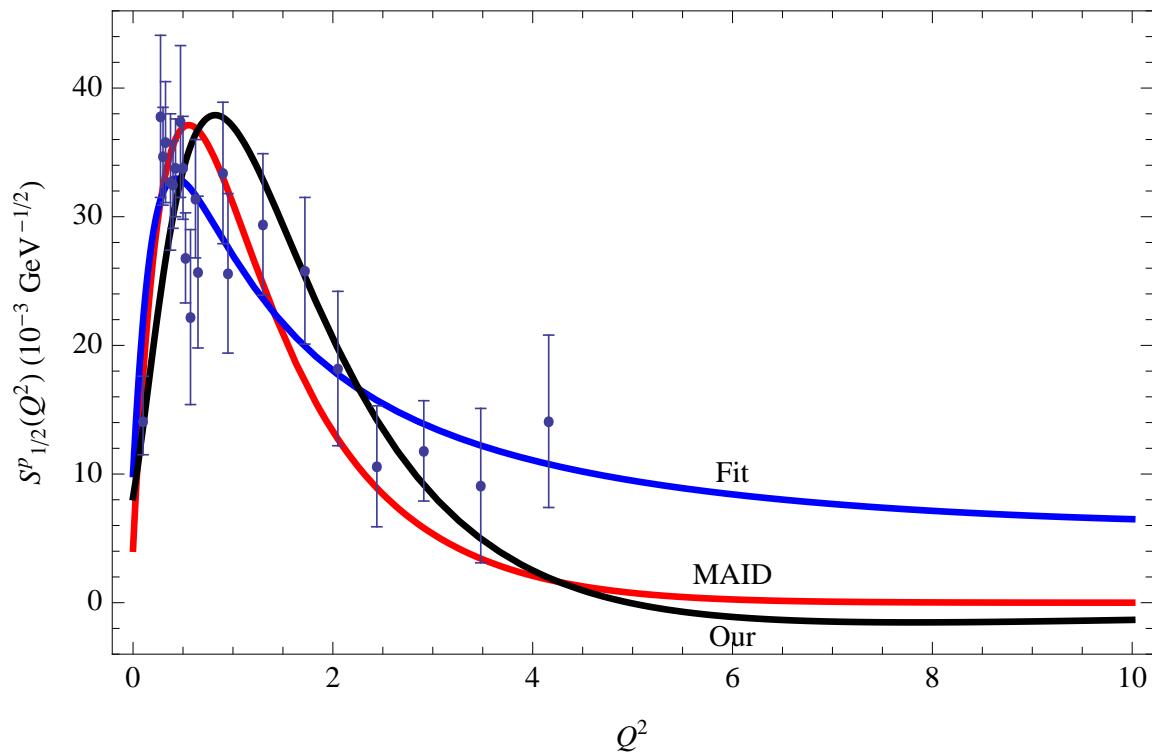
# Electromagnetic stucture of nucleons and Roper (1440)



Data: CLAS Coll at JLab, Mokeev et al, PRC86 (2012) 035203

# Electromagnetic stucture of nucleons and Roper (1440)

Helicity amplitude  $S_{1/2}^p(Q^2)$



Data: CLAS Coll at JLab, Mokeev et al, PRC86 (2012) 035203

# Nonperturbative hadron properties: GPDs/PDFs

Hadronic form factor is given by

$$F_\tau(Q^2) = \int_0^\infty dz \varphi_\tau^2(z) V(Q^2, z^2) = \int_0^1 dx \mathcal{H}_\tau(x, Q^2),$$
$$\mathcal{H}_\tau(x, Q^2) = q_\tau(x) f_\tau(x, Q^2)$$

Here

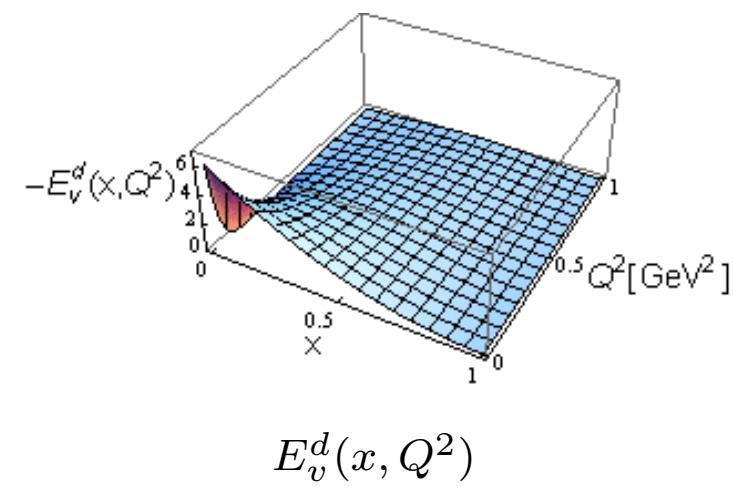
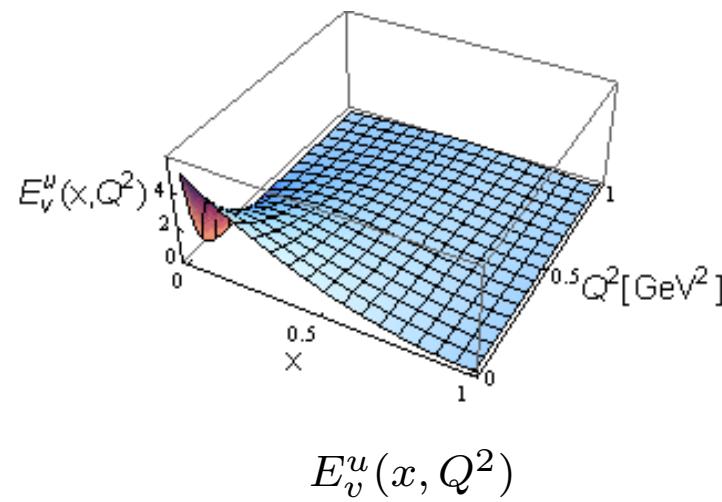
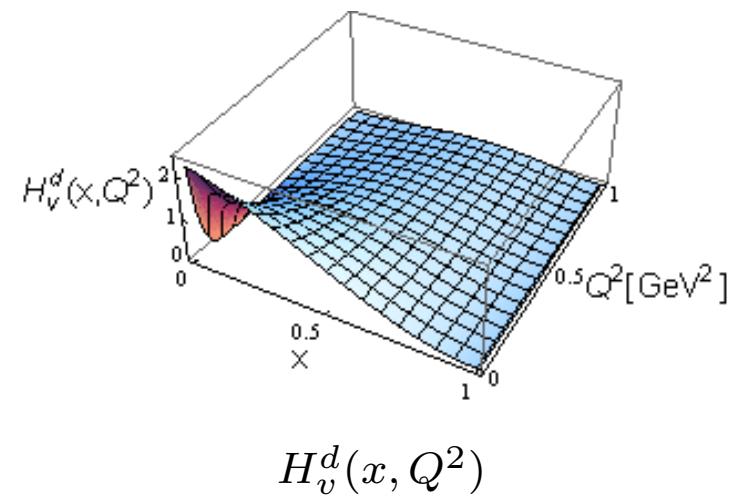
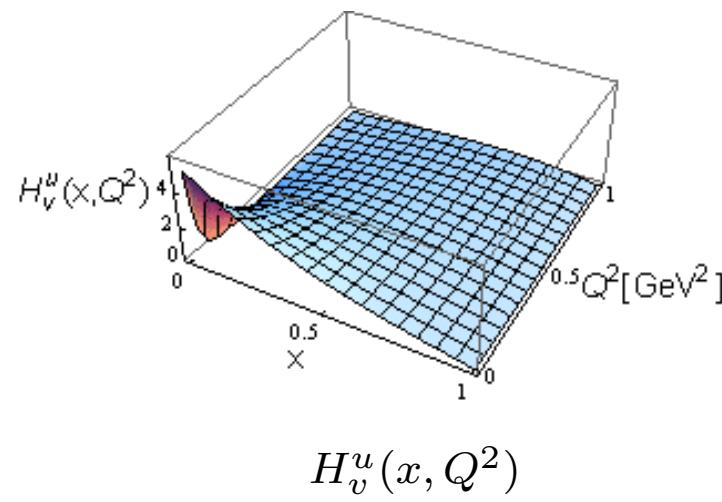
$$f_\tau(x, Q^2) = \frac{1}{(\tau + 1) \Gamma(\tau - 1)} \int_0^\infty dt t^{\tau-2} e^{-t} (2+t) V(Q^2, t(1-x))$$
$$V(Q^2, t(1-x)) \rightarrow V(Q^2, 0) \equiv 1$$

as required by model-independent result and  $f_\tau(x, Q^2) \rightarrow 1$

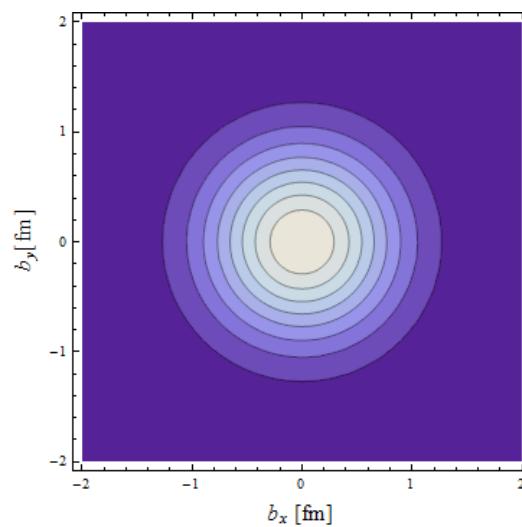
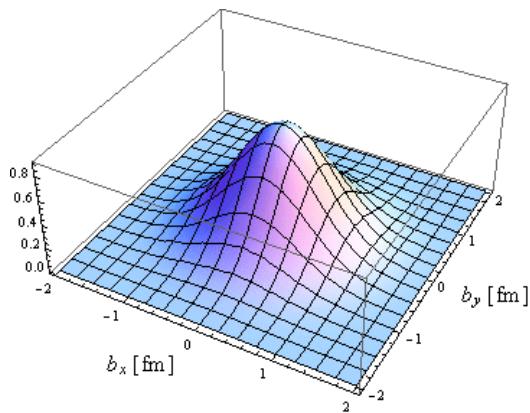
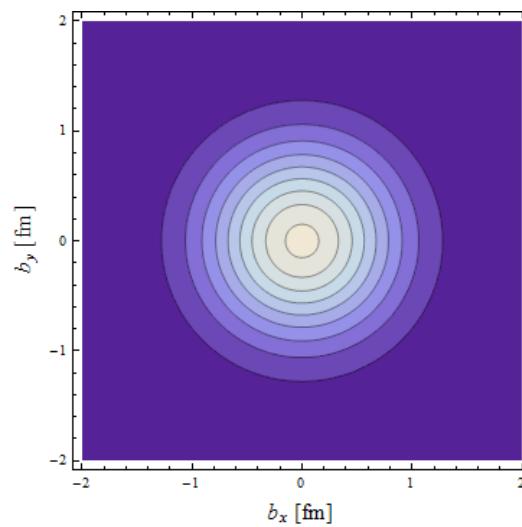
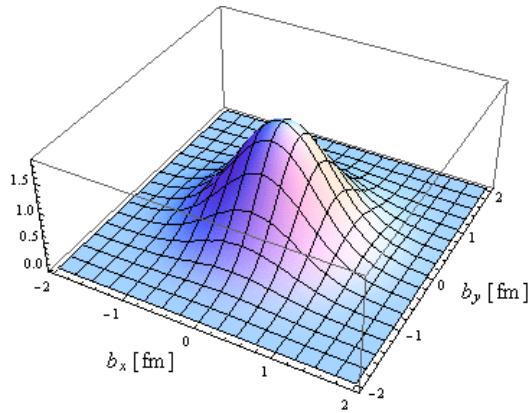
The GPD  $H_\tau(x, Q^2)$  and PDF  $q_\tau(x)$  have correct behavior at  $x \rightarrow 1$

$$H_\tau(x, Q^2) \sim q_\tau(x) \sim (1-x)^\tau$$

# Nucleon GPDs



# Nucleon PDFs



Plots for  $q(x, \mathbf{b}_\perp)$  for  $x = 0.1$ :  $u(x, \mathbf{b}_\perp)$  - upper panels,  $d(x, \mathbf{b}_\perp)$  - lower panels

# Deuteron

- Effective action in terms of AdS fields  $d^M(x, z)$  and  $V^M(x, z)$
- $d^M(x, z)$  – dual to Fock component contributing to deuteron with twist  $\tau = 6$
- $V^M(x, z)$  – dual to the electromagnetic field

$$\begin{aligned} S = & \int d^4x dz e^{-\varphi(z)} \left[ -\frac{1}{4} F_{MN}(x, z) F^{MN}(x, z) - D^M d_N^\dagger(x, z) D_M d^N(x, z) \right. \\ & - ic_2(z) F^{MN}(x, z) d_M^\dagger(x, z) d_N(x, z) \\ & + \frac{c_3(z)}{4M_d^2} \partial^M F^{NK}(x, z) \left( -d_M^\dagger(x, z) \overset{\leftrightarrow}{D}_K d_N(x, z) + \text{H.c.} \right) \\ & \left. + d_M^\dagger(x, z) \left( \mu^2 + U(z) \right) d^M(x, z) \right] \end{aligned}$$

# Deuteron

- Three EM form factors  $G_{1,2,3}$  of the deuteron are related to the charge  $G_C$ , quadrupole  $G_Q$  and magnetic  $G_M$  form factors by
- Expressions for the form factors

$$G_C = G_1 + \frac{2}{3}\tau_d G_Q, \quad G_M = G_2, \quad G_Q = G_1 - G_2 + (1 + \tau_d)G_3, \quad \tau_d = \frac{Q^2}{4M_d^2}$$

These form factors are normalized at zero recoil as

$$G_C(0) = 1, \quad G_Q(0) = M_d^2 Q_d = 25.83, \quad G_M(0) = \frac{M_d}{M_N} \mu_d = 1.714$$

- $Q_d = 7.3424 \text{ GeV}^{-2}$  and  $\mu_d = 0.8574$  – quadrupole and magnetic moments of the deuteron.

# Deuteron

- Differential cross section for the elastic e-D scattering (Rosenbluth formula)

$$d\sigma/d\Omega \sim \left[ A(Q^2) + B(Q^2) \tan^2 \frac{\theta}{2} \right]$$

- Structure functions

$$\begin{aligned} A(Q^2) &= G_C^2(Q^2) + \frac{2}{3}\tau_d G_M^2(Q^2) + \frac{8}{9}\tau_d^2 G_Q^2(Q^2), \\ B(Q^2) &= \frac{4}{3}\tau_d(1 + \tau_d)G_M^2(Q^2). \end{aligned}$$

- Scaling at large  $Q^2$  (Brodsky et al., Carlson et al.)

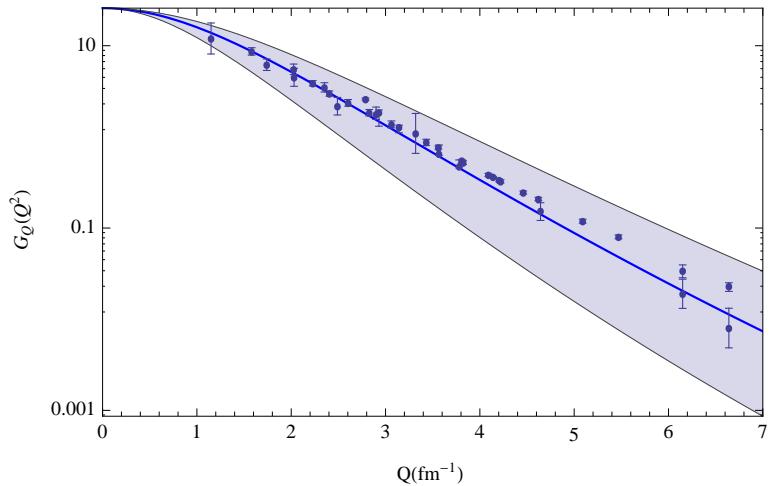
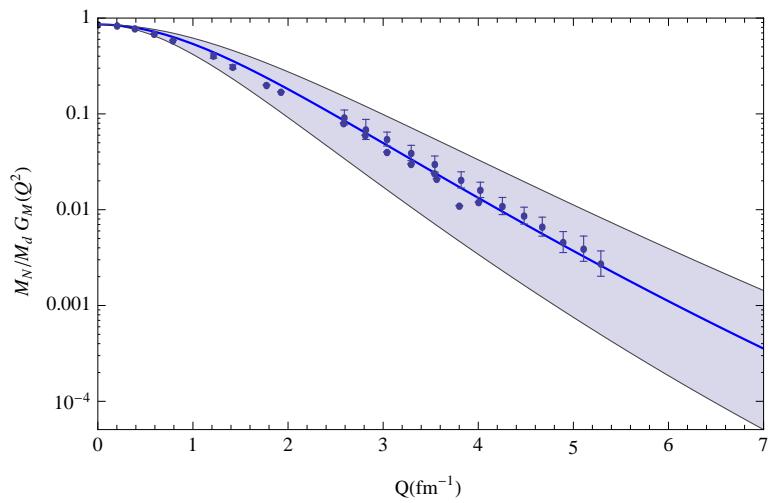
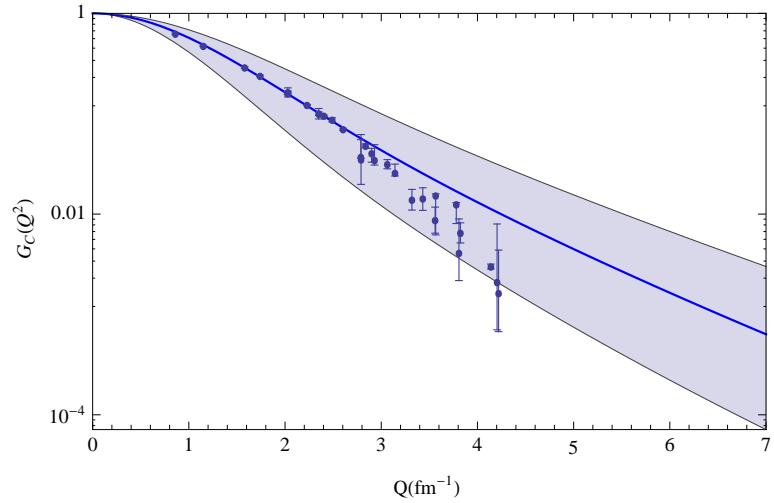
Leading :  $\sqrt{A(Q^2)} \sim \sqrt{B(Q^2)} \sim G_C(Q^2) \sim 1/Q^{10}$

Subleading :  $G_M(Q^2) \sim G_Q(Q^2) \sim 1/Q^{12}$

It fixes the  $z$  dependence of  $c_2(z)$  and  $c_3(z)$

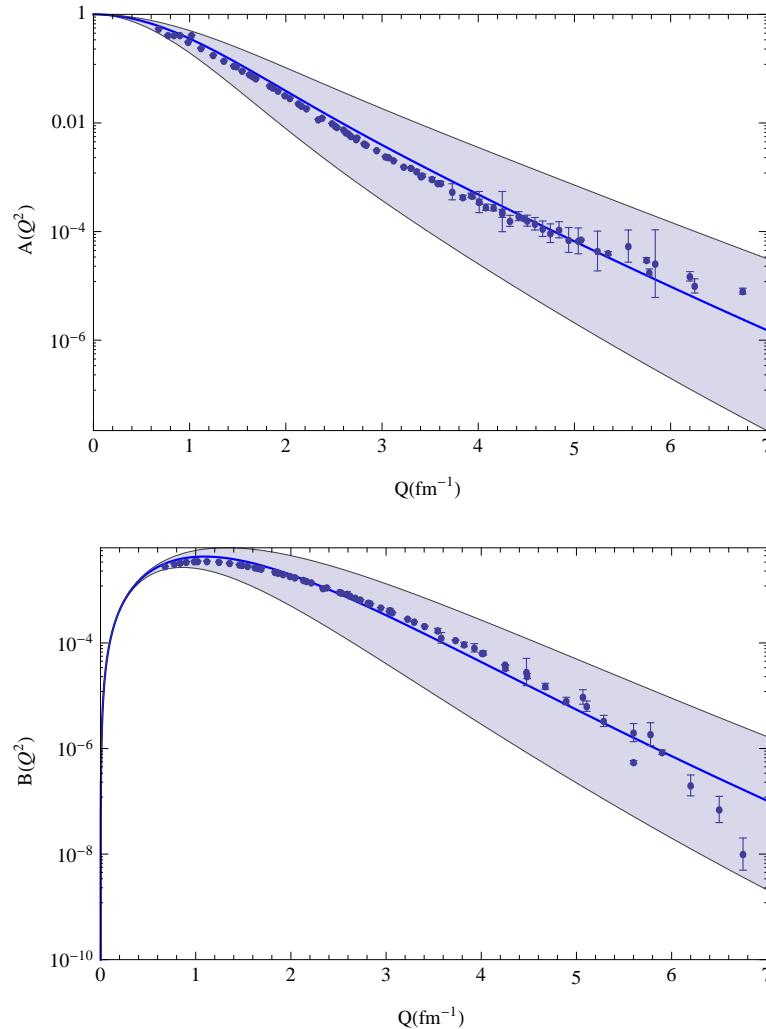
$$c_2(z) = \frac{M_d}{30M_N} \mu_d \kappa^2 z^2, \quad c_3(z) = \left( M_d^2 \mathcal{Q}_d - 1 + \frac{M_d}{30M_N} \mu_d \right) \kappa^2 z^2$$

# Deuteron



Deuteron form factors

# Deuteron



Structure Functions  $A(Q^2)$  and  $B(Q^2)$

# Deuteron

Charge radius

$$r_C = (-6G'_C(0))^{1/2} = 1.92 \text{ fm}$$

Data:  $r_C = 2.13 \pm 0.01 \text{ fm}$

Magnetic radius  $r_M = (-6G'_M(0)/G_M(0))^{1/2} = 2.24 \text{ fm}$

Data  $r_M = 1.90 \pm 0.14 \text{ fm}$ .

# Tetraquarks

- Under study at CERN, KEK, Fermilab, etc.

- $N_c$  QCD:

Mesons  $q^a \bar{q}^a$  and under  $SU(N_c)$  the  $\bar{q}^a$  transforms similar to

$$\epsilon^{a a_1 \dots a_{N_c-1}} \underbrace{q_{a_1} \dots q_{N_c-1}}_{N_c-1}$$

- Baryons  $\epsilon^{a_1 \dots a_{N_c}} \underbrace{q_{a_1} \dots q_{N_c}}_{N_c}$

- $q^a$  transforms similar to  $\epsilon^{a a_1 \dots a_{N_c-1}} \underbrace{\bar{q}_{a_1} \dots \bar{q}_{N_c-1}}_{N_c-1}$

- Multiquarks  $\epsilon_{a a_1 \dots a_{N_c-1}} \epsilon_{a b_1 \dots b_{N_c-1}} \underbrace{q^{a_1} \dots q^{a_{N_c-1}}}_{N_c-1} \underbrace{\bar{q}^{b_1} \dots \bar{q}^{b_{N_c-1}}}_{N_c-1}$

- Limit to real QCD:  $N_c = 3$

$$\text{Tetraquark } T = D^a \bar{D}^a = \left( \epsilon^{a a_1 a_2} q_{a_1} q_{a_2} \right) \left( \epsilon^{a b_1 b_2} \bar{q}_{b_1} \bar{q}_{b_2} \right)$$

is color diquark-antidiquark bound state

# Tetraquarks

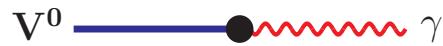
- Equation of motion from mesons case by rescaling  $\tau \rightarrow \tau + 2$
- Solutions:  $\phi_{nL}(z) = \sqrt{\frac{2\Gamma(n+1)}{\Gamma(n+L+3)}} \kappa^{L+3} z^{L+7/2} e^{-\kappa^2 z^2/2} L_n^{L+2}(\kappa^2 z^2)$
- $M_{nJL}^2 = 4\kappa^2 \left( n + \frac{L+J}{2} + 1 \right)$
- Agreement with **COMPASS Coll. at SPS (CERN)**  
for  $a_1(1414)$  with spin-parity  $J^{PC} = 1^{++}$  discovered in 2015
- Put  $n = 0, L = 1, J = 1$  and get  $M_{a_1}^2 = 8\kappa^2$  or  $M_{a_1} = 2\kappa\sqrt{2}$
- Using  $\kappa = 0.5$  GeV get  $M_{a_1} = \sqrt{2} \simeq 1.414$  GeV
- Brodsky-Teramond (superconformal case)  $M_{nLS}^2 = 4\kappa^2 \left( n + L + \frac{S}{2} + 1 \right)$
- Our  $M_{nJL}^2 = 4\kappa^2 \left( n + \frac{L+J}{2} + 1 \right)$
- Degenerate at  $J = L + S$ , when all three decouple
- Specifically for  $a_1(1414)$  with  $J^{PC} = 1^{++}$  we have  $J = L = S = 1$

# QCD Compositeness and Quark Counting Rules

QCD compositeness vs. VMD (Vector Meson Dominance model)

Brodsky, Lebed, Lyubovitskij: Phys.Lett.B764 (2017) 174; Phys.Rev.D97 (2018) 034009

- Novel idea relevant for electrocouplings of baryon resonances
- QCD compositeness (vector mesons are bound states of quarks) leads to a nontrivial  $Q^2$  dependence of vector meson - photon transition

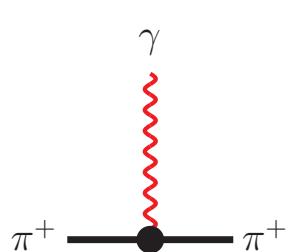


$$V^0 = \rho^0, \omega, \phi, J/\psi, \Upsilon$$

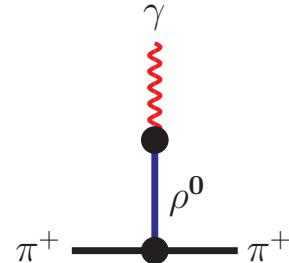
- Structure of matrix element  $G_V(g^{\mu\nu}Q^2 - Q^\mu Q^\nu)$ , where  $Q$  is Euclidean momentum of  $V^0$  and  $\gamma$
- In VMD  $G_V$  is constant
- $G_V(Q^2)$  must have  $G_V(Q^2) \sim 1/\sqrt{Q^2}$  behavior at large  $Q^2$

# QCD Compositeness and Quark Counting Rules

- Consider the pion



(a) Direct



(b)  $\rho^0$  exchange

- In VMD: contact diagram 1, vector meson diagram gives  $-Q^2/(M_V^2 + Q^2)$
- The sum is  $M_V^2/(M_V^2 + Q^2)$  scales as  $M_V^2/Q^2$
- Contact diagram is 1, resonance is  $-1 + M_V^2/Q^2$
- In pQCD: contact diagram  $1/Q^2$ , vector meson diagram is subleading  $1/Q^3$  because of falloff of the vector meson-photon form factor

# QCD Compositeness and Quark Counting Rules

- New formula for electrocouplings of two hadrons with adjustable constituent content  $n_1$  and  $n_2$

$$\begin{aligned} F_{H_{n_1} H_{n_2}}(Q^2) &= \frac{\Gamma(\frac{n_1+n_2}{2}) \Gamma(\frac{n_1+n_2}{2} - 1)}{\sqrt{\Gamma(n_1 - 1)\Gamma(n_2 - 1)}} \frac{\Gamma(a + 1)}{\Gamma(a + 1 + \frac{n_1+n_2}{2} - 1)} \\ &\sim \frac{1}{a^{(n_1+n_2)/2-1}}, \end{aligned}$$

where  $a = Q^2/(4\kappa^2)$  and  $\Gamma(n) = \int_0^\infty dx x^{n-1} e^{-x}$  is gamma function.

For  $n_1 = n_2 = n$  we get

$$F_{H_n} \sim \left(\frac{1}{Q^2}\right)^{n-1}$$

For  $n_1 = n, n_2 = 0$  we get

$$F_{H_n} \sim \left(\frac{1}{Q^2}\right)^{(n-1)/2}$$

# QCD Compositeness and Quark Counting Rules

- In particular, the scaling of the form factor corresponding to  $\gamma^* \rightarrow Z_c^+ + \pi^-$  is

$$F_{Z_c^+ \pi^-} \sim \frac{1}{Q^4}$$

in case of tetraquark structure of  $Z_c$  state, and

$$F_{Z_c^+ \pi^-} \sim \frac{1}{Q^2}$$

in the case when  $Z_c^+$  is a system of two tightly bound diquarks (Brodsky-Lebed)

For  $\gamma^* \rightarrow Z_c^+ + Z_c^-$ ,

$$F_{Z_c^+ Z_c^-} \sim \frac{1}{Q^6}$$

in case of a  $Z_c$  state with tetraquark structure, and

$$F_{Z_c^+ Z_c^-} \sim \frac{1}{Q^2}$$

in case when  $Z_c^+$  is a system of two tightly bound diquarks (Brodsky-Lebed)

# AdS/QCD at finite temperature

- Study of hadron properties at finite temperature is a promising task, since it allows for a deeper understanding of the evolution of the early Universe, the formation of hadronic matter and its phase transitions.
- Application of soft-wall AdS/QCD:

1. Herzog, PRL 98 (2007) 0916011:

Deconfinement occurs via 1st -order Hawking-Page phase transition between low  $T$  AdS and high temperature black hole

Model-dependent predictions (difficult to compare to QCD):

$$T_c^{\text{HW}} = 122 \text{ MeV} \text{ and } T_c^{\text{SW}} = 191 \text{ MeV}$$

Lattice:  $T_c^{\text{Lattice}} = 192 \pm 7 \pm 4 \text{ MeV}$

2. Other prediction for the  $T_c$  and more detailed/improved description:

in Grigoryan et al, PRD 82 (2010) 026005; Colangelo et al, PRD 83 (2011) 035015; Braga et al, PLB 774 (2017) 476; Bartz et al, PRD 94 (2016) 075022; Vega et al, EPJA 53 (2017) 217.

# AdS/QCD at finite temperature

- Popular way to introduce the  $T$  to consider the specific metric (geometry)
- AdS-Schwarzschild geometry

$$ds^2 = e^{2A(z)} \left[ f_T(z) dt^2 - (d\vec{x})^2 - \frac{dz^2}{f_T(z)} \right]$$

Here  $f_T(z) = 1 - z^4/z_H^4$ , where  $z_H$  is the position of the event horizon, which is related to the black-hole Hawking temperature  $T = 1/(\pi z_H)$ .

- The latter also represents (holography correspondence) the temperature of the boundary field theory.

# AdS/QCD at finite temperature

- In addition of  $T$ -dependence of metric we propose the  $T$  dependence of dilaton parameter

$$\kappa^2(T) = \kappa^2 \frac{\Sigma(T)}{\Sigma} .$$

using its relation to the quark condensate parameter  $\Sigma$

$$\Sigma = \langle 0 | \bar{q} q | 0 \rangle = -N_f B F^2 = -\frac{3N_f B}{64} \kappa^2 .$$

Here  $N_f$  is the number of quark flavors,  $B$  is the quark condensate parameter, and  $F$  is the pseudoscalar meson decay constant in the chiral limit at zero temperature.

# AdS/QCD at finite temperature

- $T$ -dependence of quark condensate  $\Sigma(T)$  was derived by Gasser and Leutwyler in two-loop ChTP [PLB184 (1987) 83]

$$\Sigma(T) = \Sigma \left[ 1 - \frac{N_f^2 - 1}{N_f} \frac{T^2}{12F^2} - \frac{N_f^2 - 1}{2N_f^2} \left( \frac{T^2}{12F^2} \right)^2 + \mathcal{O}(T^6) \right]$$

This result is valid for an adjustable number of quark flavors with  $N_f \geq 2$  and is given as an expansion in  $T^2$ .

For three-loop result see Gerber and Leutwyler, NPB321 (1989) 387.

- Critical temperature in ChPT (vanishing of condensate):

$$\frac{\left(T_c^{\text{QCD}}\right)^2}{12F^2} = N_f \left[ \sqrt{\frac{N_f^2 + 1}{N_f^2 - 1}} - 1 \right].$$

$T_c^{\text{QCD}} = 230 \text{ MeV}$  for  $N_f = 2$ .

Power scaling behavior at large  $N_f$ :

$$T_c^{\text{QCD}} \sim F / \sqrt{N_f}$$

# AdS/QCD at finite temperature

- In the rest frame of the AdS field with  $\vec{p} = 0$  we get EOM

$$\left[ -\frac{d^2}{dz^2} + U_J(z, T) \right] \phi_{nJ}(z, T) = M_{nJ}^2(T) \phi_{nJ}(z, T),$$

where  $U_J(z, T)$  is the effective potential at finite temperature, which can be decomposed into a zero temperature term  $U_J(z) \equiv U_J(z, 0)$  and a temperature dependent term  $\Delta U_J(z, T)$

$$U_J(z, T) = U_J(z) + \Delta U_J(z, T),$$

$$U_J(z) = \kappa^4 z^2 + 2\kappa^2(J-1) + \frac{4m^2 - 1}{4z^2},$$

$$\Delta U_J(z, T) = 2\rho(T)\kappa^2 (\kappa^2 z^2 + J - 1) + \frac{4z^2}{5z_H^4} J(J-1)(\kappa^2 z^2 - J),$$

where  $m = N + L - 2$  and  $\rho_T$  parametrizes  $T$  dependence of the dilaton:  
 $\kappa^2(T) = \kappa^2[1 + \rho(T)]$ , where

$$\begin{aligned} \rho(T) &= \delta_{T_1} \frac{T^2}{12F^2} + \delta_{T_2} \left( \frac{T^2}{12F^2} \right)^2 + \mathcal{O}(T^6), \\ \delta_{T_1} &= -\frac{N_f^2 - 1}{N_f}, \quad \delta_{T_2} = -\frac{N_f^2 - 1}{2N_f^2}. \end{aligned}$$

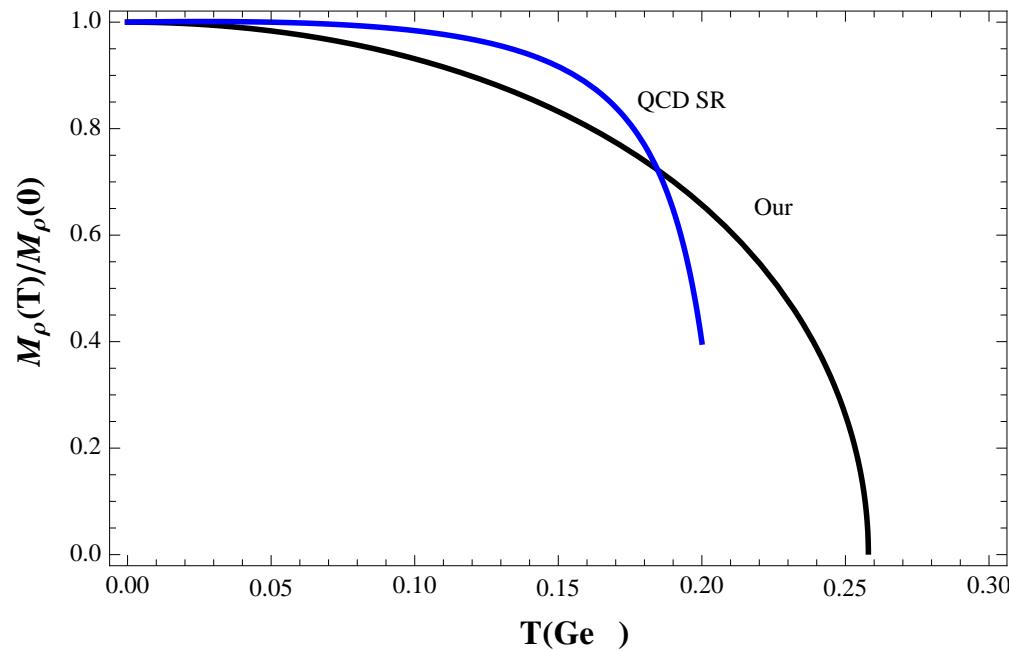
# AdS/QCD at finite temperature

- Meson mass spectrum at finite  $T$  reads:

$$\begin{aligned} M_{nJ}^2(T) &= M_{nJ}^2(0) + \Delta M_{nJ}^2(T), \\ \Delta M_{nJ}^2(T) &= \rho_T M_{nJ}^2(0) + R_{nJ} \frac{\pi^4 T^4}{\kappa^2}, \\ R_{nJ} &= \frac{4}{5} J(J-1) \left[ (m+1)(m+2) + (6n-J)(n+m+1) - nJ \right]. \end{aligned}$$

# AdS/QCD at finite temperature

- Comparison of  $M_\rho(T)/M_\rho(0)$  with result of QCD sum rules (Lowe et al)



# AdS/QCD at finite temperature

- Use pure Poincare metric with thermal dilaton

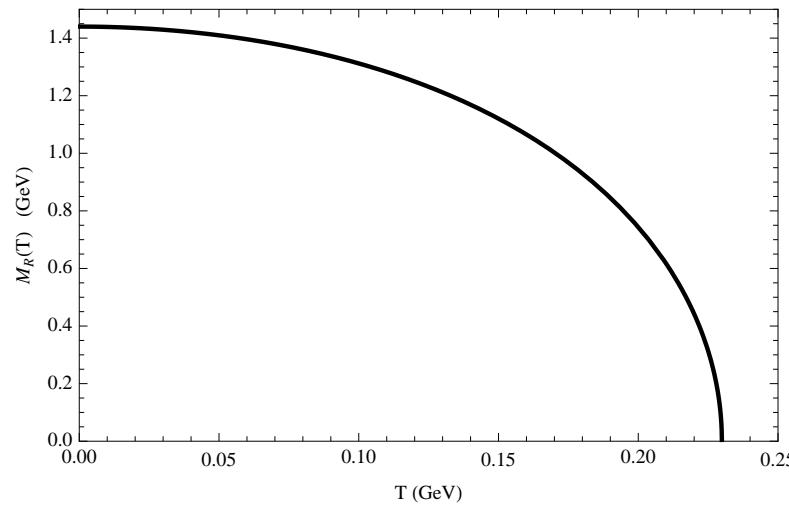
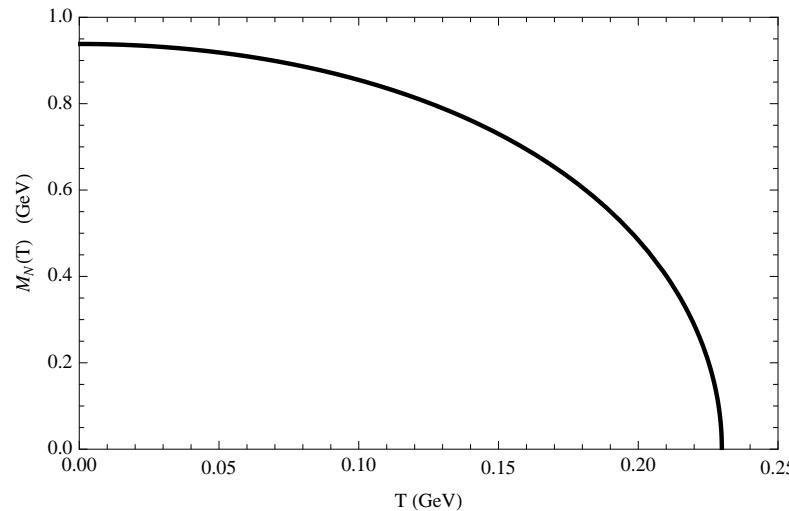
$$g_{MN} x^M x^N = \epsilon_M^a \epsilon_N^b \eta_{ab} x^M x^N = \frac{1}{z^2} (dx_\mu dx^\mu - dz^2)$$

$$\begin{aligned}\kappa^2(T) &= \kappa^2 \left[ 1 + \delta_{T_1} \frac{T^2}{12F^2} + \delta_{T_2} \left( \frac{T^2}{12F^2} \right)^2 + \mathcal{O}(T^6) \right], \\ \delta_{T_1} &= -\frac{N_f^2 - 1}{N_f}, \quad \delta_{T_2} = -\frac{N_f^2 - 1}{2N_f^2}.\end{aligned}$$

$F$  is the pseudoscalar coupling constant in the chiral limit,  $N_f$  is the number of quark flavors.

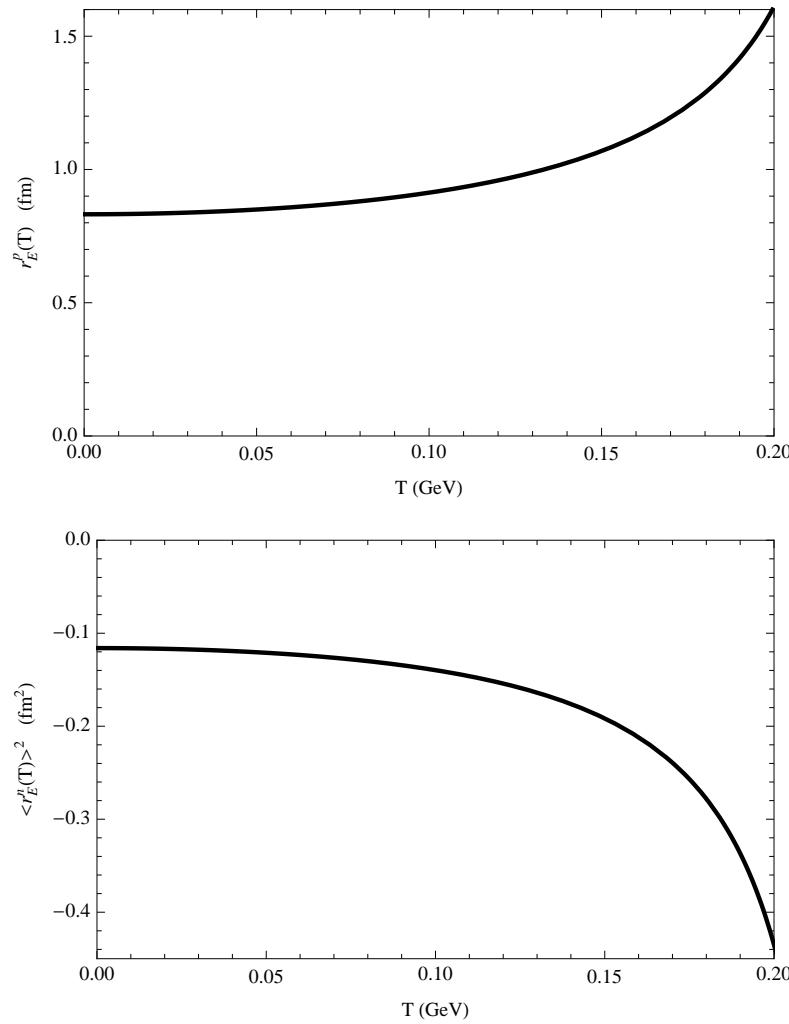
# AdS/QCD at finite temperature

- Nucleon and Roper masses up to  $T_c = 230$  MeV.



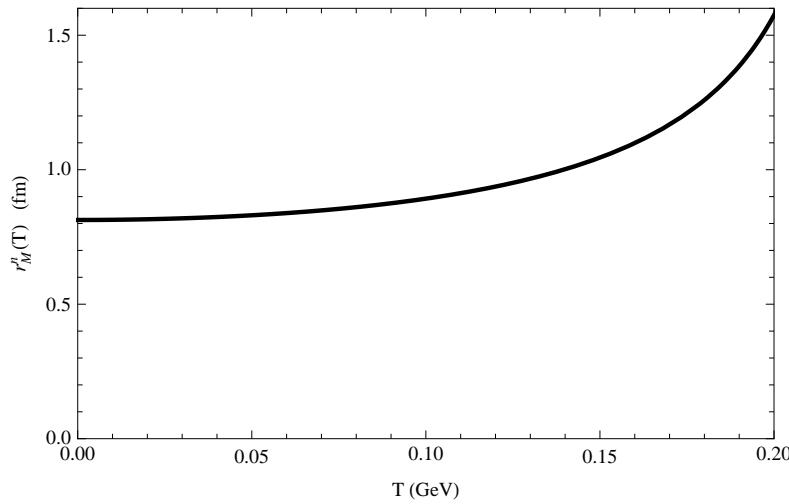
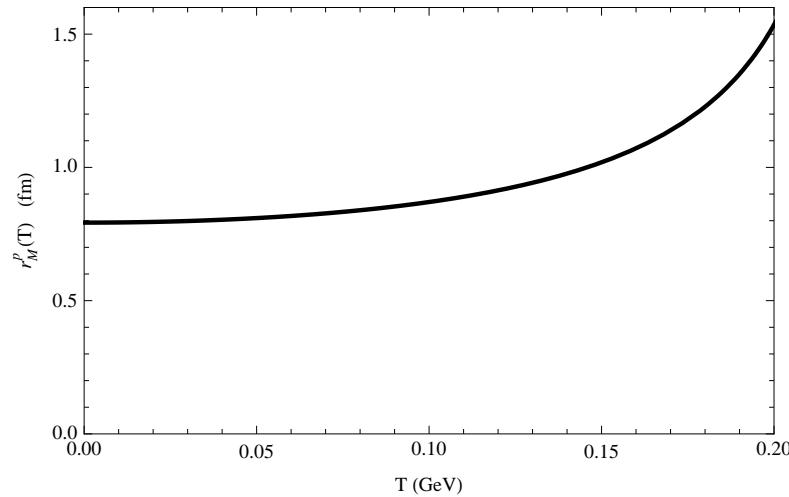
# AdS/QCD at finite temperature

- Temperature dependence of nucleon charge radii  $r_E^p$  and  $\langle r_E^2 \rangle^n$



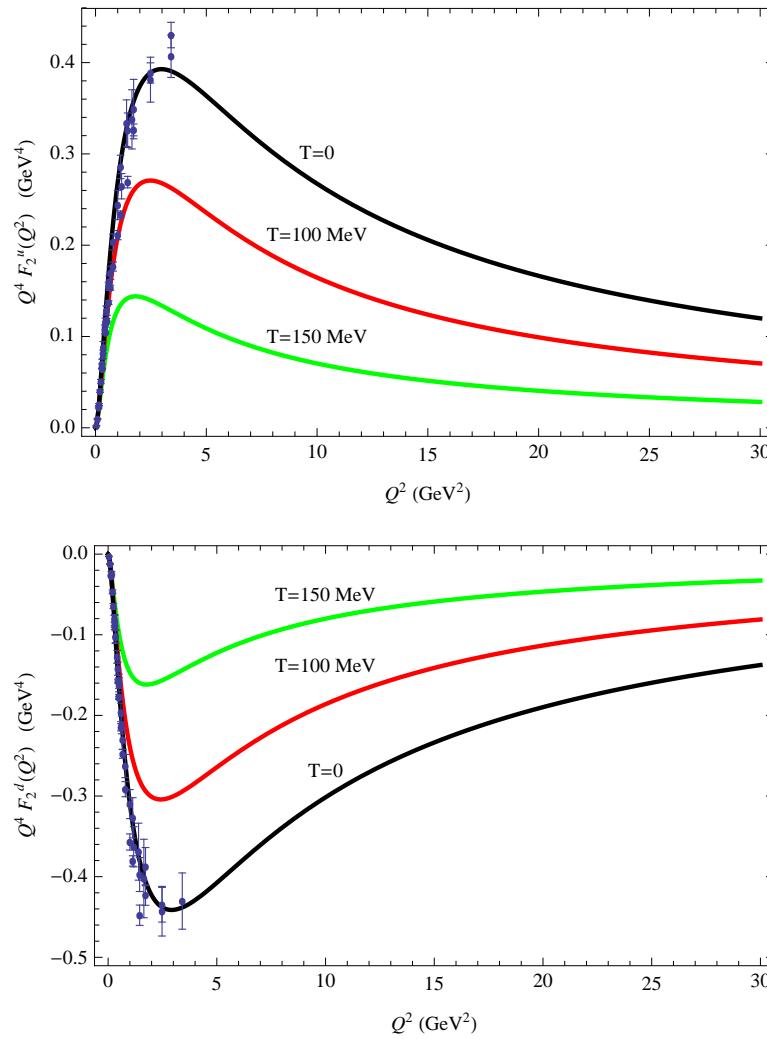
# AdS/QCD at finite temperature

- Temperature dependence of nucleon magnetic radii  $r_M^p$  and  $r_M^n$



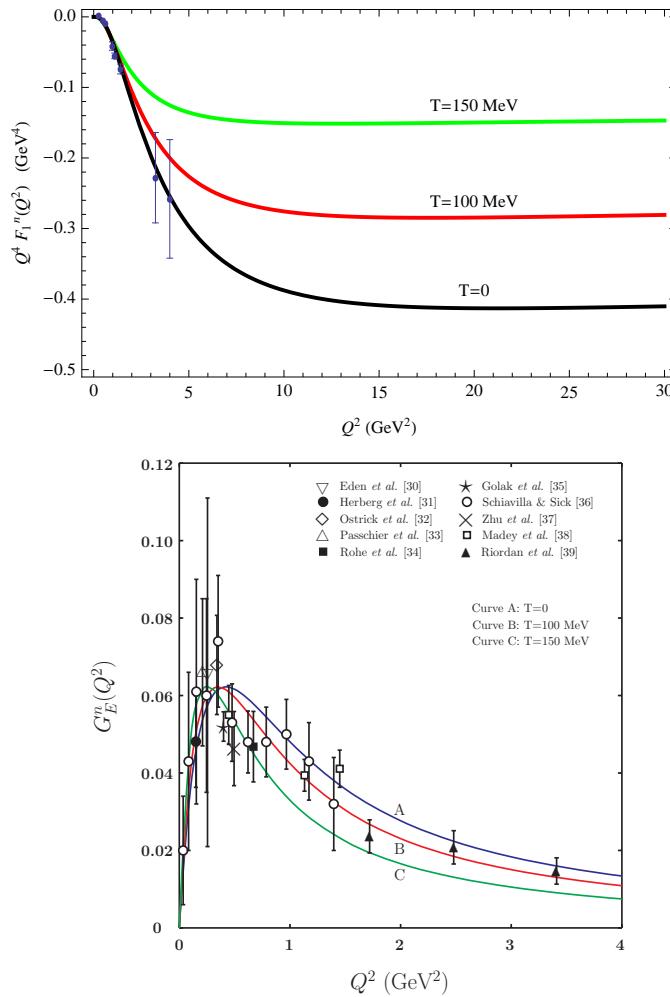
# AdS/QCD at finite temperature

- Temperature dependence of Pauli  $u$  and  $d$  quark form factors multiplied by  $Q^4$ .



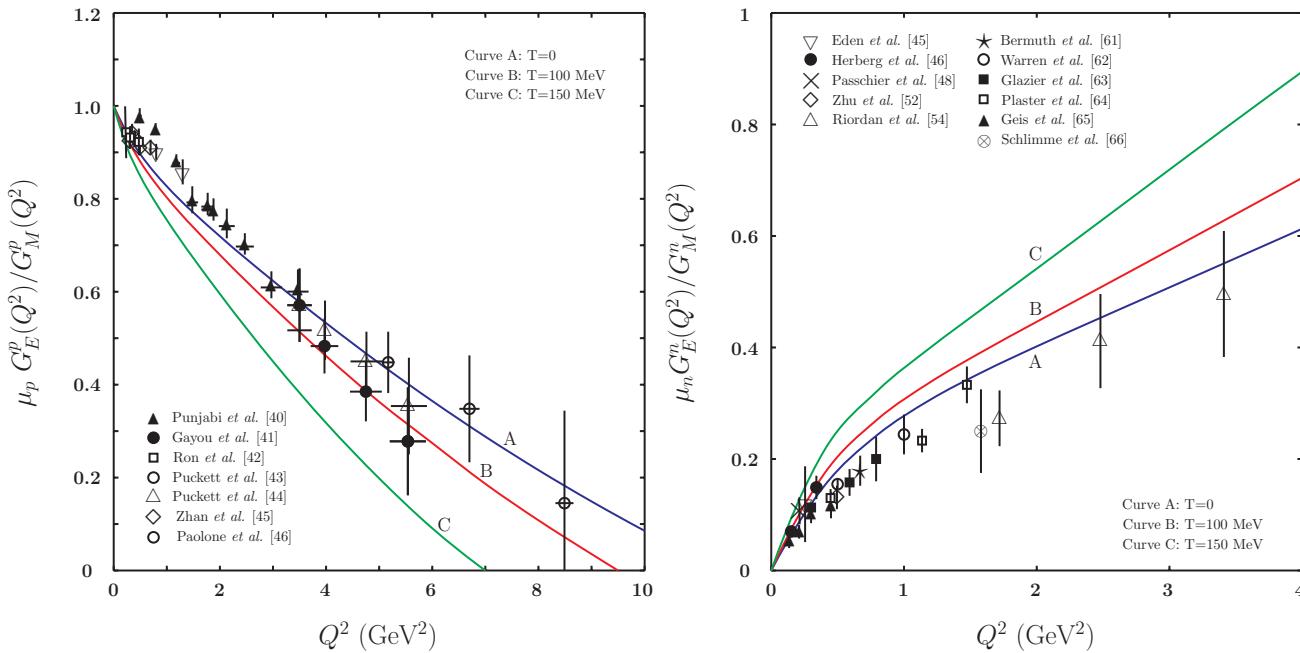
# AdS/QCD at finite temperature

- T-dependence of the Dirac and charge Sachs neutron form factor



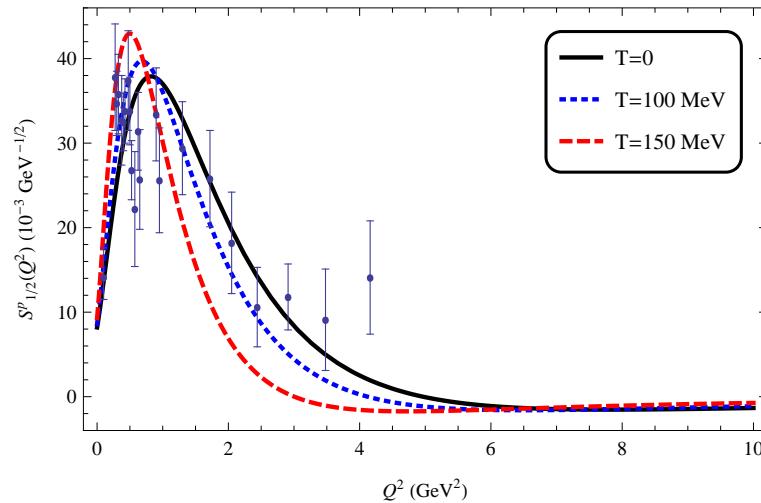
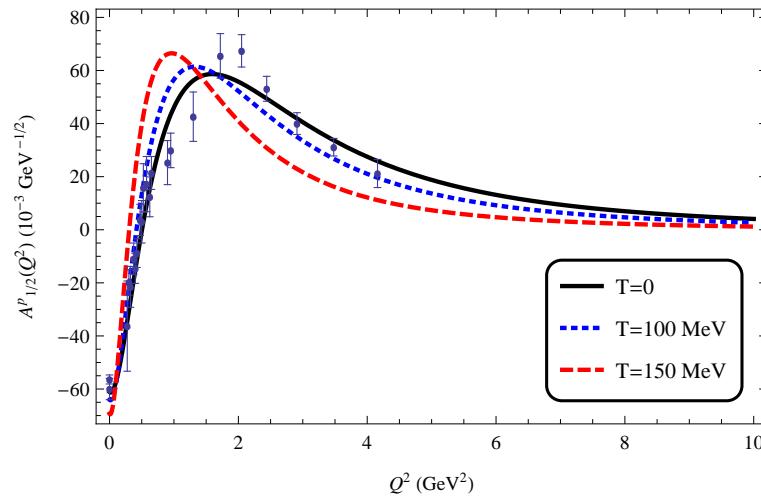
# AdS/QCD at finite temperature

- $T$  dependence of the ratios  $\mu_p G_E^p(Q^2)/G_M^p(Q^2)$  and  $\mu_n G_E^n(Q^2)/G_M^n(Q^2)$



# AdS/QCD at finite temperature

- $T$  dependence of the helicity amplitudes  $A_{1/2}^p(Q^2)$  and  $S_{1/2}^p(Q^2)$



# Summary

- AdS/QCD: Effective actions using correspondence between 5D theories on AdS manifolds including gravity and 4D gauge theory living on the boundary of AdS space
- AdS fields are dual to hadrons and exotic states
- Bulk profiles of AdS fields in 5th (holographic direction) dual to hadronic wave functions
- Applications: Regge behavior of hadron masses, correct power scaling of hadron form factors at large  $Q^2$ , extension for multiquark states (straightforward)
- Gives more realistic Light-Front Wave Functions underlying Light-Front QCD
- Extension to finite temperature