

# Directed, elliptic, and triangular flow of free protons and deuterons in Au+Au collisions at HADES energy

$$E_{lab} = 1.23 \text{ A GeV}$$

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P.Hillmann, V.Gaebel, M.Bleicher, et al., arXiv:1907.04571 [nucl-th]

THMEC, JINR, Dubna, 18th September 2019

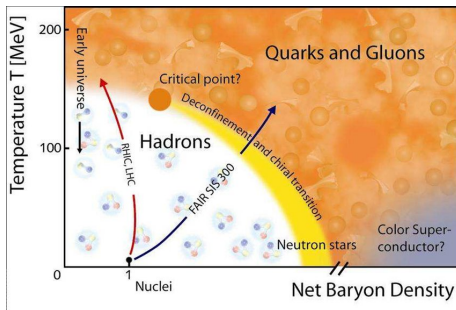


- 1 Introduction
  - Motivation
  - Collective Flow
- 2 The UrQMD model
  - The equation of state
  - Deuteron formation via coalescence
- 3 Results
  - Directed and elliptic flow
  - Higher order flow components
  - Mass number scaling
- 4 Summary

# Outline for section 1

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# Motivation



- At low energy Au+Au collisions baryon densities 3-4 times higher than the ground state density can be reached. One expects to find exotic particles or maybe even super conducting matter and a phase transition to the Quark Gluon Plasma.

# Motivation

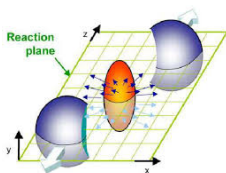
- The dynamics of the dense matter region are sensitive to the initial density and potential interactions and therefore the nuclear equation of state (EoS).
- Being sensitive to initial pressure gradients the collective flow is a promising variable to study the EoS.
- The HADES experiment performed Au+Au collisions at  $E_{lab} = 1.23$  A GeV with a huge amount of data and is able to measure even higher order flow components.
- At the HADES energy regime phase cluster formation plays an important role to the evolution of collective flow.

- Collective flow as Fourier-series of momentum distribution:

$$E \frac{d^3N}{d^3p} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T dy} \left( 1 + 2 \sum_{n=1}^{\infty} v_n \cos[n(\varphi - \Psi_{RP})] \right) \quad (1)$$

- Calculation of the flow components as average over events in a given centrality class ( $\Psi_{RP} = 0$ ):

$$v_n(p_T, y) = \langle \cos[n\varphi] \rangle \quad (2)$$



picture: Heinz, Ulrich W. J.Phys. A42 (2009) 214003

# Outline for section 2

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# The UrQMD model

- UrQMD is based on a geometrical interpretation of the nuclear cross section  $\sigma$  and therefore includes string and resonance dynamics, scattering and strangeness exchange.
- It simulates the space-time evolution of each particle including many meson and baryon species.
- Reaction criterion for the relative distance of two particles  $d$ :

$$d < \sqrt{\frac{\sigma}{\pi}} \quad (3)$$

S. A. Bass et al. Prog. Part. Nucl. Phys. 41 (1998) 225-370,  
M. Bleicher et al. J. Phys. G: Nucl. Part. Phys. 25 (1999)  
1859-1896



# The equation of state in UrQMD

- To describe the dynamics of particles at low energies and high densities, potential interactions have to be taken into account.
- For the simulations we used a hard non-momentum dependent Skyrme-type equation of state with the following potentials.
- 1 The electromagnetic Coulomb potential  $V_C^{ij}$  with  $Z$  being the charge number of the particles,  $e$  the elementary charge and  $|\mathbf{r}_i - \mathbf{r}_j|$  their relative distance:

$$V_C^{ij} = \frac{Z_i Z_j e^2}{|\mathbf{r}_i - \mathbf{r}_j|} \quad (4)$$

- 2 The strong force Yukawa potential  $V_Y^{ij}$  with  $V_0^Y = -0.498$  MeV and  $\gamma_Y = 1.4$  fm:

$$V_Y^{ij} = V_0^Y \cdot \frac{\exp(-|\mathbf{r}_i - \mathbf{r}_j|/\gamma_Y)}{|\mathbf{r}_i - \mathbf{r}_j|} \quad (5)$$

# The equation of state in UrQMD

- 3 The hadronic Skyrme potential  $V_{Sk}$  to change the stiffness of the EoS with  $\rho_{int}$  the baryon density  $\rho_0$  being the ground state baryon density:

$$V_{Sk} = \alpha \cdot \left( \frac{\rho_{int}}{\rho_0} \right) + \beta \cdot \left( \frac{\rho_{int}}{\rho_0} \right)^\gamma \quad (6)$$

Parameters	hard EoS
$\alpha$ [MeV]	-124
$\beta$ [MeV]	71
$\gamma$	2.00

Table: Parameters used in the UrQMD Skyrme potential

P.Hillmann et al., J.Phys. G45 (2018) no.8, 085101 (2018-06-25)

# Deuteron formation via coalescence

- Deuterons are formed via phase-space coalescence.
- protons and neutrons are boosted into their two-particle resframe.
- If the relative distance  $\Delta r \leq 3.575$  fm and the relative momentum  $\Delta p \leq 0.285$  GeV a deuteron is formed with the probability of 3/8 (spin-isospin coupling).

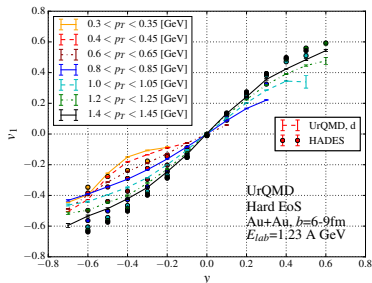
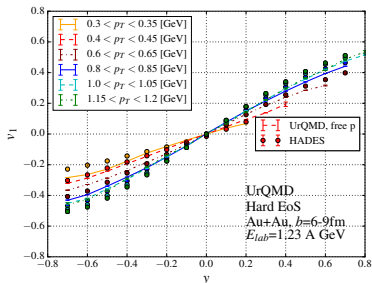
S.Sombun et al., Phys.Rev. C99 (2019) no.1, 014901 (2019-01-10)

# Outline for section 3

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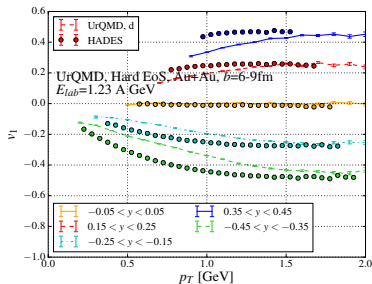
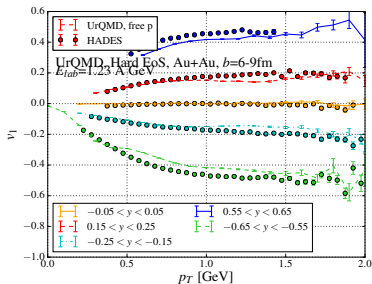
# Directed flow

HADES Data: B. Kardan et al., PoS CPOD2017 (2018) 049 and Nucl.Phys. A982 (2019) 431-434



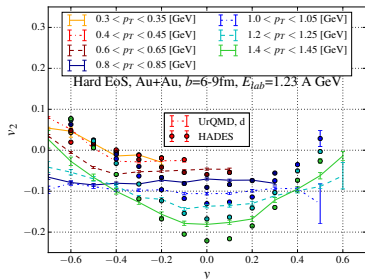
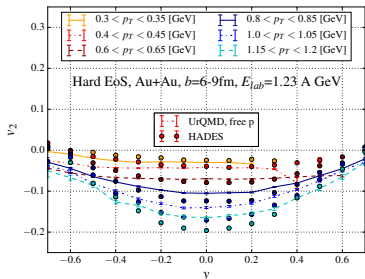
- Strong dependence on rapidity.
- d flow slope is more positive.
- Good agreement with experimental data.

# Directed flow



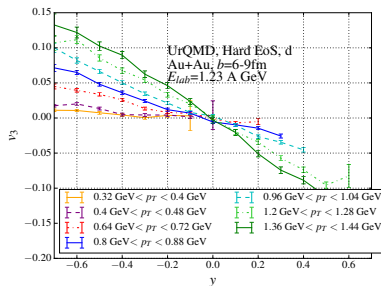
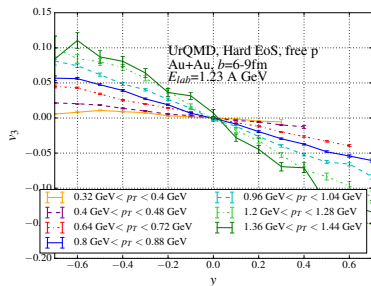
- Strong transverse momentum dependence.
- More positive flow for deuterons due to higher momentum of deuterons.
- Good agreement with experimental data.

# Elliptic flow



- Strong rapidity dependence.
- More positive flow of d due to higher momentum.
- Good agreement with experimental data.

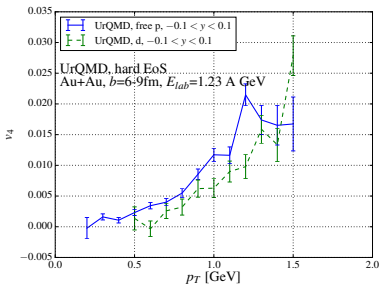
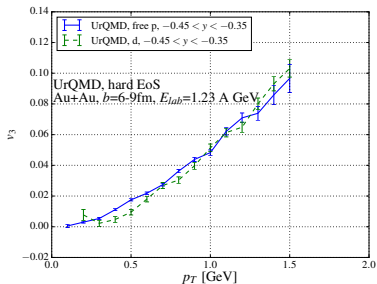
# Triangular flow



- Strong rapidity dependence.
- Flow of protons and deuterons behave similar.

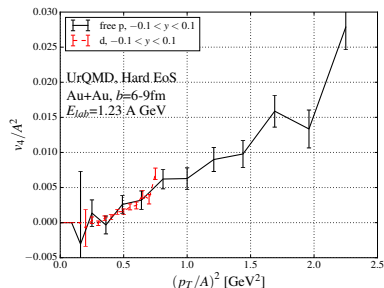
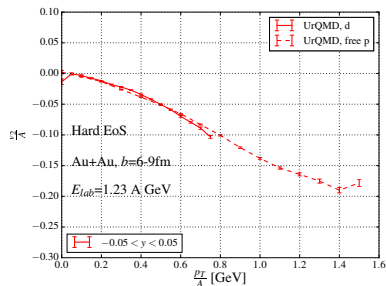


# Triangular flow



- Strong transverse momentum dependence.
- Non-zero higher order flow components with respect to reaction plane for p and d indicate interplay of initial and expansion stage of the system.

# Mass number scaling at HADES energies



- Strong transverse momentum dependence.
- Mass number scaling observable for even flow components.
- Direct consequence of coalescence.

# Outline for section 4

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- UrQMD including a hard equation of state was used to measure the collective flow of protons and deuterons in Au+Au collisions at 1.23 A GeV.
- The calculations agree with the data of the HADES experiment for both protons and deuterons.
- The  $v_3$  and  $v_4 \neq 0$  with respect to the reaction-plane indicate an interplay of initial stage and expansion stage of the fireball.
- Cluster forming nucleons have a large effect to the collective proton flow which also results in a direct mass number scaling of  $v_2(p_T)$  for the simulation.