The possibility for the experimental distinction of the different EoS at NICA energies

HMEC 17.09.2019 Dubna Rogachevsky O. JINR





MPD TPC







TPC outer walls & membrane

MPD TOF







MPD FHCal







MPD ECal







~ <u>43000</u> ECAL modules







trim coil





Solenoid assembling





BM@N

Next run (2020?)





Collaboration, Letter of intent, CDR, detectors development are started





- ★ UrQMD Prog. Part. Nucl. Phys. 41 (1998) 225
- ★ HIJING: Phys. Rev. D 44 (1991) 3501
- **AMPT:** Phys. Rev. C 72 (2005) 064901
- **Hybrid UrQMD:** Phys. Rev. C 78 (2008) 044901
- **PHSD:** Nucl. Phys. A 856 (2011) 162
- ★ VHLLE: Comput. Phys. Commun. 185 (2014) 3016
- **DC-QGSM:** will be published soon
- * 3 Fluid Dynamics: Phys. Rev. C 73 (2006) 044904
- **Theseus:** Phys. Rev. C 94 (2016) 044917

What is the QGP?



What is the elephant?





3FD model

- Distributions are separated in momentum space
 ⇒ different fluids
- Leading particles carry baryon charge
 - \Rightarrow 2 baryon-rich fluids: projectile-like and target-like

At high incident energies ($E_{lab} \gtrsim 10A \text{ GeV}$)

Produced particles populate mid-rapidity ⇒ fireball fluid





3FD: hydro model with different EOS

To quantify the "peak-dip-peak-dip" irregularity, net-proton rapidity distributions are fitted by (a, y_s and w_s are parameters of the fit)

$$\frac{dN}{dy} = a \left(\exp \left\{ -(1/w_s) \cosh(y - y_{cm} - y_s) \right\} + \exp \left\{ -(1/w_s) \cosh(y - y_{cm} + y_s) \right\} \right)$$

A reduced curvature of the spectrum at midrapidity



THESEUS: hydro model with different EOS and particlization

Three-fluid Hydrodynamics-based Event Simulator Extended by UrQMD final State interactions

Event simulation based on three-fluid hydrodynamics for collisions at energies available at the Dubna Nuclotron-based Ion Collider Facility and at the Facility for Antiproton and Ion Research in Darmstadt

P. Batyuk, D. Blaschke, M. Bleicher, Yu. B. Ivanov, Iu. Karpenko, S. Merts, M. Nahrgang, H. Petersen, and O. Rogachevsky

Phys. Rev. C 94, 044917 - Published 28 October 2016

Int.	AuAu								
√s (GeV)	4.3	4.7	5.6	6.4	7.7	11.5	19.6	27	39
EoS	hadron, 2 phase, crossover								
b(Fm)	2, 6, 11								

C_y with THESEUS implementation



Can be distinguishable with MPD at NICA

Deterministic chaos

Collections of small entities (particles or whatever) behave haphazardly, even though physical laws govern the particles individually



STAR AuAu √s=200 GeV

A system may be perfectly deterministic in principle but its behavior is completely unpredictable in practice. This phenomenon was called **deterministic chaos**.

Deterministic chaos - chaos results from deterministic process

R. Hagedorn "Remarks on the Thermodynamical Model of Strong Interactions" Nucl. Phys. B (1970).

A firebal is

a statistical equilibrium of undetermined numbers of fireballs, each of which, in turn, is considered to be ...

= selfsimilarity

Fractal dimension

Koch's arc



The **fractal dimension** of sets observed in the dynamics can be used as quantitative measure of the chaoticity

 $\boldsymbol{D} = \lim_{r \to 0} \frac{\log N(r)}{\log (1/r)}$

r - scale N(r) - number of elements in fractal at given scale

$$\boldsymbol{D}^{Koch's\,arc} = \lim_{n \to \infty} \frac{\log 4^n}{\log 3^n} = \frac{\log 4}{\log 3} = 1.261...$$

Box counting



 $N(\epsilon)$ is the number of boxes of side length ϵ required to cover the set.

STAR AuAu ηP_T space @ $\sqrt{s}=200$ GeV



Fractal dimension in ηp_{τ} space (R.O. ICHEP 2006)

Disappearance of away side jet





Ridge @ LHC pp & 7 TeV

Ridge correlation structure in high multiplicity pp collisions with CMS arXiv:1107.2196



Two-dimensional (2-D) per-trigger-particle associated yield of charged hadrons as a function of $\Delta \eta$ and $\Delta \phi$ with jet peak cutoff for better demonstration of the ridge from high multiplicity (N \geq 110) pp collisions at $\sqrt{s} = 7$ TeV, for:

$$2 < p_T^{trig} < 3 \text{ GeV/c}$$
 and $1 < p_T^{assoc} < 2 \text{ GeV/c}$
 $5 < p_T^{trig} < 6 \text{ GeV/c}$ and $1 < p_T^{assoc} < 2 \text{ GeV/c}$

Inflection point

Pythia v.6-424

10K events √s =7 TeV All charged particles







(dbyb)/M/b(dydp)	CC 4.2 A GeV/c
	1 1.5 2 2.5 Pi (GeV/c)
Le	evy distribution
d^2N	В
$\overline{2\pi p_t dp_t dy} =$	$\frac{1}{(1+(m_t-m_0)/nT)^n}$

	parameter value					
	n	Т	В	χ^2/ndf		
pC	7.45 ± 1.22	$6.86e-02 \pm 6.04e-03$	$2.29e+04 \pm 2.40e+03$	0.19		
dC	6.68 ± 1.10	$6.63e-02 \pm 6.78e-03$	$1.85e+04 \pm 2.31e+03$	0.19		
αC	6.59 ± 0.57	$7.08e-02 \pm 3.66e-03$	$6.10e+04 \pm 3.70e+03$	1.20		
CC	6.84 ± 0.39	$7.69e-02 \pm 2.39e-03$	$1.30e+05 \pm 4.55e+03$	3.20		

Interaction	Number of events		
pC	5722		
dC	3826		
αC	9643		
CC	15842		



cite

P_t^{max} distributions





- Shifts with A
- Broadening with A

Higuchi's estimation of fractal dimension

Approach to an irregular time series on the basis of the fractal theory T.Higuchi Physica D 31 (1988) 277-283

We now consider a finite set of time series observations taken at a regular interval:

 $X(1), X(2), X(3), \ldots, X(N).$

From given time series, we first construct a new time series, X_k^m , defined as follows:

$$X_k^m; X(m), X(m+k), X(m+2k), \dots, X\left(m + \left[\frac{N-m}{k}\right] \cdot k\right) \quad (m = 1, 2, \dots, k),$$

where [] denotes the Gauss' notation and both k and m are integers. m and k indicate the initial time and the interval time, respectively. For a time interval equal to k, we get k sets of new time series. In the case of k = 3 and N = 100, three time series obtained by the above process are described as follows:

 X_3^1 ; X(1), X(4), X(7),..., X(97), X(100), X_3^2 ; X(2), X(5), X(8),..., X(98), X_3^3 ; X(3), X(6), X(9),..., X(99).

Higuchi's method

We define the length of the curve, X_k^m , as follows:

$$L_m(k) = \left\{ \left(\sum_{i=1}^{\left\lfloor \frac{N-m}{k} \right\rfloor} |X(m+ik) - X(m+(i-1)\cdot k)| \right) \frac{N-1}{\left\lfloor \frac{N-m}{k} \right\rfloor \cdot k} \right\} \right/ k.$$

The term, $N - 1/[(N-m)/k] \cdot k$ represents the normalization factor for the curve length of subset time series. We define the length of the curve for the time interval k, $\langle L(k) \rangle$, as the average value over k sets of $L_m(k)$. If $\langle L(k) \rangle \propto k^{-D}$, then the curve is fractal with the dimension D.



Yet another signature of EOS with THESEUS

AuAu √s = 11.5 GeV



Summary

Reduced curvature of net-proton rapidity distribution can be used as the signuture of different EoS for nuclear matter

Fractal dimension for the multiparticle events is sensitive to the global structure of these events

Fractal dimension analysis is useful to understand features in events

STAR BES I results

Ridge effect

B. Abelev et al., Phys. Rev. C80, 064912 (2009).



S. Jowzaee, Quark Matter 2017



