

# Rare decays of heavy mesons in covariant confined quark model

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# Overview

## Motivation

### Covariant quark model

- Lagrangian
- Compositeness condition
- Computational methods
- Infrared confinement

### Decays $B \rightarrow K^* \mu\mu$ and $B_s \rightarrow \phi \mu\mu$

- Form factors
- Differential decay distribution
- Observables

## Results

- $B \rightarrow K^* \mu\mu$
- $B_s \rightarrow \phi \mu\mu$
- $B_s \rightarrow J/\psi + \eta^{(\prime)}$  (summary)

## Summary, outlook

# Motivation

## Theory and experiment

- Expected sensitiveness to new physics: rare flavor-changing b decays - possible manifestation of new hypothetical particles in loops of Feynman diagrams
- New high-energy and high-luminosity machines:
  - Rare b decays measured and measurements still ongoing, data amount increasing.
  - Angular information nowadays available for selected processes.
  - Standard model confirmed with some tensions ( $\sim 3\sigma$ ).

## Hadronic effects – quark confinement

- Source of theoretical uncertainty (beyond applicability of the pQCD).
- Alternatives with small model dependence (lattice QCD, ChPT) still not “at the point”.
- Also “safe” observables keep some model (i.e. form factor) dependence.

## Confined covariant quark model

- Lagrangian-based approach to hadronic interactions with full Lorentz invariance.
- Applicable to different multiquark states (mesons/baryons/tetraquarks).
- Limited number of free parameters, standard QFT computational techniques, convincing results.

# Mesons in covariant quark model

## Lagrangian

$$L_{\text{int}} = g_H \cdot H(x) \cdot J_H(x)$$

$$J_M(x) = \int dx_1 \int dx_2 F_M(x, x_1, x_2) \cdot \bar{q}_{f_1}^a(x_1) \Gamma_M q_{f_2}^a(x_2)$$

$$F_H(x, x_1, \dots, x_n) = \delta \left( x - \sum_{i=1}^n w_i x_i \right) \Phi_H \left( \sum_{i < j} ((x_i - x_j)^2) \right)$$

$$w_i = m_i / \sum_{j=1}^n m_j \quad \Phi_H(-k^2) = \exp(k^2/\Lambda_H^2)$$

## Free parameters

- Process with N hadrons  $\rightarrow$  N+5 parameters (at most).
  - Four constituent quark masses [ $m_{u,d} = 0.235 \text{ GeV}$ ,  $m_s = 0.424 \text{ GeV}$ ,  $m_c = 2.16 \text{ GeV}$ ,  $m_b = 5.09 \text{ GeV}$ ]
  - N hadron-size related parameters [ $\Lambda_{B_s} = 2.05 \text{ GeV}$ ,  $\Lambda_B = 1.96 \text{ GeV}$ ,  $\Lambda_{K^*} = 0.75 \text{ GeV}$ ,  $\Lambda_\phi = 0.88 \text{ GeV}$ ]
  - One universal infrared cutoff [ $\lambda_{\text{cut-off}} = 0.181 \text{ GeV}$ ]
- Numerical values extracted from fits to experimental data.
- Coupling constants  $g_H$  determined using so-called compositeness condition.

# Compositeness condition

## Quarks and hadrons:

- Interaction Lagrangian: hadrons and quarks are elementary.
- Nature: hadrons made up of quarks.

## Appropriate description of bound states

- Addressed already in sixties
  - A. Salam, Nuovo Cim. 25, 224 (1962)
  - S. Weinberg, Phys. Rev. 130, 776 (1963)
- Renormalization constant  $Z_H^{1/2}$  can be interpreted as the matrix element between the physical state and the corresponding bare state.

$$Z_H^{1/2} = \langle H_{\text{bare}} | H_{\text{dressed}} \rangle = 0 \Rightarrow$$

physical state does not contain bare state and is therefore properly described as a bound state.

## Compositeness condition (covariant quark model):

$$Z_H = 1 - \frac{3g_H^2}{4\pi^2} \tilde{\Pi}_H' (m_H^2) = 0$$

# Computation methods

## General form of Feynman diagram

- $j$  external momenta
- $n$  quark propagators
- $l$  loop integrations
- $m$  vertices

$$\Pi(p_1, \dots, p_j) = \int [d^4 k]^\ell \prod_{i_1=1}^m \Phi_{i_1+n}(-K_{i_1+n}^2) \prod_{i_3=1}^n S_{i_3}(\tilde{k}_{i_3} + \tilde{p}_{i_3})$$

$$K_{i_1+n}^2 = \sum_{i_2} (\tilde{k}_{i_1+n}^{(i_2)} + \tilde{p}_{i_1+n}^{(i_2)})^2$$

- $\tilde{k}_i$ : linear combination of loop momenta  $k_i$
- $\tilde{p}_i$ : linear combination of external momenta  $p_i$

## Schwinger representation of the quark propagator

$$\tilde{S}_q(k) = \left(m + \hat{k}\right) \int_0^\infty d\alpha e^{-\alpha(m^2 - k^2)}$$

## Calculational techniques

- Loop momenta integration

$$\int d^4 k P(k) e^{2kr} = \int d^4 k P\left(\frac{1}{2} \frac{\partial}{\partial r}\right) e^{2kr} = P\left(\frac{1}{2} \frac{\partial}{\partial r}\right) \int d^4 k e^{2kr}$$

- Operator evaluation simplification

$$\int_0^\infty d^n \alpha P\left(\frac{1}{2} \frac{\partial}{\partial r}\right) e^{-\frac{r^2}{a}} = \int_0^\infty d^n \alpha e^{-\frac{r^2}{a}} P\left(\frac{1}{2} \frac{\partial}{\partial r} - \frac{r}{a}\right), \quad r = r(\alpha_i), \quad a = a(\Lambda_H, \alpha_i)$$

# Infrared confinement

## Confinement of quarks

- Light mesons:  $m_M < \sum m_q \Rightarrow$  stable hadrons.
- Heavy mesons:  $m_M > \sum m_q \Rightarrow$  unstable hadrons  $\rightarrow$  modification needed.

## Infrared cutoff implementation:

- Unity in form of  $\delta$ -function introduced  $\Rightarrow$  single cut-off parameter.

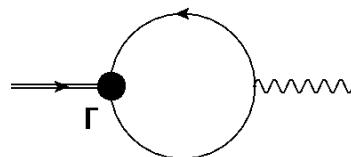
$$1 = \int_0^\infty dt \delta(t - \sum_{i=1}^n \alpha_i)$$
$$\Pi = \int_0^\infty d^n \alpha F(\alpha_1, \dots, \alpha_n) \xrightarrow{\downarrow} \Pi = \int_0^{\infty \rightarrow 1/\lambda^2} dt t^{n-1} \int_0^1 d^n \alpha \delta\left(1 - \sum_{i=1}^n \alpha_i\right) F(t\alpha_1, \dots, t\alpha_n)$$

- Universal value  $\lambda_{\text{cut-off}} = 0.181$  established for all processes.
- $\Pi$  becomes a smooth function, thresholds in the quark loop diagrams and corresponding branch points are removed.

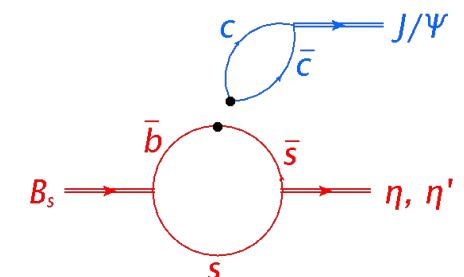
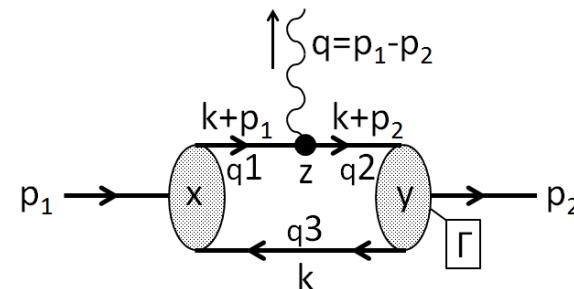
# Form factors and computations

## Intermediate objects

- Decay constants



- Form factors  
(diagram factorization)



## Flavor transition

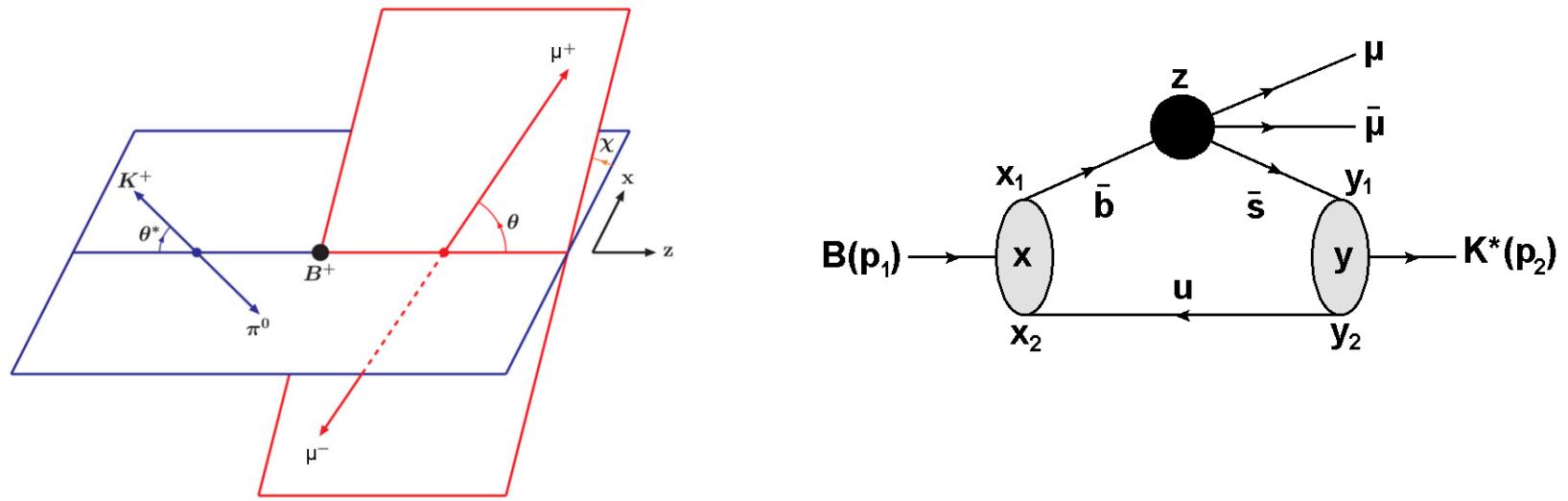
- Effective theory with Wilson coefficients

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} \lambda_t \sum_{i=1}^{10} C_i(\mu) O_i(\mu)$$

## Numerical computations

- Schwinger parameter integration done numerically.
- Programming and numerical procedures done twice independently: avoid errors and estimate numerical effects.  
(*FORTRAN: NAG integration libraries, Java: integration libraries by Torsten Nahm*).

# $B \rightarrow K^* + 2\mu$ and $B_s \rightarrow \varphi + 2\mu$ in Standard Model



**Kinematics: cascade decays considered**

- $B \rightarrow K^*(\rightarrow K\pi) + 2\mu$ .
- $B_s \rightarrow \varphi(\rightarrow KK) + 2\mu$ .

**The two processes**

- Same quantum numbers of interacting particles.
- Differ (only) in spectator quark.

# Form factors

Decay characterized in SM by 7 form factors

- Four (axial)vector form factors

$$\begin{aligned} \langle V_{[\bar{q}_3, q_2]}(p_2, \epsilon_2) | \bar{q}_2 O^\mu q_1 | P_{[\bar{q}_3, q_1]}(p_1) \rangle = & \frac{\epsilon_\nu^\dagger}{m_1 + m_2} [ -g^{\mu\nu} P \cdot q \textcolor{red}{A}_0(q^2) + P^\mu P^\nu \textcolor{red}{A}_+(q^2) \\ & + q^\mu P^\nu \textcolor{red}{A}_-(q^2) + i\varepsilon^{\mu\nu\alpha\beta} P_\alpha q_\beta \textcolor{red}{V}(q^2) ] \end{aligned}$$

- Three tensor form factors

$$\begin{aligned} \langle V_{[\bar{q}_3, q_2]}(p_2, \epsilon_2) | \bar{q}_2 [\sigma^{\mu\nu} q_\nu (1 + \gamma^5)] q_1 | P_{[\bar{q}_3, q_1]}(p_1) \rangle = & \epsilon_\nu^\dagger \left[ - \left( g^{\mu\nu} - \frac{q_\mu q_\nu}{q^2} \right) P \cdot q \textcolor{red}{a}_0(q^2) \right. \\ & \left. + \left( P^\mu P^\nu - q^\mu P^\nu \frac{p \cdot q}{q^2} \right) \textcolor{red}{a}_+(q^2) + i\varepsilon^{\mu\nu\alpha\beta} P_\alpha q_\beta \textcolor{red}{g}(q^2) \right] \end{aligned}$$

# Helicity amplitudes

## Helicity formalism

- Helicity basis – hadronic and leptonic tensor evaluated in different frames.
- Hadronic tensor parametrized through (new) form factors.
- Flavor changing information enters in the form factor redefinition.

$$L^{(k)}(m, n) = \epsilon^\mu(m)\epsilon^{\dagger\nu}(n)L_{\mu\nu}^{(k)}$$

$$H^{ij}(m, n) = \epsilon^{\dagger\mu}(m)\epsilon^\nu(n)H_{\mu\nu}^{ij}$$

$$H^{ij}(m, n) = H^i(m)H^{\dagger j}(n)$$

$$V^{(1)} = C_9^{\text{eff}} V + C_7^{\text{eff}} g \frac{2\bar{m}_b(m_1 + m_2)}{q^2},$$

$$A_0^{(1)} = C_9^{\text{eff}} A_0 + C_7^{\text{eff}} a_0 \frac{2\bar{m}_b(m_1 + m_2)}{q^2},$$

$$A_+^{(1)} = C_9^{\text{eff}} A_+ + C_7^{\text{eff}} a_+ \frac{2\bar{m}_b(m_1 + m_2)}{q^2},$$

$$A_-^{(1)} = C_9^{\text{eff}} A_- + C_7^{\text{eff}} (a_0 - a_+) \frac{2\bar{m}_b(m_1 + m_2)}{q^2} \frac{Pq}{q^2},$$

$$V^{(2)} = C_{10} V, \quad A_0^{(2)} = C_{10} A_0, \quad A_\pm^{(2)} = C_{10} A_\pm.$$

# Helicity amplitudes

## Helicity amplitudes

$$H^i(t) = \frac{1}{m_1 + m_2} \frac{m_1}{m_2} \frac{|\mathbf{p}_2|}{\sqrt{q^2}} [Pq(-A_0^i + A_+^i) + q^2 A_-^i]$$

$$H^i(\pm) = \frac{1}{m_1 + m_2} (-PqA_0^i \pm 2m_1 |\mathbf{p}_2| V^i)$$

$$H^i(0) = \frac{1}{m_1 + m_2} \frac{1}{2m_2 \sqrt{q^2}} \times [-Pq(m_1^2 - m_2^2 - q^2) A_0^i + 4m_1^2 |\mathbf{p}_2|^2 A_+^i]$$

## Full differential formula:

- Narrow-width approximation for the cascade decay is assumed.
- Symbols

→  $H_X^{ij}$  – bilinear combination of  $H^i$

$$\frac{d\Gamma_X^{ij}}{dq^2} = \frac{G_F^2}{(2\pi)^3} \left( \frac{\alpha |\lambda_t|}{2\pi} \right)^2 \frac{|\mathbf{p}_2| q^2 v}{12m_1^2} H_X^{ij} \quad \frac{d\tilde{\Gamma}_X^{ij}}{dq^2} = \frac{2m_\mu^2}{q^2} \frac{d\Gamma_X^{ij}}{dq^2}$$

# Full differential distribution

$$\begin{aligned}
\frac{d\Gamma(B \rightarrow K^*(\rightarrow K\pi) \bar{\mu}\mu)}{dq^2 d(\cos\theta) (d\chi/2\pi) d(\cos\theta^*)} = & \text{Br}(K^* \rightarrow K\pi) \times \left\{ \frac{3}{8} (1 + \cos^2\theta) \cdot \frac{3}{4} \sin^2\theta^* \cdot \frac{1}{2} \left( \frac{d\Gamma_{U_{11}}}{dq^2} + \frac{d\Gamma_{U_{22}}}{dq^2} \right) \right. \\
& + \frac{3}{4} \sin^2\theta \cdot \frac{3}{2} \cos^2\theta^* \cdot \frac{1}{2} \left( \frac{d\Gamma_{L_{11}}}{dq^2} + \frac{d\Gamma_{L_{22}}}{dq^2} \right) - \frac{3}{4} \sin^2\theta \cdot \cos 2\chi \cdot \frac{3}{4} \sin^2\theta^* \cdot \frac{1}{2} \left( \frac{d\Gamma_{T_{11}}}{dq^2} + \frac{d\Gamma_{T_{22}}}{dq^2} \right) \\
& - \frac{9}{16} \sin 2\theta \cdot \cos\chi \cdot \sin 2\theta^* \cdot \frac{1}{2} \left( \frac{d\Gamma_{I_{11}}}{dq^2} + \frac{d\Gamma_{I_{22}}}{dq^2} \right) + v \cdot \left[ -\frac{3}{4} \cos\theta \cdot \frac{3}{4} \sin^2\theta^* \cdot \frac{d\Gamma_{P_{12}}}{dq^2} \right. \\
& + \frac{9}{8} \sin\theta \cdot \cos\chi \cdot \sin 2\theta^* \cdot \frac{1}{2} \left( \frac{d\Gamma_{A_{12}}}{dq^2} + \frac{d\Gamma_{A_{21}}}{dq^2} \right) - \frac{9}{16} \sin\theta \cdot \sin\chi \cdot \sin 2\theta^* \cdot \left( \frac{d\Gamma_{II_{12}}}{dq^2} + \frac{d\Gamma_{II_{21}}}{dq^2} \right) \\
& + \frac{9}{32} \sin 2\theta \cdot \sin\chi \cdot \sin 2\theta^* \cdot \left( \frac{d\Gamma_{IA_{11}}}{dq^2} + \frac{d\Gamma_{IA_{22}}}{dq^2} \right) + \frac{9}{32} \sin^2\theta \cdot \sin 2\chi \cdot \sin^2\theta^* \cdot \left( \frac{d\Gamma_{IT_{11}}}{dq^2} + \frac{d\Gamma_{IT_{22}}}{dq^2} \right) \\
& + \frac{3}{4} \sin^2\theta \cdot \frac{3}{4} \sin^2\theta^* \cdot \frac{1}{2} \cdot \frac{d\tilde{\Gamma}_{U_{11}}}{dq^2} - \frac{3}{8} (1 + \cos^2\theta) \cdot \frac{3}{4} \sin^2\theta^* \cdot \frac{d\tilde{\Gamma}_{U_{22}}}{dq^2} \\
& + \frac{3}{2} \cos^2\theta \cdot \frac{3}{2} \cos^2\theta^* \cdot \frac{1}{2} \cdot \frac{d\tilde{\Gamma}_{L_{11}}}{dq^2} - \frac{3}{4} \sin^2\theta \cdot \frac{3}{2} \cos^2\theta^* \cdot \frac{d\tilde{\Gamma}_{L_{22}}}{dq^2} \\
& + \frac{3}{4} \sin^2\theta \cdot \cos 2\chi \cdot \frac{3}{4} \sin^2\theta^* \cdot \left( \frac{d\tilde{\Gamma}_{T_{11}}}{dq^2} + \frac{d\tilde{\Gamma}_{T_{22}}}{dq^2} \right) + \frac{9}{8} \sin 2\theta \cdot \cos\chi \cdot \sin 2\theta^* \cdot \frac{1}{2} \left( \frac{d\tilde{\Gamma}_{I_{11}}}{dq^2} + \frac{d\tilde{\Gamma}_{I_{22}}}{dq^2} \right) \\
& + \frac{3}{2} \cos^2\theta^* \cdot \frac{1}{4} \frac{d\tilde{\Gamma}_{S_{22}}}{dq^2} - \frac{9}{16}, \sin 2\theta \cdot \sin\chi \cdot \sin 2\theta^* \cdot \left( \frac{d\Gamma_{IA_{11}}}{dq^2} + \frac{d\Gamma_{IA_{22}}}{dq^2} \right) \\
& \left. - \frac{9}{16} \sin^2\theta \cdot \sin 2\chi \cdot \sin^2\theta^* \cdot \left( \frac{d\Gamma_{IT_{11}}}{dq^2} + \frac{d\Gamma_{IT_{22}}}{dq^2} \right) \right\}
\end{aligned}$$

# Alternative expression

## Expression

- Often used by other authors
- Consistency checked

$$\frac{1}{d\Gamma/dq^2} \frac{d^3\Gamma}{dcos\theta_l \, dcos\theta_k \, d\Phi} = \frac{9}{32\pi} \left[ \begin{aligned} & \frac{3}{4}(1 - F_L) \sin^2 \theta_k + F_L \cos^2 \theta_k + \frac{1}{4}(1 - F_L) \sin^2 \theta_k \cos 2\theta_l \\ & - F_L \cos^2 \theta_k \cos 2\theta_l + S_3 \sin^2 \theta_k \sin^2 \theta_l \cos 2\Phi \\ & + S_4 \sin 2\theta_k \sin 2\theta_l \cos \Phi + S_5 \sin 2\theta_k \sin \theta_l \cos \Phi \\ & + S_6 \sin^2 \theta_k \cos \theta_l + S_7 \sin 2\theta_k \sin \theta_l \sin \Phi \\ & + S_8 \sin 2\theta_k \sin 2\theta_l \sin \Phi + S_9 \sin^2 \theta_k \sin^2 \theta_l \sin 2\Phi \end{aligned} \right]$$

# Observables

## Searching for

- Small model dependence (on hadronic physics, form factors).
- Sensitivity to new physics (at short distance).
- Experimental accessibility (clear signature, high cross-section, small backgrounds).
- Ratios, asymmetries, asymmetry ratios...

## Observables for $B \rightarrow K^* \mu^+ \mu^-$ and $B_s \rightarrow \varphi(\rightarrow KK) + 2\mu$ .

- Comparison with experiment: separate integration (numerator/denominator) over relevant  $q^2$  range (bin size).

$$F_T = 1 - F_L$$

$$P_{1,2,3} = c_{1,2,3} \frac{S_{3,6,9}}{F_T}$$

$$A_{FB} = -\frac{3}{4} S_6$$

$$P'_{4,5,6} = c_{4,5,6} \frac{S_{4,5,7}}{\sqrt{F_T F_L}}$$

# Binned observables in helicity approach

$$\frac{d\Gamma}{dq^2} = \frac{1}{2} \left( \frac{d\Gamma_U^{11}}{dq^2} + \frac{d\Gamma_U^{22}}{dq^2} + \frac{d\Gamma_L^{11}}{dq^2} + \frac{d\Gamma_L^{22}}{dq^2} \right) + \frac{1}{2} \frac{d\tilde{\Gamma}_U^{11}}{dq^2} - \frac{d\tilde{\Gamma}_U^{22}}{dq^2} + \frac{1}{2} \frac{d\tilde{\Gamma}_L^{11}}{dq^2} - \frac{d\tilde{\Gamma}_L^{22}}{dq^2} + \frac{3}{2} \frac{d\tilde{\Gamma}_S^{22}}{dq^2}$$

$$F_L = \frac{\int dq^2}{\int dq^2} \frac{H_L^{11} + H_L^{22}}{H_L^{11} + H_L^{22} + H_U^{11} + H_U^{22}}$$

$$A_{FB} = -\frac{3}{2} \frac{\int dq^2}{\int dq^2} \frac{H_P^{12}}{H_L^{11} + H_L^{22} + H_U^{11} + H_U^{22}}$$

$$P_1 = -2 \frac{\int dq^2}{\int dq^2} \frac{\beta_l^2 [dT^{11} + dT^{22}]}{\beta_l^2 [dU^{11} + dU^{22}]}$$

$$P_2 = -\frac{\int dq^2}{\int dq^2} \frac{\beta_l dP^{12}}{\beta_l^2 [dU^{11} + dU^{22}]}$$

$$P_3 = -\frac{\int dq^2}{\int dq^2} \frac{\beta_l^2 [dIT^{11} + dIT^{22}]}{\beta_l^2 [dU^{11} + dU^{22}]}$$

$$P'_4 = 2 \frac{\int dq^2}{N} \frac{\beta_l^2 [dI^{11} + dI^{22}]}{N}$$

$$P'_5 = -2 \frac{\int dq^2}{N} \frac{\beta_l [dA^{12} + dA^{21}]}{N}$$

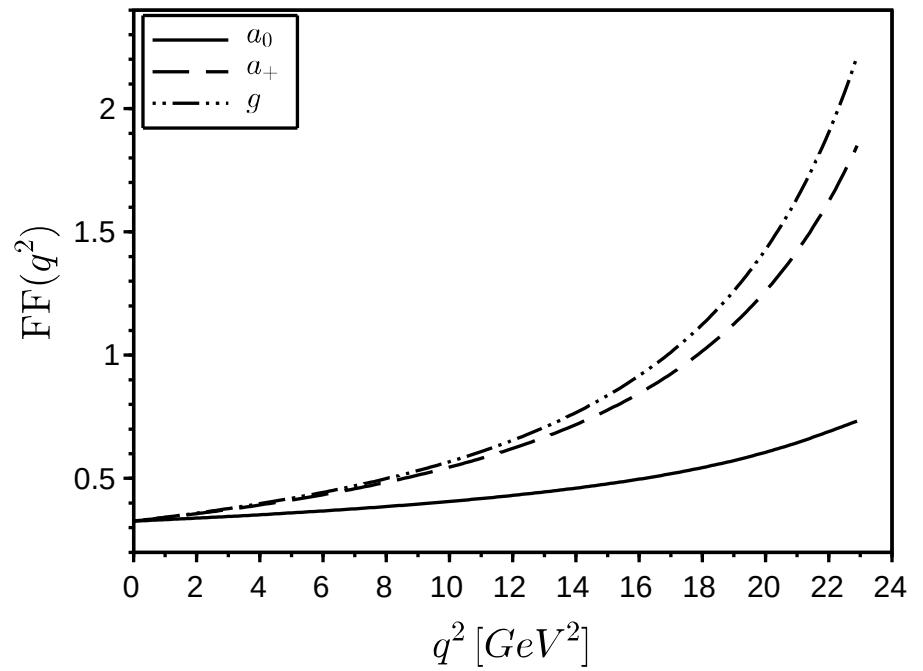
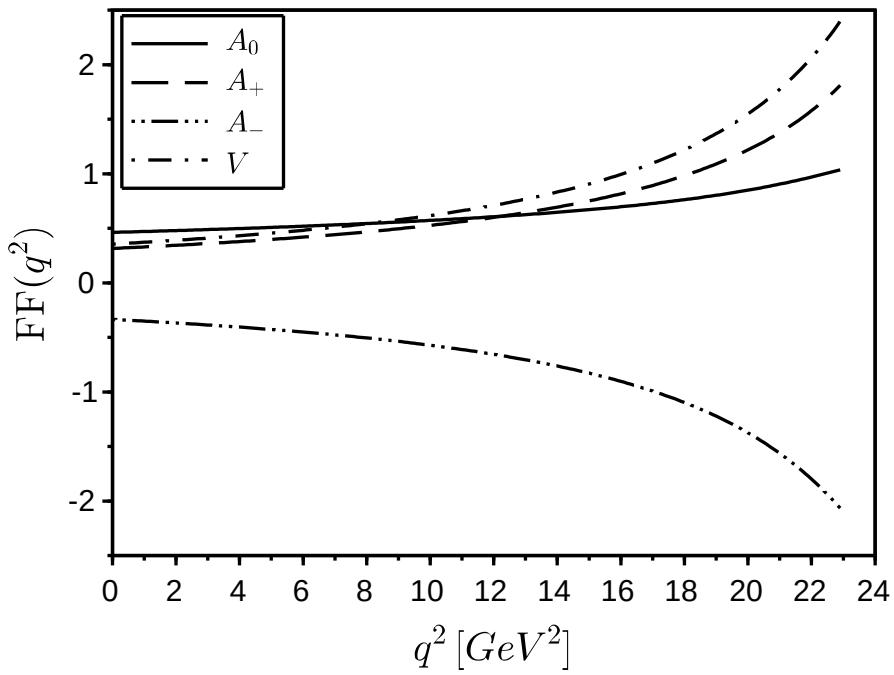
$$P_8 = 2 \frac{\int dq^2}{N} \frac{\beta_l^2 [dIA^{11} + dIA^{22}]}{N}$$

$$N = \sqrt{\int dq^2 \beta_l^2 [dU^{11} + dU^{22}] \cdot \int dq^2 \beta_l^2 [dL^{11} + dL^{22}]}$$

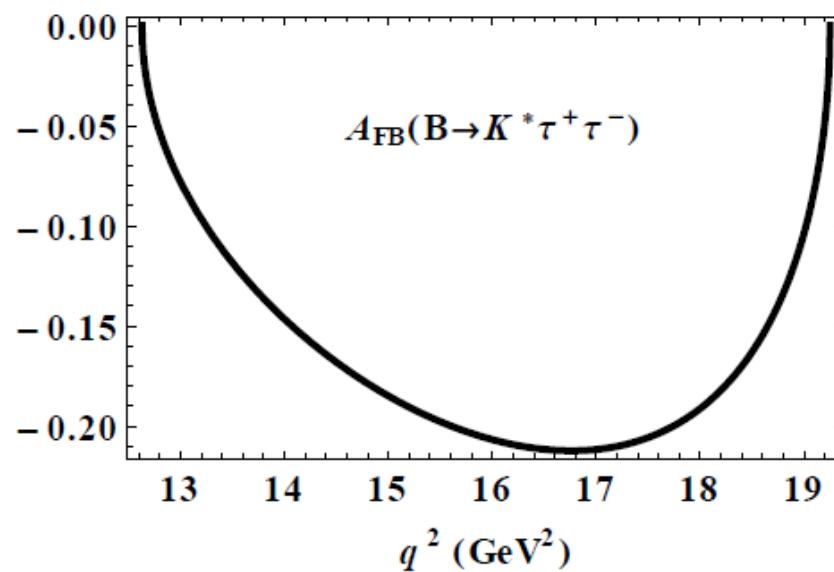
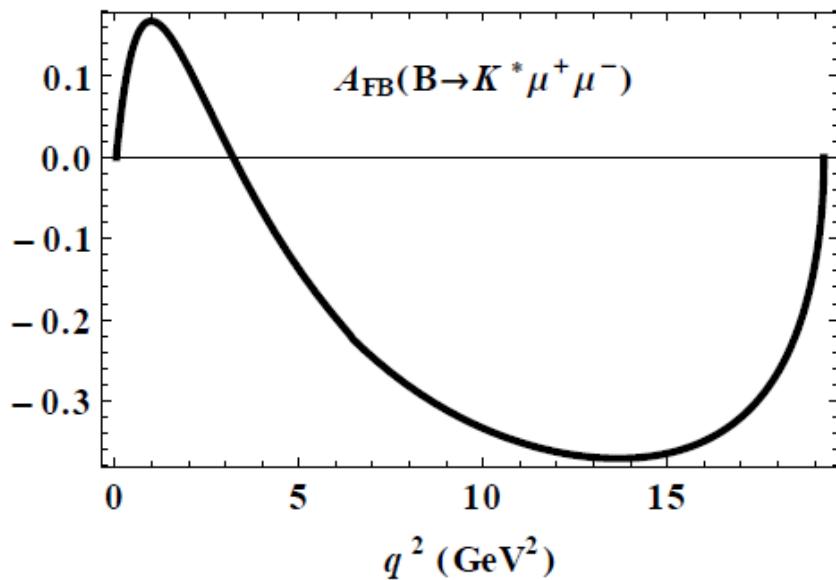
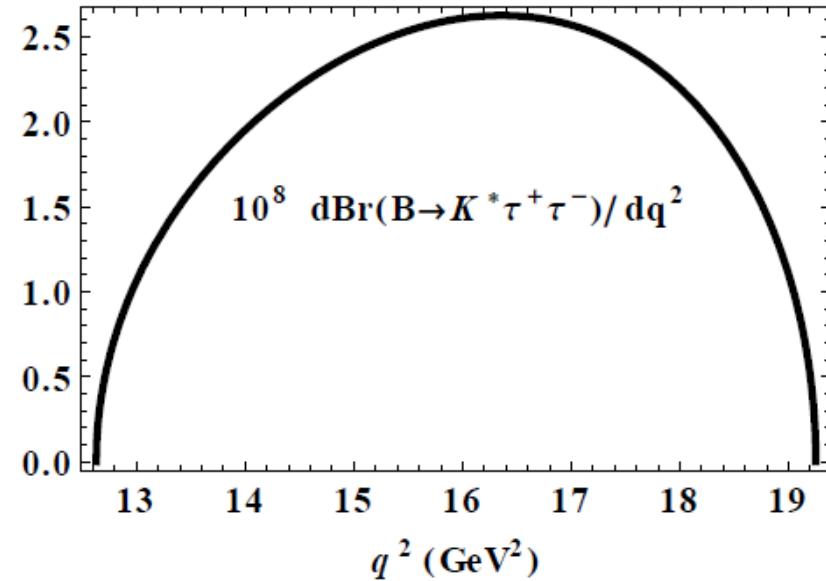
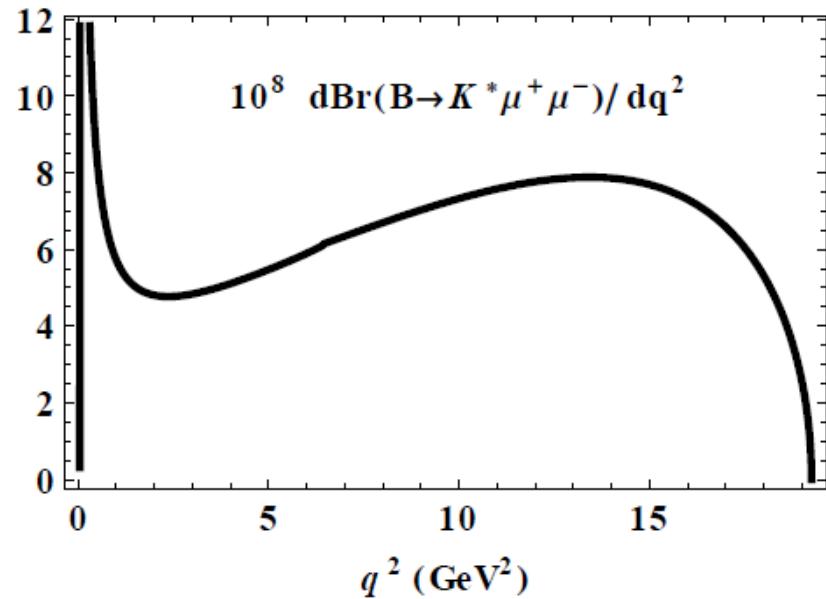
$$dX^{ij} = \frac{d\Gamma_X^{ij}}{dq^2}$$

$$\beta_l = \sqrt{\frac{1 - 4m_\mu^2}{q^2}}$$

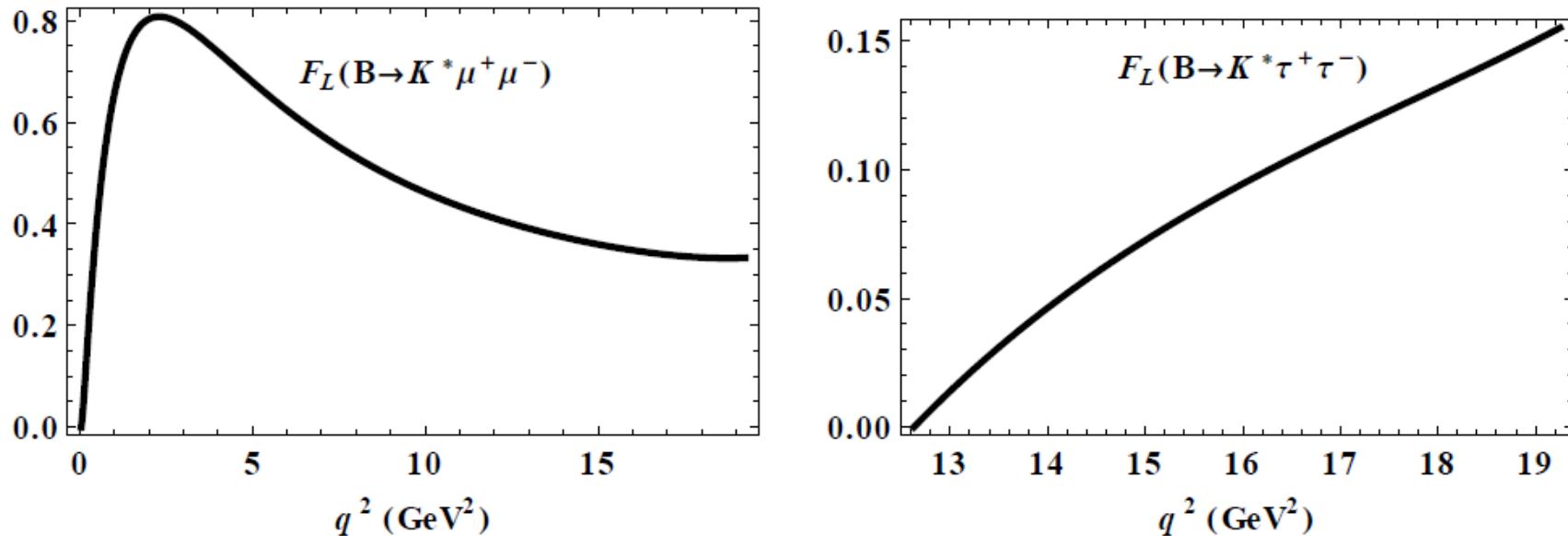
## B → K<sup>\*</sup>+2μ : form factors



## B → K\*+2μ(τ) results



## B → K<sup>\*</sup>+2μ(τ) results



	Belle [1]	LHCb [2]	CDF [3]	CQM
$\mathcal{B} \times 10^7$	$1.49_{-0.40}^{+0.45} \pm 0.12$	$0.42 \pm 0.06 \pm 0.03$	-	2.58
$A_{FB}$	$0.26_{-0.30}^{+0.27} \pm 0.07$	$-0.06_{-0.14}^{+0.13} \pm 0.04$	$0.29_{-0.23}^{+0.20} \pm 0.07$	-0.02
$F_L$	$0.67_{-0.23}^{+0.23} \pm 0.05$	$0.55 \pm 0.10 \pm 0.03$	$0.69_{-0.21}^{+0.19} \pm 0.08$	0.75

$1\text{GeV}^2 < q^2 < 6\text{GeV}^2$

[1] Belle Collaboration, Phys. Rev. Lett. 103, 171801 (2009) [[arXiv:0904.0770](https://arxiv.org/abs/0904.0770) [hep-ex]].

[2] LHCb Collaboration, Phys. Rev. Lett. 108, 181806 (2012), [LHCb-CONF-2012-008 and [arXiv:1112.3515](https://arxiv.org/abs/1112.3515) [hep-ex]].

[3] CDF Collaboration, Phys. Rev. Lett. 108, 081807 (2012) [[arXiv:1108.0695](https://arxiv.org/abs/1108.0695) [hep-ex]].

# B → K<sup>\*</sup>+2μ(τ) results

$B \rightarrow K^* \ell^+ \ell^-$

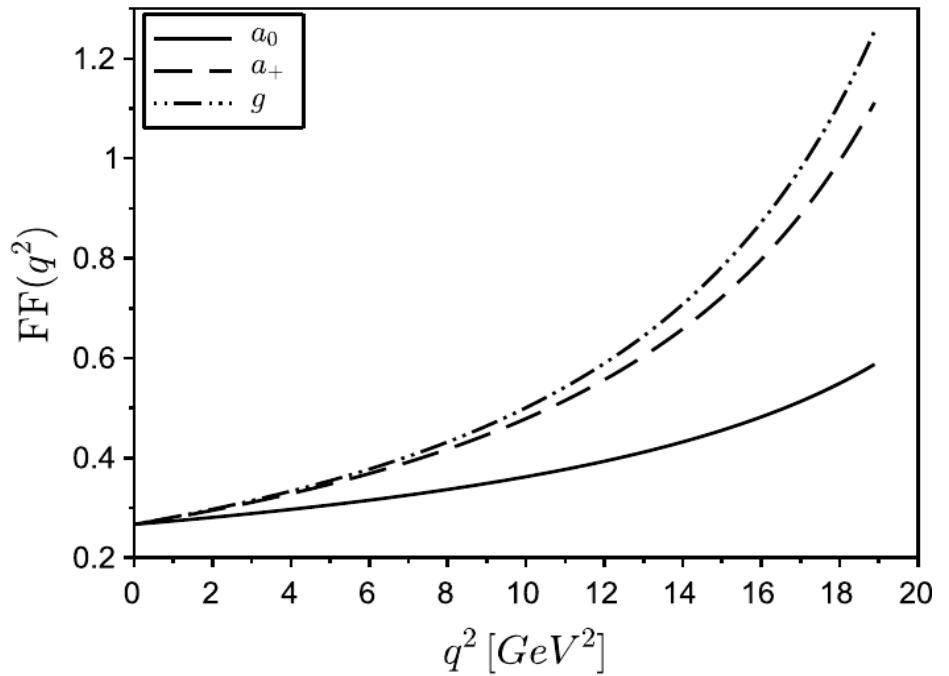
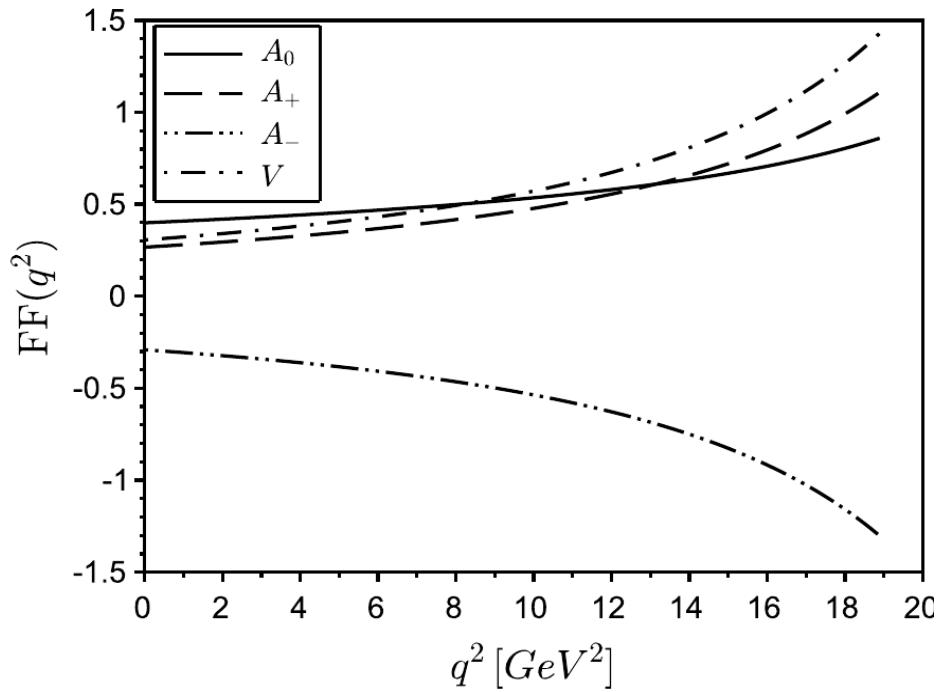
	$< A_{FB} > < F_L > < P_1 > < P_2 > < P_3 > < P'_4 > < P'_5 > < P'_8 >$							
$\mu$	-0.23	0.47	-0.48	-0.31	0.0015	1.01	-0.49	-0.010
$\tau$	-0.18	0.092	-0.74	-0.68	0.00076	1.32	-1.07	-0.0018

Bin (GeV <sup>2</sup> )	[1]	[2]	[3]	[0]	CQM
$B(10^{-7})$					
1.00–2.00	—	—	—	0.437 <sup>+0.345+0.026</sup> <sub>-0.148-0.023</sub>	0.51
0.00–2.00	1.46 <sup>+0.40</sup> <sub>-0.35</sub> ±0.11	0.61 ± 0.12 ± 0.06	—	1.446 <sup>+1.537+0.057</sup> <sub>-0.561-0.054</sub>	1.40
2.00–4.30	0.86 <sup>+0.31</sup> <sub>-0.27</sub> ±0.07	0.34 ± 0.09 ± 0.02	—	0.904 <sup>+0.664+0.061</sup> <sub>-0.314-0.055</sub>	1.13
4.30–8.68	1.37 <sup>+0.47</sup> <sub>-0.42</sub> ±0.39	0.69 ± 0.08 ± 0.05	—	2.674 <sup>+2.326+0.156</sup> <sub>-0.973-0.145</sub>	2.67
10.09–12.89	2.24 <sup>+0.44</sup> <sub>-0.40</sub> ±0.19	0.55 ± 0.09 ± 0.07	—	2.344 <sup>+2.014+0.069</sup> <sub>-1.100-0.063</sub>	2.14
14.18–16.00	1.05 <sup>+0.29</sup> <sub>-0.26</sub> ±0.08	0.63 ± 0.11 ± 0.06	—	1.290 <sup>+1.122+0.033</sup> <sub>-0.815-0.033</sub>	1.39
>16.00	2.04 <sup>+0.27</sup> <sub>-0.24</sub> ±0.16	0.50 ± 0.08 ± 0.06	—	1.450 <sup>+2.333+0.015</sup> <sub>-0.922-0.015</sub>	1.71
1.00–6.00	1.49 <sup>+0.45</sup> <sub>-0.40</sub> ±0.12	0.42 ± 0.06 ± 0.03	—	2.156 <sup>+1.646+0.138</sup> <sub>-0.742-0.123</sub>	2.58
$A_{FB}$					
1.00–2.00	—	—	—	-0.212 <sup>+0.11+0.014</sup> <sub>-0.144-0.015</sub>	-0.15
0.00–2.00	0.47 <sup>+0.26</sup> <sub>-0.22</sub> ±0.03	-0.15 ± 0.20 ± 0.06	-0.35 <sup>+0.26</sup> <sub>-0.23</sub> ±0.10	-0.136 <sup>+0.048+0.016</sup> <sub>-0.046-0.016</sub>	-0.12
2.00–4.30	0.37 <sup>+0.25</sup> <sub>-0.24</sub> ±0.10	0.05 <sup>+0.16</sup> <sub>-0.20</sub> ±0.04	0.29 <sup>+0.20</sup> <sub>-0.20</sub> ±0.15	-0.081 <sup>+0.054+0.008</sup> <sub>-0.068-0.009</sub>	-0.0059
4.30–8.68	0.45 <sup>+0.15</sup> <sub>-0.21</sub> ±0.15	0.27 <sup>+0.06</sup> <sub>-0.08</sub> ±0.02	0.01 <sup>+0.20</sup> <sub>-0.20</sub> ±0.09	0.220 <sup>+0.138+0.034</sup> <sub>-0.112-0.036</sub>	0.22
10.09–12.89	0.43 <sup>+0.18</sup> <sub>-0.20</sub> ±0.03	0.27 <sup>+0.11</sup> <sub>-0.13</sub> ±0.02	0.38 <sup>+0.16</sup> <sub>-0.16</sub> ±0.09	0.371 <sup>+0.150+0.010</sup> <sub>-0.164-0.011</sub>	0.36
14.18–16.00	0.70 <sup>+0.16</sup> <sub>-0.22</sub> ±0.10	0.47 <sup>+0.06</sup> <sub>-0.08</sub> ±0.03	0.44 <sup>+0.18</sup> <sub>-0.21</sub> ±0.10	0.404 <sup>+0.199+0.025</sup> <sub>-0.191-0.025</sub>	0.36
>16.00	0.66 <sup>+0.11</sup> <sub>-0.16</sub> ±0.04	0.16 <sup>+0.11</sup> <sub>-0.13</sub> ±0.06	0.65 <sup>+0.17</sup> <sub>-0.18</sub> ±0.16	0.360 <sup>+0.205+0.064</sup> <sub>-0.172-0.065</sub>	0.29
1.00–6.00	0.26 <sup>+0.27</sup> <sub>-0.30</sub> ±0.07	-0.06 <sup>+0.13</sup> <sub>-0.14</sub> ±0.04	0.29 <sup>+0.20</sup> <sub>-0.23</sub> ±0.07	-0.035 <sup>+0.036+0.008</sup> <sub>-0.033-0.009</sub>	0.022
$F_L$					
1.00–2.00	—	—	—	0.606 <sup>+0.179+0.031</sup> <sub>-0.229-0.024</sub>	0.78
0.00–2.00	0.29 <sup>+0.21</sup> <sub>-0.16</sub> ±0.02	0.00 <sup>+0.13</sup> <sub>-0.00</sub> ±0.02	0.30 <sup>+0.16</sup> <sub>-0.16</sub> ±0.02	0.320 <sup>+0.198+0.019</sup> <sub>-0.178-0.020</sub>	0.54
2.00–4.30	0.71 <sup>+0.24</sup> <sub>-0.24</sub> ±0.06	0.77 ± 0.15 ± 0.03	0.37 <sup>+0.22</sup> <sub>-0.24</sub> ±0.10	0.754 <sup>+0.128+0.015</sup> <sub>-0.108-0.018</sub>	0.79
4.30–8.68	0.64 <sup>+0.23</sup> <sub>-0.24</sub> ±0.07	0.60 <sup>+0.06</sup> <sub>-0.07</sub> ±0.01	0.68 <sup>+0.15</sup> <sub>-0.17</sub> ±0.09	0.634 <sup>+0.175+0.022</sup> <sub>-0.156-0.022</sub>	0.60
10.09–12.89	0.17 <sup>+0.17</sup> <sub>-0.15</sub> ±0.03	0.41 ± 0.11 ± 0.03	0.47 <sup>+0.14</sup> <sub>-0.14</sub> ±0.03	0.489 <sup>+0.163+0.014</sup> <sub>-0.140-0.013</sub>	0.42
14.18–16.00	-0.15 <sup>+0.27</sup> <sub>-0.23</sub> ±0.07	0.37 ± 0.09 ± 0.06	0.29 <sup>+0.14</sup> <sub>-0.12</sub> ±0.05	0.396 <sup>+0.141+0.004</sup> <sub>-0.141-0.004</sub>	0.36
>16.00	0.12 <sup>+0.15</sup> <sub>-0.13</sub> ±0.02	0.26 <sup>+0.10</sup> <sub>-0.08</sub> ±0.03	0.20 <sup>+0.16</sup> <sub>-0.17</sub> ±0.05	0.357 <sup>+0.074+0.003</sup> <sub>-0.133-0.003</sub>	0.34
1.00–6.00	0.67 <sup>+0.22</sup> <sub>-0.23</sub> ±0.06	0.55 ± 0.10 ± 0.03	0.69 <sup>+0.19</sup> <sub>-0.21</sub> ±0.08	0.703 <sup>+0.149+0.017</sup> <sub>-0.212-0.019</sub>	0.75

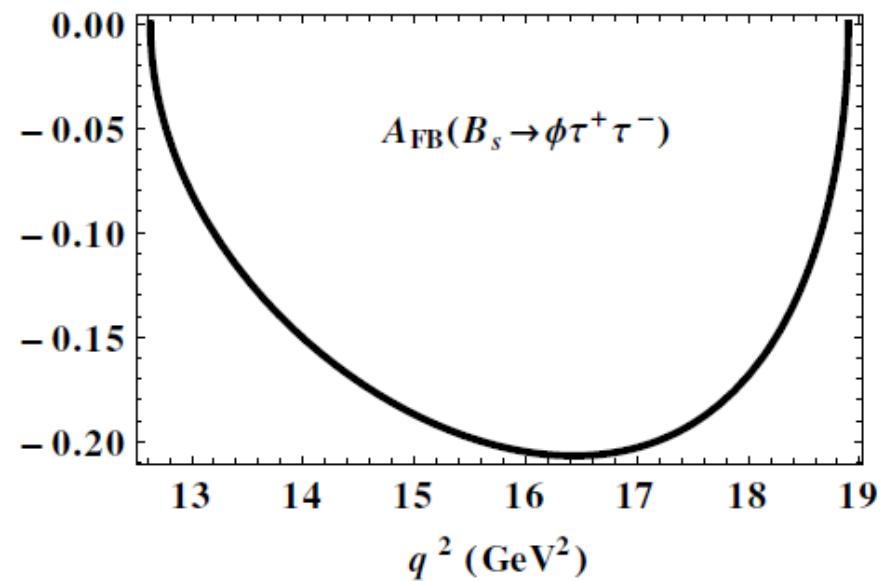
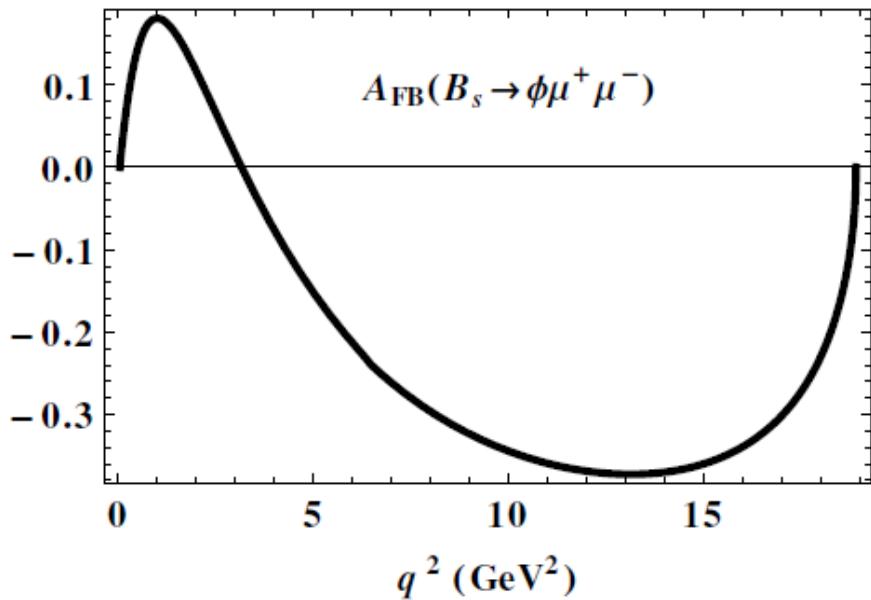
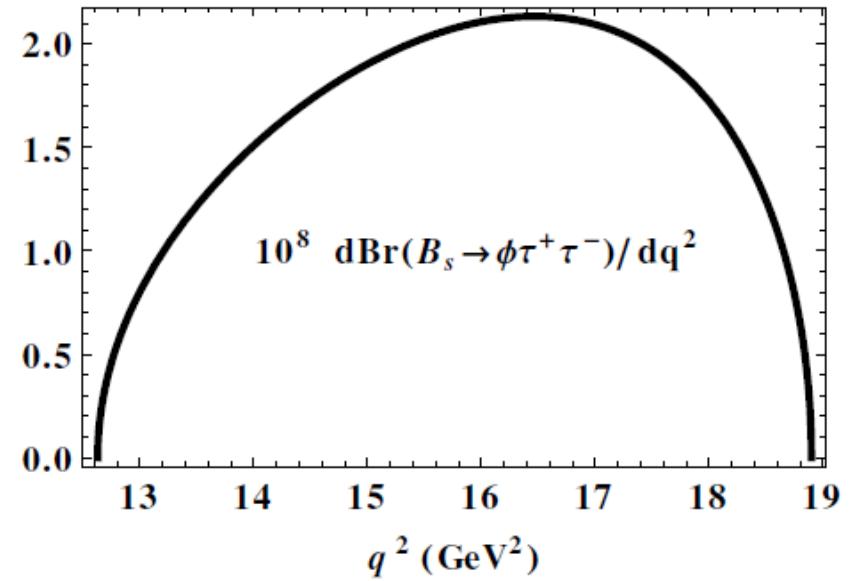
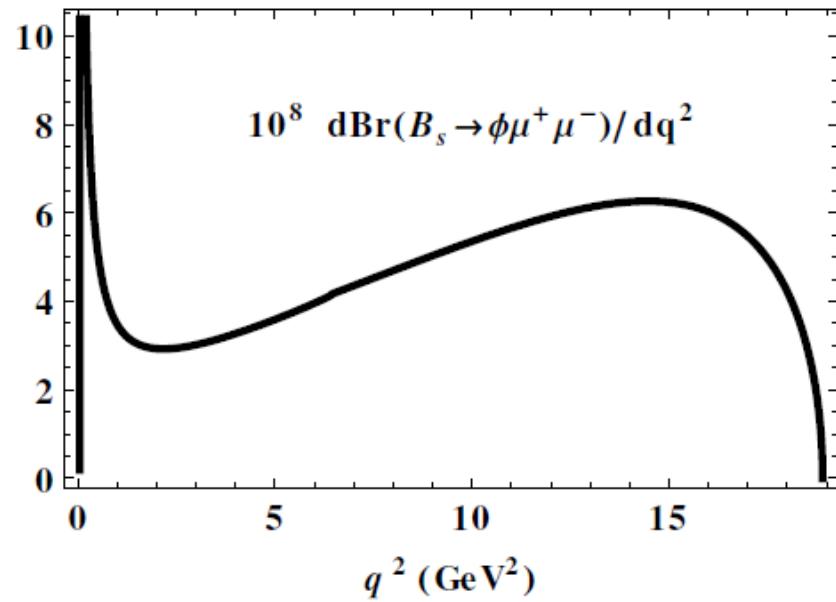
Bin (GeV <sup>2</sup> )	[0]	CQM	[0]	CQM
1–2	0.007 <sup>+0.008+0.054</sup> <sub>-0.005-0.051</sub>	-0.0115773	0.399 <sup>+0.022+0.006</sup> <sub>-0.023-0.006</sub>	0.47
0.1–2	0.007 <sup>+0.007+0.043</sup> <sub>-0.004-0.044</sub>	0.0108792	0.172 <sup>+0.009+0.018</sup> <sub>-0.009-0.018</sub>	0.22
2.00–4.30	-0.051 <sup>+0.010+0.045</sup> <sub>-0.006-0.045</sub>	-0.2665663	0.234 <sup>+0.008+0.015</sup> <sub>-0.005-0.016</sub>	0.019
4.30–8.68	-0.117 <sup>+0.009+0.056</sup> <sub>-0.009-0.052</sub>	-0.372456	-0.407 <sup>+0.048+0.008</sup> <sub>-0.037-0.006</sub>	-0.37
10.09–12.89	-0.181 <sup>+0.078+0.032</sup> <sub>-0.161-0.029</sub>	-0.470412	-0.481 <sup>+0.08+0.003</sup> <sub>-0.065-0.002</sub>	-0.41
14.18–16.00	-0.352 <sup>+0.092+0.014</sup> <sub>-0.467-0.015</sub>	-0.614669	-0.449 <sup>+0.136+0.004</sup> <sub>-0.641-0.004</sub>	-0.38
16.00–19	-0.603 <sup>+0.158+0.009</sup> <sub>-0.315-0.009</sub>	-0.777736	-0.374 <sup>+0.151+0.004</sup> <sub>-0.136-0.004</sub>	-0.30
1.00–6.00	-0.055 <sup>+0.008+0.040</sup> <sub>-0.006-0.042</sub>	-0.26338	0.084 <sup>+0.057+0.019</sup> <sub>-0.076-0.019</sub>	-0.060
$\langle P_1 \rangle$				
1–2	-0.003 <sup>+0.001+0.027</sup> <sub>-0.002-0.024</sub>	0.00435836	-0.164 <sup>+0.046+0.013</sup> <sub>-0.031-0.013</sub>	0.14
0.1–2	-0.002 <sup>+0.001+0.022</sup> <sub>-0.001-0.023</sub>	0.00189832	-0.342 <sup>+0.036+0.018</sup> <sub>-0.019-0.017</sub>	-0.15
2.00–4.30	-0.004 <sup>+0.001+0.022</sup> <sub>-0.001-0.022</sub>	0.00454996	0.569 <sup>+0.070+0.020</sup> <sub>-0.029-0.021</sub>	0.89
4.30–8.68	-0.001 <sup>+0.000+0.027</sup> <sub>-0.001-0.027</sub>	0.00224737	1.003 <sup>+0.014+0.024</sup> <sub>-0.015-0.029</sub>	1.13
10.09–12.89	0.003 <sup>+0.000+0.014</sup> <sub>-0.001-0.015</sub>	0.00151139	1.082 <sup>+0.140+0.014</sup> <sub>-0.144-0.017</sub>	1.21
14.18–16.00	0.004 <sup>+0.000+0.022</sup> <sub>-0.001-0.022</sub>	0.00101528	1.161 <sup>+0.190+0.007</sup> <sub>-0.322-0.007</sub>	1.27
16.00–19	0.003 <sup>+0.001+0.001</sup> <sub>-0.001-0.001</sub>	0.00068909	1.263 <sup>+0.119+0.004</sup> <sub>-0.248-0.004</sub>	1.33
1.00–6.00	-0.003 <sup>+0.005+0.009</sup> <sub>-0.009-0.022</sub>	0.00355465	0.555 <sup>+0.065+0.016</sup> <sub>-0.052-0.019</sub>	0.83
$\langle P'_5 \rangle$				
1–2	0.387 <sup>+0.047+0.014</sup> <sub>-0.063-0.015</sub>	0.268474	—	-0.039
0.1–2	0.533 <sup>+0.028+0.017</sup> <sub>-0.036-0.020</sub>	0.496414	—	-0.033
2.00–4.30	-0.334 <sup>+0.095+0.02</sup> <sub>-0.111-0.019</sub>	-0.423802	—	-0.026
4.30–8.68	-0.872 <sup>+0.043+0.021</sup> <sub>-0.059-0.029</sub>	-0.704599	—	-0.011
10.09–12.89	-0.893 <sup>+0.223+0.018</sup> <sub>-0.110-0.017</sub>	-0.697185	—	-0.0060
14.18–16.00	-0.779 <sup>+0.328+0.010</sup> <sub>-0.363-0.009</sub>	-0.600106	—	-0.0029
16.00–19	-0.604 <sup>+0.092+0.008</sup> <sub>-0.367-0.007</sub>	-0.449369	—	-0.0015
1.00–6.00	-0.349 <sup>+0.096+0.019</sup> <sub>-0.096-0.017</sub>	-0.394563	—	-0.023

S. Descotes-Genon, J. Matias and J. Virto, Phys. Rev. D 88, 074002 (2013), [arXiv:1307.5683].

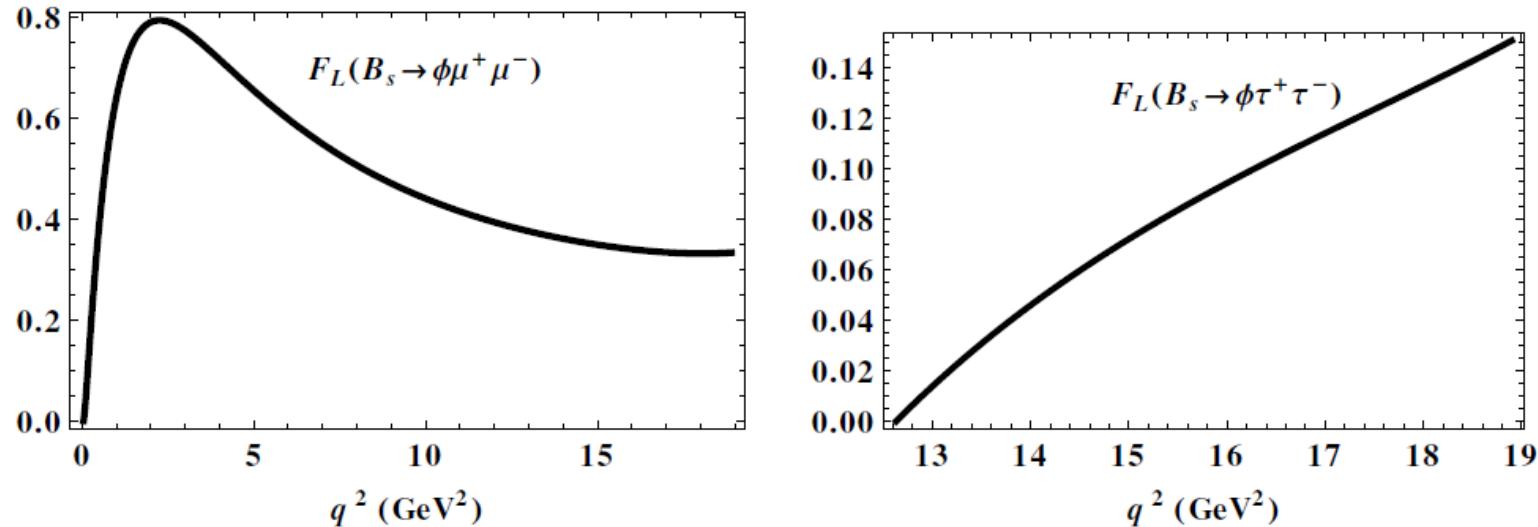
## $B_s \rightarrow \varphi + 2\mu$ : form factors



## $B_s \rightarrow \phi + 2\mu$ results



## B<sub>s</sub> → φ+2μ results




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	$B_s \rightarrow \phi\ell^+\ell^-$					
	$\langle A_{FB} \rangle$	$\langle F_L \rangle$	$\langle P_1 \rangle$	$\langle P'_4 \rangle$	$\langle S_3 \rangle$	$\langle S_4 \rangle$
μ	$-0.24 \pm 0.05$	$0.45 \pm 0.09$	$-0.52 \pm 0.1$	$1.05 \pm 0.21$	$-0.14 \pm 0.03$	$0.26 \pm 0.05$
τ	$-0.18 \pm 0.04$	$0.090 \pm 0.02$	$-0.76 \pm 0.15$	$1.33 \pm 0.27$	$-0.067 \pm 0.013$	$0.083 \pm 0.017$

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# $B_s \rightarrow \phi + 2\mu$ results

	This work	Ref. [1]	Ref. [2]	Ref. [3]	Ref. [4]	Ref. [5, 6]
$10^7 \mathcal{B}(B_s \rightarrow \phi \mu^+ \mu^-)$	$9.11 \pm 0.91$	$11.1 \pm 1.1$	19.2	$11.8 \pm 1.1$	16.4	$7.97 \pm 0.77$
$10^7 \mathcal{B}(B_s \rightarrow \phi \tau^+ \tau^-)$	$1.03 \pm 0.10$	$1.5 \pm 0.2$	2.34	$1.23 \pm 0.11$	1.51	
$10^5 \mathcal{B}(B_s \rightarrow \phi \gamma)$	$2.39 \pm 0.24$	$3.8 \pm 0.4$				$3.52 \pm 0.34$
$10^5 \mathcal{B}(B_s \rightarrow \phi \nu \bar{\nu})$	$0.84 \pm 0.08$	$0.796 \pm 0.080$			1.165	$< 540$
$10^2 \mathcal{B}(B_s \rightarrow \phi J/\psi)$	$0.16 \pm 0.02$	$0.113 \pm 0.016$				$0.108 \pm 0.009$

- [1] R. N. Faustov and V. O. Galkin, Eur. Phys. J. C 73, no. 10, 2593 (2013) [arXiv:1309.2160 [hep-ph]].
- [2] U. O. Yilmaz, Eur. Phys. J. C 58 (2008) 555 [arXiv:0806.0269 [hep-ph]].
- [3] Y. L. Wu, M. Zhong and Y. B. Zuo, Int. J. Mod. Phys. A 21 (2006) 6125 [hep-ph/0604007].
- [4] C. Q. Geng and C. C. Liu, J. Phys. G 29 (2003) 1103 [hep-ph/0303246].
- [5] R. Aaij et al. [LHCb Collaboration], JHEP 1509, 179 (2015) [arXiv:1506.08777 [hep-ex]].
- [6] K. A. Olive et al. [Particle Data Group Collaboration], Chin. Phys. C 38, 090001 (2014).

# $B_s \rightarrow \phi + 2\mu$ results

$10^7 \mathcal{B}(B_s \rightarrow \phi \mu^+ \mu^-)$	2 loop	1 loop	SM [7]	Expt. [5]
[0.1, 2]	$0.99 \pm 0.1$	$0.86 \pm 0.09$	$1.81 \pm 0.36$	$1.11 \pm 0.16$
[2, 5]	$0.90 \pm 0.09$	$0.95 \pm 0.1$	$1.88 \pm 0.31$	$0.77 \pm 0.14$
[5, 8]	--	$1.25 \pm 0.13$	$2.25 \pm 0.41$	$0.96 \pm 0.15$
[15, 19]	$1.89 \pm 0.19$	$1.95 \pm 0.20$	$2.20 \pm 0.16$	$1.62 \pm 0.20$
$F_L(B_s \rightarrow \phi \mu^+ \mu^-)$	2 loop	1 loop	SM [4]	Expt. [3]
[0.1, 2]	$0.37 \pm 0.04$	$0.46 \pm 0.05$	$0.46 \pm 0.09$	$0.20 \pm 0.09$
[2, 5]	$0.72 \pm 0.07$	$0.74 \pm 0.07$	$0.79 \pm 0.03$	$0.68 \pm 0.15$
[5, 8]	--	$0.57 \pm 0.06$	$0.65 \pm 0.05$	$0.54 \pm 0.10$
[15, 19]	$0.34 \pm 0.03$	$0.34 \pm 0.03$	$0.36 \pm 0.02$	$0.29 \pm 0.07$
$P_1(B_s \rightarrow \phi \mu^+ \mu^-)$	2 loop	1 loop	SM [4]	Expt. [3]
[0.1, 2]	$0.013 \pm 0.001$	$0.012 \pm 0.001$	$0.11 \pm 0.08$	$-0.13 \pm 0.33$
[2, 5]	$-0.26 \pm 0.03$	$-0.31 \pm 0.03$	$-0.10 \pm 0.09$	$-0.38 \pm 1.47$
[5, 8]	--	$-0.39 \pm 0.04$	$-0.20 \pm 0.10$	$-0.44 \pm 1.27$
[15, 19]	$-0.77 \pm 0.08$	$-0.77 \pm 0.08$	$-0.69 \pm 0.03$	$-0.25 \pm 0.34$
$P'_4(B_s \rightarrow \phi \mu^+ \mu^-)$	2 loop	1 loop	SM [4]	Expt. [3]
[0.1, 2]	$-0.18 \pm 0.02$	$-0.15 \pm 0.02$	$-0.28 \pm 0.14$	$-1.35 \pm 1.46$
[2, 5]	$0.86 \pm 0.09$	$0.96 \pm 0.1$	$0.80 \pm 0.11$	$2.02 \pm 1.84$
[5, 8]	--	$1.15 \pm 0.12$	$1.06 \pm 0.06$	$0.40 \pm 0.72$
[15, 19]	$1.33 \pm 0.13$	$1.33 \pm 0.13$	$1.30 \pm 0.01$	$0.62 \pm 0.49$

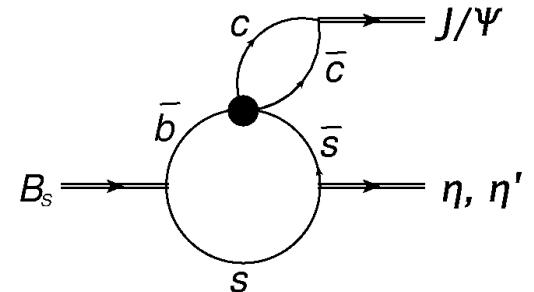
$P'_6(B_s \rightarrow \phi \mu^+ \mu^-)$	2 loop	1 loop	SM [7]	Expt. [5]
[0.1, 2]	$-0.016 \pm 0.002$	0	$-0.06 \pm 0.02$	$-0.10 \pm 0.30$
[2, 5]	$-0.015 \pm 0.002$	0	$-0.05 \pm 0.02$	$0.06 \pm 0.49$
[5, 8]	--	0	$-0.02 \pm 0.01$	$-0.08 \pm 0.40$
[15, 19]	--	0	$-0.00 \pm 0.07$	$-0.29 \pm 0.24$
$S_3(B_s \rightarrow \phi \mu^+ \mu^-)$	2 loop	1 loop	SM [4]	Expt. [3]
[0.1, 2]	$0.0031 \pm 0.0003$	$0.0023 \pm 0.0002$	$0.02 \pm 0.02$	$-0.05 \pm 0.13$
[2, 5]	$-0.035 \pm 0.004$	$-0.039 \pm 0.004$	$-0.01 \pm 0.01$	$-0.06 \pm 0.21$
[5, 8]	--	$-0.082 \pm 0.008$	$-0.03 \pm 0.02$	$-0.10 \pm 0.25$
[15, 19]	$-0.25 \pm 0.03$	$-0.25 \pm 0.03$	$-0.22 \pm 0.01$	$-0.09 \pm 0.12$
$S_4(B_s \rightarrow \phi \mu^+ \mu^-)$	2 loop	1 loop	SM [4]	Expt. [3]
[0.1, 2]	$-0.038 \pm 0.004$	$-0.031 \pm 0.003$	$-0.06 \pm 0.03$	$-0.27 \pm 0.23$
[2, 5]	$0.19 \pm 0.02$	$0.21 \pm 0.02$	$0.16 \pm 0.03$	$0.47 \pm 0.37$
[5, 8]	--	$0.28 \pm 0.03$	$0.25 \pm 0.02$	$0.10 \pm 0.17$
[15, 19]	$0.31 \pm 0.03$	$0.31 \pm 0.03$	$0.31 \pm 0.00$	$0.14 \pm 0.11$
$S_7(B_s \rightarrow \phi \mu^+ \mu^-)$	2 loop	1 loop	SM [4]	Expt. [3]
[0.1, 2]	$0.0065 \pm 0.0007$	0	$0.03 \pm 0.01$	$0.04 \pm 0.12$
[2, 5]	$0.0065 \pm 0.0007$	0	$0.02 \pm 0.01$	$-0.03 \pm 0.21$
[5, 8]	--	0	$0.01 \pm 0.00$	$0.04 \pm 0.18$
[15, 19]	$0.00066 \pm 0.00007$	0	$0.00 \pm 0.03$	$0.13 \pm 0.11$

[7] S. Descotes-Genon, L. Hofer, J. Matias and J. Virto, arXiv:1510.04239 [hep-ph].

# $B_s \rightarrow J/\Psi + \eta^{(\prime)}$ (summary)

## ■ $B_s \rightarrow J/\Psi + \eta$ and $B_s \rightarrow J/\Psi + \eta'$ :

- Measured by Belle [PRL 108, 181808 (2012)] and LHCb [Nucl. Phys. B867 (2013)547]
- Light-strange quark mixing



$$B_S^0 : s\bar{b} \quad \eta : \frac{1}{\sqrt{2}} \sin \delta (u\bar{u} + d\bar{d}) - \cos \delta (s\bar{s}) \quad \eta' : \frac{1}{\sqrt{2}} \cos \delta (u\bar{u} + d\bar{d}) + \sin \delta (s\bar{s})$$

$$\begin{aligned} \mathcal{L}_\eta(x) = & g_\eta \eta(x) \iint dx_1 dx_2 \delta \left( x - \frac{1}{2}x_1 - \frac{1}{2}x_2 \right) \phi_\eta \left[ (x_1 - x_2)^2 \right] \\ & \times \left\{ \frac{1}{\sqrt{2}} \cos(\delta) [\bar{u}(x_1) i\gamma^5 u(x_2) + \bar{d}(x_1) i\gamma^5 d(x_2)] - \sin(\delta) [\bar{s}(x_1) i\gamma^5 s(x_2)] \right\} \end{aligned}$$

$$\mathcal{L}_{\text{eff}} = \frac{G_F}{\sqrt{2}} V_{cb} V_{cs}^* \sum_i C_i Q_i \quad Q_1 = (\bar{c}_{a_1} b_{a_2})_{V-A} (\bar{s}_{a_2} c_{a_1})_{V-A} \quad Q_2 = \dots$$

$$(\bar{\psi}\psi)_{V-A} = \bar{\psi} O^\mu \psi, \quad O^\mu = \gamma^\mu (1 - \gamma^5) \quad (\bar{\psi}\psi)_{V+A} = \bar{\psi} O_+^\mu \psi, \quad O_+^\mu = \gamma^\mu (1 + \gamma^5)$$

# $B_s \rightarrow J/\psi + \eta^{(\prime)}$ (summary)

## Model over-constrained

$$\begin{array}{cccccc} \eta \rightarrow \gamma\gamma & \eta' \rightarrow \gamma\gamma & \rho \rightarrow \eta\gamma & \varphi \rightarrow \eta\gamma & \varphi \rightarrow \eta'\gamma \\ B_d \rightarrow J/\psi \eta & B_d \rightarrow J/\psi \eta' & \omega \rightarrow \eta\gamma & \eta' \rightarrow \omega\gamma \end{array}$$

## Results ( $\times 10^{-4}$ )

$$\mathcal{B}_{\text{CQM}}(J/\psi \eta) = 4.67$$

$$\mathcal{B}_{\text{Belle}}(J/\psi \eta) = 5.10 \pm 1.12$$

$$\mathcal{B}_{\text{CQM}}(J/\psi \eta') = 4.04$$

$$\mathcal{B}_{\text{Belle}}(J/\psi \eta') = 3.71 \pm 0.95$$

$$R = \frac{\Gamma(J/\psi + \eta')}{\Gamma(J/\psi + \eta)} = \begin{cases} 0.73 \pm 0.14 \pm 0.02 & \text{Belle} \\ 0.90 \pm 0.09_{-0.02}^{+0.06} & \text{LHCb} \end{cases}$$

$$R^{\text{theor}} = \underbrace{\frac{|\mathbf{q}_{\eta'}|^3}{|\mathbf{q}_\eta|^3} \tan^2 \delta}_{\approx 1.04} \times \underbrace{\left( \frac{F_+^{B_s \eta'}}{F_+^{B_s \eta}} \right)^2}_{\approx 0.83} \approx 0.86.$$

$\mathbf{q}$  - momentum of the outgoing particles in the rest frame of the decaying particle.

# Conclusion

## Summary

- CQM – relativistic, Lagrangian-based with limited number of free parameters, well suited for description of heavy hadron decays.
- Additional cross-check of the theory-data consistency with hadronic effects described by the covariant quark model: No significant deviation from the SM observed.

## Outlook

- Further processes can be evaluated and agreement with the SM checked [recently measured by LHCb and CMS:  $B_S^0 \rightarrow \mu^+ \mu^-$   $B_s^0 \rightarrow K_S^0 K^*(892)^0$ ].

**Thank for your attention!**