

# Polarization effects and new physics searches

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*Polarization data has often been the graveyard of fashionable theories.  
If theorists had their way, they might just ban such measurements altogether out of self-protection.*

*J.D. Bjorken  
St. Croix, 1987*



# Main Topics

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- Spin density matrices of real and virtual photons
- Polarization in Thomson scattering
- Virtual photon/graviton polarization at LHC
  
- Spin-gravity interactions
- Equivalence principle with spin
- Spin Precession in Bianchi-1 and 9 Universe
- Gravity induced transitions to sterile Dirac neutrinos and dark matter



# Spin density matrix: photons

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- Expansion of 2(transverse)d matrix to Pauli matrices: coefficients - Stokes parameters:  $\beta_1, \beta_2, \beta_3$
- (Anti)Symmetric part – (Circular)Linear polarization
- Scattering of unpolarized photons results in linear polarization perpendicular to scattering plane (used for gravity waves search)
- Scalar QED:  $\beta_3 = \sin^2\theta / (1 + \cos^2\theta)$
- Spinor QED Compton:  $\beta_3 = \sin^2\theta / (z + 1/z - \sin^2\theta)$
- Same for final photon energy fraction  $z \rightarrow 1$



# Virtual photons density matrix

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- 3 component of wf  $\rightarrow$  8 parameters
- Circular  $\rightarrow$  3 components of vector
- Linear  $\rightarrow$  5 components of symmetric traceless tensor
- Partons collision  $\rightarrow$  tensor polarized photons  $\rightarrow$  angular distributions of final particles
- Annihilation of quarks to leptons  $\rightarrow$
- $d\sigma \sim 1 + \cos^2\theta$



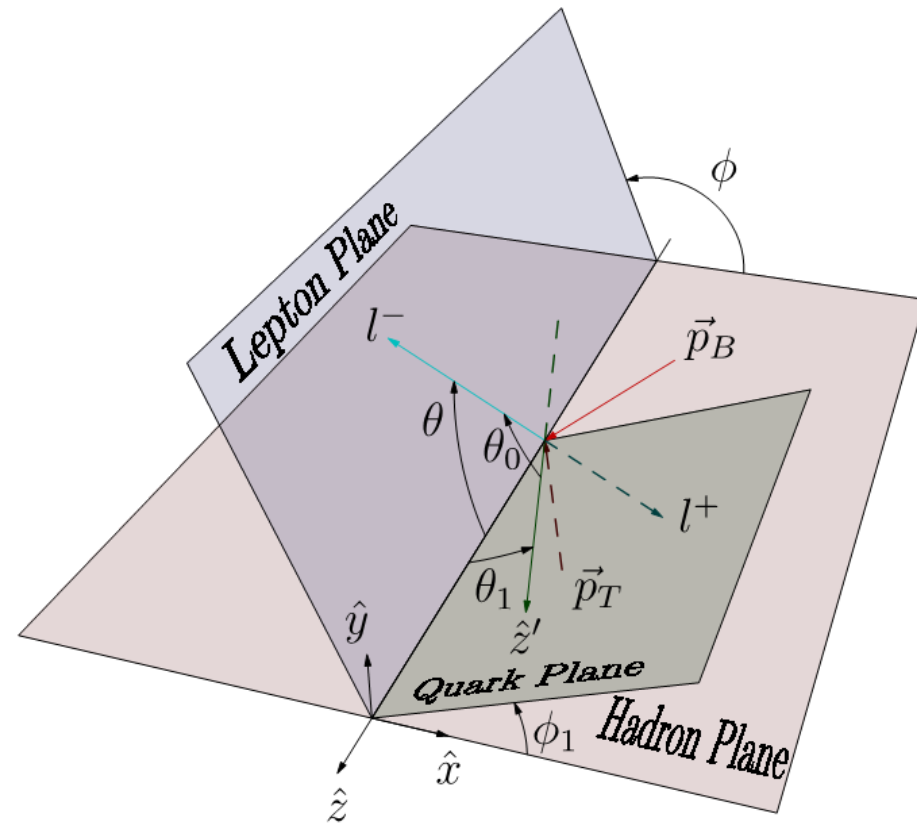
# Angular distributions

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- SM gauge bosons: detailed check of production mechanisms
- Higgs – spin 0 – isotropic distributions
- Gravitons – spin 2 – 4 component density matrix –  $\cos^4\theta$  enters – searched for and not found
- Any s-channel resonance – slow decrease with angle/transverse momentum

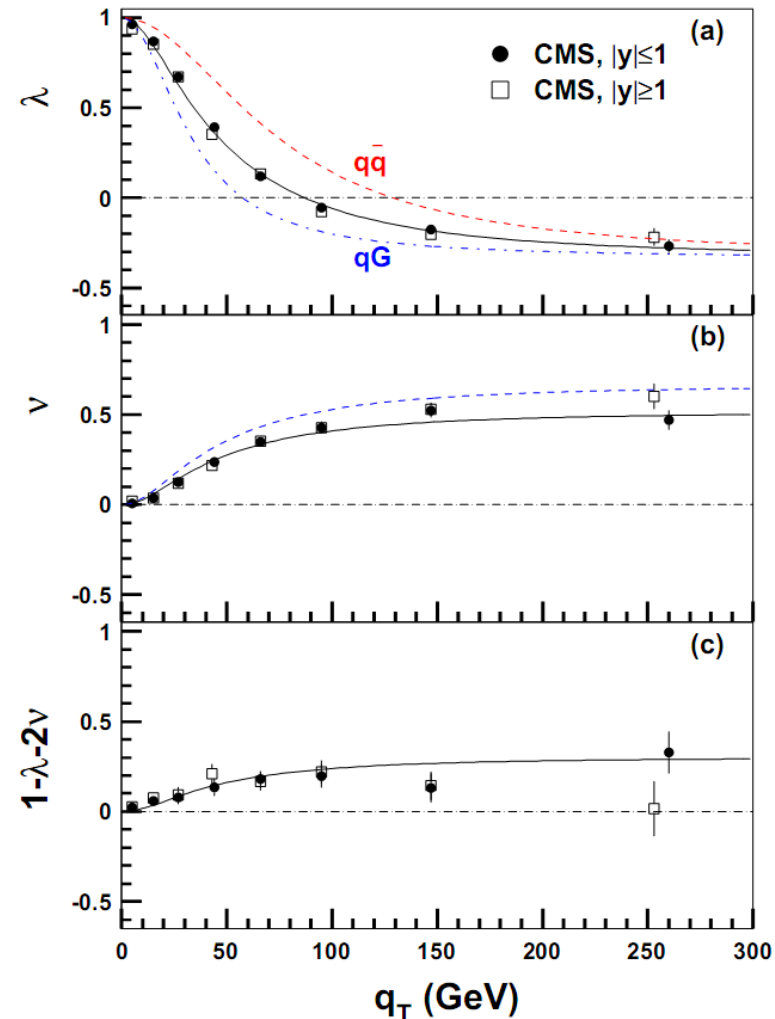
# Detailed tests of SM at LHC

- Interpretation of Angular Distributions of Z-boson Production at Colliders; Jen-Chieh Peng, Wen-Chen Chang, Randall Evan McClellan, and Oleg Teryaev; 1511.09893 and PLB
- Geometrical picture
- Non-coplanarity – disbalance of quark and hadron planes



# CMS (8 TeV) data

- Necessity to account for
- $qq$  - 41.5(1.6)%
- $qG$  - 58.5(1.6)%
- $\langle \cos 2\varphi_1 \rangle = 0.77$





# Spin-gravity interactions

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- 1. Dirac equation
- Gauge structure of gravity manifested; limit of classical gravity - FW transformation
- 2. Matrix elements of Energy- Momentum Tensor
- May be studied in non-gravitational experiments/theory
- Simple interpretation in comparison to EM field case





# Gravitational Formfactors

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$$\langle p' | T_{q,g}^{\mu\nu} | p \rangle = \bar{u}(p') \left[ A_{q,g}(\Delta^2) \gamma^{(\mu} p^{\nu)} + B_{q,g}(\Delta^2) P^{(\mu} i \sigma^{\nu)\alpha} \Delta_\alpha / 2M \right] u(p)$$

- Conservation laws - zero Anomalous Gravitomagnetic Moment :  $\mu_G = J$  (g=2)

$$P_{q,g} = A_{q,g}(0) \quad A_q(0) + A_g(0) = 1$$

$$J_{q,g} = \frac{1}{2} [A_{q,g}(0) + B_{q,g}(0)] \quad A_q(0) + B_q(0) + A_g(0) + B_g(0) = 1$$

- May be extracted from high-energy experiments/NPQCD calculations
- Describe the partition of angular momentum between quarks and gluons
- Describe interaction with both classical and TeV gravity

# Generalized Parton Diistributions (related to matrix elements of non local operators ) – models for both EM and Gravitational Formfactors (Selyugin,OT '09)

- Smaller mass square radius (attraction vs repulsion!?)

$$\rho(b) = \sum_q e_q \int dx q(x, b) = \int d^2q F_1(Q^2 = q^2) e^{i\vec{q}\vec{b}}$$

$$= \int_0^\infty \frac{qdq}{2\pi} J_0(qb) \frac{G_E(q^2) + \tau G_M(q^2)}{1 + \tau}$$

$$\rho_0^{\text{Gr}}(b) = \frac{1}{2\pi} \int_0^\infty dq q J_0(qb) A(q^2)$$

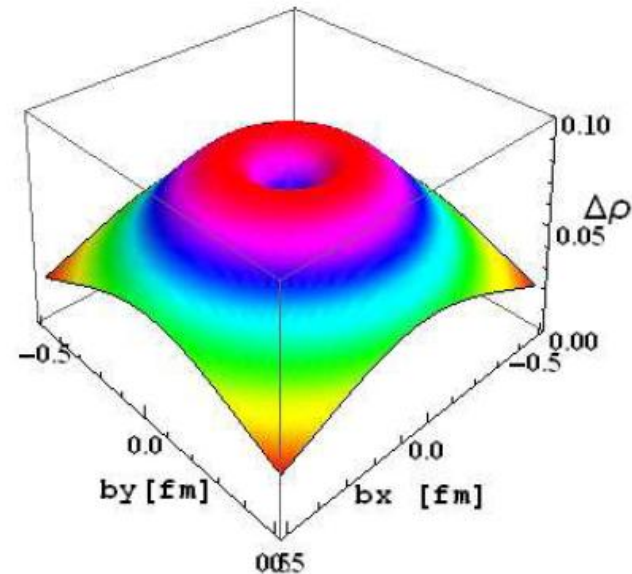


FIG. 17: Difference in the forms of charge density  $F_1^P$  and "matter" density ( $A$ )



# Electromagnetism vs Gravity

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- Interaction – field vs metric deviation

$$M = \langle P' | J_q^\mu | P \rangle A_\mu(q)$$

$$M = \frac{1}{2} \sum_{q,G} \langle P' | T_{q,G}^{\mu\nu} | P \rangle h_{\mu\nu}(q)$$

- Static limit

$$\langle P | J_q^\mu | P \rangle = 2e_q P^\mu$$

$$\sum_{q,G} \langle P | T_i^{\mu\nu} | P \rangle = 2P^\mu P^\nu$$
$$h_{00} = 2\phi(x)$$

$$M_0 = \langle P | J_q^\mu | P \rangle A_\mu = 2e_q M \phi(q)$$

$$M_0 = \frac{1}{2} \sum_{q,G} \langle P | T_i^{\mu\nu} | P \rangle h_{\mu\nu} = 2M \cdot M \phi(q)$$

- Mass as charge – equivalence principle



# Gravitomagnetism

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- Gravitomagnetic field (weak, except in gravity waves) – action on spin from  $M = \frac{1}{2} \sum_{q,G} \langle P' | T_{q,G}^{\mu\nu} | P \rangle h_{\mu\nu}(q)$

$$\vec{H}_J = \frac{1}{2} \text{rot} \vec{g}; \quad \vec{g}_i \equiv g_{0i}$$

spin dragging twice  
smaller than EM

- Lorentz force – similar to EM case: factor  $1/2$  cancelled with 2 from frequency same as EM

$$h_{00} = 2\phi(x)$$

Larmor

$$\omega_J = \frac{\mu_G}{J} H_J = \frac{H_L}{2} = \omega_L \quad \vec{H}_L = \text{rot} \vec{g}$$

- Orbital and Spin momenta dragging – the same - Equivalence principle



# Equivalence principle

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- Newtonian – “Falling elevator” – well known and checked (also for elementary particles)
- Post-Newtonian – gravity action on SPIN – known since 1962 (Kobzarev and Okun’); rederived from conservation laws - Kobzarev and Zakharov
- Anomalous gravitomagnetic (and electric-CP-odd) moment is ZERO or
- Classical and QUANTUM rotators behave in the SAME way
- - not checked on purpose but in fact checked in atomic spins experiments at % level (Silenko, OT’07)



# Experimental test of PNEP

- Reinterpretation of the data on G(EDM) search

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LETTERS

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Search for a Coupling of the Earth's Gravitational Field to Nuclear Spins in Atomic Mercury

B. J. Venema, P. K. Majumder, S. K. Lamoreaux, B. R. Heckel, and E. N. Fortson

Physics Department, FM-15, University of Washington, Seattle, Washington 98195

(Received 25 September 1991)

- If (CP-odd!)  $G_{EDM}=0 \rightarrow$  constraint for AGM (Silenko, OT'07) from Earth rotation – was considered as obvious (but it is just EP!) background

$$\mathcal{H} = -g\mu_N \mathbf{B} \cdot \mathbf{S} - \zeta \hbar \boldsymbol{\omega} \cdot \mathbf{S}, \quad \zeta = 1 + \chi$$

$$|\chi(^{201}\text{Hg}) + 0.369\chi(^{199}\text{Hg})| < 0.042 \quad (95\% \text{C.L.})$$

# Equivalence principle for moving particles

- Compare gravity and acceleration: gravity provides EXTRA space components of metrics

$$h_{zz} = h_{xx} = h_{yy} = h_{00}$$

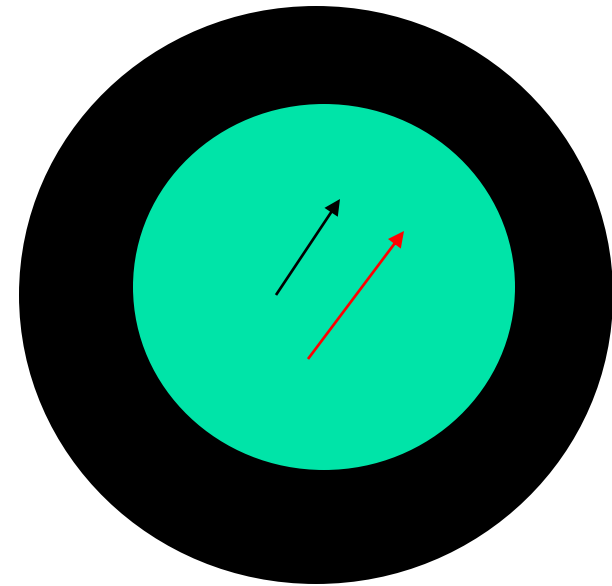
- Matrix elements DIFFER

$$\mathcal{M}_g = (\epsilon^2 + p^2)h_{00}(q), \quad \mathcal{M}_a = \epsilon^2 h_{00}(q)$$

- Ratio of accelerations:  $R = \frac{\epsilon^2 + p^2}{\epsilon^2}$  - confirmed by explicit solution of Dirac equation (Silenko, OT, '05)
- Arbitrary fields – Obukhov, Silenko, OT '09, '11, '13

# Cosmological implications of PNEP

- Necessary condition for Mach's Principle (in the spirit of Weinberg's textbook) -
- Lense-Thirring inside massive rotating empty shell (=model of Universe)
- For flat "Universe" - precession frequency equal to that of shell rotation
- Simple observation-Must be the same for classical and **quantum** rotators – PNEP!
- More elaborate models - Tests for cosmology ?!







# Manifestation of equivalence principle (cf with EM)

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- Classical and quantum rotators rotate with the same frequency (EM: spin  $\frac{1}{2}$  – twice faster); Dirac eq. analysis (Obukhov, Silenko, OT) – for strong fields
- Velocity rotates twice faster than classical rotator- **helicity changes** (EM – helicity of Dirac fermion conserved – used for AMM measurement) –BUT conserved in the rotating comoving frame

# Dirac Eq and Foldy - Wouthausen transformation

- Metric of the type

$$ds^2 = V^2 c^2 dt^2 - \delta_{\hat{a}\hat{b}} W^{\hat{a}}{}_c W^{\hat{b}}{}_d (dx^c - K^c c dt)(dx^d - K^d c dt).$$

- Tetrads in Schwinger gauge

$$e_{\hat{0}}^0 = V \delta_{\hat{0}}^0, \quad e_{\hat{0}}^{\hat{a}} = W^{\hat{a}}{}_b (\delta_{\hat{0}}^b - c K^b \delta_{\hat{0}}^0),$$

$$e_{\hat{a}}^0 = \frac{1}{V} (\delta_{\hat{a}}^0 + \delta_{\hat{a}}^i c K^i), \quad e_{\hat{a}}^i = \delta_{\hat{a}}^i W^b{}_{\hat{a}}, \quad a = 1, 2, 3,$$

- Dirac eq  $(i\hbar \gamma^\alpha D_\alpha - mc)\Psi = 0, \quad \alpha = 0, 1, 2, 3.$

$$D_\alpha = e_\alpha^i D_i, \quad D_i = \partial_i + \frac{iq}{\hbar} A_i + \frac{i}{4} \sigma^{\alpha\beta} \Gamma_{i\alpha\beta}.$$

# Dirac hamiltonian

## ■ Connection

$$\Gamma_{ia\hat{0}} = \frac{c^2}{V} W^b_{\hat{a}} \partial_b V e_i^{\hat{0}} - \frac{c}{V} Q_{(a\hat{b})} e_i^{\hat{b}},$$

$$\Gamma_{ia\hat{b}} = \frac{c}{V} Q_{[a\hat{b}]} e_i^{\hat{0}} + (C_{a\hat{b}\hat{c}} + C_{a\hat{c}\hat{b}} + C_{\hat{c}\hat{b}a}) e_i^{\hat{c}}.$$

$$Q_{a\hat{b}} = g_{a\hat{c}} W^d_{\hat{b}} \left( \frac{1}{c} \dot{W}^{\hat{c}}_d + K^e \partial_e W^{\hat{c}}_d + W^{\hat{c}}_e \partial_d K^e \right),$$

$$C_{a\hat{b}}^{\hat{c}} = W^d_{\hat{a}} W^e_{\hat{b}} \partial_{[d} W^{\hat{c}}_{e]}, \quad C_{a\hat{b}\hat{c}} = g_{\hat{c}\hat{d}} C_{a\hat{b}}^{\hat{d}}.$$

## ■ Hermitian Hamiltonian

$$i\hbar \frac{\partial \psi}{\partial t} = \mathcal{H} \psi, \quad \psi = (\sqrt{-g} e_0^0)^{\frac{1}{2}} \Psi.$$

$$\begin{aligned} \mathcal{H} = & \beta mc^2 V + q\Phi + \frac{c}{2} (\pi_b \mathcal{F}^b_a \alpha^a + \alpha^a \mathcal{F}^b_a \pi_b) \\ & + \frac{c}{2} (\mathbf{K} \cdot \boldsymbol{\pi} + \boldsymbol{\pi} \cdot \mathbf{K}) + \frac{\hbar c}{4} (\boldsymbol{\Xi} \cdot \boldsymbol{\Sigma} - Y \gamma_5). \end{aligned}$$

$$Y = V \epsilon^{\hat{a}\hat{b}\hat{c}} \Gamma_{a\hat{b}\hat{c}} = -V \epsilon^{\hat{a}\hat{b}\hat{c}} C_{a\hat{b}\hat{c}},$$

$$\Xi_a = \frac{V}{c} \epsilon_{a\hat{b}\hat{c}} \Gamma_0^{\hat{b}\hat{c}} = \epsilon_{a\hat{b}\hat{c}} Q^{\hat{b}\hat{c}}.$$

# Foldy-Wouthuysen transformation

- Even and odd parts  $\mathcal{H} = \beta\mathcal{M} + \mathcal{E} + \mathcal{O}, \quad \beta\mathcal{M} = \mathcal{M}\beta,$   
 $\beta\mathcal{E} = \mathcal{E}\beta, \quad \beta\mathcal{O} = -\mathcal{O}\beta.$

- FW transformation (Silenko '08)

$$U = \frac{\beta\epsilon + \beta\mathcal{M} - \mathcal{O}}{\sqrt{(\beta\epsilon + \beta\mathcal{M} - \mathcal{O})^2}}, \quad \psi_{\text{FW}} = U\psi, \quad \mathcal{H}_{\text{FW}} = U\mathcal{H}U^{-1} - i\hbar U\partial_t U^{-1},$$

$$U^{-1} = \beta \frac{\beta\epsilon + \beta\mathcal{M} - \mathcal{O}}{\sqrt{(\beta\epsilon + \beta\mathcal{M} - \mathcal{O})^2}}, \quad \epsilon = \sqrt{\mathcal{M}^2 + \mathcal{O}^2}.$$

$$\mathcal{H}' = \beta\epsilon + \mathcal{E} + \frac{1}{2T}([T, [T, (\beta\epsilon + Z)]] + \beta[O, [O, \mathcal{M}]] - [O, [O, Z]]) \quad \mathcal{H}' = \beta\epsilon + \mathcal{E}' + \mathcal{O}', \quad \beta\mathcal{E}' = \mathcal{E}'\beta, \quad \beta\mathcal{O}' = -\mathcal{O}'\beta,$$

$$T = \sqrt{(\beta\epsilon + \beta\mathcal{M} - \mathcal{O})^2} - [(\epsilon + \mathcal{M}), [(\epsilon + \mathcal{M}), Z]] - [(\epsilon + \mathcal{M}), [\mathcal{M}, \mathcal{O}]]$$

$$Z = \mathcal{E} - i\hbar \frac{\partial}{\partial t} - \beta\{O, [(\epsilon + \mathcal{M}), Z]\} + \beta\{(\epsilon + \mathcal{M}), [O, Z]\} \frac{1}{T},$$

$$\mathcal{H}_{\text{FW}} = \beta\epsilon + \mathcal{E}' + \frac{1}{4}\beta\left\{O'^2, \frac{1}{\epsilon}\right\}.$$

# FW for arbitrary gravitational field

## ■ Result

$$\mathcal{H}_{\text{FW}} = \mathcal{H}_{\text{FW}}^{(1)} + \mathcal{H}_{\text{FW}}^{(2)}$$

$$\epsilon' = \sqrt{m^2 c^4 V^2 + \frac{c^2}{4} \delta^{ac} \{p_b, \mathcal{F}^b{}_a\} \{p_d, \mathcal{F}^d{}_c\}},$$

$$\mathcal{T} = 2\epsilon'^2 + \{\epsilon', mc^2 V\}.$$

$$\mathcal{M} = mc^2 V,$$

$$\mathcal{E} = q\Phi + \frac{c}{2}(\mathbf{K} \cdot \boldsymbol{\pi} + \boldsymbol{\pi} \cdot \mathbf{K}) + \frac{\hbar c}{4} \boldsymbol{\Xi} \cdot \boldsymbol{\Sigma},$$

$$\mathcal{O} = \frac{c}{2}(\boldsymbol{\pi}_b \mathcal{F}^b{}_a \alpha^a + \alpha^a \mathcal{F}^b{}_a \boldsymbol{\pi}_b) - \frac{\hbar c}{4} Y \gamma_5.$$

$$\begin{aligned} \mathcal{H}_{\text{FW}}^{(1)} = & \beta \epsilon' + \frac{\hbar c^2}{16} \left\{ \frac{1}{\epsilon'}, (2\epsilon^{cae} \Pi_e \{p_b, \mathcal{F}^d{}_c \partial_d \mathcal{F}^b{}_a\} \right. \\ & \left. + \Pi^a \{p_b, \mathcal{F}^b{}_a Y\}) \right\} \\ & + \frac{\hbar m c^4}{4} \epsilon^{cae} \Pi_e \left\{ \frac{1}{\mathcal{T}}, \{p_d, \mathcal{F}^d{}_c \mathcal{F}^b{}_a \partial_b V\} \right\}, \end{aligned}$$

$$\begin{aligned} \mathcal{H}_{\text{FW}}^{(2)} = & \frac{c}{2} (K^a p_a + p_a K^a) + \frac{\hbar c}{4} \Sigma_a \Xi^a \\ & + \frac{\hbar c^2}{16} \left\{ \frac{1}{\mathcal{T}}, \left\{ \Sigma_a \{p_e, \mathcal{F}^e{}_b\}, \left\{ p_f, \left[ \epsilon^{abc} \left( \frac{1}{c} \mathcal{F}^f{}_c \right. \right. \right. \right. \right. \right. \right. \\ & \left. \left. \left. \left. \left. \left. - \mathcal{F}^d{}_c \partial_d K^f + K^d \partial_d \mathcal{F}^f{}_c \right) \right. \right. \right. \right. \right. \\ & \left. \left. \left. \left. \left. \left. - \frac{1}{2} \mathcal{F}^f{}_d (\delta^{db} \Xi^a - \delta^{da} \Xi^b) \right] \right] \right] \right\} \right\}, \end{aligned}$$



# Operator EOM

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- Polarization operator  $\mathbf{\Pi} = \beta \mathbf{\Sigma}$

$$\frac{d\mathbf{\Pi}}{dt} = \frac{i}{\hbar} [\mathcal{H}_{\text{FW}}, \mathbf{\Pi}] = \mathbf{\Omega}_{(1)} \times \mathbf{\Sigma} + \mathbf{\Omega}_{(2)} \times \mathbf{\Pi}.$$

- Angular velocities

$$\begin{aligned} \Omega_{(1)}^a = & \frac{mc^4}{2} \left\{ \frac{1}{\mathcal{T}}, \{p_e, \epsilon^{abc} \mathcal{F}_b^e \mathcal{F}_c^d \partial_d V\} \right\} \\ & + \frac{c^2}{8} \left\{ \frac{1}{\epsilon^f}, \{p_e, (2\epsilon^{abc} \mathcal{F}_b^d \partial_d \mathcal{F}_c^e + \delta^{ab} \mathcal{F}_b^e Y)\} \right\}, \end{aligned}$$

$$\begin{aligned} \Omega_{(2)}^a = & \frac{\hbar c^2}{8} \left\{ \frac{1}{\mathcal{T}}, \left\{ \{p_e, \mathcal{F}_b^e\}, \left\{ p_f, \left[ \epsilon^{abc} \left( \frac{1}{c} \dot{\mathcal{F}}_c^f \right. \right. \right. \right. \right. \right. \right. \\ & \left. \left. \left. \left. \left. - \mathcal{F}_c^d \partial_d K^f + K^d \partial_d \mathcal{F}_c^f \right) \right. \right. \right. \right. \\ & \left. \left. \left. \left. \left. - \frac{1}{2} \mathcal{F}_d^f (\delta^{db} \Xi^a - \delta^{da} \Xi^b) \right] \right] \right\} \right\} + \frac{c}{2} \Xi^a. \end{aligned}$$



# Semi-classical limit

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- Average spin

$$\frac{ds}{dt} = \mathbf{\Omega} \times s = (\mathbf{\Omega}_{(1)} + \mathbf{\Omega}_{(2)}) \times s,$$

$$\Omega_{(1)}^a = \frac{c^2}{\epsilon'} \mathcal{F}^d {}_c P_d \left( \frac{1}{2} Y \delta^{ac} - \epsilon^{aef} V C_{ef}{}^c + \frac{\epsilon'}{\epsilon' + mc^2 V} \epsilon^{abc} W^e {}_b \partial_e V \right),$$

$$\Omega_{(2)}^a = \frac{c}{2} \Xi^a - \frac{c^3}{\epsilon'(\epsilon' + mc^2 V)} \epsilon^{abc} Q_{(bd)} \delta^{dn} \mathcal{F}^k {}_n P_k \mathcal{F}^l {}_c P_l,$$

# Application to anisotropic universe (Kamenshchik,OT)

- Bianchi-1 Universe

$$ds^2 = dt^2 - a^2(t)(dx^1)^2 - b^2(t)(dx^2)^2 - c^2(t)(dx^3)^2.$$

- Particular case  $W_1^1 = a(t), W_2^2 = b(t), W_3^3 = c(t).$

$$W_1^1 = \frac{1}{a(t)}, W_2^2 = \frac{1}{b(t)}, W_3^3 = \frac{1}{c(t)}.$$

- No anholonomy  $\Upsilon = 0$

$$\Omega_{(2)}^i = \frac{\gamma}{\gamma+1} v_2 v_3 \left( \frac{\dot{b}}{b} - \frac{\dot{c}}{c} \right).$$
$$Q_{ii} = -\frac{\dot{a}}{a}, Q_{22} = -\frac{\dot{b}}{b}, Q_{33} = -\frac{\dot{c}}{c}.$$





# Kasner solution

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- t-dependence

$$a(t) = a_0 t^{p_1}, \quad b(t) = b_0 t^{p_2}, \quad c(t) = c_0 t^{p_3},$$

$$p_1 + p_2 + p_3 = 1, \quad p_1^2 + p_2^2 + p_3^2 = 1.$$

- Euler-type expressions

$$\Omega_{(2)}^i = \frac{\gamma}{\gamma + 1} v_2 v_3 \left( \frac{p_2 - p_3}{t} \right)$$



# Heckmann-Schucking solution

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- Dust admixture

$$a(t) = a_0 t^{p_1} (t_0 + t)^{\frac{2}{3} - p_1}, \quad b(t) = b_0 t^{p_2} (t_0 + t)^{\frac{2}{3} - p_2}, \\ c(t) = c_0 t^{p_3} (t_0 + t)^{\frac{2}{3} - p_3}.$$

- Modification:

$$\Omega_{(2)}^i = \frac{\gamma}{\gamma + 1} v_2 v_3 \frac{(p_2 - p_3)t_0}{t(t_0 + t)} \\ = \frac{\gamma}{\gamma + 1} v_2 v_3 \frac{(p_2 - p_3)t_0}{t^2} \left( 1 + o\left(\frac{t_0}{t}\right) \right)$$



# Biancki-IX Universe

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- Metric  $W_a^{\hat{b}} = \begin{pmatrix} -a \sin x^3 & a \sin x^1 \cos x^3 & 0 \\ b \cos x^3 & b \sin x^1 \sin x^3 & 0 \\ 0 & c \cos x^1 & c \end{pmatrix}$   $W_{\hat{b}}^c = \begin{pmatrix} -\frac{1}{a} \sin x^3 & \frac{1}{b} \cos x^3 & 0 \\ \frac{1}{a} \cos x^3 & \frac{1}{b} \sin x^3 & 0 \\ -\frac{1}{a} \frac{\cos x^1 \cos x^3}{\sin x^1} & -\frac{1}{b} \frac{\sin x^3 \cos x^1}{\sin x^1} & \frac{1}{c} \end{pmatrix}$

- Anholonomy coefficients

- $C_{\hat{1}\hat{2}}^{\hat{3}} = \frac{c}{ab}$  + cyclic permutations

- -> non-zero  $\Upsilon = 2 \left( \frac{c}{ab} + \frac{b}{ac} + \frac{a}{bc} \right)$

$$\Omega_{(1)}^{\hat{1}} = v^{\hat{1}} \left( \frac{c}{ab} + \frac{b}{ac} - \frac{a}{bc} \right)$$



# Approach to singularity

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- Chaotic oscillations – sequence of Kasner regimes

$$p_1 = -\frac{u}{1+u+u^2}, \quad p_2 = \frac{1+u}{1+u+u^2}, \quad p_3 = \frac{u(1+u)}{1+u+u^2}$$

- If Lifshitz-Khalatnikov parameter  $u > 1$  – “epochs”

$$p'_1 = p_2(u-1), \quad p'_2 = p_1(u-1), \quad p'_3 = p_3(u-1)$$

- If  $u < 1$  – “eras”

$$p'_1 = p_1 \left( \frac{1}{u} \right), \quad p'_2 = p_3 \left( \frac{1}{u} \right), \quad p'_3 = p_2 \left( \frac{1}{u} \right)$$

- Change of eras – chaotic mapping of  $[0,1]$  interval

$$Tx = \left\{ \frac{1}{x} \right\}, \quad x_{s+1} = \left\{ \frac{1}{x_s} \right\}$$



# Angular velocities

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- New epoch:  $u \rightarrow -u$
- New era – changed sign

$$\Omega_{(2)}^{\hat{1}} = \frac{\gamma}{(\gamma + 1)t} v_2 v_3 \cdot \frac{1 - u^2}{1 + u + u^2},$$

$$\Omega_{(2)}^{\hat{2}} = \frac{\gamma}{(\gamma + 1)t} v_1 v_3 \cdot \frac{2u + u^2}{1 + u + u^2},$$

$$\Omega_{(2)}^{\hat{3}} = -\frac{\gamma}{(\gamma + 1)t} v_1 v_2 \cdot \frac{1 + 2u}{1 + u + u^2}.$$

- Odd velocity

$$\Omega_{(1)}^{\hat{1}} \sim -v^{\hat{1}}(t) \left( -1 - \frac{2u}{1+u+u^2} \right),$$

$$\Omega_{(1)}^{\hat{b}} \sim v^{\hat{b}}(t) \left( -1 - \frac{2u}{1+u+u^2} \right), \quad b = 2, 3.$$

$$\Omega_{(1)}^{\hat{2}} \sim -v^{\hat{2}}(t) \left( -1 - \frac{2u-2}{1-u+u^2} \right),$$

$$\Omega_{(1)}^{\hat{a}} \sim v^{\hat{a}}(t) \left( -1 - \frac{2u-2}{1-u+u^2} \right), \quad a = 1, 3.$$

- New epoch
- New era - preserved



# Possible applications

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- Anisotropy (c.f. crystals)  $\sim$  magnetic field
- Spin precession + equivalence principle = helicity flip ( $\sim$ AMM effect)
- Dirac neutrino – transformed to sterile component in early (bounced) Universe
- Angular velocity  $\sim 1/t \rightarrow$  amount of decoupled  $\sim 1$
- Possible new candidate for dark matter?!
- Other fields AFTER inflation?



# CONCLUSIONS

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- Polarization – extra sensitive tests
- Gravity leads to spin effects related to Kobzarev-Okun equivalence principle
- Bianchi universe – spin precession and neutrino helicity flip

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- 
- **BACKUP SLIDES**





# Semi-classical limit

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- Average spin precession

$$\frac{d\vec{s}}{dt} = \vec{\Omega} \times \vec{s} = (\vec{\Omega}_{(1)} + \vec{\Omega}_{(2)}) \times \vec{s}.$$

- Angular velocity contributions

$$\Omega_{(1)}^{\hat{a}} = \frac{1}{\varepsilon'} W_{\hat{c}}^d P_d \left( \frac{1}{2} \Upsilon \delta^{\hat{a}\hat{c}} - \varepsilon^{\hat{a}\hat{e}\hat{f}} C_{\hat{e}\hat{f}}^{\hat{c}} \right),$$
$$\Omega_{(2)}^{\hat{a}} = \frac{1}{2} \Xi^{\hat{a}} - \frac{1}{\varepsilon'(\varepsilon' + m)} \varepsilon^{\hat{a}\hat{b}\hat{c}} Q_{(\hat{b}\hat{d})} \delta^{\hat{d}\hat{n}} W_{\hat{n}}^k P_k W_{\hat{c}}^l P_l.$$

# Torsion – acts only on spin

Dirac eq+FW transformation-Obukhov,Silenko,OT

## ■ Hermitian Dirac Hamiltonian

$$e_i^{\hat{0}} = V \delta_i^0, \quad e_i^{\hat{a}} = W^{\hat{a}}_b (\delta_i^b - cK^b \delta_i^0) \quad \mathcal{H} = \beta mc^2 V + q\Phi + \frac{c}{2} (\pi_b \mathcal{F}^b_a \alpha^a + \alpha^a \mathcal{F}^b_a \pi_b)$$

$$ds^2 = V^2 c^2 dt^2 - \delta_{\hat{a}\hat{b}} W^{\hat{a}}_c W^{\hat{b}}_d (dx^c - K^c c dt) (dx^d - K^d c dt) \quad + \frac{c}{2} (\mathbf{K} \cdot \boldsymbol{\pi} + \boldsymbol{\pi} \cdot \mathbf{K}) + \frac{\hbar c}{4} (\boldsymbol{\Xi} \cdot \boldsymbol{\Sigma} - \Upsilon \gamma_5),$$

$$\mathcal{F}^b_a = V W^b_{\hat{a}}, \quad \Upsilon = V \epsilon^{\hat{a}\hat{b}\hat{c}} \Gamma_{\hat{a}\hat{b}\hat{c}}, \quad \Xi^a = \frac{V}{c} \epsilon^{\hat{a}\hat{b}\hat{c}} (\Gamma_{\hat{0}\hat{b}\hat{c}} + \Gamma_{\hat{b}\hat{c}\hat{0}} + \Gamma_{\hat{c}\hat{0}\hat{b}})$$

## ■ Spin-torsion coupling

$$- \frac{\hbar c V}{4} (\boldsymbol{\Sigma} \cdot \check{\mathbf{T}} + c \gamma_5 \check{T}^{\hat{0}})$$

$$\check{T}^\alpha = - \frac{1}{2} \eta^{\alpha\mu\nu\lambda} T_{\mu\nu\lambda}$$

## ■ FW – semiclassical limit - precession

$$\Omega^{(T)} = - \frac{c}{2} \check{\mathbf{T}} + \beta \frac{c^3}{8} \left\{ \frac{1}{\epsilon'}, \{p, \check{T}^{\hat{0}}\} \right\} + \frac{c}{8} \left\{ \frac{c^2}{\epsilon'(\epsilon' + mc^2)}, (\{p^2, \check{\mathbf{T}}\} - \{p, (p \cdot \check{\mathbf{T}})\}) \right\}$$

# Experimental bounds for torsion

- Magnetic field+rotation+torsion

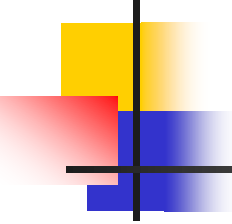
$$H = -g_N \frac{\mu_N}{\hbar} \mathbf{B} \cdot \mathbf{s} - \boldsymbol{\omega} \cdot \mathbf{s} - \frac{c}{2} \tilde{\mathbf{T}} \cdot \mathbf{s},$$

- Same '92 EDM experiment

$$\frac{\hbar c}{4} |\tilde{\mathbf{T}}| \cdot |\cos \Theta| < 2.2 \times 10^{-21} \text{ eV}, \quad |\tilde{\mathbf{T}}| \cdot |\cos \Theta| < 4.3 \times 10^{-14} \text{ m}^{-1}$$

- New(based on Gemmel et al '10)

$$\frac{\hbar c}{2} |\tilde{\mathbf{T}}| \cdot |(1 - \mathcal{G}) \cos \Theta| < 4.1 \times 10^{-22} \text{ eV}, \quad |\tilde{\mathbf{T}}| \cdot |\cos \Theta| < 2.4 \times 10^{-15} \text{ m}^{-1},$$
$$\mathcal{G} = g_{He}/g_{Xe}$$

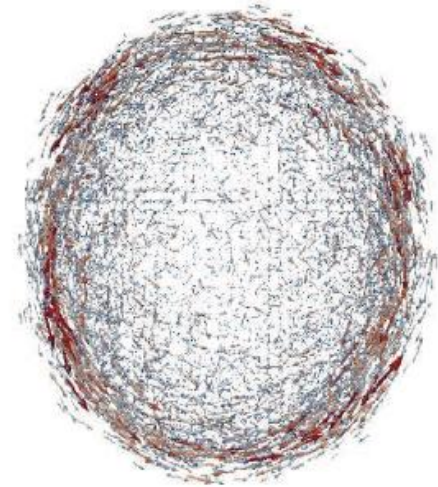
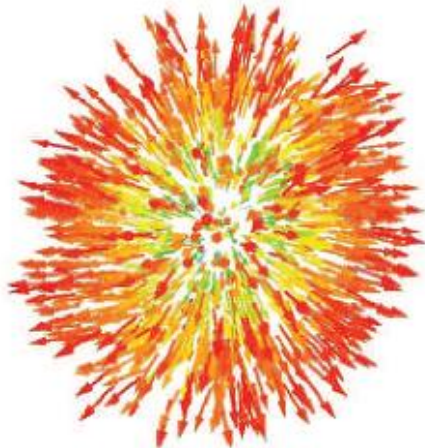
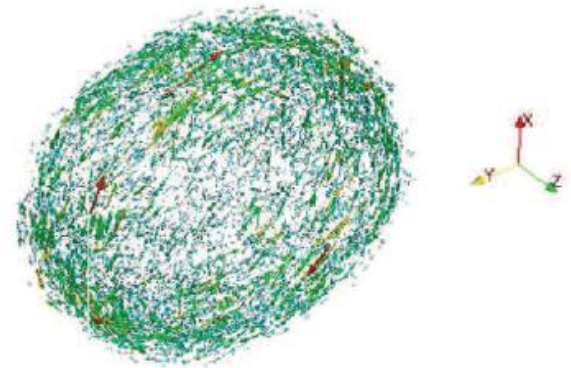
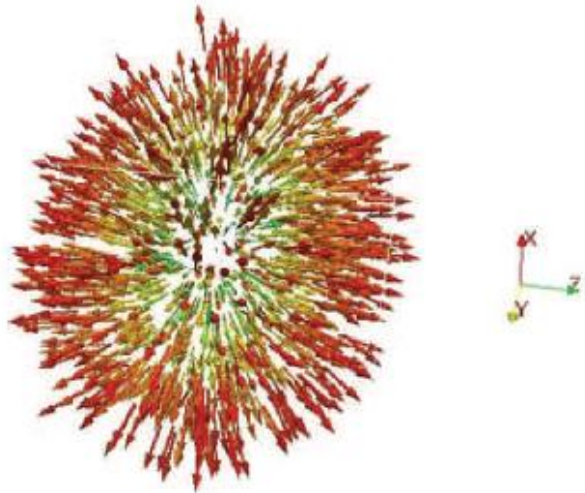


# Microworld: where is the fastest possible rotation?

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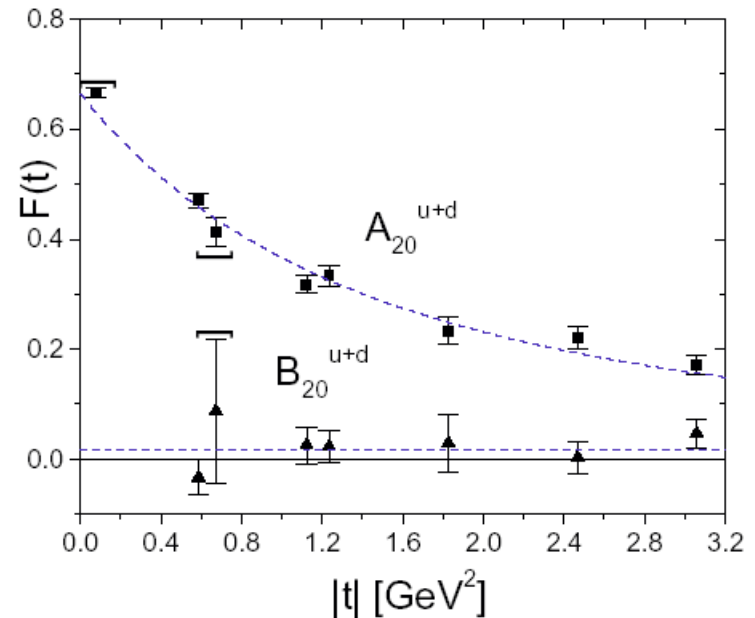
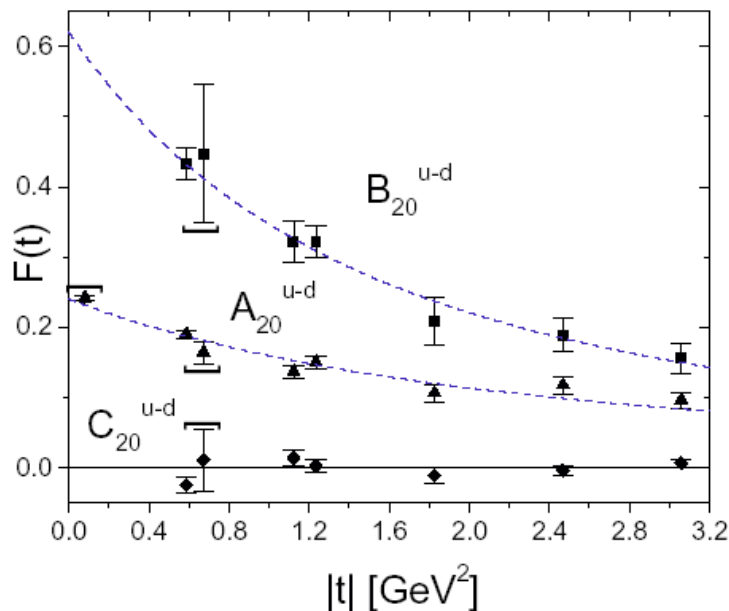
- Non-central heavy ion collisions ( $\sim c/\text{Compton wavelength}$ ) – “small Bang”
- Differential rotation – vorticity
- Leads to hyperons polarization – should be larger at small energy – predicted in 2010 (Rogachevsky, Sorin, OT) now found by STAR@RHIC
- Calculation in quark - gluon string model (Baznat, Gudima, Sorin, OT, PRC'13)

# Structure of velocity and vorticity fields (NICA@JINR-5 GeV/c)



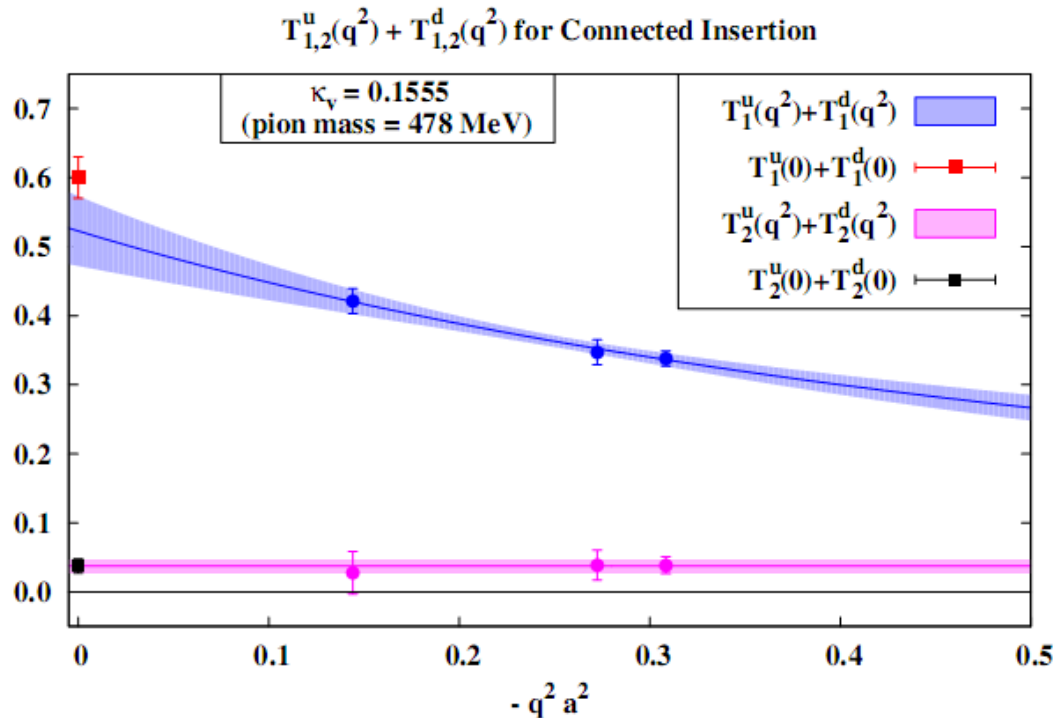
# Generalization of Equivalence principle

- Various arguments:  $AGM \approx 0$  separately for quarks and gluons – most clear from the lattice (LHPC/SESAM)



# Recent lattice study (M. Deka et al. [arXiv:1312.4816](https://arxiv.org/abs/1312.4816); cf plenary talk of K.F. Liu)

- Sum of u and d for Dirac (T1) and Pauli (T2) FFs



# Extended Equivalence

## Principle=Exact EquiPartition

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- In pQCD – violated
- Reason – in the case of ExEP- no smooth transition for zero fermion mass limit (Milton, 73)
- Conjecture (O.T., 2001 – prior to lattice data) – valid in NP QCD – zero quark mass limit is safe due to chiral symmetry breaking
- Supported by generic smallness of  $E$  (isoscalar AMM)





# Sum rules for EMT (and OAM)

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- First (seminal) example: X. Ji's sum rule ('96). Gravity counterpart – OT'99
- Burkardt sum rule – looks similar: can it be derived from EMT?
- Yes, if provide correct prescription to gluonic pole (OT'14)

# Pole prescription and Burkardt SR

- Pole prescription (dynamics!) provides ("T-odd") symmetric part!

- SR:  $\sum \int dx T(x, x) = 0$  (but relation of gluon Sivers to twist 3 still not found – prediction!)  $\sum \int \int dx_1 dx_2 \frac{T(x_1, x_2)}{x_1 - x_2 + i\varepsilon} = 0$

- Can it be valid separately for each quark flavour: nodes (related to "sign problem")?
- Valid if structures forbidden for TOTAL EMT do not appear for each flavour
- Structure contains besides S gauge vector n: If GI separation of EMT – forbidden: SR valid separately!

# Another manifestation of post-Newtonian (E)EP for spin 1 hadrons

- Tensor polarization - coupling of gravity to spin in forward matrix elements - inclusive processes
- Second moments of tensor distributions should sum to zero

$$\langle P, S | \bar{\psi}(0) \gamma^\nu D^{\nu_1} \dots D^{\nu_n} \psi(0) | P, S \rangle_{\mu^2} = i^{-n} M^2 S^{\nu\nu_1} P^{\nu_2} \dots P^{\nu_n} \int_0^1 C_q^T(x) x^n dx$$

$$\sum_q \langle P, S | T_i^{\mu\nu} | P, S \rangle_{\mu^2} = 2P^\mu P^\nu (1 - \delta(\mu^2)) + 2M^2 S^{\mu\nu} \delta_1(\mu^2)$$

$$\langle P, S | T_g^{\mu\nu} | P, S \rangle_{\mu^2} = 2P^\mu P^\nu \delta(\mu^2) - 2M^2 S^{\mu\nu} \delta_1(\mu^2)$$

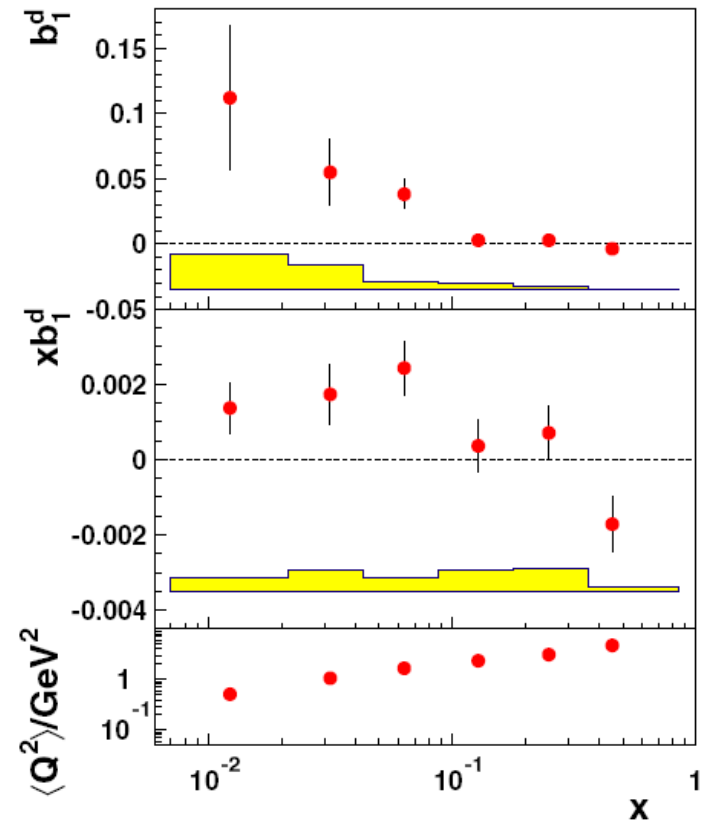
$$\sum_q \int_0^1 C_i^T(x) x dx = \delta_1(\mu^2) = 0 \text{ for ExEP}$$

# HERMES – data on tensor spin structure function

PRL 95, 242001 (2005)

- Isoscalar target – proportional to the sum of u and d quarks – combination required by EEP
- Second moments – compatible to zero better than the first one (collective glue  $\ll$  sea) – for valence:

$$\int_0^1 C_i^T(x) dx = 0.$$





# Are more accurate data possible?

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- HERMES – unlikely
- JLab may provide information about collective sea and glue in deuteron and indirect new test of Equivalence Principle



# CONCLUSIONS

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- Spin-gravity interactions may be probed directly in gravitational (inertial) experiments and indirectly – studying EMT matrix element
- Torsion and EP are tested in EDM experiments
- SR's for deuteron tensor polarization- indirectly probe EP and its extension separately for quarks and gluons



# EEP and AdS/QCD

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- Recent development – calculation of Rho formfactors in Holographic QCD (Grigoryan, Radyushkin)
- Provides  $g=2$  identically!
- Experimental test at time –like region possible